

## Choosing an Appropriate Bin width

The bin width (class interval width) determines the number of intervals and affects how the histogram looks.

- Too many intervals  $\rightarrow$  Too detailed, looks 'clumpy'
- Too few intervals  $\rightarrow$  oversimplified, lacks detail

Two common rules help determine bin width:

### 1. Sturges' Rule

- Number of intervals  $\approx 1 + \log_2(N)$  (or  $1 + 3.3 \log_{10}(N)$ )
- This rule works best for small datasets but may underestimate intervals for larger datasets

### 2. Rice Rule

- Number of intervals  $= 2 \times (\text{cube root of } N)$
- Preferred for larger data sets

## Relative frequency Histograms

### Summary of frequency polygons

A frequency polygon is a graph that helps visualize the shape of a dataset's distribution. It works similarly to histogram but connects data points with lines instead of using bars.

### How to create a frequency polygon

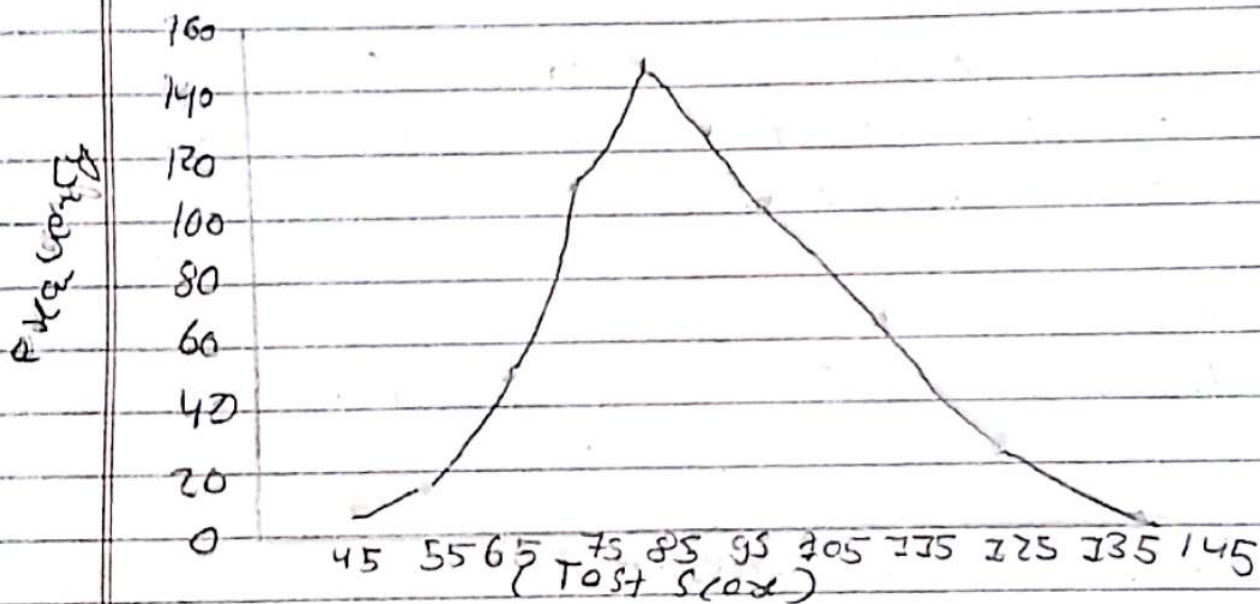
Begin by grouping data into class intervals, similar to histograms. Then calculate

class frequencies (how many values fall into each interval)

Midpoints of class intervals (used for plotting)

### Example Psychology Test Scores

Interval (Lower limit - Upper limit)	MidPoint	Frequency
39.5 - 49.5	45	3
49.5 - 59.5	55	18
59.5 - 69.5	65	53
69.5 - 79.5	75	107
79.5 - 89.5	85	147



The psychology test scores skew right because high scores trail off more gradually.

### Cumulative frequency Polygon

A cumulative frequency polygon (also called an ogive) represents the total count of observations up to a given class interval.

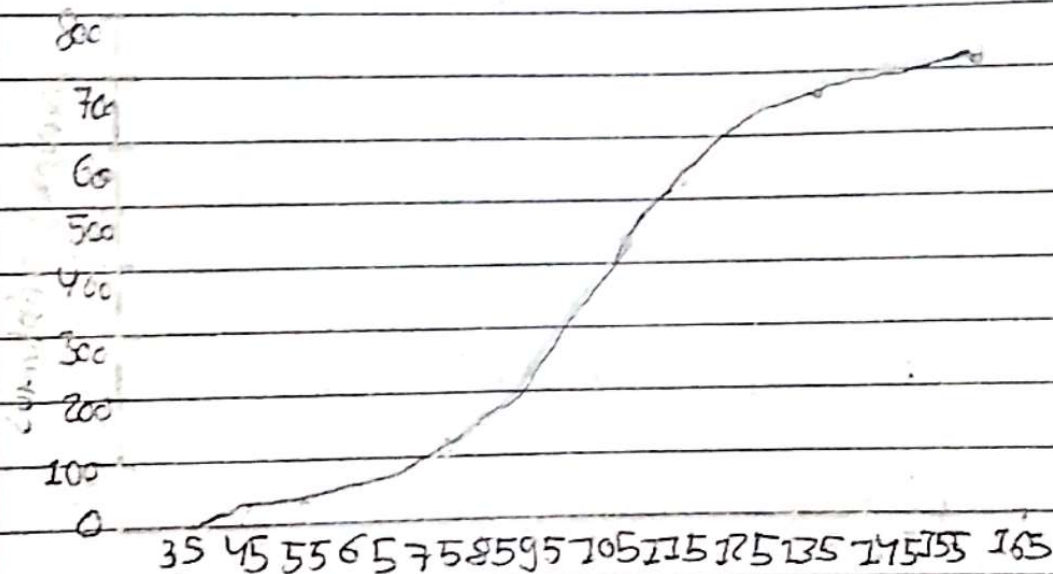
How to create a cumulative frequency polygon

- Instead of plotting raw frequencies, each  $y$ -value is the cumulative total of all previous frequencies



- Instead of plotting raw frequencies, each Y-value is the cumulative total of all previous frequencies
- The final cumulative frequency equals the total number of observations

Interval (lower limit - upper limit)	Midpoint	Frequency	Cumulative frequency
39.5 - 49.5	45	3	3
49.5 - 59.5	55	10	13
59.5 - 69.5	65	53	66
69.5 - 79.5	75	107	173
79.5 - 89.5	85	147	320
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Key Insights from a cumulative frequency polygon

- Helps determine percentiles and medians easily

The cumulative frequency of 55 corresponds to 13 students, meaning 13 students scored 55 or lower

## Overlaid Frequency Polygons

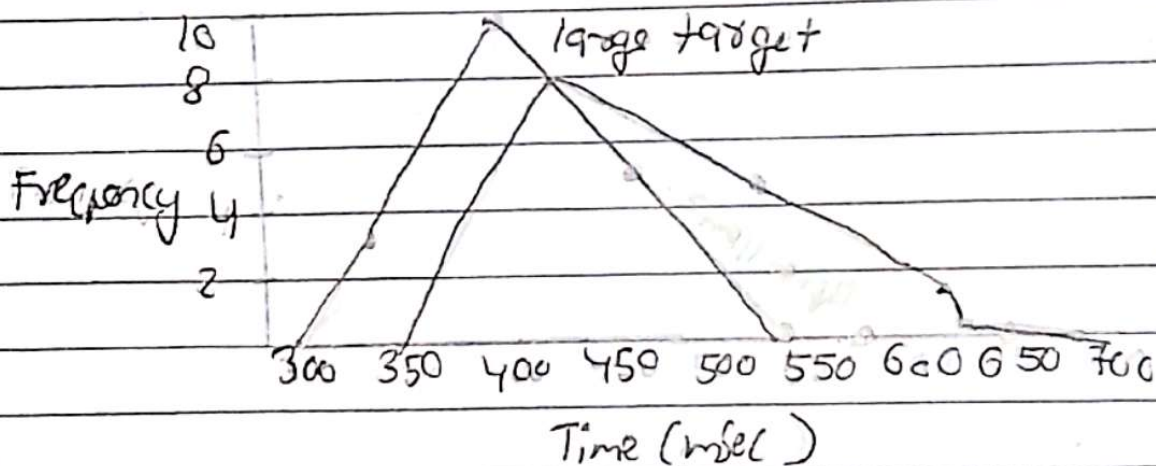
Comparing two or more datasets is easier with frequency polygons than histograms, since multiple distributions can be plotted together.

### Two datasets Cussos' Movement Speeds

small target (harder, takes longer)

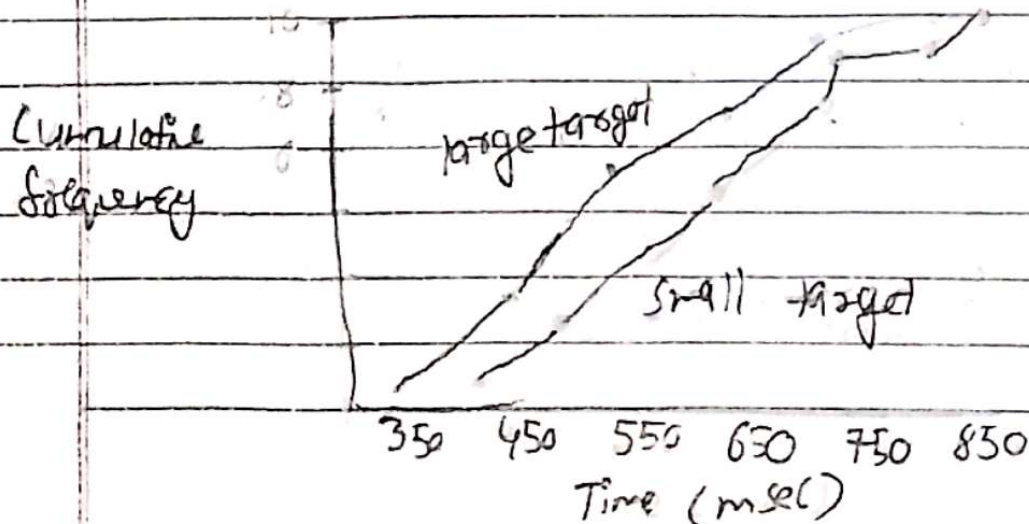
large target (easier, takes less time)

A frequency polygon overlays both distributions.



The small target curve is shifted right, meaning longer reaction times.

### Overlaid Cumulative Frequency Polygon



The small target polygon is below the large target polygon, indicating larger completion times for smaller targets.

### Key Takeaways

- Frequency polygons help visualize distributions
- Cumulative frequency polygons help analyze percentile rankings
- Overlaid frequency polygons make it easy to compare multiple datasets