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**Pearson Edexcel**
International
Advanced Level

Centre Number

Candidate Number

# Core Mathematics C12

**Advanced Subsidiary**

Wednesday 23 May 2018 – Morning
**Time: 2 hours 30 minutes**

Paper Reference
**WMA01/01**

**You must have:**
Mathematical Formulae and Statistical Tables (Blue)

Total Marks

**Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
  – *there may be more space than you need*.
- You should show sufficient working to make your methods clear.  Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information

- The total mark for this paper is 125.
- The marks for **each** question are shown in brackets
  – *use this as a guide as to how much time to spend on each question*.

## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

*Turn over* ▶

**Pearson**

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1. The table below shows corresponding values of $x$ and $y$ for $y = \dfrac{1}{\sqrt{(x+1)}}$, with the values for $y$ rounded to 3 decimal places where necessary.

| $x$ | 0 | 3 | 6 | 9 | 12 | 15 |
|---|---|---|---|---|---|---|
| $y$ | 1 | 0.5 | 0.378 | 0.316 | 0.277 | |

(a) Complete the table by giving the value of $y$ corresponding to $x = 15$

**(1)**

(b) Use the trapezium rule with all the values of $y$ from the completed table to find an approximate value for

$$\int_{0}^{15} \frac{1}{\sqrt{(x+1)}} \, dx$$

giving your answer to 2 decimal places.

**(4)**

**Question 1 continued**

**(Total 5 marks)**

Q1

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**2.**
$$f(x) = ax^3 + 2x^2 + bx - 3$$

where $a$ and $b$ are constants.

When $f(x)$ is divided by $(2x - 1)$ the remainder is 1

(a) Show that
$$a + 4b = 28$$

**(2)**

When $f(x)$ is divided by $(x + 1)$ the remainder is $-17$

(b) Find the value of $a$ and the value of $b$.

**(4)**

**Question 2 continued**

**(Total 6 marks)**

Q2

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**3.** The line $l_1$ passes through the points $A(-1, 4)$ and $B(5, -8)$

(a) Find the gradient of $l_1$

**(2)**

The line $l_2$ is perpendicular to the line $l_1$ and passes through the point $B(5, -8)$

(b) Find an equation for $l_2$ in the form $ax + by + c = 0$, where $a$, $b$ and $c$ are integers.

**(4)**

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**Question 3 continued**

(Total 6 marks)

Q3

**Turn over**

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**4.** Given that

$$y = \frac{64x^6}{25}, \quad x > 0$$

express each of the following in the form $kx^n$ where $k$ and $n$ are constants.

(a) $y^{-\frac{1}{2}}$

**(3)**

(b) $(25y)^{\frac{2}{3}}$

**(2)**

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**Question 4 continued**

**(Total 5 marks)**

Q4

**Turn over**

**5.** (a) Find the first 4 terms, in ascending powers of $x$, of the binomial expansion of

$$\left(1 + \frac{x}{3}\right)^{18}$$

giving each term in its simplest form.

**(4)**

(b) Use the answer to part (a) to find an estimated value for $\left(\dfrac{31}{30}\right)^{18}$, stating the value of $x$

that you have used and showing your working. Give your estimate to 4 decimal places.

**(3)**

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**Question 5 continued**

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**Question 5 continued**

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**Question 5 continued**

**(Total 7 marks)**

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**6.** Find the exact values of $x$ for which

$$2\log_5(x + 5) - \log_5(2x + 2) = 2$$

Give your answers as simplified surds.

**(7)**

**Question 6 continued**

**(Total 7 marks)**

Q6

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7. A sequence is defined by

$$u_1 = 3$$
$$u_{n+1} = u_n - 5, \qquad n \geqslant 1$$

Find the values of

(a) $u_2$, $u_3$ and $u_4$

**(2)**

(b) $u_{100}$

**(3)**

(c) $\displaystyle\sum_{i=1}^{100} u_i$

**(3)**

P 5 1 4 0 4 A 0 1 6 4 8

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**Question 7 continued**

Q7

**(Total 8 marks)**

**8.** The equation $(k-4)x^2 - 4x + k - 2 = 0$, where $k$ is a constant, has no real roots.

(a) Show that $k$ satisfies the inequality

$$k^2 - 6k + 4 > 0$$

**(3)**

(b) Find the exact range of possible values for $k$.

**(4)**

**Question 8 continued**

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**Q8**

**(Total 7 marks)**

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**9.** A cyclist aims to travel a total of 1200 km over a number of days.
He cycles 12 km on day 1
He increases the distance that he cycles each day by 6% of the distance cycled on the previous day, until he reaches the total of 1200 km.

(a) Show that on day 8 he cycles approximately 18 km.

**(3)**

He reaches his total of 1200 km on day $N$, where $N$ is a positive integer.

(b) Find the value of $N$.

**(4)**

The cyclist stops when he reaches 1200 km.

(c) Find the distance that he cycles on day $N$. Give your answer to the nearest km.

**(2)**

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**Question 9 continued**

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**Question 9 continued**

**Question 9 continued**

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(Total 9 marks)

Q9

P5 1 4 0 4 A 0 2 3 4 8

**10.**



Diagram not drawn to scale

**Figure 1**

Figure 1 shows a semicircle with centre $O$ and radius $3\,cm$. $XY$ is the diameter of this semicircle. The point $Z$ is on the circumference such that angle $XOZ = 1.3$ radians. The shaded region enclosed by the chord $XZ$, the arc $ZY$ and the diameter $XY$ is a template for a badge.

Find, giving each answer to 3 significant figures,

(a) the length of the chord $XZ$,

**(2)**

(b) the perimeter of the template $XZYX$,

**(4)**

(c) the area of the template.

**(4)**

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**Question 10 continued**

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**Question 10 continued**

**Question 10 continued**

**(Total 10 marks)**

**Q10**

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**11.** The curve $C$ has equation $y = f(x)$, $x > 0$, where

$$f'(x) = \frac{5x^2 + 4}{2\sqrt{x}} - 5$$

It is given that the point $P(4, 14)$ lies on $C$.

(a) Find $f(x)$, writing each term in a simplified form.

**(6)**

(b) Find the equation of the tangent to $C$ at the point $P$, giving your answer in the form $y = mx + c$, where $m$ and $c$ are constants.

**(4)**

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**Question 11 continued**

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**Question 11 continued**

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**Question 11 continued**

Q11

(Total 10 marks)

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**12.** [*In this question solutions based entirely on graphical or numerical methods are not acceptable.*]

(i) Solve for $0 \leqslant x < 360°$,

$$5\sin(x + 65°) + 2 = 0$$

giving your answers in degrees to one decimal place.

**(4)**

(ii) Find, for $0 \leqslant \theta < 2\pi$, all the solutions of

$$12\sin^2\theta + \cos\theta = 6$$

giving your answers in radians to 3 significant figures.

**(6)**

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**Question 12 continued**

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**Question 12 continued**

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**Question 12 continued**

**(Total 10 marks)**

**Q12**

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**13.** The point $A(9, -13)$ lies on a circle $C$ with centre the origin and radius $r$.

(a) Find the exact value of $r$.

**(2)**

(b) Find an equation of the circle $C$.

**(1)**

A straight line through point $A$ has equation $2y + 3x = k$, where $k$ is a constant.

(c) Find the value of $k$.

**(1)**

This straight line cuts the circle again at the point $B$.

(d) Find the exact coordinates of point $B$.

**(6)**

**Question 13 continued**

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**Question 13 continued**

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**Question 13 continued**

**Q13**

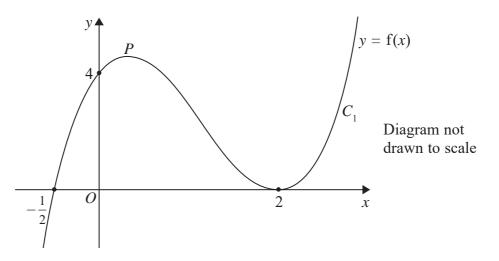**(Total 10 marks)**

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**14.**



**Figure 2**

Figure 2 shows a sketch of the curve $C_1$ with equation $y = f(x)$ where

$$f(x) = (x - 2)^2(2x + 1), \quad x \in \mathbb{R}$$

The curve crosses the $x$-axis at $\left(-\dfrac{1}{2}, 0\right)$, touches it at $(2, 0)$ and crosses the

$y$-axis at $(0, 4)$. There is a maximum turning point at the point marked $P$.

(a) Use $f'(x)$ to find the exact coordinates of the turning point $P$.

**(7)**

A second curve $C_2$ has equation $y = f(x + 1)$.

(b) Write down an equation of the curve $C_2$
You may leave your equation in a factorised form.

**(1)**

(c) Use your answer to part (b) to find the coordinates of the point where the curve $C_2$
meets the $y$-axis.

**(2)**

(d) Write down the coordinates of the two turning points on the curve $C_2$

**(2)**

(e) Sketch the curve $C_2$, with equation $y = f(x + 1)$, giving the coordinates of the points
where the curve crosses or touches the $x$-axis.

**(3)**

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**Question 14 continued**

**Turn over**

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**Question 14 continued**

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**Question 14 continued**

**(Total 15 marks)**

Q14

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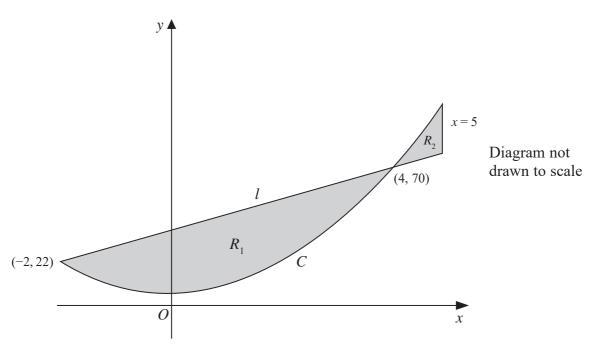
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**15.**



**Figure 3**

A design for a logo consists of two finite regions $R_1$ and $R_2$, shown shaded in Figure 3.

The region $R_1$ is bounded by the straight line $l$ and the curve $C$.

The region $R_2$ is bounded by the straight line $l$, the curve $C$ and the line with equation $x = 5$

The line $l$ has equation $y = 8x + 38$

The curve $C$ has equation $y = 4x^2 + 6$

Given that the line $l$ meets the curve $C$ at the points $(-2, 22)$ and $(4, 70)$, use integration to find

(a) the area of the larger lower region, labelled $R_1$

**(6)**

(b) the exact value of the total area of the two shaded regions.

**(3)**

Given that

$$\frac{\text{Area of } R_1}{\text{Area of } R_2} = k$$

(c) find the value of $k$.

**(1)**

**Question 15 continued**

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**Question 15 continued**

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**Question 15 continued**

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**Question 15 continued**

**Q15**

**(Total 10 marks)**

**TOTAL FOR PAPER: 125 MARKS**

**END**

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