

Please check the examination details below before entering your candidate information

Candidate surname		Other names	
Centre Number		Candidate Number	
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Pearson Edexcel International Advanced Level

Thursday 8 June 2023

Morning (Time: 1 hour 30 minutes) **Paper reference** **WFM02/01**

Mathematics

International Advanced Subsidiary/Advanced Level

Further Pure Mathematics F2

You must have:
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

Candidates may use any calculator allowed by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear.
Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets
– *use this as a guide as to how much time to spend on each question.*

Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

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Question 1 continued

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Question 1 continued

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(Total for Question 1 is 7 marks)

Question 2 continued

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Question 2 continued

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(Total for Question 2 is 10 marks)

3.

In this question you must show all stages of your working.

Solutions relying on calculator technology are not acceptable.

Given that

$$\frac{x+2}{x+4} \leq \frac{x}{k(x-1)}$$

where k is a positive constant,

(a) show that

$$(x+4)(x-1)(px^2+qx+r) \leq 0$$

where p , q and r are expressions in terms of k to be determined.

(3)

(b) Hence, or otherwise, determine the values for x for which

$$\frac{x+2}{x+4} \leq \frac{x}{3(x-1)}$$

(4)

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Question 3 continued

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(Total for Question 3 is 7 marks)

4. (a) Determine the general solution of the differential equation

$$\frac{d^2y}{dx^2} - 8\frac{dy}{dx} + 16y = 48x^2 - 34 \quad (5)$$

Given that $y = 4$ and $\frac{dy}{dx} = 21$ at $x = 0$

- (b) determine the particular solution of the differential equation. (4)

- (c) Hence find the value of y at $x = -2$, giving your answer in the form $pe^q + r$ where p, q and r are integers to be determined. (2)

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Question 5 continued

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Question 5 continued

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(Total for Question 5 is 7 marks)

Question 6 continued

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Question 6 continued

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(Total for Question 6 is 9 marks)

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7. (a) Show that the substitution $z = y^{-2}$ transforms the differential equation

$$x \frac{dy}{dx} + y + 4x^2 y^3 \ln x = 0 \quad x > 0 \quad (\text{I})$$

into the differential equation

$$\frac{dz}{dx} - \frac{2z}{x} = 8x \ln x \quad x > 0 \quad (\text{II}) \quad (5)$$

- (b) By solving differential equation (II), determine the general solution of differential equation (I), giving your answer in the form $y^2 = f(x)$

(6)

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Question 7 continued

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Question 7 continued

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(Total for Question 7 is 11 marks)

8.

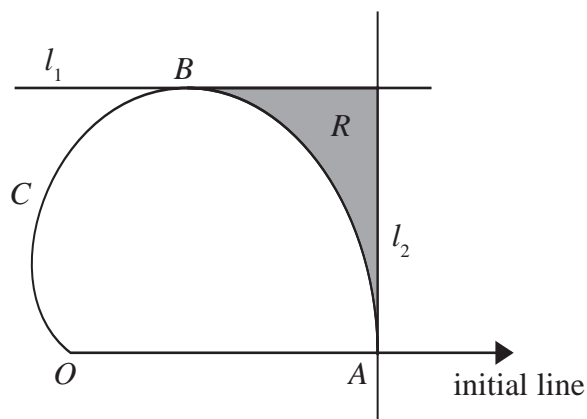


Figure 1

Figure 1 shows a sketch of the curve C with equation

$$r = 6(1 + \cos \theta) \quad 0 \leq \theta \leq \pi$$

Given that C meets the initial line at the point A , as shown in Figure 1,

- (a) write down the polar coordinates of A .

(1)

The line l_1 , also shown in Figure 1, is the tangent to C at the point B and is parallel to the initial line.

- (b) Use calculus to determine the polar coordinates of B .

(4)

The line l_2 , also shown in Figure 1, is the tangent to C at A and is perpendicular to the initial line.

The region R , shown shaded in Figure 1, is bounded by C , l_1 and l_2

- (c) Use algebraic integration to find the exact area of R , giving your answer in the form $p\sqrt{3} + q\pi$ where p and q are constants to be determined.

(8)

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Question 8 continued

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Question 8 continued

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(Total for Question 8 is 13 marks)**TOTAL FOR PAPER IS 75 MARKS**