

Introduction to Supervised Learning

Machine Learning

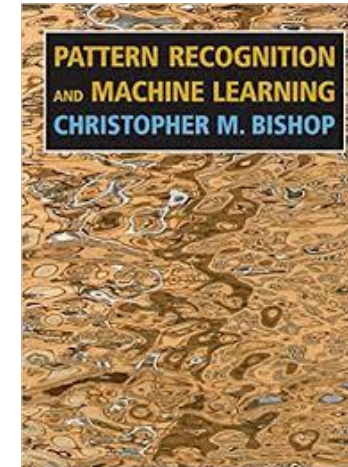
Daniele Loiacono



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References

- ❑ This slides are based on material of [prof. Marcello Restelli](#)
- ❑ *Pattern Recognition and Machine Learning*, Bishop
 - ▶ Chapter 1



What is supervised learning?

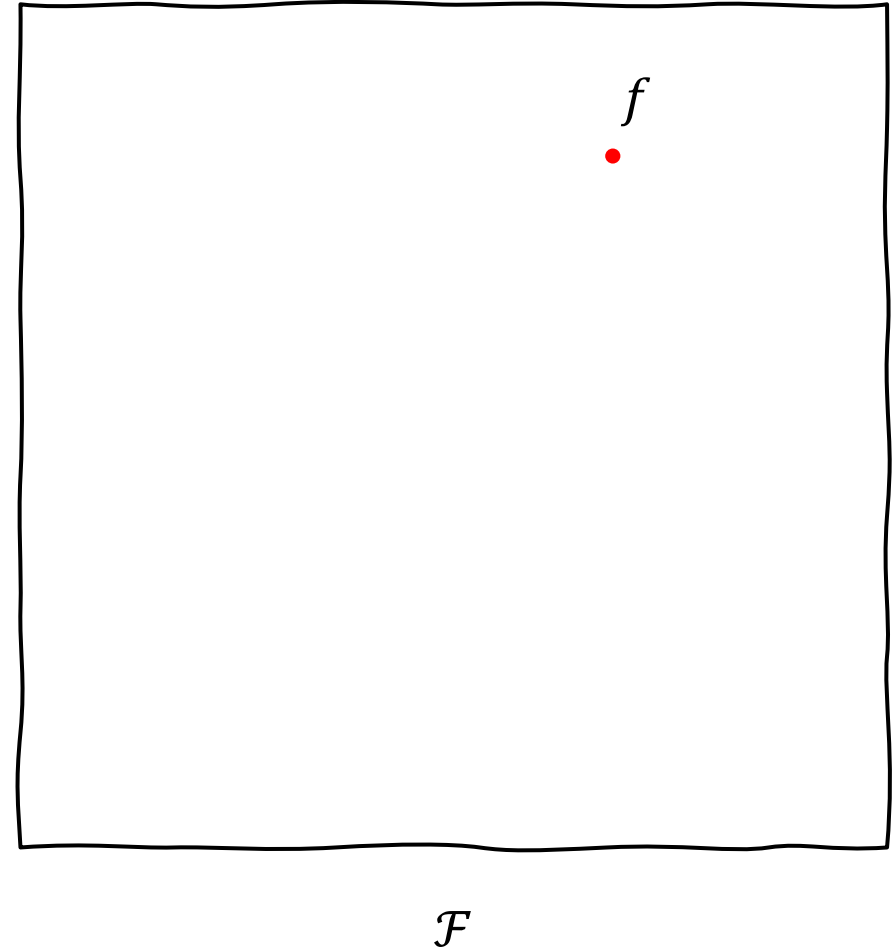
- ❑ It is the most popular and well established learning paradigm
- ❑ Data from an unknown function that maps an input x to an output t : $\mathcal{D} = \{\langle x, t \rangle\}$
- ❑ Goal: learn a good approximation of f
- ❑ Input variables x are usually called **features** or **attributes**
- ❑ Output variables t are also called **targets** or **labels**
- ❑ Tasks
 - ▶ **Classification** if t is discrete
 - ▶ **Regression** if t is continuous
 - ▶ **Probability estimation** if t is a probability

When to apply supervised learning?

- ❑ When human cannot perform the task
 - ▶ e.g., DNA analysis
- ❑ When human can perform the task but **cannot explain how**
 - ▶ e.g., medical image analysis
- ❑ When the task **changes over time**
 - ▶ e.g., stocks price prediction
- ❑ When the the task is **user-specific**
 - ▶ e.g., movie recommendation

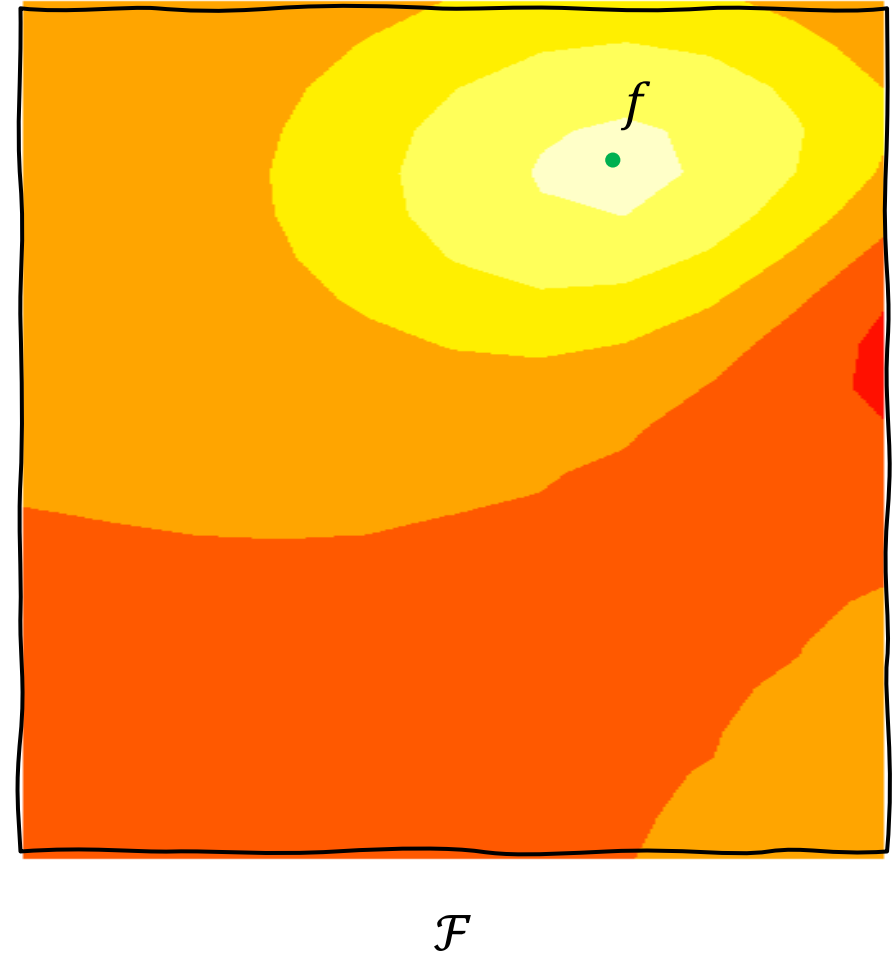
Overview of Supervised Learning

- We want to **approximate** a function f given a data set \mathcal{D}
- The steps are



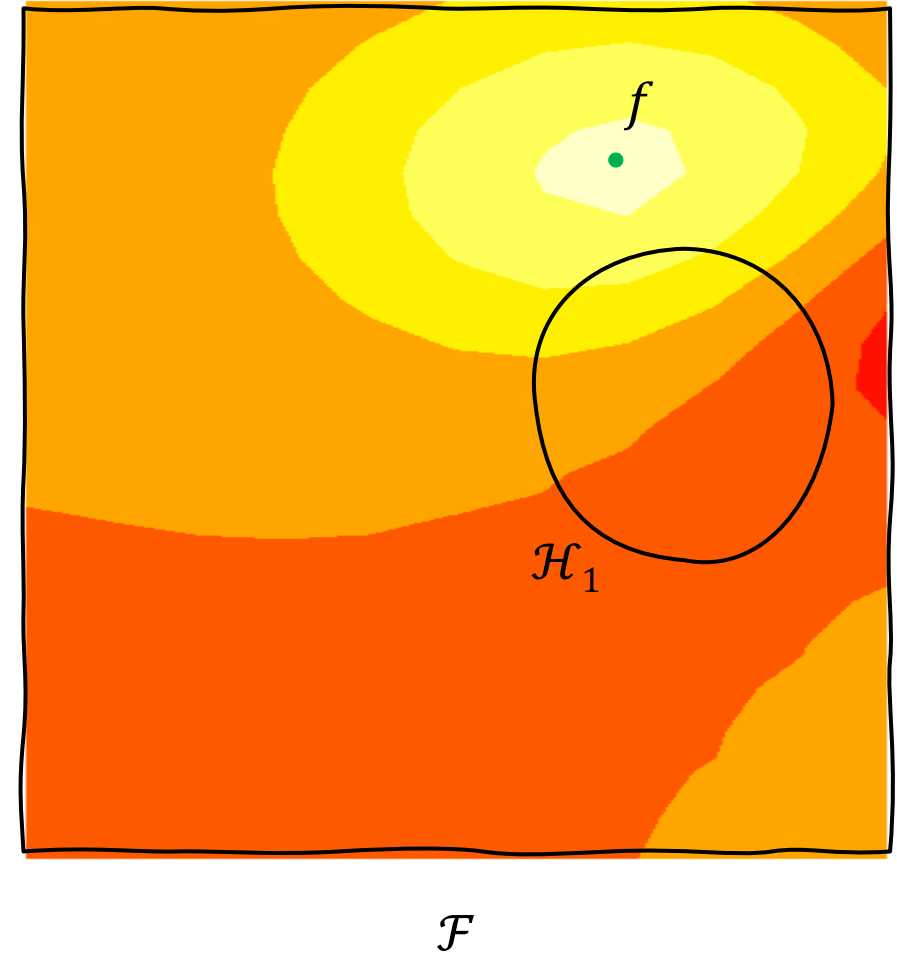
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 - ▶ Define a **loss function** \mathcal{L}



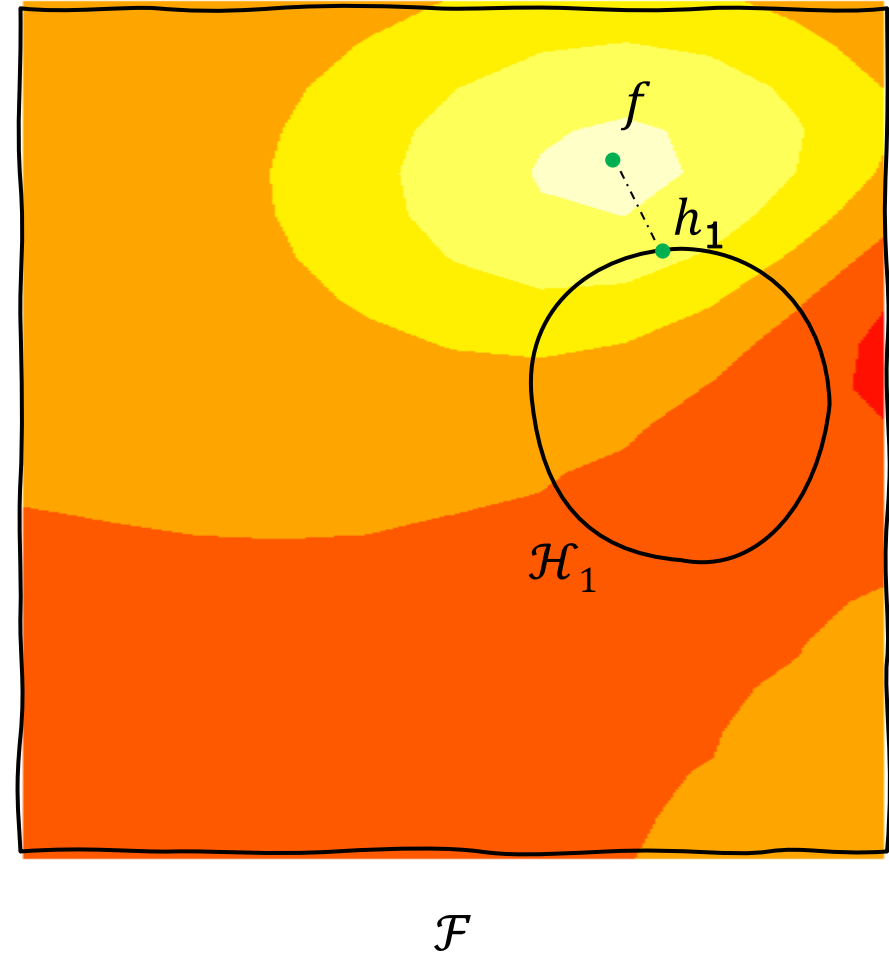
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 - ▶ Define a **loss function** \mathcal{L}
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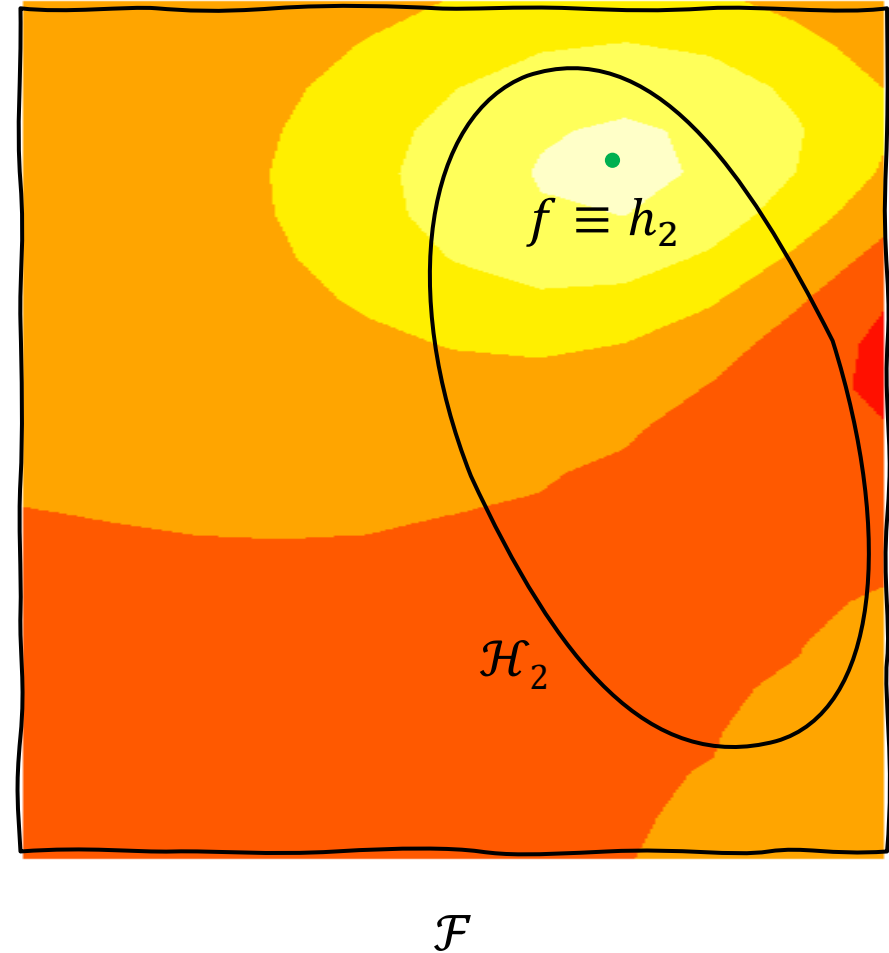
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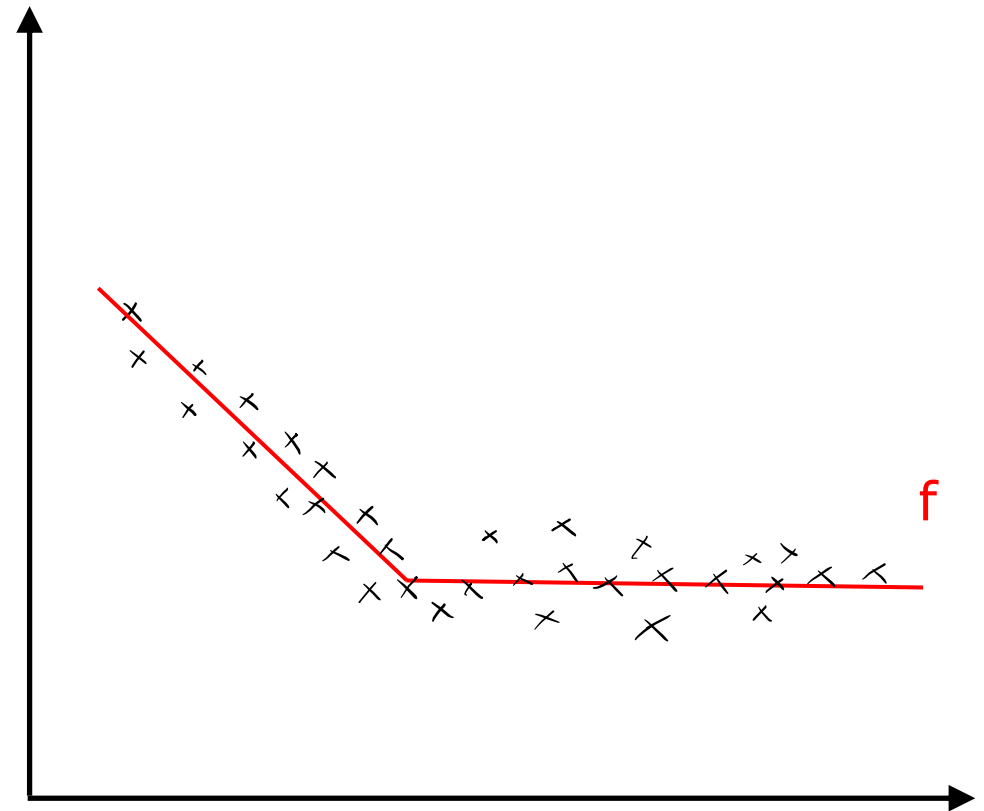
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- What if we enlarge the hypothesis space?
 - ▶ We can approximate f without error!



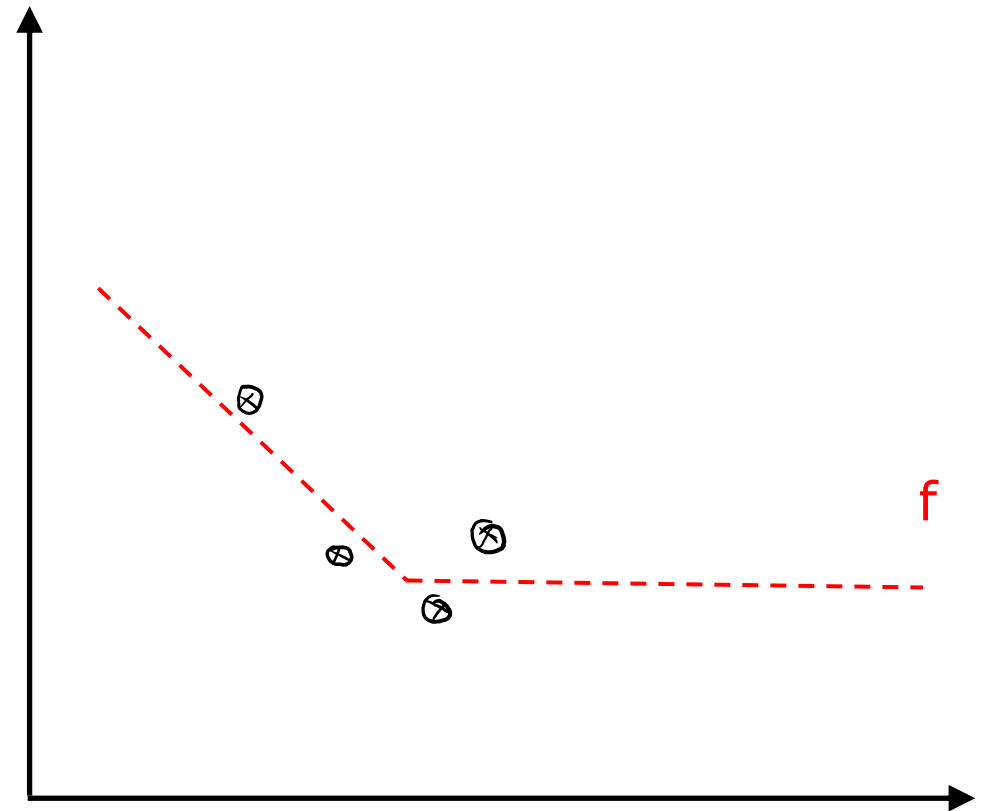
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 - ▶ We can approximate f without error!
 - ▶ But we don't know f !



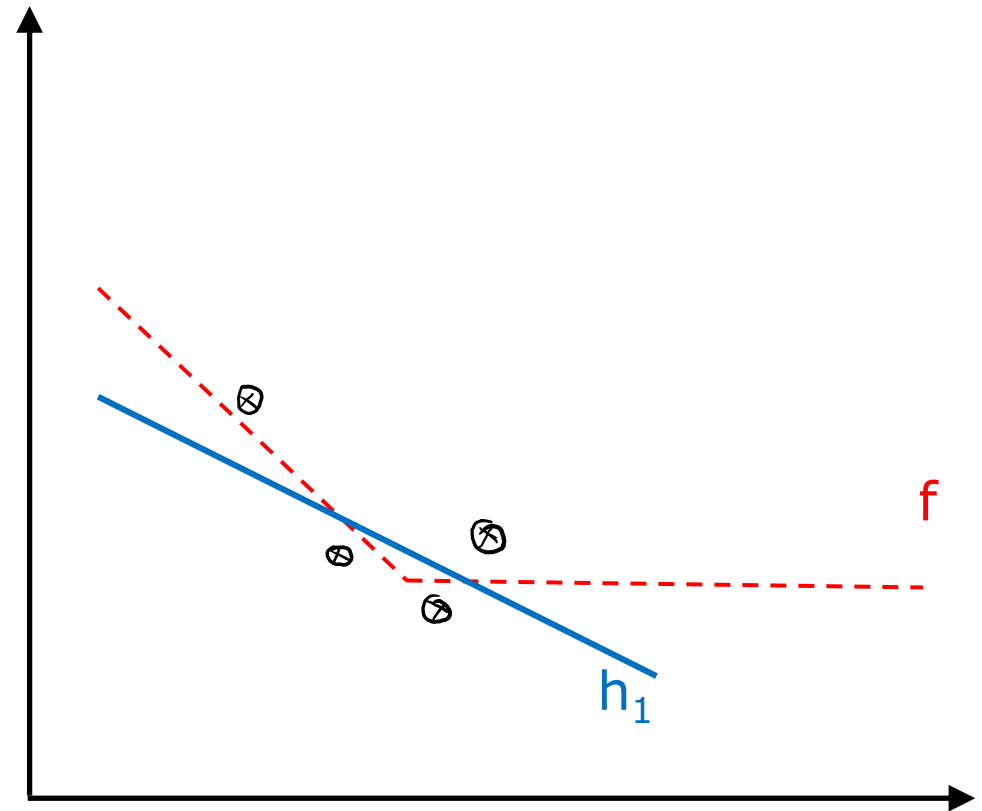
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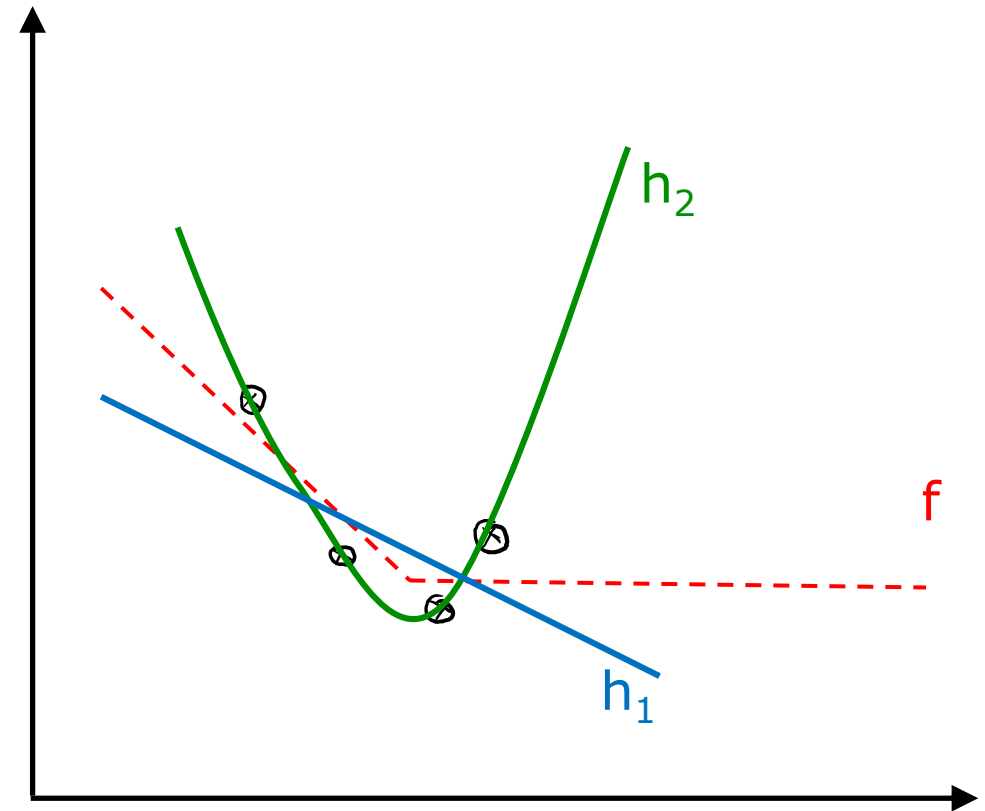
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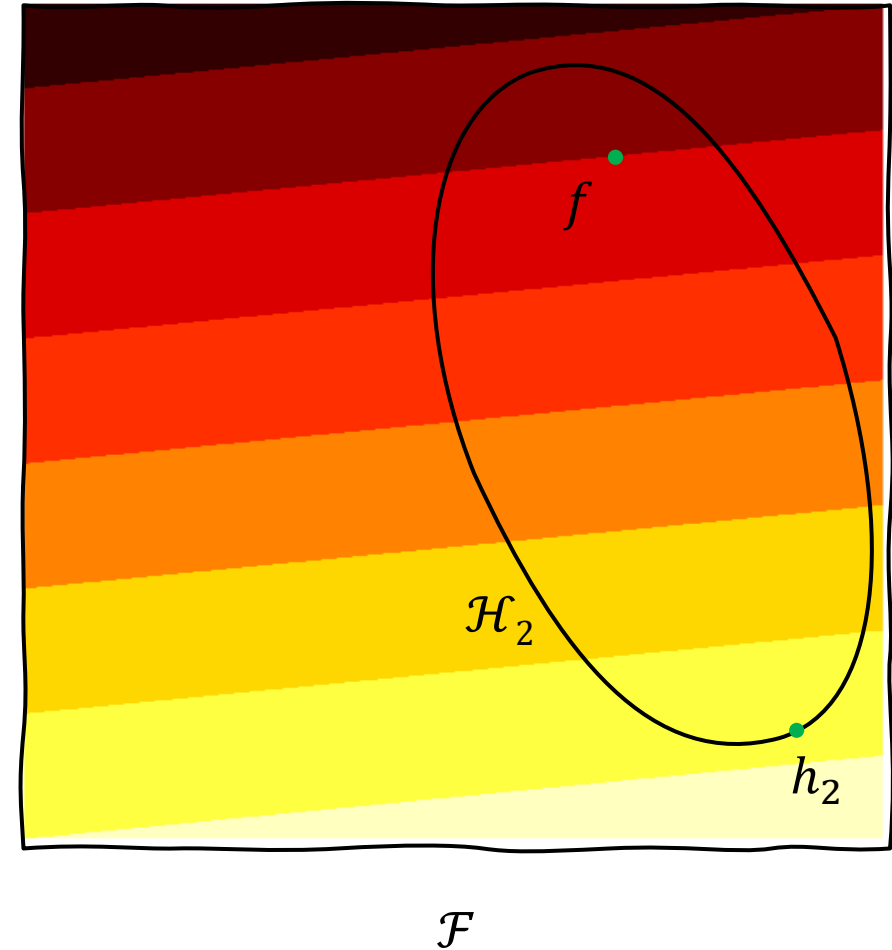
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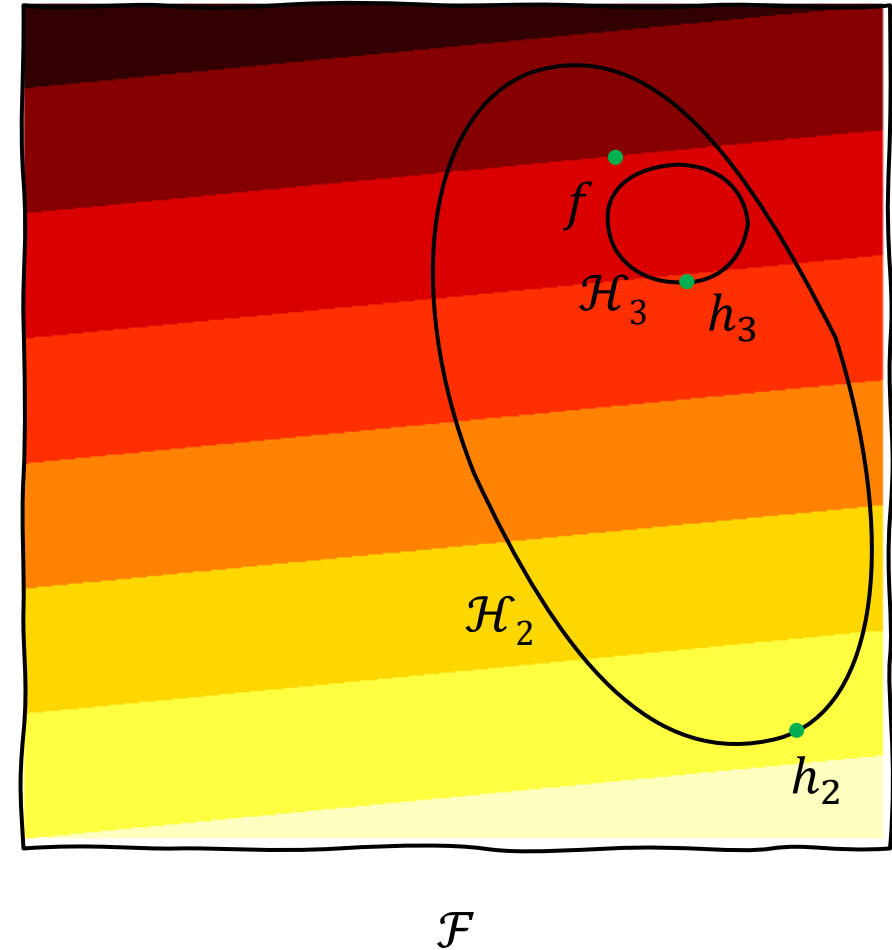
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Elements of Supervised Learning Algorithms

Representation

Evaluation

Optimization

Examples of representation

- ❑ Linear models
- ❑ Instance-based
- ❑ Decision trees
- ❑ Set of rules
- ❑ Graphical models
- ❑ Neural networks
- ❑ Gaussian Processes
- ❑ Support vector machines
- ❑ Model ensembles
- ❑ etc.

Examples of evaluation

- ❑ Accuracy
- ❑ Precision and recall
- ❑ Squared Error
- ❑ Likelihood
- ❑ Posterior probability
- ❑ Cost/Utility
- ❑ Margin
- ❑ Entropy
- ❑ KL divergence
- ❑ etc.

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Examples of optimization

- ❑ Combinatorial optimization
 - ▶ e.g.: Greedy search
- ❑ Convex optimization
 - ▶ e.g.: Gradient descent
- ❑ Constrained optimization
 - ▶ e.g.: Linear programming

A Supervised Learning Taxonomy

- ❑ Parametric vs Nonparametric
 - ▶ Parametric: **fixed and finite** number of parameters
 - ▶ Nonparametric: the number of parameters **depends on the training set**
- ❑ Frequentist vs Bayesian
 - ▶ Frequentist: use probabilities to model the **sampling** process
 - ▶ Bayesian: use probability to **model uncertainty** about the estimate
- ❑ Empirical Risk Minimization vs Structural Risk Minimization
 - ▶ Empirical Risk: Error over the **training set**
 - ▶ Structural Risk: Balance training error with **model complexity**
- ❑ Direct vs Generative vs Discriminative
 - ▶ Generative: Learns the **joint** probability distribution $p(x, t)$
 - ▶ Discriminative: Learns the **conditional** probability distribution $p(t|x)$

Direct, Discriminative, or Generative

- Our goal, is learn from **data** a **function** that maps **inputs** to **outputs**

$$\mathcal{D} = \{\langle x, t \rangle\} \Rightarrow t = f(x)$$

- **Direct approach**

- ▶ Learn directly an approximation of f from \mathcal{D}

- **Discriminative approach**

- ▶ Model **conditional density** $p(t|x)$
- ▶ Marginalize to find **conditional mean** $\mathbb{E}[t|x] = \int t \cdot p(t|x) dt$

- **Generative approach**

- ▶ Model **joint density** $p(x, t)$
- ▶ Infer **conditional density** $p(t|x)$
- ▶ Marginalize to find **conditional mean** $\mathbb{E}[t|x] = \int t \cdot p(t|x) dt$