Mark Scheme (Results) January 2007

GCE

GCE Mathematics

Statistics S2 (6684)



January 2007 6684 Statistics S2 Mark Scheme

Question Number	Scheme	Marks
1. (a)	A random variable; function of known observations (from a population). data OK	B1 B1 (2)
(b) (i)	Yes	B1 (1)
(ii)	No	B1 (1)
		Total 4
2.		
(a)	$P(J \ge 10) = 1 - P(J \le 9)$ or =1-P(J<10)	M1
	= 1 - 0.9919 implies method	
	= 0.0081 awrt 0.0081	A1 (2)
(b)	$P(K \le 1) = P(K = 0) + P(K = 1)$ both, implied below even with '25' missing	M1
	= $(0.73)^{25} + 25(0.73)^{24}(0.27)$ clear attempt at '25' required	M1
	= 0.00392 awrt 0.0039 implies M	A1 (3) Total 5

Question Number	S	cheme	Marks
3. (a)	Let W represent the number of white plus $W \sim B(12,0.45)$ $P(W = 5) = P(W \le 5) - P(W \le 4)$	use of ${}^{2}C_{5}0.45^{5}0.55^{7}$ or equivalent award B1M1 values from correct table implies B	B1 M1
	= 0.2225	awrt 0.222(5)	A1 (3)
(b)	$P(W \ge 7) = 1 - P(W \le 6)$	or =1- $P(W < 7)$	M1
	= 1 - 0.7393	implies method	
	= 0.2607	awrt 0.261	A1 (2)
(c)	P(3 contain more white than coloured)	$= \frac{10!}{3!7!} (0.2607)^3 (1 - 0.2607)^7 \text{ use of B,n=10}$	M1A1∫
	= 0	.256654 awrt 0.257	A1 (3)
(d)	mean = $np = 22.5$; $var = npq = 12.375$	5	B1B1
	$P(W > 25) \approx P\left(Z > \frac{25.5 - 22.5}{\sqrt{12.375}}\right)$	\pm standardise with σ and $\mu;$ ± 0.5 c.c.	M1;M1
	$\approx P(Z > 0.8528)$	awrt 0.85	A1
	≈1 − 0.8023	'one minus'	M1
	≈0.1977	awrt 0.197 or 0.198	A1
			(7)
			Total 15

Question Number	Scheme		Marks
4. (a)	$\lambda > 10$ or large	μ ok	B1
(a)	N > 10 of farge	μ or	(1)
(b)	The Poisson is discrete and the normal	is continuous.	B1 (1)
			(1)
(c)	Let Y represent the number of yachts h	ired in winter	
	$P(Y<3) = P(Y \le 2)$	$P(Y \le 2) \& Po(5)$	M1
	=0.1247	awrt 0.125	A1
			(2)
(d)	Let <i>X</i> represent the number of yachts hired in summer $X \sim Po(25)$.		
	-	n be implied by standardisation below	B1
	$P(X > 30) \approx P\left(Z > \frac{30.5 - 25}{5}\right)$		DI
	$P(X > 30) \approx P(Z > \frac{1}{5})$	± standardise with 25 & 5; ±0.5 c.c.	M1;M1
	$\approx P(Z > 1.1)$	1.1	A1
	≈ 1 – 0.8643	'one minus'	M1
			IVII
	≈ 0.1357	awrt 0.136	A1 (6)
(e)	0.105716	1270 (1) 16	(0)
	no. of weeks $= 0.1357 \times 16$	ANS (d)x16	M1
	= 2.17 or 2 or 3	ans>16 M0A0	A1 ∫
			(2)
			Total 12

Question Number	Scheme	Marks
5. (a)	$f(x) = \begin{cases} \frac{1}{\beta - \alpha}, & \alpha < x < \beta, \\ 0, & \text{otherwise.} \end{cases}$ function including inequality, 0 otherwise	B1,B1 (2)
(b)	$\frac{\alpha + \beta}{2} = 2$, $\frac{3 - \alpha}{\beta - \alpha} = \frac{5}{8}$ or equivalent	B1,B1
	$\alpha + \beta = 4$ $3\alpha + 5\beta = 24$	
	$3(4-\beta)+5\beta=24$ attempt to solve 2 eqns $\beta=6$	M1
	$\alpha = -2$ both	A1 (4)
(c)	$E(X) = \frac{150 + 0}{2} = 75 \text{ cm}$ 75	B1 (1)
(d)	Standard deviation = $\sqrt{\frac{1}{12}(150-0)^2}$	M1
	$= 43.30127$ cm $25\sqrt{3}$ or awrt 43.3	A1 (2)
(e)	$P(X < 30) + P(X > 120) = \frac{30}{150} + \frac{30}{150}$ 1st or at least one fraction, + or double	M1,M1
	$=\frac{60}{150}$ or $\frac{2}{5}$ or 0.4 or equivalent fraction	A1
		(3)
		Total 12

Question Number	Scheme		Marks
6. (a)	$H_0: p = 0.20, H_1: p < 0.20$		B1,B1
	Let <i>X</i> represent the number of people buying far	nily size bar. $X \sim B (30, 0.20)$	
	$P(X \leq 2) = 0.0442 \qquad \text{or } P(X \leq 2)$ $P(X \leq 3) =$ $CR X \leq 2$		M1A1
	0.0442 < 5%, so significant. Significant		M1
	There is evidence that the no. of family size bars	sold is lower than usual.	A1 (6)
(b)	$H_0: p = 0.02, H_1: p \neq 0.02$	$\lambda = 4$ etc ok both	B1
	Let Y represent the number of gigantic bars sold.		
	$Y \sim B (200, 0.02) \implies Y \sim Po (4)$	can be implied below	M1
	$P(Y = 0) = 0.0183$ and $P(Y \le 8) = 0.9786 \Rightarrow P$	$(Y \ge 9) = 0.0214$ first, either	B1,B1
	Critical region $Y = 0 \cup Y \ge 9$	$Y \leq 0$ ok	B1,B1
	N.B. Accept exact Bin: 0.0176 and 0.0202		
(c)	Significance level = $0.0183 + 0.0214 = 0.0397$	awrt 0.04	B1 (1)
			Total 13

Question Number	Scheme	
7. (a)	$1 - F(0.3) = 1 - (2 \times 0.3^2 - 0.3^3)$ 'one minus' required = 0.847	M1 A1 (2)
(b)	F(0.60) = 0.5040 $F(0.59) = 0.4908$ both required awrt 0.5, 0.49 $0.5 lies between therefore median value lies between 0.59 and 0.60.$	M1A1 B1 (3)
(c)	$f(x) = \begin{cases} -3x^2 + 4x, & 0 \le x \le 1, \\ 0, & \text{otherwise.} \end{cases}$ attempt to differentiate, all correct	M1A1 (2)
(d)	$\int_0^1 x f(x) dx = \int_0^1 -3x^3 + 4x^2 dx$ attempt to integrate $x f(x)$	M1
	$= \left[\frac{-3x^4}{4} + \frac{4x^3}{3} \right]_0^1$ sub in limits	M1
	$= \frac{7}{12} \text{ or } 0.58\dot{3} \text{ or } 0.583 \text{ or equivalent fraction}$	A1 (3)
(e)	$\frac{df(x)}{dx} = -6x + 4 = 0$ attempt to differentiate f(x) and equate to 0	M1
	$x = \frac{2}{3}$ or $0.\dot{6}$ or 0.667	A1
(f)	mean < median < mode, therefore negative skew. Any pair, cao	(2) B1,B1 (2)
		Total 14