

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				

**Pearson Edexcel International Advanced Level**

**Monday 23 October 2023**

Afternoon (Time: 1 hour 30 minutes) **Paper reference** **WMA14/01**

**Mathematics**

**International Advanced Level**

**Pure Mathematics P4**

**You must have:**  
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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**Pearson**

1. (a) Find the first four terms, in ascending powers of  $x$ , of the binomial expansion of

$$\frac{8}{(2 - 5x)^2}$$

writing each term in simplest form.

(4)

- (b) Find the range of values of  $x$  for which this expansion is valid.

(1)

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**Question 1 continued**

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**(Total for Question 1 is 5 marks)**

2.

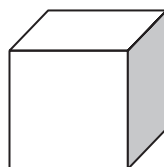
 $x \text{ cm}$ **Figure 1**

Figure 1 shows a cube which is increasing in size.

At time  $t$  seconds,

- the length of each edge of the cube is  $x \text{ cm}$
- the surface area of the cube is  $S \text{ cm}^2$
- the volume of the cube is  $V \text{ cm}^3$

Given that the surface area of the cube is increasing at a constant rate of  $4 \text{ cm}^2 \text{ s}^{-1}$

(a) show that  $\frac{dx}{dt} = \frac{k}{x}$  where  $k$  is a constant to be found,

(4)

(b) show that  $\frac{dV}{dt} = V^p$  where  $p$  is a constant to be found.

(3)

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**Question 2 continued**

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**(Total for Question 2 is 7 marks)**

3.

**In this question you must show all stages of your working.**

**Solutions based on calculator technology are not acceptable.**

- (i) Use integration by parts to find the exact value of

$$\int_0^4 x^2 e^{2x} \, dx$$

giving your answer in simplest form.

(5)

- (ii) Use integration by substitution to show that

$$\int_3^{\frac{21}{2}} \frac{4x}{(2x-1)^2} \, dx = a + \ln b$$

where  $a$  and  $b$  are constants to be found.

(7)

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## Question 3 continued

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**Question 3 continued**

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**(Total for Question 3 is 12 marks)**

4. (a) Prove by contradiction that for all positive numbers  $k$

$$k + \frac{9}{k} \geq 6 \quad (4)$$

- (b) Show that the result in part (a) is not true for all real numbers.

(1)

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**Question 4 continued**

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**(Total for Question 4 is 5 marks)**

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**Question 5 continued**

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**Question 5 continued**

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**Question 5 continued**

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**(Total for Question 5 is 10 marks)**





## Question 6 continued

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**Question 7 continued**

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**Question 7 continued**

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**Question 7 continued**

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**(Total for Question 7 is 12 marks)**

8.

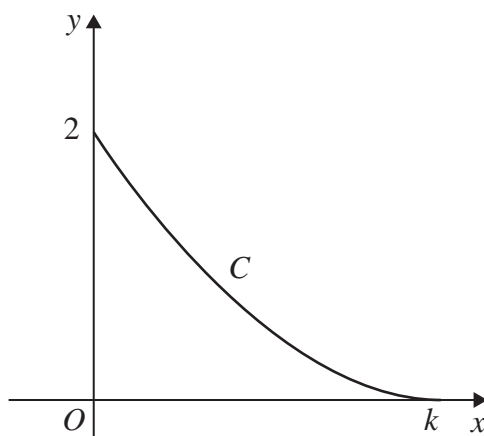


Figure 3

Figure 3 shows a sketch of the curve  $C$  with parametric equations

$$x = 6t - 3\sin 2t \quad y = 2\cos t \quad 0 \leq t \leq \frac{\pi}{2}$$

The curve meets the  $y$ -axis at 2 and the  $x$ -axis at  $k$ , where  $k$  is a constant.

(a) State the value of  $k$ .

(1)

(b) Use parametric differentiation to show that

$$\frac{dy}{dx} = \lambda \operatorname{cosec} t$$

where  $\lambda$  is a constant to be found.

(4)

The point  $P$  with parameter  $t = \frac{\pi}{4}$  lies on  $C$ .

The tangent to  $C$  at the point  $P$  cuts the  $y$ -axis at the point  $N$ .

(c) Find the exact  $y$  coordinate of  $N$ , giving your answer in simplest form.

(3)

The region bounded by the curve, the  $x$ -axis and the  $y$ -axis is rotated through  $2\pi$  radians about the  $x$ -axis to form a solid of revolution.

(d) (i) Show that the volume of this solid is given by

$$\int_0^\alpha \beta(1 - \cos 4t) dt$$

where  $\alpha$  and  $\beta$  are constants to be found.

(ii) Hence, using algebraic integration, find the exact volume of this solid.

(6)





## Question 8 continued

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**Question 8 continued**

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**Question 8 continued**

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**(Total for Question 8 is 14 marks)****TOTAL FOR PAPER IS 75 MARKS**