

(1.)

$$(a.) f_{\frac{1}{2}}(x) = \begin{cases} \frac{1}{\sqrt{2\pi}} e^{-\frac{x^2}{2}} & x > 0 \\ 0 & \text{elsewhere} \end{cases}$$

3.7.29.61

余寧睿

(b.)  $0.68 > 6$

(c.)  $1.96$

(d.)  $f_Q(x) = \frac{1}{2^{\frac{1}{2}} \Gamma(\frac{1}{2})} x^{-\frac{1}{2}} e^{-\frac{x}{2}}$

(E.)  $E[Q] = 1$

(f.)  $\text{Std}[Q] = 2$

(H.)  $P(Q < 1) = 1 - \int_1^{\infty} \frac{1}{\sqrt{2\pi}} x^{-\frac{1}{2}} e^{-\frac{x}{2}} = \frac{1}{\sqrt{2\pi}} = 0.758$

(2.)

(a.)  $f_T(t) = e^{-x}$

(i.)  $\frac{e^{-\frac{1}{3}}}{3} = \frac{32}{1000}$

(b.)  $E[T] = 1$

$= 0.032 \dots$

$\approx 3\%$

(c.)  $\text{Std}[T] = 1$

(d.)  $P(T > 1) = \frac{1}{e} = 0.3679$

假設  $P(T_3 > 1)$  的機率為 3%，機率太小，故接受。

(E.)  $\frac{e^{-\frac{1}{3}}}{\Gamma(1) \times 3} = \frac{e^{-\frac{1}{3}}}{3}$

(f.)  $E[X] = 3$

(g.)  $\text{Std}[X] = 3$

(H.)  $P(T_3 > 3) = \frac{e^{-1}}{\Gamma(1) \times 3} = \frac{e^{-1}}{3}$