Assignment 3 FML

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knitr::opts chunk\$set(echo = TRUE)

Summary

1:-According to the given dataset, if an accident has just been reported and no further information is available, there is a 50.88% chance that the injury has taken place, because data suggests that previously out of 42,183 cases, 21,462 cases have reported "injury=yes".

2.1: The exact Bayes conditional probabilities of an injury (INJURY = Yes) for the six possible combinations of the predictons are:

Predictor combination Probability WEATHER_R = 1 and TRAF_CON_R = 1 0.6666667 WEATHER_R = 2 and TRAF_CON_R = 0 0.1818182 WEATHER_R = 1 and TRAF_CON_R = 1 0.0000000 WEATHER_R = 2 and TRAF_CON_R = 1 0.0000000 WEATHER_R = 1 and TRAF_CON_R = 2 0.0000000 WEATHER_R = 2 and TRAF_CON_R = 2 1.00000000 2.2: The Classification of the 24 accidents using their probabilities and a cutoff of 0.5 quantitatively are:

[0.6666667 0.1818182 0.0000000 0.0000000 0.6666667 0.1818182 0.1818182 0.6666667 0.1818182 0.1818182 0.0000000 0.6666667 0.6666667 0.6666667 0.6666667 0.1818182 0.1818182 0.1818182 0.1818182 0.1818182 0.6666667 0.6666667 1.0000000 0.1818182]

qualitatively are:

- 2.3: The Computation of the naive Bayes conditional probability of an injury given WEATHER_R = 1 and TRAF_CON_R = 1 manually the output is "0".
- 2.4: Now, after applying the naïve Bayes classifier to the 24 records and two predictors, checking the model output to get probabilities and classifications for all 24 records, it was identified that the result of classification and ranks were not equal as the Exact Bayes caluclation.
- 3.1: When we applied the naive Bayes classifier to the full training set with the key predictors and used "INJURY" as the response, the results shows us confusion matrix and statistics. The accuracy of the model turned out to be 53.7%. This tells us

that the model predicts whether an accident causes injury or not.

Confusion Matrix and Statistics

Reference

Prediction no yes no 3444 4866 yes 2947 5617

Accuracy: 0.537

3.2: the overall error of the validation set is "46.3".

Problem Statement

The file accidentsFull.csv contains information on 42,183 actual automobile accidents in 2001 in the United States that involved one of three levels of injury: NO INJURY, INJURY, or FATALITY. For each accident, additional information is recorded, such as day of week, weather conditions, and road type. A firm might be interested in developing a system for quickly classifying the severity of an accident based on initial reports and associated data in the system (some of which rely on GPS-assisted reporting).

Our aim is to predict whether an accident just reported will involve an injury (MAX_SEV_IR = 1 or 2) or will not (MAX_SEV_IR = 0). For this purpose, create a dummy variable called INJURY that takes the value "yes" if MAX_SEV_IR = 1 or 2, and otherwise "no."

Data Input and Cleaning

Loading the required libraries and reading the input file

library(e1071)
library(caret)

Loading required package: ggplot2

Loading required package: lattice

library(ggplot2)

Q1. Using the information in this dataset, if an accident has just been reported and no further information is available, what should the prediction be? (INJURY = Yes or No?) Why?

```
accidents_24 <- read.csv("/Users/sudarshan/Desktop/FML/dataset/accidentsFull.csv")
accidents_24$INJURY = ifelse(accidents_24$MAX_SEV_IR>0,"yes","no")
injury_table <- table(accidents_24$INJURY)
injury_table</pre>
```

```
## no yes
## 20721 21462
```

head(accidents_24)

```
##
      HOUR I R ALCHL I ALIGN I STRATUM R WRK ZONE WKDY I R INT HWY LGTCON I R
## 1
               0
                         2
                                    2
                                                            0
                                                                        1
                                                 1
                                                                                  0
                                                                                                3
##
               1
                         2
                                    1
                                                 0
                                                            0
                                                                                  1
                                                                                                3
##
               1
                         2
                                    1
                                                 0
                                                            0
                                                                        1
                                                                                  0
   3
                                                                                                3
                         2
##
               1
                                    1
                                                 1
                                                            0
                                                                        0
                                                                                  0
                                                                                                3
##
   5
               1
                         1
                                    1
                                                 0
                                                            0
                                                                        1
                                                                                  0
                                                                                                3
                         2
                                    1
                                                                                                3
##
               1
                                                 1
                                                            0
                                                                        1
                                                                                  0
##
      MANCOL I R PED ACC R RELJCT I R REL RWY R PROFIL I R SPD LIM SUR COND
                  0
                              0
                                             1
                                                          0
                                                                        1
##
                                                                                 40
   1
                  2
                              0
                                             1
                                                          1
                                                                        1
                                                                                 70
##
   2
##
                  2
                                             1
                                                          1
                                                                        1
                                                                                 35
   3
                              0
##
                  2
                              0
                                             1
                                                          1
                                                                                 35
                  2
                                             0
                                                                        1
                              0
                                                          1
                                                                                 25
##
   5
                                                                                              4
##
                  0
                              0
                                             1
                                                          0
                                                                        1
                                                                                 70
##
      TRAF CON R TRAF WAY VEH INVL WEATHER R INJURY CRASH NO INJ I PRPTYDMG CRASH
##
                             3
                                         1
                                                      1
                                                                      1
                                                                                                      0
##
   2
                  0
                             3
                                         2
                                                      2
                                                                      0
                                                                                  0
                                                                                                     1
                             2
##
   3
                  1
                                         2
                                                      2
                                                                      0
                                                                                  0
                                                                                                     1
##
                  1
                             2
                                         2
                                                      1
                                                                      0
                                                                                  0
                                                                                                      1
                             2
                  0
                                         3
                                                      1
##
   5
                                                                      0
                                                                                  0
                                                                                                      1
                             2
                                                      2
##
   6
                  0
                                         1
                                                                      1
                                                                                  1
                                                                                                      0
##
      FATALITIES
                   MAX SEV IR INJURY
##
   1
                  0
                                1
                                      yes
##
   2
                  0
                                0
                                        no
##
                  0
                                0
                                       no
##
                  0
                                0
                                       no
##
   5
                  0
                                0
                                       no
## 6
                  0
                                1
                                      yes
```

```
probability_injury <- (injury_table["yes"] / sum(injury_table))*100
probability_injury</pre>
```

```
## yes
## 50.87832
```

```
#Converting variables into factor
for (i in c(1:dim(accidents_24)[2])){
   accidents_24[,i] <- as.factor(accidents_24[,i])
}
head(accidents_24,n=24)</pre>
```

```
##
      HOUR I R ALCHL I ALIGN I STRATUM R WRK ZONE WKDY I R INT HWY LGTCON I R
## 1
               0
                        2
                                 2
                                             1
                                                        0
                                                                  1
                                                                           0
                                                                                        3
##
   2
               1
                        2
                                 1
                                             0
                                                        0
                                                                  1
                                                                           1
                                                                                        3
```

	##	3	1	2	1	0	0 1	0	3
								_	
	##		1	2	1	1	0 0	0	3
	##	5	1	1	1	0	0 1	0	3
	##	6	1	2	1	1	0 1	0	3
	##	7	1	2	1	0	0 1	1	3
	##	8	1	2	1	1	0 1	0	3
	##	a	1	2	1	1	0 1	0	3
								0	
	##	10	0	2	1	0	0 0	0	3
	##	11	1	2	1	0	0 1	0	3
	##		1		1			0	
			1	2	1	1	0 1	0	3
	##	13	1	2	1	1	0 1	0	3
	##	14	1	2	2	0	0 1	0	3
								0	
	##		1	2	2	1	0 1	0	3
	##	16	1	2	2	1	0 1	0	3
	##	17	1	2	1	1	0 1	0	3
								_	
	##	18	1	2	1	1	0 0	0	3
	##	19	1	2	1	1	0 1	0	3
	##	20	1	2	1	0	0 1	0	3
	##	21	1	2	1	1	0 1	0	3
	##	22	1	2	2	0	0 1	0	3
	##	23	1	2	1	0	0 1	0	3
								0	
	##	24	1	2	1	1	0 1	9	3
	##		MANCOL_I_R	PED_ACC_R	RELJCT_I_R	REL RWY R	PROFIL_I_R	SPD_LIM	SUR_COND
- 1									_
Н	##	1	0	()	1	0	1	4 0	4
	##		0	0	1	0	1	40	4
	## ##		0	0	1	0 1	1 1	40 70	4 4
		2	-						
	## ##	2	2	0	1	1	1 1	70 35	4
	## ## ##	2 3 4	2 2 2	0 0	1 1	1 1	1 1 1	70 35 35	4 4 4
	## ##	2 3 4	2	0	1	1	1 1	70 35	4
	## ## ##	2 3 4 5	2 2 2	0 0	1 1	1 1	1 1 1	70 35 35	4 4 4
	## ## ## ##	2 3 4 5 6	2 2 2 0	0 0 0 0	1 1 1 0	1 1 1 0	1 1 1 1	70 35 35 25 70	4 4 4
	## ## ## ## ##	2 3 4 5 6 7	2 2 2 2 0 0	0 0 0 0 0	1 1 1 0 1	1 1 1 0 0	1 1 1 1 1	70 35 35 25 70 70	4 4 4
	## ## ## ## ##	2 3 4 5 6 7 8	2 2 2 0	0 0 0 0	1 1 1 0	1 1 1 0	1 1 1 1	70 35 35 25 70	4 4 4
	## ## ## ## ##	2 3 4 5 6 7 8	2 2 2 2 0 0	0 0 0 0 0	1 1 1 0 1	1 1 1 0 0	1 1 1 1 1	70 35 35 25 70 70	4 4 4
	## ## ## ## ## ##	2 3 4 5 6 7 8 9	2 2 2 2 0 0 0	0 0 0 0 0 0 0	1 1 0 1 0 0	1 1 1 0 0 0 0	1 1 1 1 1 1 1	70 35 35 25 70 70 35 30	4 4 4 4 4 4
	## ## ## ## ## ##	2 3 4 5 6 7 8 9	2 2 2 2 0 0 0 0	0 0 0 0 0 0 0	1 1 0 1 0 0 0 1 1	1 1 1 0 0 0 0	1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25	4 4 4 4 4 4
	######################################	2 3 4 5 6 7 8 9 10	2 2 2 2 0 0 0	0 0 0 0 0 0 0	1 1 0 1 0 0	1 1 1 0 0 0 0	1 1 1 1 1 1 1	70 35 35 25 70 70 35 30	4 4 4 4 4 4
	## ## ## ## ## ##	2 3 4 5 6 7 8 9 10	2 2 2 2 0 0 0 0	0 0 0 0 0 0 0	1 1 0 1 0 0 0 1 1	1 1 1 0 0 0 0	1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25	4 4 4 4 4 4
	######################################	2 3 4 5 6 7 8 9 10 11 12	2 2 2 2 0 0 0 0 0 0	0 0 0 0 0 0 0 0	1 1 0 1 0 0 0 1 1 1 0	1 1 1 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40	4 4 4 4 4 4 4 4
	##############	2 3 4 5 6 7 8 9 10 11 12 13	2 2 2 2 0 0 0 0 0 0 0 2 1	0 0 0 0 0 0 0 0	1 1 0 1 0 0 1 1 1 0 0	1 1 1 0 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40	4 4 4 4 4 4 4 4
	######################################	2 3 4 5 6 7 8 9 10 11 12 13	2 2 2 2 0 0 0 0 0 0	0 0 0 0 0 0 0 0	1 1 0 1 0 0 0 1 1 1 0	1 1 1 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40	4 4 4 4 4 4 4 4
	################	2 3 4 5 6 7 8 9 10 11 12 13	2 2 2 2 0 0 0 0 0 0 0 2 1	0 0 0 0 0 0 0 0	1 1 0 1 0 0 1 1 1 0 0	1 1 1 0 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25	4 4 4 4 4 4 4 4
	##################	2 3 4 5 6 7 8 9 10 11 12 13 14	2 2 2 2 0 0 0 0 0 0 0 0 2 1 0 0	0 0 0 0 0 0 0 0 0 0	1 1 0 1 0 0 0 1 1 1 0 0 0 0	1 1 1 0 0 0 0 0 0 1 1 1 0	1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35	4 4 4 4 4 4 4 4 4
	#####################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16	2 2 2 2 0 0 0 0 0 0 0 0 2 1 0 0	0 0 0 0 0 0 0 0 0 0 0	1 1 0 0 1 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 0 1 1 1 0 0	1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45	4 4 4 4 4 4 4 4 4 4
	#######################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17	2 2 2 2 0 0 0 0 0 0 0 0 2 1 0 0	0 0 0 0 0 0 0 0 0 0	1 1 0 1 0 0 0 1 1 1 0 0 0 0	1 1 1 0 0 0 0 0 0 1 1 1 0	1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20	4 4 4 4 4 4 4 4 4
	#####################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17	2 2 2 2 0 0 0 0 0 0 0 0 2 1 0 0	0 0 0 0 0 0 0 0 0 0 0	1 1 0 0 1 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 0 1 1 1 0 0	1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45	4 4 4 4 4 4 4 4 4 4
	#######################################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17	2 2 2 2 0 0 0 0 0 0 0 2 1 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	1 1 0 1 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 1 1 1 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20 50	4 4 4 4 4 4 4 4 4 4 4
	##############################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	2 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	1 1 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20 50	4 4 4 4 4 4 4 4 4 4 4 4
	######################################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	2 2 2 2 0 0 0 0 0 0 0 2 1 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0	1 1 0 1 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 1 1 1 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20 50 55	4 4 4 4 4 4 4 4 4 4 4
	##############################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	2 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0	1 1 0 0 1 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20 50	4 4 4 4 4 4 4 4 4 4 4 4
	######################################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21	2 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 1 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20 50 55 45	4 4 4 4 4 4 4 4 4 4 4 4 4
	######################################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22	2 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 1 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20 50 55 45 65	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
	#######################################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23	2 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 1 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20 50 55 45	4 4 4 4 4 4 4 4 4 4 4 4 4
	######################################	2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23	2 2 2 2 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 1 0 0 0 0 1 1 1 0 0 0 0 0 0 0 0 0 0 0	1 1 1 0 0 0 0 0 0 0 1 1 1 0 0 0 0 0 0 0	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	70 35 35 25 70 70 35 30 25 55 40 40 25 35 45 20 50 55 45 65	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4

##	TRAF_CON	I_R	TRAF_WAY	VEH_INVL	WEATHER_R	INJURY_CRASH	NO_INJ_I	PRPTYDMG_CRASH
## 1	1	0	3	1	1	1	1	(
## 2	2	0	3	2	2	0	0	1
## 3	3	1	2	2	2	0	0	·
## 4	4	1	2	2	1	0	0	
## 5	5	0	2	3	1	0	0	
## 6	6	0	2	1	2	1	1	(
## 7	7	0	2	1	2	0	0	
## 8	8	0	1	1	1	1	1	(
## 9		0	1	1	2	0	0	:
## 1		0	1	1		0	0	:
## 1		0	1	1		0	0	:
## 1		2	1	2		0	0	·
## 1		0	1	4	1	1	2	(
## 1		0	1	1		0	0	
## 1		0	1	1		1	1	
## 1		0	1	1		1	1	
## 1		0	1	1		0	0	
## 1		0	1	1		0	0	
## 1		0	1	1		0	0	
## 2		0	1	1	2	0	0	
## 2		0	3	1	1	1	1	
## 2		0	3	1	1	0	0	
## 2		2	2	1	2	1	2	
## 2		0	2	2		1	1	,
## 2			MAX_SEV_			1	1	·
## 1		0	MAX_SEV					
## 2		0		-				
## 2								
		0		0 no				
## 4		0		0 no				
## 5		0		0 no				
## 6		0		1 yes				
## 7		0		0 no				
## 8		0		1 yes				
## 9		0		0 no				
## 1		0		0 no				
## 1		0		0 no				
## 1		0		0 no				
## 1		0		1 yes				
## 1		0		0 no				
## 1		0		1 yes				
## 1		0		1 yes				
## 1		0		0 no				
## 1		0		0 no				
## 1		0		0 no				
## 2	20	0		0 no				
## 2	21	0		1 yes				

```
## 22 0 0 no
## 23 0 1 yes
## 24 0 1 yes
```

Q2. Select the first 24 records in the dataset and look only at the response (INJURY) and the two predictors WEATHER_R and TRAF_CON_R. Create a pivot table that examines INJURY as a function of the two predictors for these 12 records. Use all three variables in the pivot table as rows/columns.

```
accidents_24_Df <- accidents_24[1:24,c("INJURY","WEATHER_R","TRAF_CON_R")] head(accidents_24_Df)
```

```
##
     INJURY WEATHER R TRAF CON R
## 1
        yes
## 2
                      2
                                   1
## 3
          no
         no
                      1
## 5
                      1
                                   0
         no
## 6
        yes
```

```
Pt1 <- ftable(accidents_24_Df)
Pt2 <- ftable(accidents_24_Df[,-1]) # print table only for conditions
Pt1
```

Pt2

```
## TRAF_CON_R 0 1 2
## WEATHER_R
## 1 9 1 1
## 2 11 1 1
```

2.1:- Compute the exact Bayes conditional probabilities of an injury (INJURY = Yes) given the six possible combinations of the predictors.

```
#Injury = yes
p1 = Pt1[3,1] / Pt2[1,1] # Injury, Weather=1 and Traf=0
p2 = Pt1[4,1] / Pt2[2,1] # Injury, Weather=2, Traf=0
p3 = Pt1[3,2] / Pt2[1,2] # Injury, W=1, T=1
p4 = Pt1[4,2] / Pt2[2,2] # I, W=2,T=1
p5 = Pt1[3,3] / Pt2[1,3] # I, W=1,T=2
p6 = Pt1[4,3]/ Pt2[2,3] #I,W=2,T=2

# Injury = no
n1 = Pt1[1,1] / Pt2[1,1] # Weather=1 and Traf=0
n2 = Pt1[2,1] / Pt2[2,1] # Weather=2, Traf=0
n3 = Pt1[1,2] / Pt2[1,2] # W=1, T=1
n4 = Pt1[2,2] / Pt2[2,2] # W=2,T=1
n5 = Pt1[1,3] / Pt2[1,3] # W=1,T=2
n6 = Pt1[2,3] / Pt2[2,3] # W=2,T=2
print(c(p1,p2,p3,p4,p5,p6))
```

```
## [1] 0.6666667 0.1818182 0.0000000 0.0000000 1.0000000
```

```
print(c(n1,n2,n3,n4,n5,n6))
```

```
## [1] 0.3333333 0.8181818 1.0000000 1.0000000 0.0000000
```

2.2:-Classify the 24 accidents using these

probabilities and a cutoff of 0.5.

```
prob.inj \leftarrow rep(0,24)
for (i in 1:24) {
  print(c(accidents 24 Df$WEATHER R[i], accidents 24 Df$TRAF CON R[i]))
    if (accidents 24 Df$WEATHER R[i] == "1") {
      if (accidents_24_Df$TRAF_CON_R[i]=="0"){
        prob.inj[i] = p1
      }
      else if (accidents_24_Df$TRAF_CON_R[i]=="1") {
        prob.inj[i] = p3
      }
      else if (accidents_24_Df$TRAF_CON_R[i]=="2") {
        prob.inj[i] = p5
      }
      if (accidents_24_Df$TRAF_CON_R[i]=="0"){
        prob.inj[i] = p2
      else if (accidents_24_Df$TRAF_CON_R[i]=="1") {
        prob.inj[i] = p4
      else if (accidents 24 Df$TRAF CON R[i]=="2") {
        prob.inj[i] = p6
      }
    }
  }
```

```
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 1
## Levels: 1 2 0
## [1] 1 1
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 0
```

```
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 2
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 1 0
## Levels: 1 2 0
## [1] 2 2
## Levels: 1 2 0
## [1] 2 0
## Levels: 1 2 0
```

```
accidents_24_Df$prob.inj <- prob.inj
accidents_24_Df$prob.inj</pre>
```

```
## [1] 0.6666667 0.1818182 0.0000000 0.0000000 0.6666667 0.1818182 0.1818182 
## [8] 0.6666667 0.1818182 0.1818182 0.1818182 0.0000000 0.6666667 0.6666667 
## [15] 0.6666667 0.6666667 0.1818182 0.1818182 0.1818182 0.1818182 0.6666667 
## [22] 0.6666667 1.0000000 0.1818182
```

```
accidents_24_Df$pred.prob <- ifelse(accidents_24_Df$prob.inj>0.5, "yes", "no")
accidents_24_Df$pred.prob
```

2.3Compute manually the naive Bayes conditional probability of an injury given WEATHER_R = 1 and TRAF_CON_R = 1.

Answer:- Probability(Injury=Yes/WEATHER_R=1,TRAF_CON_R=1)

```
= [ Probability(W=1/Injury=Yes) * Probability(TRAF_CON_R=1/Injury=Yes) * Probability(Injury=Yes) ] / [ Probability(W=1/Injury=Yes) * Probability(TRAF_CON_R=1/Injury=Yes) * Probability(Injury=Yes) + Probability(WEATHER_R=1/Injury=No) * Probability(TRAF_CON_R=1/Injury=No) * Probability(Injury=No) ]
```

= [6/9 * 0/9 * 9/24] / [6/9 * 0/9 * 9/24 + 5/15 * 2/15 * 15/24] =The result will be "0" Because the numerator is zero.

2.4:- Run a naive Bayes classifier on the 24 records and two predictors. Check the model output to obtain probabilities and classifications for all 24 records. Compare this to the exact Bayes classification. Are the resulting classifications equivalent? Is the ranking (= ordering) of observations equivalent?

```
## [1] 0.571428571 0.250000000 0.002244949 0.008919722 0.571428571 0.250000000 ## [7] 0.250000000 0.571428571 0.250000000 0.250000000 0.250000000 0.666666667 ## [13] 0.571428571 0.571428571 0.571428571 0.571428571 0.250000000 0.250000000 ## [19] 0.250000000 0.250000000 0.571428571 0.571428571 0.333333333 0.250000000
```

library(klaR)

```
## Loading required package: MASS
```

```
#Loading the klaR package

# Creating a variable named formula
formula <- INJURY ~ TRAF_CON_R + WEATHER_R
# Training the Naive Bayes model with Laplace

accidents_24_Df$INJURY <- as.factor(accidents_24_Df$INJURY)
nb2 <- NaiveBayes(formula,data = accidents_24_Df, laplace = 1)

# Making predictions with the model
predict(nb2, newdata = accidents_24_Df[, c("INJURY", "WEATHER_R", "TRAF_CON_R")])</pre>
```

```
## $class
##
     1
                               7
         2
             3
                  4
                          6
                                   8
                                          10
                                              11
                                                               15
                                                                        17
                                                                                     20
                                       9
                                                   12
                                                       13
                                                           14
                                                                    16
                                                                            18
                                                                                 19
  yes
##
        no
            no
                 no yes
                         no
                             no yes
                                      no
                                          no
                                              no yes yes yes yes
                                                                        no
                                                                            no
                                                                                no
                                                                                     nο
##
            23
    21
        22
                 24
##
   yes yes
            no
##
   Levels: no yes
##
##
   $posterior
##
                         yes
      0.4285714 0.571428571
##
   1
##
      0.7500000 0.250000000
##
   3
      0.9977551 0.002244949
      0.9910803 0.008919722
##
##
      0.4285714 0.571428571
##
      0.7500000 0.250000000
      0.7500000 0.250000000
##
## 8
     0.4285714 0.571428571
      0.7500000 0.250000000
   10 0.7500000 0.250000000
## 11 0.7500000 0.250000000
   12 0.3333333 0.666666667
  13 0.4285714 0.571428571
   14 0.4285714 0.571428571
   15 0.4285714 0.571428571
   16 0.4285714 0.571428571
   17 0.7500000 0.250000000
   18 0.7500000 0.250000000
## 19 0.7500000 0.250000000
   20 0.7500000 0.250000000
## 21 0.4285714 0.571428571
## 22 0.4285714 0.571428571
## 23 0.6666667 0.3333333333
## 24 0.7500000 0.250000000
```

```
predict(nb2, newdata = accidents_24_Df[, c("INJURY", "WEATHER_R", "TRAF_CON_R")], typ
e = "raw")
```

```
## $class
##
     1
                               7
                                               11
         2
             3
                  4
                      5
                          6
                                   8
                                          10
                                                   12
                                                                15
                                                                        17
                                                                                     20
                                       9
                                                       13
                                                           14
                                                                    16
                                                                            18
                                                                                 19
  yes
##
                         no
        no
            no
                 no yes
                             no yes
                                      no
                                          no
                                              no yes yes yes yes
                                                                        no
                                                                            no
                                                                                 no
                                                                                     nο
##
            23
    21
        22
                 24
##
  yes yes
            no
##
   Levels: no yes
##
## $posterior
##
                         yes
      0.4285714 0.571428571
##
   1
##
      0.7500000 0.250000000
##
   3
      0.9977551 0.002244949
      0.9910803 0.008919722
##
##
      0.4285714 0.571428571
##
      0.7500000 0.250000000
      0.7500000 0.250000000
##
## 8
      0.4285714 0.571428571
      0.7500000 0.250000000
   10 0.7500000 0.250000000
## 11 0.7500000 0.250000000
   12 0.3333333 0.666666667
   13 0.4285714 0.571428571
   14 0.4285714 0.571428571
   15 0.4285714 0.571428571
   16 0.4285714 0.571428571
   17 0.7500000 0.250000000
   18 0.7500000 0.250000000
## 19 0.7500000 0.250000000
   20 0.7500000 0.250000000
## 21 0.4285714 0.571428571
## 22 0.4285714 0.571428571
## 23 0.6666667 0.3333333333
## 24 0.7500000 0.250000000
```

```
#predictions
```

#raw probabilities

```
# Comparing Both naive Bayes model and exact Bayes classification
classification_match <- all(accidents_24_Df$nbpred.prob == accidents_24_Df$prob.inj)
probability_match <- all.equal(accidents_24_Df$nbpred.prob, accidents_24_Df$prob.inj)

# Checking if classifications and rankings are equal
if (classification_match && is.na(probability_match)) {
   cat("The resulting classifications and rankings are equal.\n")
} else {
   cat("The resulting classifications and rankings are not equal.\n")
}</pre>
```

The resulting classifications and rankings are not equal.

Q3, Let us now return to the entire dataset. Partition the data into training (60%) and validation (40%). 3.1, Run a naive Bayes classifier on the complete training set with the relevant predictors(and INJURY as the response). Note that all predictors are categorical. Show the confusion matrix.

```
##
## Naive Bayes Classifier for Discrete Predictors
##
## Call:
## naiveBayes.default(x = X, y = Y, laplace = laplace)
##
## A-priori probabilities:
## Y
##
          no
                   yes
## 0.4939745 0.5060255
##
## Conditional probabilities:
##
        HOUR I R
## Y
                            1
```

```
##
         0.5689490 0.4310510
##
     yes 0.5703131 0.4296869
##
##
        ALIGN I
## Y
                  1
                            2
     no 0.8712206 0.1287794
##
##
     yes 0.8652300 0.1347700
##
##
        WRK ZONE
##
  Y
##
     no 0.97664374 0.02335626
##
     yes 0.97727805 0.02272195
##
##
        WKDY I R
## Y
                            1
##
     no 0.2194049 0.7805951
##
     yes 0.2381510 0.7618490
##
##
        INT HWY
## Y
                                   1
##
        0.8513837786 0.1481362982 0.0004799232
##
     yes 0.8593737800 0.1397673147 0.0008589053
##
##
        LGTCON I R
## Y
##
     no 0.6870101 0.1251000 0.1878899
##
     yes 0.7014914 0.1096275 0.1888811
##
##
        PROFIL I R
## Y
##
     no 0.7531595 0.2468405
##
     yes 0.7633326 0.2366674
##
##
        SPD LIM
## Y
                                 10
                                               15
                                                             20
                                                                           25
     no 0.0000799872 0.0004799232 0.0043992961 0.0085586306 0.1121420573
##
     yes 0.0001561646 0.0003123292 0.0040602795 0.0039041149 0.0906535488
##
##
        SPD LIM
## Y
                    30
                                 35
                                               40
                                                             45
                                                                           50
##
     no 0.0860662294 0.1896496561 0.0962246041 0.1553351464 0.0407934730
##
     yes 0.0860466932 0.2123057703 0.1068946670 0.1574139143 0.0394315609
##
        SPD LIM
## Y
                    55
                                 60
                                               65
                                                             70
                                                                           75
     no 0.1590145577 0.0355143177 0.0645496721 0.0409534474 0.0062390018
##
##
     ves 0.1549152807 0.0430233466 0.0621535098 0.0311548372 0.0075739830
##
##
        SUR_COND
```

```
## Y
##
     no 0.774196129 0.176931691 0.016717325 0.028155495 0.003999360
     yes 0.815725775 0.151245413 0.010697275 0.016709612 0.005621926
##
##
##
        TRAF CON R
## Y
                            1
##
     no 0.6566149 0.1902096 0.1531755
##
     yes 0.6213009 0.2191770 0.1595221
##
##
        {\tt TRAF\_WAY}
## Y
                                          3
     no 0.57998720 0.36690130 0.05311150
##
     yes 0.56063090 0.39743890 0.04193019
##
##
        WEATHER R
##
## Y
##
     no 0.8390657 0.1609343
     yes 0.8744437 0.1255563
##
```

3

[1] 3

#Creating the confusion matrix using the train.df, the prediction and the classes
confusionMatrix(train.df\$INJURY, predict(nbTotal, train.df[, vars]), positive = "ye
s")

```
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
                no yes
##
          no 5097 7405
##
          yes 4230 8577
##
##
                  Accuracy: 0.5403
                    95% CI: (0.5341, 0.5464)
##
       No Information Rate: 0.6315
##
       P-Value [Acc > NIR] : 1
##
##
##
                     Kappa : 0.0776
##
##
    Mcnemar's Test P-Value : <2e-16
##
##
               Sensitivity: 0.5367
##
               Specificity: 0.5465
##
            Pos Pred Value: 0.6697
            Neg Pred Value: 0.4077
##
##
                Prevalence: 0.6315
            Detection Rate: 0.3389
##
      Detection Prevalence: 0.5060
##
##
         Balanced Accuracy: 0.5416
##
##
          'Positive' Class : yes
```

3.2, What is the overall error of the validation set?

```
confusionMatrix(valid.df$INJURY, predict(nbTotal, valid.df[, vars]), positive = "ye
s")
```

```
## Confusion Matrix and Statistics
##
             Reference
##
## Prediction
                no yes
##
          no 3203 5016
##
          yes 2862 5793
##
##
                  Accuracy : 0.5331
                    95% CI: (0.5256, 0.5407)
##
       No Information Rate: 0.6406
##
       P-Value [Acc > NIR] : 1
##
##
##
                     Kappa : 0.0594
##
    Mcnemar's Test P-Value : <2e-16
##
##
##
               Sensitivity: 0.5359
##
               Specificity: 0.5281
##
            Pos Pred Value: 0.6693
            Neg Pred Value: 0.3897
##
##
                Prevalence: 0.6406
            Detection Rate: 0.3433
##
      Detection Prevalence: 0.5129
##
##
         Balanced Accuracy: 0.5320
##
##
          'Positive' Class : yes
##
```

```
#Calculating the overall error

ver=1-0.5331
verp=ver*100
paste("Overall Error: ",verp)
```

```
## [1] "Overall Error: 46.69"
```

###CONCLUSION

Using two predictors both times, the Naive Bayes classifier was applied to first predict injury outcomes in a data set of 24 records and subsequently to the whole data set.

Using the exact Bayes classifier for the first 24 records, we identified that the most risky combination for drivers is WEATHER_CON=2,TRAF_CON=0 since the injury is max at "1" in this case.

The model has a validation error of 46.3% and a training set accuracy of 53.7%, showing a modest level of prediction. However, it makes the assumption that the prediction variables are independent, which may not always be the case in real-world situations and might result in errors. But for classification and ranking, we may use the Naive Bayes classifier.

While Naive Bayes is a simple and effective algorithm for injury outcome prediction, it's crucial to remember its limitations.