# THE ANNALS of APPLIED STATISTICS

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# INTRODUCTION TO DISCUSSION OF "COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS"

BY BERNARD W. SILVERMAN

University of Oxford

# COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS

#### By Pengsheng Ji and Jiashun Jin<sup>2</sup>

University of Georgia and Carnegie Mellon University

We have collected and cleaned two network data sets: Coauthorship and Citation networks for statisticians. The data sets are based on all research papers published in four of the top journals in statistics from 2003 to the first half of 2012. We analyze the data sets from many different perspectives, focusing on (a) productivity, patterns and trends, (b) centrality and (c) community structures.

For (a), we find that over the 10-year period, both the average number of papers per author and the fraction of self citations have been decreasing, but the proportion of distant citations has been increasing. These findings are consistent with the belief that the statistics community has become increasingly more collaborative, competitive and globalized.

For (b), we have identified the most prolific/collaborative/highly cited authors. We have also identified a handful of "hot" papers, suggesting "Variable Selection" as one of the "hot" areas.

For (c), we have identified about 15 meaningful communities or research groups, including large-size ones such as "Spatial Statistics," "Large-Scale Multiple Testing" and "Variable Selection" as well as small-size ones such as "Dimensional Reduction," "Bayes," "Quantile Regression" and "Theoretical Machine Learning."

Our findings shed light on research habits, trends and topological patterns of statisticians. The data sets provide a fertile ground for future research on social networks.

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*Key words and phrases.* Adjacent rand index, centrality, collaboration, community detection, Degree Corrected Block Model, productivity, social network, spectral clustering.

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# DISCUSSION OF "COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS"

#### By Pedro Regueiro, Abel Rodríguez and Juan Sosa

University of California

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### DISCUSSION OF "COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS"<sup>1</sup>

#### BY SONG WANG AND KARL ROHE

University of Wisconsin, Madison

Pengsheng Ji and Jiashun Jin have collected and analyzed a fun and fascinating data set that we are eager to use as an example in a course on Statistical Network Analysis. In this comment, we partition the core of the paper citation graph and interpret the clusters by analyzing the paper abstracts using bag-of-words. Under the Stochastic Block Model (SBM), the eigengap reveals the number of clusters. We find several eigengaps and that there are still clusters beyond the largest eigengap. Through this illustration, we argue against a simplistic interpretation of model selection results from the Stochastic Block Model (SBM) literature. In short, don't mind the gap.

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Key words and phrases. Networks, spectral clustering, text analysis, eigengap.

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# DISCUSSION OF "COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS"<sup>1</sup>

#### BY VISHESH KARWA AND SONJA PETROVIĆ

Harvard University and Illinois Institute of Technology

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# DISCUSSION OF "COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS"

BY MLADEN KOLAR\* AND MATT TADDY\*,†

University of Chicago\* and Microsoft Research<sup>†</sup>

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# DISCUSSION OF "COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS"

#### BY FORREST W. CRAWFORD

Yale School of Public Health

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# REJOINDER: "COAUTHORSHIP AND CITATION NETWORKS FOR STATISTICIANS"

#### BY PENGSHENG JI AND JIASHUN JIN

University of Georgia and Carnegie Mellon University

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#### SMOOTH PRINCIPAL COMPONENT ANALYSIS OVER TWO-DIMENSIONAL MANIFOLDS WITH AN APPLICATION TO NEUROIMAGING

By Eardi Lila\*,†, John A. D. Aston\*,1 and Laura M. Sangalli†

*University of Cambridge*\* and Politecnico di Milano<sup>†</sup>

Motivated by the analysis of high-dimensional neuroimaging signals located over the cortical surface, we introduce a novel Principal Component Analysis technique that can handle functional data located over a two-dimensional manifold. For this purpose a regularization approach is adopted, introducing a smoothing penalty coherent with the geodesic distance over the manifold. The model introduced can be applied to any manifold topology, and can naturally handle missing data and functional samples evaluated in different grids of points. We approach the discretization task by means of finite element analysis, and propose an efficient iterative algorithm for its resolution. We compare the performances of the proposed algorithm with other approaches classically adopted in literature. We finally apply the proposed method to resting state functional magnetic resonance imaging data from the Human Connectome Project, where the method shows substantial differential variations between brain regions that were not apparent with other approaches.

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# LINKING LUNG AIRWAY STRUCTURE TO PULMONARY FUNCTION VIA COMPOSITE BRIDGE REGRESSION

By Kun Chen<sup>1,2,\*</sup>, Eric A. Hoffman<sup>1,†</sup>, Indu Seetharaman<sup>‡</sup>, Feiran Jiao<sup>†</sup>, Ching-Long Lin<sup>1,†</sup> and Kung-Sik Chan<sup>1,†</sup>

University of Connecticut,\* University of Iowa<sup>†</sup> and Kansas State University <sup>‡</sup>

The human lung airway is a complex inverted tree-like structure. Detailed airway measurements can be extracted from MDCT-scanned lung images, such as segmental wall thickness, airway diameter, parent-child branch angles, etc. The wealth of lung airway data provides a unique opportunity for advancing our understanding of the fundamental structure-function relationships within the lung. An important problem is to construct and identify important lung airway features in normal subjects and connect these to standardized pulmonary function test results such as FEV1%. Among other things, the problem is complicated by the fact that a particular airway feature may be an important (relevant) predictor only when it pertains to segments of certain generations. Thus, the key is an efficient, consistent method for simultaneously conducting group selection (lung airway feature types) and within-group variable selection (airway generations), i.e., bi-level selection. Here we streamline a comprehensive procedure to process the lung airway data via imputation, normalization, transformation and groupwise principal component analysis, and then adopt a new composite penalized regression approach for conducting bi-level feature selection. As a prototype of composite penalization, the proposed composite bridge regression method is shown to admit an efficient algorithm, enjoy bi-level oracle properties and outperform several existing methods. We analyze the MDCT lung image data from a cohort of 132 subjects with normal lung function. Our results show that lung function in terms of FEV1% is promoted by having a less dense and more homogeneous lung comprising an airway whose segments enjoy more heterogeneity in wall thicknesses, larger mean diameters, lumen areas and branch angles. These data hold the potential of defining more accurately the "normal" subject population with borderline atypical lung functions that are clearly influenced by many genetic and environmental factors.

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# CATEGORICAL DATA FUSION USING AUXILIARY INFORMATION<sup>1</sup>

By Bailey K. Fosdick\*, Maria DeYoreo<sup>†</sup> and Jerome P. Reiter<sup>†</sup>

Colorado State University\* and Duke University†

In data fusion, analysts seek to combine information from two databases comprised of disjoint sets of individuals, in which some variables appear in both databases and other variables appear in only one database. Most data fusion techniques rely on variants of conditional independence assumptions. When inappropriate, these assumptions can result in unreliable inferences. We propose a data fusion technique that allows analysts to easily incorporate auxiliary information on the dependence structure of variables not observed jointly; we refer to this auxiliary information as glue. With this technique, we fuse two marketing surveys from the book publisher HarperCollins using glue from the online, rapid-response polling company CivicScience. The fused data enable estimation of associations between people's preferences for authors and for learning about new books. The analysis also serves as a case study on the potential for using online surveys to aid data fusion.

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# INVESTIGATING DIFFERENCES IN BRAIN FUNCTIONAL NETWORKS USING HIERARCHICAL COVARIATE-ADJUSTED INDEPENDENT COMPONENT ANALYSIS<sup>1</sup>

#### BY RAN SHI AND YING GUO

#### Emory University

Human brains perform tasks via complex functional networks consisting of separated brain regions. A popular approach to characterize brain functional networks in fMRI studies is independent component analysis (ICA), which is a powerful method to reconstruct latent source signals from their linear mixtures. In many fMRI studies, an important goal is to investigate how brain functional networks change according to specific clinical and demographic variabilities. Existing ICA methods, however, cannot directly incorporate covariate effects in ICA decomposition. Heuristic post-ICA analysis to address this need can be inaccurate and inefficient. In this paper, we propose a hierarchical covariate-adjusted ICA (hc-ICA) model that provides a formal statistical framework for estimating covariate effects and testing differences between brain functional networks. Our method provides a more reliable and powerful statistical tool for evaluating group differences in brain functional networks while appropriately controlling for potential confounding factors. We present an analytically tractable EM algorithm to obtain maximum likelihood estimates of our model. We also develop a subspace-based approximate EM that runs significantly faster while retaining high accuracy. To test the differences in functional networks, we introduce a voxel-wise approximate inference procedure which eliminates the need of computationally expensive covariance matrix estimation and inversion. We demonstrate the advantages of our methods over the existing method via simulation studies. We apply our method to an fMRI study to investigate differences in brain functional networks associated with post-traumatic stress disorder (PTSD).

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# IMPROVING COVARIATE BALANCE IN 2<sup>K</sup> FACTORIAL DESIGNS VIA RERANDOMIZATION WITH AN APPLICATION TO A NEW YORK CITY DEPARTMENT OF EDUCATION HIGH SCHOOL STUDY

BY ZACH BRANSON, TIRTHANKAR DASGUPTA AND DONALD B. RUBIN

#### Harvard University

A few years ago, the New York Department of Education (NYDE) was planning to conduct an experiment involving five new intervention programs for a selected set of New York City high schools. The goal was to estimate the causal effects of these programs and their interactions on the schools' performance. For each of the schools, about 50 premeasured covariates were available. The schools could be randomly assigned to the 32 treatment combinations of this 2<sup>5</sup> factorial experiment, but such an allocation could have resulted in a huge covariate imbalance across treatment groups. Standard methods used to prevent confounding of treatment effects with covariate effects (e.g., blocking) were not intuitive due to the large number of covariates. In this paper, we explore how the recently proposed and studied method of rerandomization can be applied to this problem and other factorial experiments. We propose how to implement rerandomization in factorial experiments, extend the theoretical properties of rerandomization from single-factor experiments to  $2^K$  factorial designs, and demonstrate, using the NYDE data, how such a designed experiment can improve precision of estimated factorial effects.

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### PREDICTING MELBOURNE AMBULANCE DEMAND USING KERNEL WARPING<sup>1</sup>

#### BY ZHENGYI ZHOU AND DAVID S. MATTESON

#### Cornell University

Predicting ambulance demand accurately in fine resolutions in space and time is critical for ambulance fleet management and dynamic deployment. Typical challenges include data sparsity at high resolutions and the need to respect complex urban spatial domains. To provide spatial density predictions for ambulance demand in Melbourne, Australia, as it varies over hourly intervals, we propose a predictive spatio-temporal kernel warping method. To predict for each hour, we build a kernel density estimator on a sparse set of the most similar data from relevant past time periods (labeled data), but warp these kernels to a larger set of past data irregardless of time periods (point cloud). The point cloud represents the spatial structure and geographical characteristics of Melbourne, including complex boundaries, road networks and neighborhoods. Borrowing from manifold learning, kernel warping is performed through a graph Laplacian of the point cloud and can be interpreted as a regularization toward, and a prior imposed for, spatial features. Kernel bandwidth and degree of warping are efficiently estimated via crossvalidation, and can be made time- and/or location-specific. Our proposed model gives significantly more accurate predictions compared to a current industry practice, an unwarped kernel density estimation and a time-varying Gaussian mixture model.

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# MAXIMIZING THE INFORMATION CONTENT OF A BALANCED MATCHED SAMPLE IN A STUDY OF THE ECONOMIC PERFORMANCE OF GREEN BUILDINGS<sup>1</sup>

#### BY CINAR KILCIOGLU AND JOSÉ R. ZUBIZARRETA

#### Columbia University

Buildings have a major impact on the environment through excessive use of resources, such as energy and water, and large carbon dioxide emissions. In this paper we revisit a previously published study about the economics of environmentally sustainable buildings and estimate the effect of green building practices on market rents. For this, we use new matching methods that take advantage of the clustered structure of the buildings data. We propose a general framework for matching in observational studies and specific matching methods within this framework that simultaneously achieve three goals: (i) maximize the information content of a matched sample (and, in some cases, also minimize the variance of a difference-in-means effect estimator); (ii) form the matches using a flexible matching structure (such as a one-tomany/many-to-one structure); and (iii) directly attain covariate balance as specified-before matching-by the investigator. To our knowledge, existing matching methods are only able to achieve, at most, two of these goals simultaneously. Also, unlike most matching methods, the proposed methods do not require estimation of the propensity score or other dimensionality reduction techniques, although with the proposed methods these can be used as additional balancing covariates in the context of (iii). Using these matching methods, we find that green buildings have 3.3% higher rental rates per square foot than otherwise similar buildings without green ratings—a moderately larger effect than the one found by the prior study.

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#### MODELING CONCURRENCY AND SELECTIVE MIXING IN HETEROSEXUAL PARTNERSHIP NETWORKS WITH APPLICATIONS TO SEXUALLY TRANSMITTED DISEASES<sup>1</sup>

#### BY RYAN ADMIRAAL AND MARK S. HANDCOCK

Murdoch University and University of California, Los Angeles

Network-based models for sexually transmitted disease transmission rely on initial partnership networks incorporating structures that may be related to risk of infection. In particular, initial networks should reflect the level of concurrency and attribute-based selective mixing observed in the population of interest. We consider momentary degree distributions as measures of concurrency and propensities for people of certain types to form partnerships with each other as a measure of attribute-based selective mixing. Estimation of momentary degree distributions and mixing patterns typically relies on cross-sectional survey data, and, in the context of heterosexual networks, we describe how this results in two sets of reports that need not be consistent with each other. The reported momentary degree distributions and mixing totals are related through a series of constraints, however. We provide a method to incorporate those in jointly estimating momentary degree distributions and mixing totals. We develop a method to simulate heterosexual networks consistent with these momentary degree distributions and mixing totals, applying it to data obtained from the National Longitudinal Study of Adolescent Health. We first use the momentary degree distributions and mixing totals as mean value parameters to estimate the natural parameters for an exponential-family random graph model and then use a Markov chain Monte Carlo algorithm to simulate person-level heterosexual partnership networks.

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# INFERRING ROOTED POPULATION TREES USING ASYMMETRIC NEIGHBOR JOINING

By Yongliang Zhai and Alexandre Bouchard-Côté<sup>1</sup>

# University of British Columbia

We introduce a new inference method to estimate evolutionary distances for any two populations to their most recent common ancestral population using single-nucleotide polymorphism allele frequencies. Our model takes fixation into consideration, making it nonreversible, and guarantees that the distribution of reconstructed ancestral frequencies is contained on the interval [0, 1]. To scale this method to large numbers of populations, we introduce the asymmetric neighbor joining algorithm, an efficient method for reconstructing rooted bifurcating nonclock trees. Asymmetric neighbor joining provides a scalable rooting method applicable to any nonreversible evolutionary modeling setups. We explore the statistical properties of asymmetric neighbor joining, and demonstrate its accuracy on synthetic data. We validate our method by reconstructing rooted phylogenetic trees from the Human Genome Diversity Panel data. Our results are obtained without using an outgroup, and are consistent with the prevalent recent single-origin model.

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# MODELLING THE EFFECT OF THE EL NIÑO-SOUTHERN OSCILLATION ON EXTREME SPATIAL TEMPERATURE EVENTS OVER AUSTRALIA

BY HUGO C. WINTER<sup>1</sup>, JONATHAN A. TAWN AND SIMON J. BROWN<sup>2</sup>

EDF Energy R&D UK Centre, Lancaster University and Met Office Hadley Centre

When assessing the risk posed by high temperatures, it is necessary to consider not only the temperature at separate sites but also how many sites are expected to be hot at the same time. Hot events that cover a large area have the potential to put a great strain on health services and cause devastation to agriculture, leading to high death tolls and much economic damage. Southeastern Australia experienced a severe heatwave in early 2009; 374 people died in the state of Victoria and Melbourne recorded its highest temperature since records began in 1859 [Nairn and Fawcett (2013)]. One area of particular interest in climate science is the effect of large-scale climatic phenomena, such as the El Niño-Southern Oscillation (ENSO), on extreme temperatures. Here, we develop a framework based upon extreme value theory to estimate the effect of ENSO on extreme temperatures across Australia. This approach permits us to estimate the change in temperatures with ENSO at important sites, such as Melbourne, and also whether we are more likely to observe hot temperatures over a larger spatial extent during a particular phase of ENSO. To this end, we design a set of measures that can be used to effectively summarise many important spatial aspects of an extreme temperature event. These measures are estimated using our extreme value framework and we validate whether we can accurately replicate the 2009 Australian heatwave, before using the model to estimate the probability of having a more severe event than has been observed.

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# THE SCREENING AND RANKING ALGORITHM FOR CHANGE-POINTS DETECTION IN MULTIPLE SAMPLES<sup>1</sup>

By Chi Song<sup>2</sup>, Xiaoyi Min<sup>2</sup> and Heping Zhang

Ohio State University, Georgia State University and Yale University

The chromosome copy number variation (CNV) is the deviation of genomic regions from their normal copy number states, which may associate with many human diseases. Current genetic studies usually collect hundreds to thousands of samples to study the association between CNV and diseases. CNVs can be called by detecting the change-points in mean for sequences of array-based intensity measurements. Although multiple samples are of interest, the majority of the available CNV calling methods are single sample based. Only a few multiple sample methods have been proposed using scan statistics that are computationally intensive and designed toward either common or rare change-points detection. In this paper, we propose a novel multiple sample method by adaptively combining the scan statistic of the screening and ranking algorithm (SaRa), which is computationally efficient and is able to detect both common and rare change-points. We prove that asymptotically this method can find the true change-points with almost certainty and show in theory that multiple sample methods are superior to single sample methods when shared change-points are of interest. Additionally, we report extensive simulation studies to examine the performance of our proposed method. Finally, using our proposed method as well as two competing approaches, we attempt to detect CNVs in the data from the Primary Open-Angle Glaucoma Genes and Environment study, and conclude that our method is faster and requires less information while our ability to detect the CNVs is comparable or better.

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# COX REGRESSION WITH EXCLUSION FREQUENCY-BASED WEIGHTS TO IDENTIFY NEUROIMAGING MARKERS RELEVANT TO HUNTINGTON'S DISEASE ONSET

# By Tanya P. Garcia<sup>1</sup> and Samuel Müller<sup>2</sup>

Texas A&M University and University of Sydney

Biomedical studies of neuroimaging and genomics collect large amounts of data on a small subset of subjects so as to not miss informative predictors. An important goal is identifying those predictors that provide better visualization of the data and that could serve as cost-effective measures for future clinical trials. Identifying such predictors is challenging, however, when the predictors are naturally interrelated and the response is a failure time prone to censoring. We propose to handle these challenges with a novel variable selection technique. Our approach casts the problem into several smaller dimensional settings and extracts from this intermediary step the relative importance of each predictor through data-driven weights called exclusion frequencies. The exclusion frequencies are used as weights in a weighted Lasso, and results yield low false discovery rates and a high geometric mean of sensitivity and specificity. We illustrate the method's advantages over existing ones in an extensive simulation study, and use the method to identify relevant neuroimaging markers associated with Huntington's disease onset.

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# BAYESIAN NONPARAMETRIC MULTIRESOLUTION ESTIMATION FOR THE AMERICAN COMMUNITY SURVEY

## BY TERRANCE D. SAVITSKY

U.S. Bureau of Labor Statistics

Bayesian hierarchical methods implemented for small area estimation focus on reducing the noise variation in published government official statistics by borrowing information among dependent response values. Even the most flexible models confine parameters defined at the finest scale to link to each data observation in a one-to-one construction. We propose a Bayesian multiresolution formulation that utilizes an ensemble of observations at a variety of coarse scales in space and time to additively nest parameters we define at a finer scale, which serve as our focus for estimation. Our construction is motivated by and applied to the estimation of 1-year period employment totals, indexed by county, from statistics published at coarser areal domains and multi-year periods in the American Community Survey (ACS). We construct a nonparametric mixture of Gaussian processes as the prior on a set of regression coefficients of county-indexed latent functions over multiple survey years. We evaluate a modified Dirichlet process prior that incorporates county-year predictors as the mixing measure. Each county-year parameter of a latent function is estimated from multiple coarse-scale observations in space and time to which it links. The multiresolution formulation is evaluated on synthetic data and applied to the ACS.

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# DYNAMIC SOCIAL NETWORKS BASED ON MOVEMENT<sup>1</sup>

BY HENRY R. SCHARF\*, MEVIN B. HOOTEN<sup>†,\*</sup>, BAILEY K. FOSDICK\*, DEVIN S. JOHNSON<sup>‡</sup>, JOSH M. LONDON<sup>‡</sup> AND JOHN W. DURBAN<sup>§</sup>

Colorado State University\*, U.S. Geological Survey, Colorado Cooperative Fish and Wildlife Research Unit<sup>†</sup>, NOAA Alaska Fisheries Science Center<sup>‡</sup> and NOAA Southwest Fisheries Science Center<sup>§</sup>

Network modeling techniques provide a means for quantifying social structure in populations of individuals. Data used to define social connectivity are often expensive to collect and based on case-specific, ad hoc criteria. Moreover, in applications involving animal social networks, collection of these data is often opportunistic and can be invasive. Frequently, the social network of interest for a given population is closely related to the way individuals move. Thus, telemetry data, which are minimally invasive and relatively inexpensive to collect, present an alternative source of information. We develop a framework for using telemetry data to infer social relationships among animals. To achieve this, we propose a Bayesian hierarchical model with an underlying dynamic social network controlling movement of individuals via two mechanisms: an attractive effect and an aligning effect. We demonstrate the model and its ability to accurately identify complex social behavior in simulation, and apply our model to telemetry data arising from killer whales. Using auxiliary information about the study population, we investigate model validity and find the inferred dynamic social network is consistent with killer whale ecology and expert knowledge.

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# LOCALLY ADAPTIVE DYNAMIC NETWORKS<sup>1</sup>

# BY DANIELE DURANTE AND DAVID B. DUNSON

University of Padova and Duke University

Our focus is on realistically modeling and forecasting dynamic networks of face-to-face contacts among individuals. Important aspects of such data that lead to problems with current methods include the tendency of the contacts to move between periods of slow and rapid changes, and the dynamic heterogeneity in the actors' connectivity behaviors. Motivated by this application, we develop a novel method for Locally Adaptive DYnamic (LADY) network inference. The proposed model relies on a dynamic latent space representation in which each actor's position evolves in time via stochastic differential equations. Using a state-space representation for these stochastic processes and Pólya-gamma data augmentation, we develop an efficient MCMC algorithm for posterior inference along with tractable procedures for online updating and forecasting of future networks. We evaluate performance in simulation studies, and consider an application to face-to-face contacts among individuals in a primary school.

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Key words and phrases. Face-to-face dynamic contact network, latent space, nested Gaussian process, online updating, Pólya-gamma, state-space model.

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# ESTIMATING ODDS RATIOS UNDER A CASE-BACKGROUND DESIGN WITH AN APPLICATION TO A STUDY OF SORAFENIB ACCESSIBILITY

## BY JOHN H. SPIVACK AND BIN CHENG

Icahn School of Medicine at Mount Sinai and Columbia University

In certain epidemiologic studies such as those involving stress disorders, sexual harassment, alcohol addiction or epidemiological criminology, exposure data are readily available from cases but not from controls because it is socially inconvenient or even unethical to determine who qualifies as a true control subject. Consequently, it is impractical or even infeasible to use a case-control design to establish the case-exposure association in such situations. To address this issue, we propose a case-background design where in addition to a sample of exposure information from cases, an independent sample of exposure information from the background population is taken, without knowing the case status of the sampled subjects. We develop a semiparametric method to estimate the odds ratio and show that the estimator is strongly consistent and asymptotically normally distributed. Simulation studies indicate that the estimators perform satisfactorily in finite samples and against violations of assumptions. The proposed method is applied to a Sorafenib accessibility study of patients with advanced hepatocellular carcinoma.

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# A STATISTICAL MODEL TO ASSESS (ALLELE-SPECIFIC) ASSOCIATIONS BETWEEN GENE EXPRESSION AND EPIGENETIC FEATURES USING SEQUENCING DATA

By Naim U. Rashid $^*$ , Wei Sun $^\dagger$  and Joseph G. Ibrahim $^*$ 

University of North Carolina at Chapel Hill\* and Fred Hutchinson Cancer Research Center<sup>†</sup>

Sequencing techniques have been widely used to assess gene expression (i.e., RNA-seq) or the presence of epigenetic features (e.g., DNase-seq to identify open chromatin regions). In contrast to traditional microarray platforms, sequencing data are typically summarized in the form of discrete counts, and they are able to delineate allele-specific signals, which are not available from microarrays. The presence of epigenetic features are often associated with gene expression, both of which have been shown to be affected by DNA polymorphisms. However, joint models with the flexibility to assess interactions between gene expression, epigenetic features and DNA polymorphisms are currently lacking. In this paper, we develop a statistical model to assess the associations between gene expression and epigenetic features using sequencing data, while explicitly modeling the effects of DNA polymorphisms in either an allele-specific or nonallele-specific manner. We show that in doing so we provide the flexibility to detect associations between gene expression and epigenetic features, as well as conditional associations given DNA polymorphisms. We evaluate the performance of our method using simulations and apply our method to study the association between gene expression and the presence of DNase I Hypersensitive sites (DHSs) in HapMap individuals. Our model can be generalized to exploring the relationships between DNA polymorphisms and any two types of sequencing experiments, a useful feature as the variety of sequencing experiments continue to expand.

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# IMPROVING ICE SHEET MODEL CALIBRATION USING PALEOCLIMATE AND MODERN DATA

By Won Chang  $^{1,2,*}$  , Murali Haran  $^{1,3,\dagger}$  , Patrick Applegate  $^{1,3,\dagger}$  and David Pollard  $^{1,3,4,\dagger}$ 

University of Cincinnati\* and Pennsylvania State University<sup>†</sup>

Human-induced climate change may cause significant ice volume loss from the West Antarctic Ice Sheet (WAIS). Projections of ice volume change from ice sheet models and corresponding future sea-level rise have large uncertainties due to poorly constrained input parameters. In most future applications to date, model calibration has utilized only modern or recent (decadal) observations, leaving input parameters that control the long-term behavior of WAIS largely unconstrained. Many paleo-observations are in the form of localized time series, while modern observations are non-Gaussian spatial data; combining information across these types poses nontrivial statistical challenges. Here we introduce a computationally efficient calibration approach that utilizes both modern and paleo-observations to generate better constrained ice volume projections. Using fast emulators built upon principal component analysis and a reduced dimension calibration model, we can efficiently handle high-dimensional and non-Gaussian data. We apply our calibration approach to the PSU3D-ICE model which can realistically simulate long-term behavior of WAIS. Our results show that using paleoobservations in calibration significantly reduces parametric uncertainty, resulting in sharper projections about the future state of WAIS. One benefit of using paleo-observations is found to be that unrealistic simulations with overshoots in past ice retreat and projected future regrowth are eliminated.

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## BAYESIAN INFERENCE FOR THE BROWN-RESNICK PROCESS, WITH AN APPLICATION TO EXTREME LOW TEMPERATURES<sup>1</sup>

By Emeric Thibaud\*, Juha Aalto $^\dagger$ , Daniel S. Cooley\*, Anthony C. Davison $^\ddagger$  and Juha Heikkinen $^\S$ 

Colorado State University\*, Finnish Meteorological Institute<sup>†</sup>, Ecole Polytechnique Fédérale de Lausanne<sup>‡</sup> and Natural Resources Institute Finland<sup>§</sup>

The Brown–Resnick max-stable process has proven to be well suited for modeling extremes of complex environmental processes, but in many applications its likelihood function is intractable and inference must be based on a composite likelihood, thereby preventing the use of classical Bayesian techniques. In this paper we exploit a case in which the full likelihood of a Brown–Resnick process can be calculated, using componentwise maxima and their partitions in terms of individual events, and we propose two new approaches to inference. The first estimates the partitions using declustering, while the second uses random partitions in a Markov chain Monte Carlo algorithm. We use these approaches to construct a Bayesian hierarchical model for extreme low temperatures in northern Fennoscandia.

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### A LAG FUNCTIONAL LINEAR MODEL FOR PREDICTION OF MAGNETIZATION TRANSFER RATIO IN MULTIPLE SCLEROSIS LESIONS

By Gina-Maria Pomann\*,1,3, Ana-Maria Staicu $^{\dagger,2,3}$ , Edgar J. Lobaton $^{\dagger}$ , Amanda F. Mejia $^{3,5}$ , Blake E. Dewey $^{\$}$ , Daniel S. Reich $^{\$}$ , Elizabeth M. Sweeney $^{\P,3,4}$  and Russell T. Shinohara $^{\parallel,3,6}$ 

Duke University\*, North Carolina State University<sup>†</sup>, Indiana University Bloomington<sup>‡</sup>, National Institute of Neurological Disorders and Stroke<sup>§</sup>, Rice University<sup>¶</sup> and University of Pennsylvania<sup>∥</sup>

We propose a lag functional linear model to predict a response using multiple functional predictors observed at discrete grids with noise. Two procedures are proposed to estimate the regression parameter functions: (1) an approach that ensures smoothness for each value of time using generalized cross-validation; and (2) a global smoothing approach using a restricted maximum likelihood framework. Numerical studies are presented to analyze predictive accuracy in many realistic scenarios. The methods are employed to estimate a magnetic resonance imaging (MRI)-based measure of tissue damage (the magnetization transfer ratio, or MTR) in multiple sclerosis (MS) lesions, a disease that causes damage to the myelin sheaths around axons in the central nervous system. Our method of estimation of MTR within lesions is useful retrospectively in research applications where MTR was not acquired, as well as in clinical practice settings where acquiring MTR is not currently part of the standard of care. The model facilitates the use of commonly acquired imaging modalities to estimate MTR within lesions, and outperforms cross-sectional models that do not account for temporal patterns of lesion development and repair.

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## BOOTSTRAP AGGREGATING CONTINUAL REASSESSMENT METHOD FOR DOSE FINDING IN DRUG-COMBINATION TRIALS<sup>1</sup>

#### BY RUITAO LIN AND GUOSHENG YIN

#### University of Hong Kong

Phase I drug-combination trials are becoming commonplace in oncology. Most of the current dose-finding designs aim to quantify the toxicity probability space using certain prespecified yet complicated models. These models need to characterize not only each individual drug's toxicity profile, but also their interaction effects, which often leads to multi-parameter models. We propose a novel Bayesian adaptive design for drug-combination trials based on a robust dimension-reduction method. We continuously update the order of dose combinations and reduce the two-dimensional searching space to a one-dimensional line based on the estimated order. As a result, the common approaches to single-agent dose finding, such as the continual reassessment method (CRM), can be applied to drug-combination trials. We further utilize the ensemble technique in machine learning, the so-called bootstrap aggregating (bagging) in conjunction with Bayesian model averaging, to enhance the efficiency and reduce the variability of the proposed method. We conduct extensive simulation studies to examine the operating characteristics of the proposed method under various scenarios. Compared with existing competitive designs, the bagging CRM demonstrates its precision and robustness in terms of pinning down the correct dose combination. We apply the proposed bagging CRM to two recent cancer clinical trials with combined drugs for dose finding.

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## A PHYLOGENETIC LATENT FEATURE MODEL FOR CLONAL DECONVOLUTION<sup>1</sup>

By Francesco Marass\*, Florent Mouliere\*, Ke Yuan<sup>†</sup>, Nitzan Rosenfeld\* and Florian Markowetz\*

University of Cambridge\* and University of Glasgow<sup>†</sup>

Tumours develop in an evolutionary process, in which the accumulation of mutations produces subpopulations of cells with distinct mutational profiles, called clones. This process leads to the genetic heterogeneity widely observed in tumour sequencing data, but identifying the genotypes and frequencies of the different clones is still a major challenge. Here, we present Cloe, a phylogenetic latent feature model to deconvolute tumour sequencing data into a set of related genotypes. Our approach extends latent feature models by placing the features as nodes in a latent tree. The resulting model can capture both the acquisition and the loss of mutations, as well as episodes of convergent evolution. We establish the validity of Cloe on synthetic data and assess its performance on controlled biological data, comparing our reconstructions to those of several published state-of-the-art methods. We show that our method provides highly accurate reconstructions and identifies the number of clones, their genotypes and frequencies even at a modest sequencing depth. As a proof of concept, we apply our model to clinical data from three cases with chronic lymphocytic leukaemia and one case with acute myeloid leukaemia.

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### EXPLOITING TIMSS AND PIRLS COMBINED DATA: MULTIVARIATE MULTILEVEL MODELLING OF STUDENT ACHIEVEMENT<sup>1</sup>

# By Leonardo Grilli\*, Fulvia Pennoni<sup>†</sup>, Carla Rampichini\* and Isabella Romeo<sup>‡</sup>

University of Florence,\* University of Milano-Bicocca<sup>†</sup> and Mario Negri<sup>‡</sup>

We illustrate how to perform a multivariate multilevel analysis in the complex setting of large-scale assessment surveys, dealing with plausible values and accounting for the survey design. In particular, we consider the Italian sample of the TIMSS&PIRLS 2011 Combined International Database on fourth grade students. The multivariate approach jointly considers educational achievement in Reading, Mathematics and Science, thus allowing us to test for differential associations of the covariates with the three outcomes, and to estimate the residual correlations among pairs of outcomes within and between classes. Multilevel modelling allows us to disentangle student and contextual factors affecting achievement. We also account for territorial differences in wealth by means of an index from an external data source. The model residuals point out classes with high or low performance. As educational achievement is measured by plausible values, the estimates are obtained through multiple imputation formulas.

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Key words and phrases. Hierarchical linear model, large-scale assessment data, multiple imputation, plausible values, school effectiveness, secondary data analysis.

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