Surname	Other na	mes
Pearson Edexcel GCE	Centre Number	Candidate Number
Further F Mathema		
Advanced/Advan		
	ced Subsidiary  Morning	Paper Reference <b>6669/01</b>

Candidates may use any calculator allowed by the regulations of the Joint Council for Qualifications. Calculators must not have the facility for symbolic algebra manipulation, differentiation and integration, or have retrievable mathematical formulae stored in them.

## Instructions

- Use **black** ink or ball-point pen.
- If pencil is used for diagrams/sketches/graphs it must be dark (HB or B). Coloured pencils and highlighter pens must not be used.
- **Fill in the boxes** at the top of this page with your name, centre number and candidate number.
- Answer all questions and ensure that your answers to parts of questions are clearly labelled.
- Answer the questions in the spaces provided
   there may be more space than you need.
- You should show sufficient working to make your methods clear. Answers without working may not gain full credit.
- When a calculator is used, the answer should be given to an appropriate degree of accuracy.

## Information

- The total mark for this paper is 75.
- The marks for each question are shown in brackets
   use this as a guide as to how much time to spend on each question.

## **Advice**

- Read each question carefully before you start to answer it.
- Try to answer every question.
- Check your answers if you have time at the end.

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1.  $(-2 \ 1 \ -3)$ nt

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$\mathbf{A} = \mathbf{A}$	k	1	3	, where $k$ is a constar
	2	-1	k	

Given that the matrix $A$ is singular, find the possible values of $k$ .				

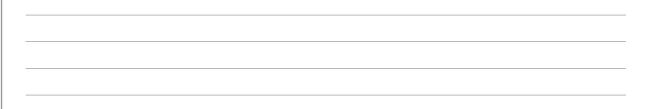


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**2.** The curve C has equation

$$y = \frac{x^2}{8} - \ln x, \quad 2 \leqslant x \leqslant 3$$

Find the length of the curve <i>C</i> giving you	r answer in	the form p	$\rho + \ln q$ ,	where $p$	and $q$	are
rational numbers to be found.						
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**3.** (a) Prove that

$$\frac{d(\operatorname{arcoth} x)}{dx} = \frac{1}{1 - x^2}$$

**(3)** 

Given that  $y = (\operatorname{arcoth} x)^2$ ,

(b) show that

$$(1 - x^2)\frac{d^2y}{dx^2} - 2x\frac{dy}{dx} = \frac{k}{1 - x^2}$$

where k is a constant to be determined.

**(5)** 

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Question 3 continued	
Question 5 continued	

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**4.** (i) Find, without using a calculator,

$$\int_{3}^{5} \frac{1}{\sqrt{15 + 2x - x^2}} \, \mathrm{d}x$$

giving your answer as a multiple of  $\pi$ .

**(5)** 

- (ii)
- (a) Show that

$$5\cosh x - 4\sinh x = \frac{e^{2x} + 9}{2e^x}$$

**(3)** 

(b) Hence, using the substitution  $u = e^x$  or otherwise, find

$$\int \frac{1}{5\cosh x - 4\sinh x} \, \mathrm{d}x$$

**(4)** 

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5. The hyperbola H has equation

$$\frac{x^2}{16} - \frac{y^2}{9} = 1$$

The point P (4 sec  $\theta$ , 3 tan  $\theta$ ),  $0 < \theta < \frac{\pi}{2}$ , lies on H.

(a) Show that an equation of the normal to H at the point P is

$$3y + 4x\sin\theta = 25\tan\theta$$

(5)

The line l is the directrix of H for which x > 0

The normal to H at P crosses the line l at the point Q. Given that  $\theta = \frac{\pi}{4}$ 

(b) find the y coordinate of Q, giving your answer in the form  $a + b\sqrt{2}$ , where a and b are rational numbers to be found.





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6.

$$\mathbf{M} = \begin{pmatrix} p & -2 & 0 \\ -2 & 6 & -2 \\ 0 & -2 & q \end{pmatrix}$$

where p and q are constants.

Given that  $\begin{pmatrix} 2 \\ -2 \\ 1 \end{pmatrix}$  is an eigenvector of the matrix **M**,

(a) find the eigenvalue corresponding to this eigenvector,

(3)

(b) find the value of p and the value of q.

**(3)** 

Given that 6 is another eigenvalue of M,

(c) find a corresponding eigenvector.

**(2)** 

Given that  $\begin{pmatrix} 1 \\ 2 \\ 2 \end{pmatrix}$  is a third eigenvector of **M** with eigenvalue 3

(d) find a matrix **P** and a diagonal matrix **D** such that

$$\mathbf{P}^{\mathrm{T}}\mathbf{M}\mathbf{P} = \mathbf{D}$$

(3)

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Question 6 continued	



$$I_n = \int \frac{\sin nx}{\sin x} \, \mathrm{d}x, \quad n \geqslant 1$$

(a) prove that, for  $n \ge 3$ 

$$I_n - I_{n-2} = \int 2\cos(n-1)x \,\mathrm{d}x$$

(b) Hence, showing each step of your working, find the exact value of

$$\int_{\frac{\pi}{12}}^{\frac{\pi}{6}} \frac{\sin 5x}{\sin x} \, \mathrm{d}x$$

giving your answer in the form  $\frac{1}{12}(a\pi + b\sqrt{3} + c)$ , where a, b and c are integers to be found.

**(7)** 

**(3)** 

**8.** The plane  $\Pi_1$  has equation

$$x - 5y - 2z = 3$$

The plane  $\Pi_2$  has equation

$$\mathbf{r} = \mathbf{i} + 2\mathbf{j} + \mathbf{k} + \lambda(\mathbf{i} + 4\mathbf{j} + 3\mathbf{k}) + \mu(2\mathbf{i} - \mathbf{j} + \mathbf{k})$$

where  $\lambda$  and  $\mu$  are scalar parameters.

(a) Show that  $\Pi_1$  is perpendicular to  $\Pi_2$ 

**(4)** 

(b) Find a cartesian equation for  $\Pi_2$ 

**(2)** 

(c) Find an equation for the line of intersection of  $\Pi_1$  and  $\Pi_2$  giving your answer in the form  $(\mathbf{r} - \mathbf{a}) \times \mathbf{b} = \mathbf{0}$ , where  $\mathbf{a}$  and  $\mathbf{b}$  are constant vectors to be found.

**(6)** 

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Question 8 continued	

