Please check the examination details below before entering your candidate information		
Candidate surname	Other	names
Pearson Edexcel International Advanced Level	Centre Number	Candidate Number
Time 1 hour 30 minutes	Paper reference V	VME02/01
Mathematics		
International Advanced Mechanics M2	d Subsidiary/Ad	vanced Level
You must have: Mathematical Formulae and Stat	istical Tables (Yellow),	calculator Total Marks

Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use black ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You should show sufficient working to make your methods clear.
  - Answers without working may not gain full credit.
- Whenever a numerical value of g is required, take  $g = 9.8 \,\mathrm{m\,s^{-2}}$ , and give your answer to either 2 significant figures or 3 significant figures.

## Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for each question are shown in brackets
  - use this as a guide as to how much time to spend on each question.

## Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.
- Good luck with your examination.

Turn over ►







1.	A motorcyclist and his motorcycle have a combined mass of 480 kg.
	The motorcyclist drives down a straight road that is inclined at an angle $\theta$ to the horizontal
	where $\sin \theta = \frac{1}{12}$ , with the engine of the motorcycle working at 3.5 kW. The motorcycle
	is moving at a constant speed of $V \text{m s}^{-1}$ . The resistance to the motion of the motorcycle is modelled as a constant force with magnitude $20V$ newtons.
	Find the value of $V$ . (5

88	$\times\!\!\times\!\!\times$
$\otimes$	$\times\!\!\times\!\!\times$
×	$\times\!\!\times\!\!\times$
X	
$\otimes$	$\times\!\!\times\!\!\times$
$\otimes$	$\ggg$
$\otimes$	$\times\!\!\times\!\!\times$
$\otimes$	$\times\!\!\times\!\!\times$
$\times$	$\times\!\!\times\!\!\times$
88	$\times\!\!\times\!\!\!\times$
X	<b>4</b>
×	ш
$\otimes$	60
$\times$	
$\otimes$	
$\langle \zeta \rangle$	S
88	$\cong$
90	
$\approx$	
$\otimes$	***
$\otimes$	
$\otimes$	
$\otimes$	ŮĽ.
$\times$	₩
$\otimes$	
$\otimes$	
88	2
$\otimes$	
$\otimes$	$\bowtie$
$\otimes$	
×	
$\otimes$	DO NOT WRITE IN THIS AREA
$\otimes$	$\approx$
×	رپ
$\otimes$	
X	
$\propto$	$\bowtie$
$\bigotimes$	$\times\!\!\times\!\!\times$
X	>>>
$\langle \rangle$	$\times\!\!\times\!\!\times$
$\otimes$	$\times\!\!\times\!\!\times$
$\propto$	$\times\!\!\times\!\!\times$
$\otimes$	$\times\!\!\times\!\!\times$
$\otimes$	$\Longrightarrow$
$\otimes$	$\otimes\!$
×	$\times\!\!\times\!\!\times$
$\times$	$\times\!\!\times\!\!\times$
×	$\times\!\!\times\!\!\times$
$\otimes$	
$\otimes$	$\times\!\!\times\!\!\times$
$\otimes$	$\infty$
$\times$	
$\otimes$	ш
X	OC.
88	
×	
$\otimes$	S
$\otimes$	2
$\stackrel{\times}{\times}$	SE
	THIS
*	SEL I
*	NAMES
	*NTHIS
	EINTHIS
	TEXN THIS
	STEN THIS
	RITEANTHIS
	WRITE IN THIS
	WRITEINTHIS
	TWRITEINTHIS
	OT WRITE IN THIS
	NOT WRITE IN THIS
	NOT WRITE IN THIS
	O NOT WRITE IN THIS AREA
	SO NOT WRITE IN THIS
	DO NOT WRITE IN THIS
	00
	A DC
	AREA
	SAREA
	S AREA DC
	S AREA DC
	S AREA DC
	ITHIS AREA DC
	ITHIS AREA DC
	IN THIS AREA DC
	EIN THIS AREA DC
	TE IN THIS AREA
	HE IN THIS AREA
	HE IN THIS AREA
	HE IN THIS AREA
	RITE IN THIS AREA DO

Question 1 continued	
	Q1
(Total 5 marks)	



2.	A particle $P$ of mass 1.5 kg moves under the action of a single force $\mathbf{F}$ newtons.
	At time t seconds, $t \ge 0$ , P has velocity $\mathbf{v}  \mathbf{m}  \mathbf{s}^{-1}$ , where
	$\mathbf{v} = (5t^2 - t^3)\mathbf{i} + (2t^3 - 8t)\mathbf{j}$
	(a) Find <b>F</b> when $t = 2$
	(4)
	At time $t = 0$ , $P$ is at the origin $O$ .
	(b) Find the position vector of $P$ relative to $O$ at the instant when $P$ is moving in the direction of the vector $\mathbf{j}$
	(4)



	Question 2 continued	blank
Q2		02
(Total 8 marks)	(Total 8 marks)	



**3.** 

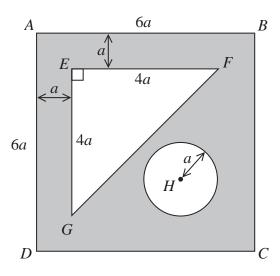


Figure 1

The uniform lamina ABCD is a square of side 6a. The template T, shown shaded in Figure 1, is formed by removing the right-angled triangle EFG and the circle, centre H and radius a, from the square lamina.

Triangle EFG has EF = EG = 4a, with EF parallel to AB and EG parallel to AD. The distance between AB and EF is a and the distance between AD and EG is a.

The point H lies on AC and the distance of H from BC is 2a.

(b) Find the value of k giving your engager to 2 decimal places

(a) Show that the centre of mass of 
$$T$$
 is a distance  $\frac{4(67 - 3\pi)}{3(28 - \pi)}a$  from  $AD$ .

The template T is suspended from the ceiling by two light inextensible vertical strings. One string is attached to T at A and the other string is attached to T at B so that T hangs in equilibrium with AB horizontal.

The weight of T is W. The tension in the string attached to T at B is kW, where k is a constant.

(0)	rind the value of k, giving your answer to 2 decimal places.	
		3)



	Leave
	blank
Question 3 continued	
<b>V W W W W W W W W W W</b>	



	Leave blank
Question 3 continued	
	Q3
(T-4-19 1 N	
(Total 8 marks)	



4.

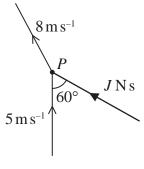


Figure 2

A particle P of mass 0.3 kg is moving with speed  $5\,\mathrm{m\,s^{-1}}$  along a straight line on a smooth horizontal plane. The particle receives a horizontal impulse of magnitude  $J\,\mathrm{N\,s}$ . The speed of P immediately after receiving the impulse is  $8\,\mathrm{m\,s^{-1}}$ . The angle between the direction of motion of P before it receives the impulse and the direction of the impulse is  $60^\circ$ , as shown in Figure 2.

Find the value of $J$ .	(6)

Question 4 continued	blank
<b>Q.1</b> 001011111111111111111111111111111111	
	Q4
(Total 6 marks)	



5.

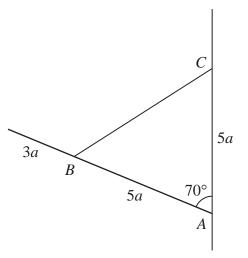


Figure 3

A uniform rod, of length 8a and mass M, has one end freely hinged to a fixed point A on a vertical wall. One end of a light inextensible string is attached to the rod at the point B, where AB = 5a. The other end of the string is attached to the wall at the point C, where AC = 5a and C is vertically above A. The rod rests in equilibrium in a vertical plane perpendicular to the wall with angle  $BAC = 70^{\circ}$ , as shown in Figure 3.

(a) Find, in terms of M and g, the tension in the string.

**(3)** 

The magnitude of the force acting on the rod at A is  $\lambda Mg$ , where  $\lambda$  is a constant.

(b) Find, to 2 significant figures, the value of  $\lambda$ .

**(6)** 

		ě			
					4
	/	۷.	4	۵	_
	1	۳		۴	٠
١		/			
	И				6
	6	à.			
					į
					è
	2	ę	7		è
	ζ	3	ě	þ	ì
	Š	į	Ē		
	ξ	Ì			
3	S				
	S				
>	S		2		>
>	3				
	3	ŀ	2		2
		ŀ	2		2
		ŀ			2
		ŀ	2		
		į	>		
		į	>		
		į	>		
		į	>		
?		į	>		
>					
>					
?					
<pre></pre>					
> > > >					
		į			

	Leave
	blank
Question 5 continued	




Question 5 continued	blank
	-
	-
	_
	_
	_
	-
	_
	-
	-
	-
	_
	_
	_
	_
	_
	_
	-
	-
	-
	-
	-
	_
	-
	-
	-
	Q5
(Total 9 marks)	
(=2.50.7 11.00.110)	



**6.** 

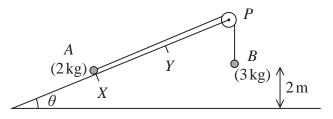


Figure 4

Two particles, A and B, of mass  $2 \log$  and  $3 \log$  respectively, are connected by a light inextensible string. Particle A is held at rest at the point X on a fixed rough ramp that is inclined at an angle  $\theta$  to the horizontal, where  $\tan \theta = \frac{5}{12}$ . The string passes over a small smooth pulley P that is fixed at the top of the ramp. Particle B hangs vertically below P,  $2 \mod$  above the ground, as shown in Figure 4.

The particles are released from rest with the string taut so that A moves up the ramp and the section of the string from A to P is parallel to a line of greatest slope of the ramp.

The coefficient of friction between A and the ramp is  $\frac{3}{8}$ 

Air resistance is ignored.

(a) Find the potential energy lost by the system as A moves 2 m up the ramp.

(b) Find the work done against friction as A moves 2 m up the ramp.

(4)

**(3)** 

When B hits the ground, B is brought to rest by the impact and does not rebound and A continues to move up the ramp.

(c) Use the work-energy principle to find the speed of B at the instant before it hits the ground.

**(4)** 

Particle A comes to instantaneous rest at the point Y on the ramp, where XY = (2 + d) m.

(d) Use the work-energy principle to find the value of d.

**(4)** 

	Leave
	blank
Question 6 continued	



Question 6 continued	

\$\$\$\$\$\$\$
****
*****
*****
*****
******
XX <del>XX</del> XX
000000
VA.
XX
$\times$
$\times$
8
0000000
0
۵
*****
*****
~~~~~
*****
*****
*****
~~~~~
XXXXX
X 62 X
XXXXX
<u> </u>
×2×
× <del>**</del> ×
<u> </u>
9
$\infty$
$\otimes \otimes \otimes \otimes$
~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~
A
EA
REA
VREA
AREA
S AREA
S AREA
HIS AREA
THIS AREA
THIS AREA
IN THIS AREA
EIN THIS AREA
TE IN THIS AREA
TE IN THIS AREA
RITE IN THIS AREA
WRITE IN THIS AREA
WRITE IN THIS AREA
T WRITE IN THIS AREA
WRITE IN THIS AREA
OT WRITE IN THIS AREA
IOT WRITE IN THIS AREA
O NOT WRITE IN THIS AREA
OO NOT WRITE IN THIS AREA
O NOT WRITE IN THIS AREA
OO NOT WRITE IN THIS AREA

Question 6 continued	blank
	Q6
(Total 15 marks)	
(Total 13 marks)	



7. [In this question, the unit vectors **i** and **j** are in a vertical plane, **i** being horizontal and **j** being vertically upwards.]

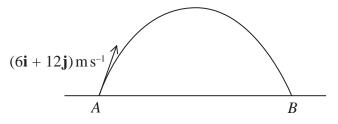


Figure 5

A small ball is projected with velocity  $(6\mathbf{i} + 12\mathbf{j}) \,\mathrm{m} \,\mathrm{s}^{-1}$  from a fixed point A on horizontal ground. The ball hits the ground at the point B, as shown in Figure 5. The motion of the ball is modelled as a particle moving freely under gravity.

(a) Find the distance AB.

**(4)** 

When the height of the ball above the ground is more than h metres, the speed of the ball is less than  $10\,\mathrm{m\,s^{-1}}$ 

(b) Find the smallest possible value of h.

**(4)** 

When the ball is at the point *C* on its path, the direction of motion of the ball is perpendicular to the direction of motion of the ball at the instant before it hits the ground at *B*.

(c) Find, in terms of  $\mathbf{i}$  and  $\mathbf{j}$ , the velocity of the ball when it is at C.

**(3)** 





	Leave
	blank
Question 7 continued	



	Leav
Question 7 continued	blan
Question / continued	
	-
	-
	_
	-
	-
	_
	-
	-
	-
	-
	-
	_
	-
	-
	_
	-
	-
	_
	-
	_
	_
	-
	-
	_
	-
	-
	-
	-
	_
	_
	-

Question 7 continued	
	(Total 11 marks



**8.** Particles *A*, *B* and *C*, of masses 2*m*, *m* and 3*m* respectively, lie at rest in a straight line on a smooth horizontal plane with *B* between *A* and *C*. Particle *A* is projected towards particle *B* with speed 2*u* and collides directly with *B*.

The coefficient of restitution between each pair of particles is e.

- (a) (i) Show that the speed of B immediately after the collision with A is  $\frac{4}{3}u(1+e)$ 
  - (ii) Find the speed of A immediately after the collision with B.

**(7)** 

At the instant when A collides with B, particle C is projected with speed u towards B so that B and C collide directly.

(b) Show that there will be a second collision between A and B.

	/			
1	17	h	. 1	


	Leave
	blank
Question 8 continued	



nestion 8 continued	

	blank
Question 8 continued	



Question 8 continued	Leave blank
	Q8
(Total 13 marks)	
TOTAL FOR PAPER: 75 MARKS END	