



Fig. 1 A standard Snakes and Ladders

#### RULES:

- The game of Snakes and Ladders is played on a board with a  $10 \times 10$  grid.
- Players roll a single die and moving the corresponding number of squares.
- If the player lands you on the head of the Snake, you must go back to the square at the Snake tail.
- If you land at the bottom of a Ladder, you instantly climb to the top of that Ladder
- If a player rolls a die that would advance them beyond square 100, they stay at the same place.

#### MARKOV PROCESS:

- each square is a state.
- square of 100 as the only absorbing state
- with no memory of previous states is known

#### Probability Distribution:

$$\pi_i = (0, 0, \dots, 1) \text{ for states } i = 0, 1, \dots, n.$$

R, representing all of the transitions.

$R = \{(8, 30), (15, 47), (20, 39), (23, 76), (28, 50), (33, 70), (41, 62), (57, 83), (66, 89),$   
 $(79, 99), (13, 4), (35, 11), (61, 14), (69, 32), (81, 43), (85, 17), (87, 31), (91, 25),$   
 $(95, 67), (97, 58)\}.$

six equally probable options: rolling a 1, 2, 3, 4, 5 or 6.

transition matrix.

$$P_{101 \times 101} = \begin{matrix} & \begin{matrix} 0 & 1 & 2 & 3 & 4 & 5 & 6 & 7 & \dots & 35 & \dots & 61 & \dots & 97 & 98 & 99 & 100 \end{matrix} \\ \begin{matrix} 0 \\ 1 \\ 2 \\ \vdots \\ \vdots \\ 97 \\ 98 \\ 99 \\ 100 \end{matrix} & \left( \begin{array}{cccccccccccccccccccc} 0 & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & 0 & 0 & 0 & \dots & 0 & 0 & \dots & 0 & 0 & 0 & 0 \\ 0 & 0 & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \frac{1}{6} & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & 0 & 0 & 0 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ 97 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \dots & 0 & 0 & \dots & 0 & \frac{4}{6} & \frac{1}{6} & \frac{1}{6} \\ 98 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \dots & 0 & 0 & \dots & 0 & \frac{4}{6} & \frac{1}{6} & \frac{1}{6} \\ 99 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & \frac{5}{6} & \frac{1}{6} \\ 100 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \end{array} \right) \end{matrix}$$

It should be reduced to a 81 × 81 dimension.

