Surname	Other r	names
Pearson Edexcel GCE	Centre Number	Candidate Number
Further P Mathema Advanced/Advance	itics FP2	
Wednesday 6 June 2018 - Time: 1 hour 30 minute:	•	Paper Reference 6668/01

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
 there may be more space than you need.
- You should show sufficient working to make your methods clear.
 Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

Information

- The total mark for this paper is 75.
- The marks for each question are shown in brackets
 use this as a guide as to how much time to spend on each question.

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

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1. (a) Express $\frac{1}{(r+3)(r+4)}$ in partial fractions.

(1)

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(b) Hence, using the method of differences, show that

$$\sum_{r=1}^{n} \frac{1}{(r+3)(r+4)} = \frac{n}{a(n+a)}$$

where a is a constant to be found.

(5)

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(c)	Find the exact value of	r=15	$\overline{(r+3)(r+4)}$

(2)

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A transformation from the z-plane to the w-plane is given by

$$w = \frac{1 - iz}{z}, \qquad z \neq 0$$

The transformation maps points on the real axis in the z-plane onto the line l in the

Find an equation of the line l.

(4)

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(4)

(5)

3. (a) By writing $\frac{\pi}{12} = \frac{\pi}{3} - \frac{\pi}{4}$, show that

(i)
$$\sin\left(\frac{\pi}{12}\right) = \frac{1}{4}\left(\sqrt{6} - \sqrt{2}\right)$$

(ii)
$$\cos\left(\frac{\pi}{12}\right) = \frac{1}{4}\left(\sqrt{6} + \sqrt{2}\right)$$

(b) Hence find the exact values of z for which

$$z^4 = 4\left(\cos\frac{\pi}{3} + i\sin\frac{\pi}{3}\right)$$

Give your answers in the form z = a + ib where $a, b \in \mathbb{R}$





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5.

$$y\frac{\mathrm{d}^2 y}{\mathrm{d}x^2} + 3x\frac{\mathrm{d}y}{\mathrm{d}x} - 3y^2 = 0$$

Given that at x = 0, y = 2 and $\frac{dy}{dx} = 1$

(a) show that, at x = 0, $\frac{d^3y}{dx^3} = \frac{3}{2}$

(6)

(b)	Find a s	series	solution	for y	v up	to	and	including	the	term	in	x^3
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6. (a) Find the general solution of the differential equa	tion
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$$6\frac{d^2y}{dx^2} + 5\frac{dy}{dx} - 6y = x - 6x^2$$
(8)

(b) Find the particular solution for which $y = 0$ and	$\frac{\mathrm{d}y}{\mathrm{d}x} = \frac{3}{2} \text{when } x = 0$	(5)
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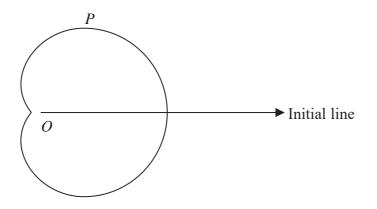


Figure 1

The curve C shown in Figure 1 has polar equation

$$r=2+\sqrt{3}\cos\theta, \qquad 0\leqslant\theta<2\pi$$

The tangent to C at the point P is parallel to the initial line.

(a) Show that
$$OP = \frac{1}{2}(3 + \sqrt{7})$$

(6)

(b) Find the exact area enclosed by the curve C.

(6)

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8. (a) Using the substitution $t = x^2$, or otherwise, find

$$\int 2x^5 e^{-x^2} dx$$

(6)

(b) Hence find the general solution of the differential equation

$$x\frac{\mathrm{d}y}{\mathrm{d}x} + 4y = 2x^2 \mathrm{e}^{-x^2}$$

giving your answer in the form y = f(x).

(4)

Given that y = 0 when x = 1

(c) find the particular solution of this differential equation, giving your solution in the form y = f(x).

(3)

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