

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				
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**Pearson Edexcel International Advanced Level**

**Time** 1 hour 30 minutes **Paper reference** **WFM01/01**

**Mathematics**

**International Advanced Subsidiary/Advanced Level**

**Further Pure Mathematics F1**

**You must have:**  
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 9 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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Q:1/1/1/



1.  $z_1 = 3 + 3i$        $z_2 = p + qi$        $p, q \in \mathbb{R}$

Given that  $|z_1 z_2| = 15\sqrt{2}$

(a) determine  $|z_2|$  (2)

Given also that  $p = -4$

(b) determine the possible values of  $q$  (2)

(c) Show  $z_1$  and the possible positions for  $z_2$  on the same Argand diagram. (2)

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**Question 1 continued**

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**(Total for Question 1 is 6 marks)**

2.

$$f(x) = 10 - 2x - \frac{1}{2\sqrt{x}} - \frac{1}{x^3} \quad x > 0$$

(a) Show that the equation  $f(x) = 0$  has a root  $\alpha$  in the interval  $[0.4, 0.5]$  (2)

(b) Determine  $f'(x)$ . (3)

(c) Using  $x_0 = 0.5$  as a first approximation to  $\alpha$ , apply the Newton-Raphson procedure once to  $f(x)$  to find a second approximation to  $\alpha$ , giving your answer to 3 decimal places. (2)

The equation  $f(x) = 0$  has another root  $\beta$  in the interval  $[4.8, 4.9]$

(d) Use linear interpolation once on the interval  $[4.8, 4.9]$  to find an approximation to  $\beta$ , giving your answer to 3 decimal places. (2)

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**(Total for Question 2 is 9 marks)**

3.  $\mathbf{M} = \begin{pmatrix} k & k \\ 3 & 5 \end{pmatrix}$  where  $k$  is a non-zero constant

(a) Determine  $\mathbf{M}^{-1}$ , giving your answer in simplest form in terms of  $k$ .

(2)

Hence, given that  $\mathbf{N}^{-1} = \begin{pmatrix} k & k \\ 4 & -1 \end{pmatrix}$

(b) determine  $(\mathbf{MN})^{-1}$ , giving your answer in simplest form in terms of  $k$ .

(2)

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**Question 3 continued**

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**(Total for Question 3 is 4 marks)**

4.

$$f(z) = 2z^4 - 19z^3 + Az^2 + Bz - 156$$

where  $A$  and  $B$  are constants.

The complex number  $5 - i$  is a root of the equation  $f(z) = 0$

- (a) Write down another complex root of this equation. (1)
- (b) Solve the equation  $f(z) = 0$  completely. (5)
- (c) Determine the value of  $A$  and the value of  $B$ . (2)

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**Question 4 continued**

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**(Total for Question 4 is 8 marks)**





**Question 5 continued**

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**(Total for Question 5 is 10 marks)**



**Question 6 continued**

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**(Total for Question 6 is 11 marks)**

$$\mathbf{A} = \begin{pmatrix} -\frac{\sqrt{3}}{2} & -\frac{1}{2} \\ \frac{1}{2} & -\frac{\sqrt{3}}{2} \end{pmatrix}$$

- (f) Given that the area of parallelogram  $P'$  is 20 square units, determine the area of parallelogram  $P$





**Question 7 continued**

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**Question 7 continued**

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**(Total for Question 7 is 9 marks)**

8. (a) Use the standard results for  $\sum_{r=1}^n r^2$  and  $\sum_{r=1}^n r$  to show that for all positive integers  $n$

$$\sum_{r=0}^n (r+1)(r+2) = \frac{1}{3}(n+1)(n+2)(n+3) \quad (5)$$

- (b) Hence determine the value of

$$10 \times 11 + 11 \times 12 + 12 \times 13 + \dots + 100 \times 101 \quad (3)$$

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**Question 8 continued**

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**(Total for Question 8 is 8 marks)**

9. (i) A sequence of numbers is defined by

$$u_1 = 3$$

$$u_{n+1} = 2u_n - 2^{n+1} \quad n \geq 1$$

Prove by induction that, for  $n \in \mathbb{N}$

$$u_n = 5 \times 2^{n-1} - n \times 2^n \quad (5)$$

- (ii) Prove by induction that, for  $n \in \mathbb{N}$

$$f(n) = 5^{n+2} - 4n - 9$$

is divisible by 16 (5)

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**Question 9 continued**

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**Question 9 continued**

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**(Total for Question 9 is 10 marks)****TOTAL FOR PAPER: 75 MARKS****END**