Algorithm 2 ProperLoop(L, P, S)1: $G_P^S := \text{the } S \text{ induced subgraph of } G_P;$

3: **for** each $C \in SCC$:

if $C \subset L$ and $R^-(C) \subseteq R^-(L)$ then return C

else if $R^-(C) \neq \emptyset$ and $R^-(C) \subset R^-(L)$ then return C

2: SCC := the set of SCCs of G_P^S ;

else if $R^-(C) = \emptyset$ or $R^-(C) = R^-(L)$ then **for** each atom $a \in C$:

> $G^* := \text{the } C \setminus \{a\} \text{ induced subgraph of } G_P^S;$ SCC^* := the set of SCCs of G^* ;

append new elements from SCC^* to SCC;

else

 $G_C := \text{the } C \setminus head(R^-(C) \setminus R^-(L)) \text{ induced subgraph}$

 $SCC_C :=$ the set of SCCs of G_C ;

append new elements from SCC_C to SCC;

13: 14: 15: return L

of $G_{\mathcal{D}}^{S}$:

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