

TCS/TIT-405**B. TECH. (CS & IT) (FOURTH SEMESTER)
MID SEMESTER EXAMINATION, 2018****THEORY OF COMPUTATION****Time : 1 : 30 Hours****Maximum Marks : 50**

Note : (i) This question paper contains two Sections.

(ii) Both Sections are compulsory.

Section—A

1. Fill in the blanks : (1×5=5 Marks)

(a) The transition function maps in Deterministic Finite Automata.

(b) The transition function maps in Non-Deterministic Finite Automata.

(c) Consider the regular expression $(0 + 1)^n$. The minimum state finite automation that recognizes the language represented by this regular expression contains states.

(d) Given an arbitrary non-deterministic finite automation (NFA) with N states, the maximum number of states in an equivalent minimized DFA is

(2)

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- (e) The symbol " Δ " in FA with output denotes

2. Attempt any *five* parts : (3×5=15 Marks)

- What do you understand by Finite Automata ? Define its types with examples.
- How many substrings (of all lengths inclusive) can be formed from a character string of length n ? Assume all characters to be distinct. Prove your answer with an example.
- Define Finite Automata with output (Moore and Mealy machines).
- Define Set, Power Set and Subset with the help of examples.
- Write Pumping Lemma for regular language.
- Give the regular expression over $\{0, 1\}$ to denote the set of proper non-null substrings of the string "0010".

Section—B

3. Attempt any *two* parts of choice from (a), (b) and (c). (5×2=10 Marks)

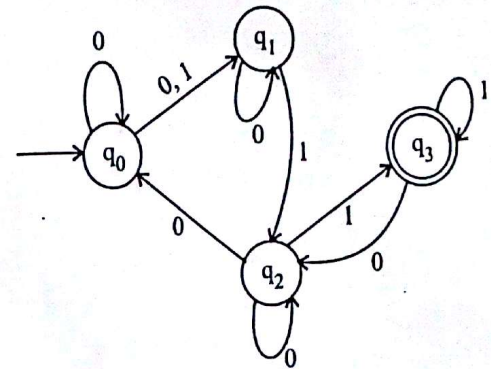
- Explain the theory of automata, computability and complexity.

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(3)

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- (b) Convert the following NFA into equivalent DFA :



- Design the DFA for the following regular expression :

$$(0 + 11(1 + 0)^*1 + 00 + 101)$$

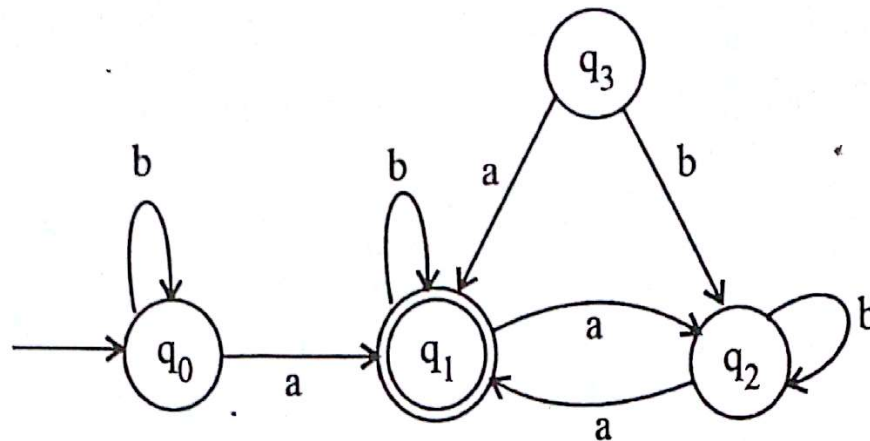
4. Attempt any *two* parts of choice from (a), (b) and (c). (5×2=10 Marks)

- Give minimal DFA that performs as a Mod-3 1's counter, i. e., outputs a 1 each time the number of 1's in the input sequence is a multiple of 3.
- Draw a minimum state deterministic finite automation accepting the language $L = \{w | w \text{ belongs to } \{0, 1\}^*, \text{ number of 0's and 1's in } w \text{ are divisible by 3 and 5}\}$.

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- (c) Derive the regular expression of the following Finite Automata :



5. Attempt any *two* parts of choice from (a), (b) and (c). (5×2=10 Marks)

(a) Design a Finite Automata to recognize the strings containing odd number of 0's and odd number of 1's over $\Sigma = \{0, 1\}$.

(b) Design a DFA for the language over $\Sigma = \{0, 1\}$ such that the Decimal equivalent of the Binary string is divisible by 3.

(c) Prove that the language $L = \{a^n b^n / n \geq 1\}$ is not regular.