

Please check the examination details below before entering your candidate information

Candidate surname					Other names				
Centre Number					Candidate Number				

**Pearson Edexcel International Advanced Level**

**Friday 9 June 2023**

Afternoon (Time: 1 hour 30 minutes) **Paper reference** **WMA14/01**

**Mathematics**

**International Advanced Level**

**Pure Mathematics P4**

**You must have:**  
Mathematical Formulae and Statistical Tables (Yellow), calculator

Total Marks

**Candidates may use any calculator permitted by Pearson regulations. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.**

### Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B).
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer **all** questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided  
– *there may be more space than you need.*
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- Inexact answers should be given to three significant figures unless otherwise stated.

### Information

- A booklet 'Mathematical Formulae and Statistical Tables' is provided.
- There are 8 questions in this question paper. The total mark for this paper is 75.
- The marks for **each** question are shown in brackets  
– *use this as a guide as to how much time to spend on each question.*

### Advice

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.
- If you change your mind about an answer, cross it out and put your new answer and any working underneath.

Turn over ►

P74329A

©2023 Pearson Education Ltd.  
N:1/1/1/





**Question 1 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 1 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 1 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 1 is 9 marks)**

A Cartesian coordinate system with a horizontal x-axis and a vertical y-axis. The origin is labeled  $O$ . A closed curve, labeled  $C$ , is plotted. The curve is symmetric about the y-axis and has a cusp at the origin  $O$ . It extends into both the first and second quadrants. A point  $P$  is marked on the curve in the first quadrant.

Figure 1 shows a sketch of part of the curve  $C$  with equation

The point  $P$  lies on  $C$  and has  $x$  coordinate 2

- The tangent to  $C$  at  $P$  crosses the  $x$ -axis at the point  $Q$ .

- (c) Find the  $x$  coordinate of  $Q$ , giving your answer in the form  $\frac{a \ln 2 + b}{c \ln 2 + d}$  where  $a, b, c$  and  $d$  are integers to be found.
- (3)**

## Question 2 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 2 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA





**Question 2 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 2 is 10 marks)**

3. 
$$f(x) = \frac{8x - 5}{(2x - 1)(4x - 3)} \quad x > 1$$

(a) Express  $f(x)$  in partial fractions.

(3)

(b) Hence find  $\int f(x) dx$

(3)

(c) Use the answer to part (b) to find the value of  $k$  for which

$$\int_k^{3k} f(x) dx = \frac{1}{2} \ln 20$$

(5)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



## Question 3 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 7 4 3 2 9 A 0 1 1 3 2

**Question 3 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 3 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 3 is 11 marks)**

P 7 4 3 2 9 A 0 1 3 3 2

4. Relative to a fixed origin  $O$ ,
- the point  $A$  has position vector  $4\mathbf{i} + 8\mathbf{j} + \mathbf{k}$
  - the point  $B$  has position vector  $5\mathbf{i} + 6\mathbf{j} + 3\mathbf{k}$
  - the point  $P$  has position vector  $2\mathbf{i} - 2\mathbf{j} + \mathbf{k}$

The straight line  $l$  passes through  $A$  and  $B$ .

- (a) Find a vector equation for  $l$ .

(2)

The point  $C$  lies on  $l$  so that  $PC$  is perpendicular to  $l$ .

- (b) Find the coordinates of  $C$ .

(4)

The point  $P'$  is the reflection of  $P$  in the line  $l$ .

- (c) Find the coordinates of  $P'$

(2)

- (d) Hence find  $|\overrightarrow{PP'}|$ , giving your answer as a simplified surd.

(2)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



## This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



**Question 4 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA





**Question 4 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 4 is 10 marks)**

5. (i) Find

$$\int x^2 e^x dx$$

(4)

(ii) Use the substitution  $u = \sqrt{1 - 3x}$  to show that

$$\int \frac{27x}{\sqrt{1 - 3x}} dx = -2(1 - 3x)^{\frac{1}{2}}(Ax + B) + k$$

where  $A$  and  $B$  are integers to be found and  $k$  is an arbitrary constant.

(6)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



## Question 5 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 5 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 5 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 5 is 10 marks)**

P 7 4 3 2 9 A 0 2 1 3 2

6.

**In this question you must show all stages of your working.**

**Solutions relying entirely on calculator technology are not acceptable.**

The temperature,  $\theta^\circ\text{C}$ , of a car engine,  $t$  minutes after the engine is turned off, is modelled by the differential equation

$$\frac{d\theta}{dt} = -k(\theta - 15)^2$$

where  $k$  is a constant.

Given that the temperature of the car engine

- is  $85^\circ\text{C}$  at the instant the engine is turned off
- is  $40^\circ\text{C}$  exactly 10 minutes after the engine is turned off

(a) solve the differential equation to show that, according to the model

$$\theta = \frac{at + b}{ct + d}$$

where  $a$ ,  $b$ ,  $c$  and  $d$  are integers to be found.

(7)

(b) Hence find, according to the model, the time taken for the temperature of the car engine to reach  $20^\circ\text{C}$ . Give your answer to the nearest minute.

(2)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



## This image shows a single sheet of white paper with horizontal ruling lines. The lines are evenly spaced and run across the width of the page. There are no margins, text, or other markings on the paper.



**Question 6 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA





**Question 6 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 6 is 9 marks)**

P 7 4 3 2 9 A 0 2 5 3 2

7. Use proof by contradiction to prove that  $\sqrt{7}$  is irrational.

(You may assume that if  $k$  is an integer and  $k^2$  is a multiple of 7 then  $k$  is a multiple of 7) (4)

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 7 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 7 is 4 marks)**

8.

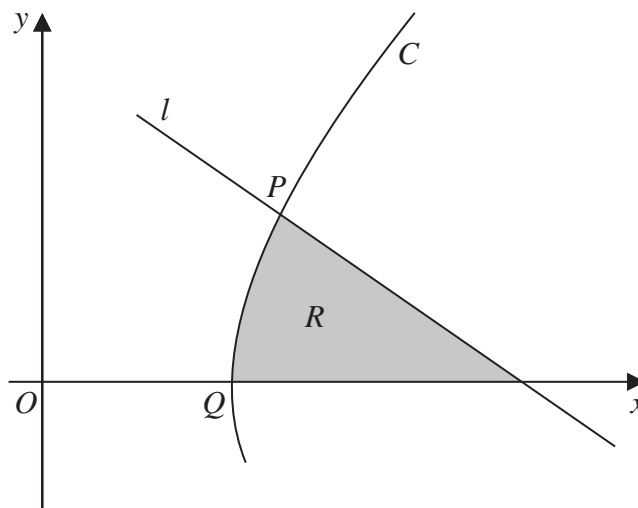


Figure 2

Figure 2 shows a sketch of part of the curve  $C$  with parametric equations

$$x = t + \frac{1}{t} \quad y = t - \frac{1}{t} \quad t > 0.7$$

The curve  $C$  intersects the  $x$ -axis at the point  $Q$ .

(a) Find the  $x$  coordinate of  $Q$ .

(1)

The line  $l$  is the normal to  $C$  at the point  $P$  as shown in Figure 2.

Given that  $t = 2$  at  $P$

(b) write down the coordinates of  $P$

(1)

(c) Using calculus, show that an equation of  $l$  is

$$3x + 5y = 15$$

(3)

The region,  $R$ , shown shaded in Figure 2 is bounded by the curve  $C$ , the line  $l$  and the  $x$ -axis.

(d) Using algebraic integration, find the exact volume of the solid of revolution formed when the region  $R$  is rotated through  $2\pi$  radians about the  $x$ -axis.

(7)



## Question 8 continued

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 7 4 3 2 9 A 0 2 9 3 2

**Question 8 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



**Question 8 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA



P 7 4 3 2 9 A 0 3 1 3 2

**Question 8 continued**

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

DO NOT WRITE IN THIS AREA

**(Total for Question 8 is 12 marks)****TOTAL FOR PAPER IS 75 MARKS**