



Adaptive Huffman Coding: Analysis and Applications



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饮水思源 · 爱国荣校

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Introduction



Our Research is inspired
by the Bad Wine in Cover's
Textbook



One bottle of wine is bad, and we can quickly find it by mixing several bottles of wine and tasting them, once given the probability of each wine being bad.

“ ”



What if the probability is dynamic?

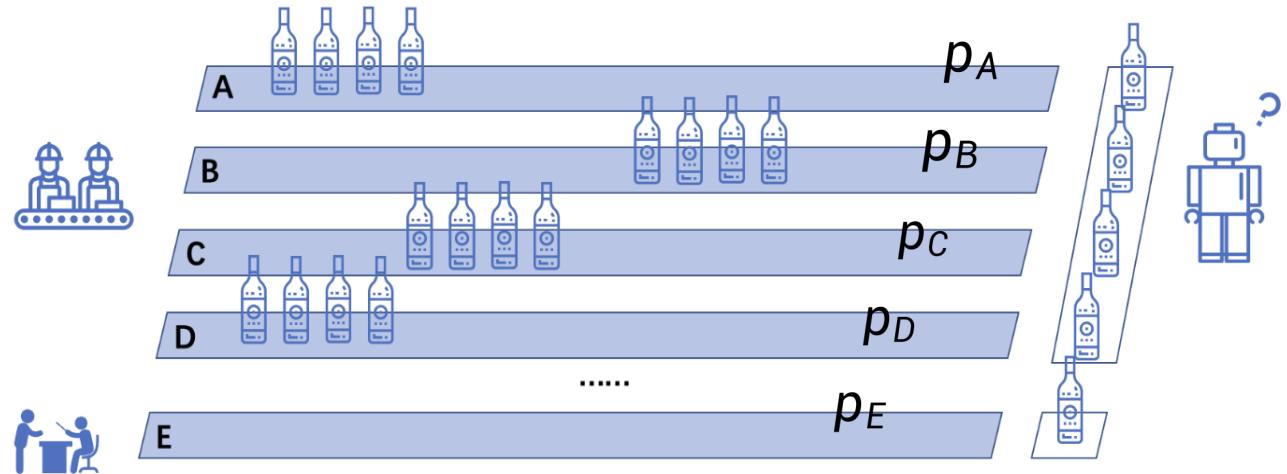


Probability Distribution is Unknown!

What's checking strategy
to quickly find the bad
wine pipeline?

We could use Adaptive
Huffman Coding !

Bad Wine Pipeline



receive exactly one bad wine at a time

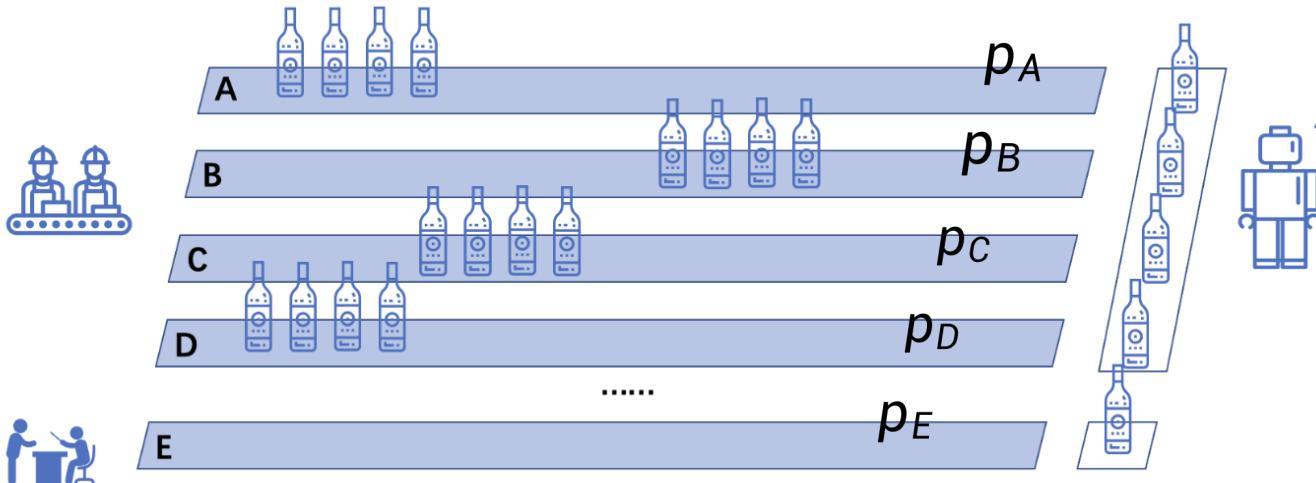
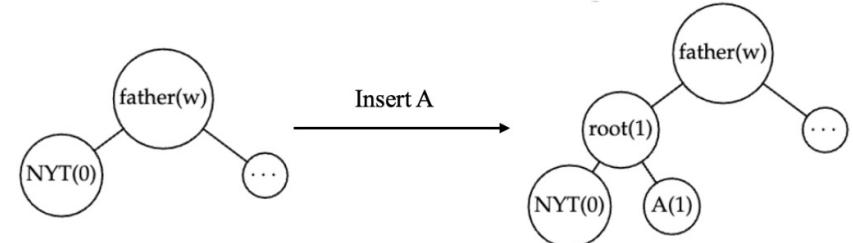




Solutiiion: Adaptive Huffman Tree



Equal to insert a symbol A into Adaptive Huffman Tree !



Every time robot spots a bad wine in pipeline A, p_A should increase, and we should correspondingly change our strategy.





Adaptive Huffman Coding Algorithm



Definition 1. NYT node stands for 'Not Yet Transmitted'. In the building procedure of an adaptive Huffman tree, it serves as auxiliary node. In data compression and transmission procedure, it's an escape code.

Definition 2. The weight of a node is the number of times it appears, which is denoted by the number in the bracket of the node.

Definition 3. Block: a group of nodes who have the same weight.

Definition 4. Node Number: The number of a node is up to the structure of Adaptive Huffman Tree. Starting at 1, it increases from left to the right, bottom to the top.

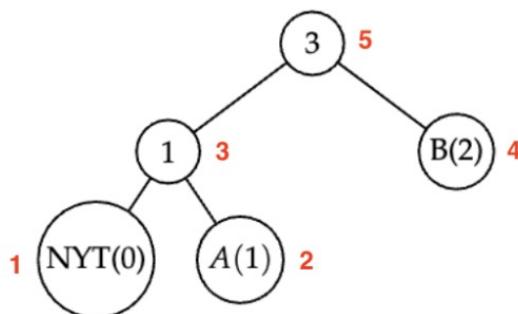
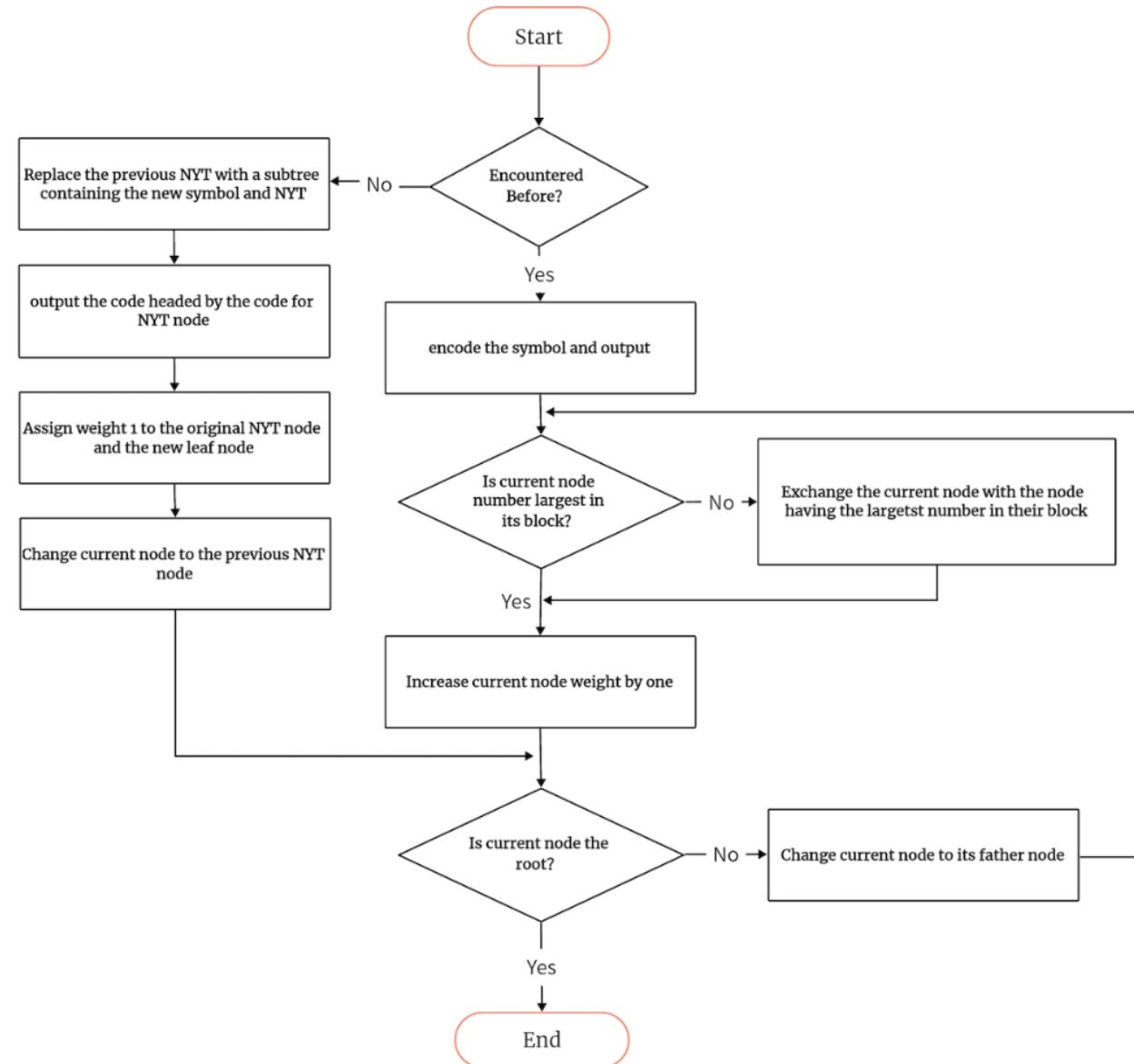


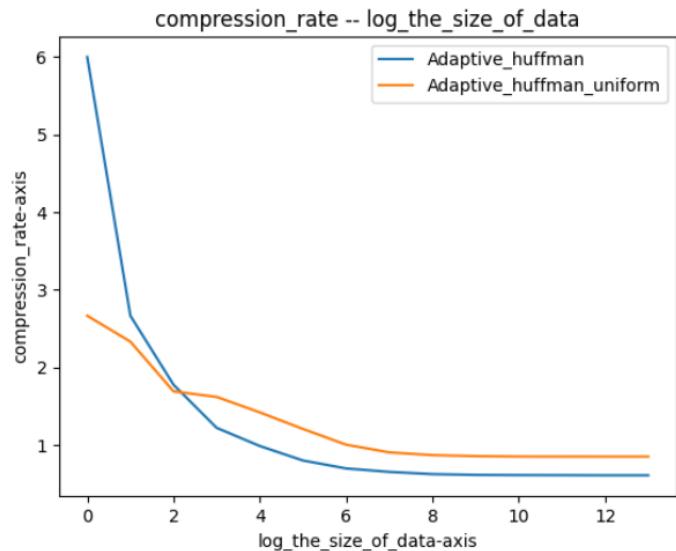
Figure 3: the number of nodes



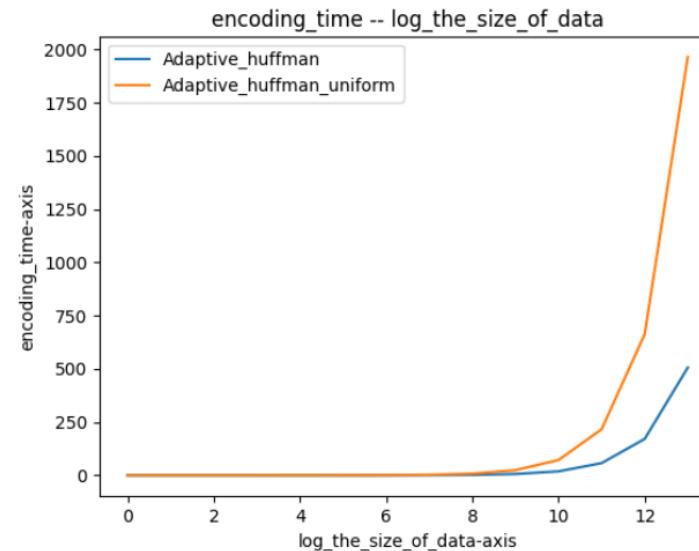
Performance from an encoding perspective



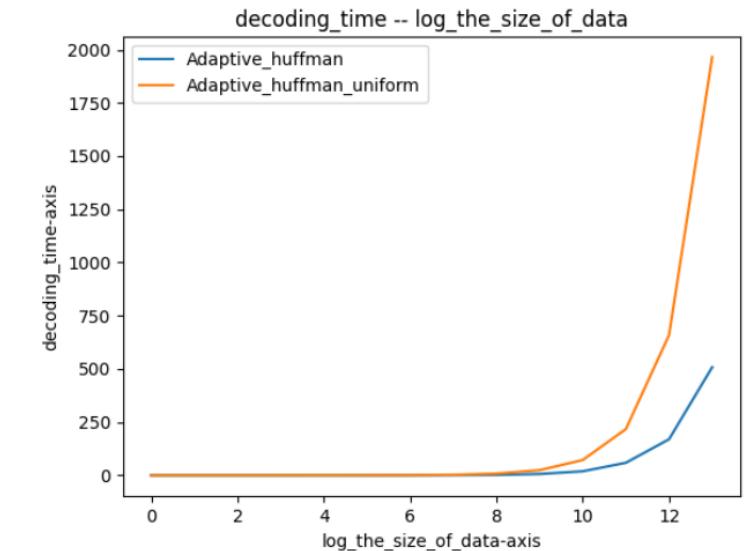
The best interval for the size of message is $[2^7, 2^{12}]$ in our experiment environment!



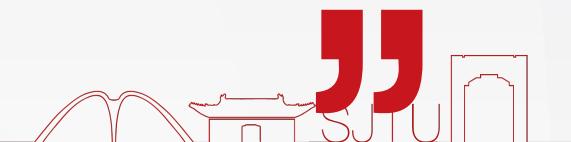
compression rate



encoding time



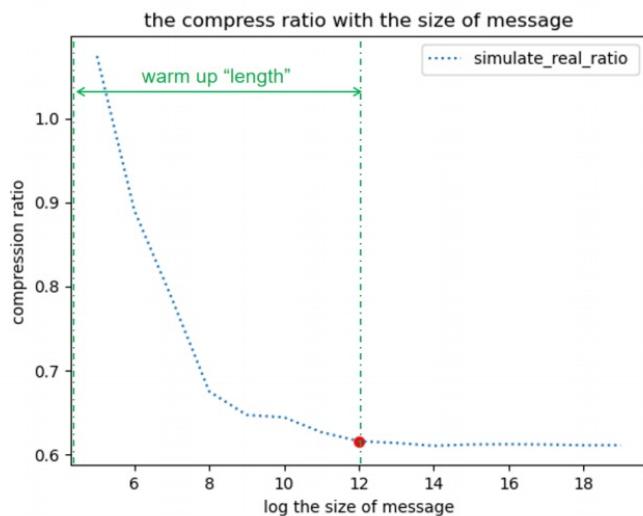
decoding time



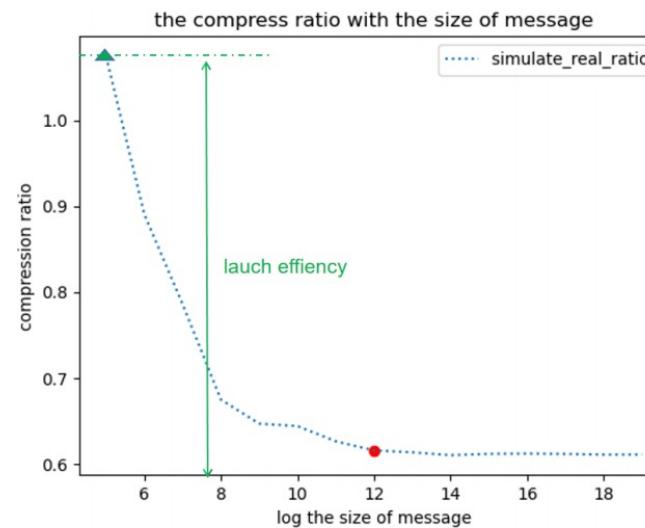
Metrics: How to measure the "learning" velocity



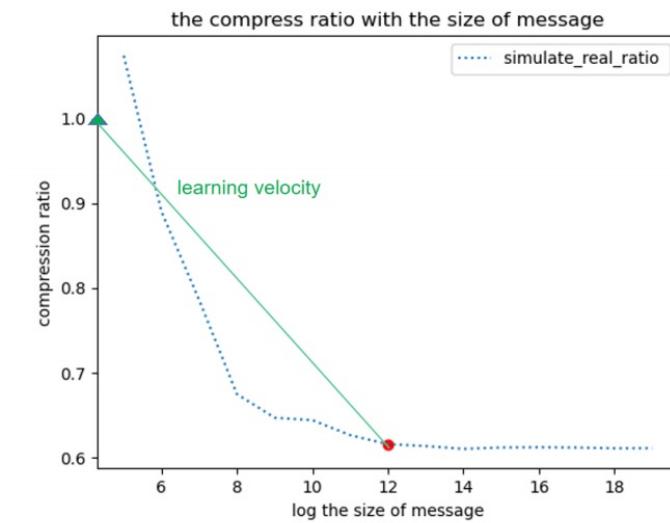
Definition: the convergence state: when the length of message is doubled, the decrease of compression ratio is less than 0.01 continuously.



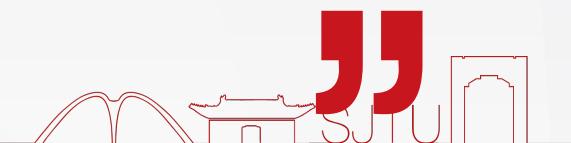
Warm-up length



Launch efficiency



Learning velocity



CONCLUSION:

- 1) The **continuity** of letters makes warm-up easy!
- 2) The **uniform** distribution makes the launch efficiency worse!
- 3) The **regularity** of letters makes learning fast!

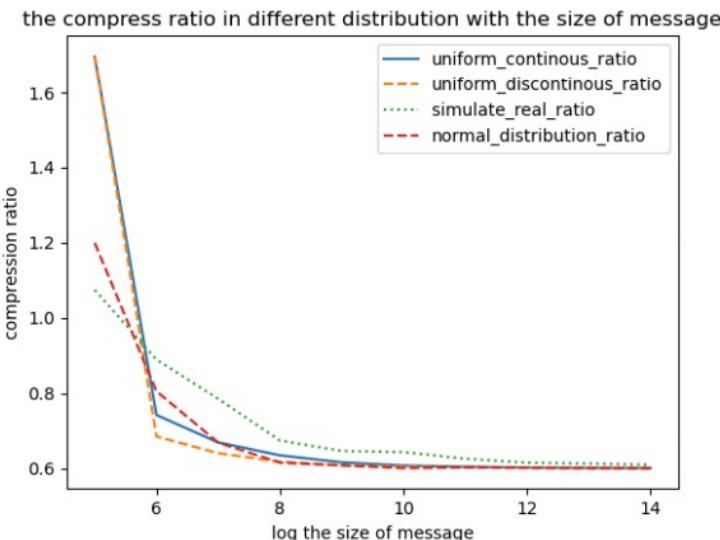


Figure 8: The compression ratio with the size of message in different distribution

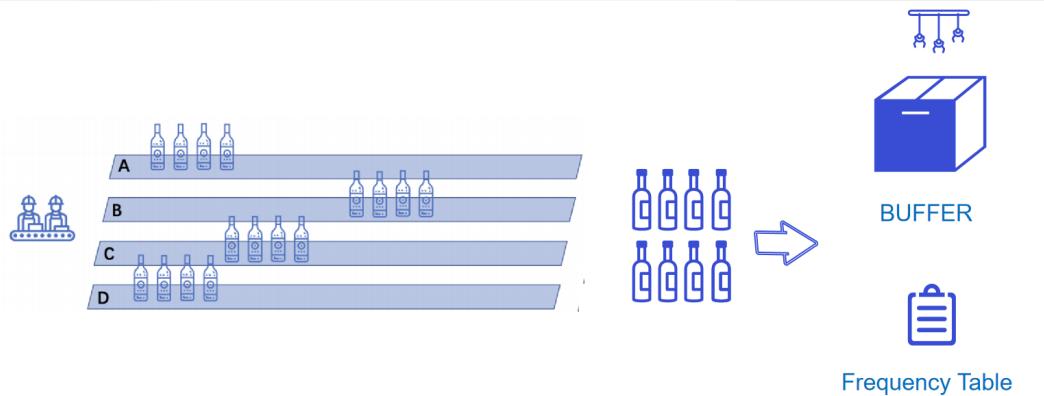
Table 1: The metrics of different probability distribution

distribution	$L_{warm}/(\text{byte})$	$R_v/1$	$E_{\text{launch}}/1$	$v_{\text{learning}}/\log(\text{byte})^{-1}$
continuous uniform	2^9	0.383	1.698	0.0425
discontinuous uniform	2^{18}	0.381	1.698	0.0477
simulation	2^{12}	0.384	1.074	0.0320
normal	2^8	0.384	1.2	0.0480





Accelerate the learning velocity: Buffer makes surprise!



Algorithm 1 Algorithm of Adaptive with Buffer

```

Input: message ,buffersize
Output: deliver code to the decoder
1: while message.remain.size > 0 do
2:   while Buffer.size <= BufferMaxSize and message.remain.size > 0 do
3:     Buffer.Push( message.remain.pop())
4:     Get the Statistical frequency table of the elements in buffer .
5:     Deliver this table to the receiver.
6:     Using this statistical frequency table to update the Huffman Tree in decoder and
      encoder.
7:     Using the updated Huffman Tree to encode the elements in buffer. And deliver the
      code to the decoder.
8:   end while
9: end while

```

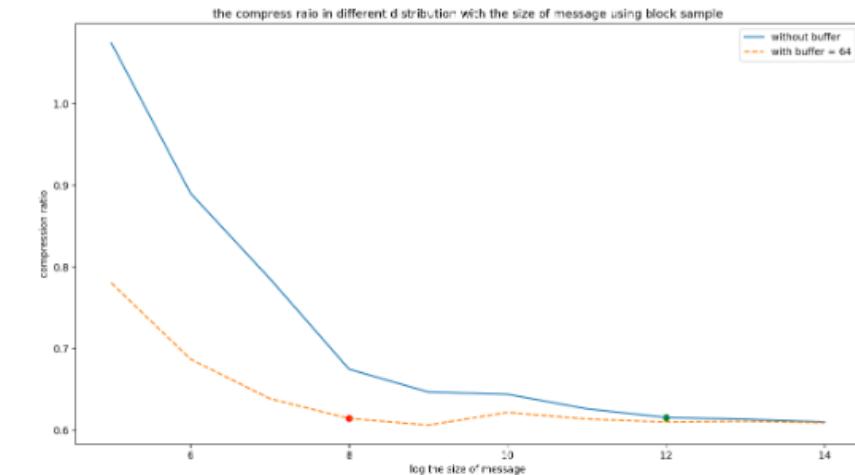


Figure 9: The compression ratio with the size of message

Table 2: The metrics of different probability distribution

distribution	$L_{warm}/(\text{byte})$	$R_v/1$	$E_{\text{launch}}/1$	$v_{\text{learning}}/\log(\text{byte})^{-1}$
with buffer	2^8	0.387	0.78	0.0483
without buffer	2^{12}	0.384	1.074	0.0320





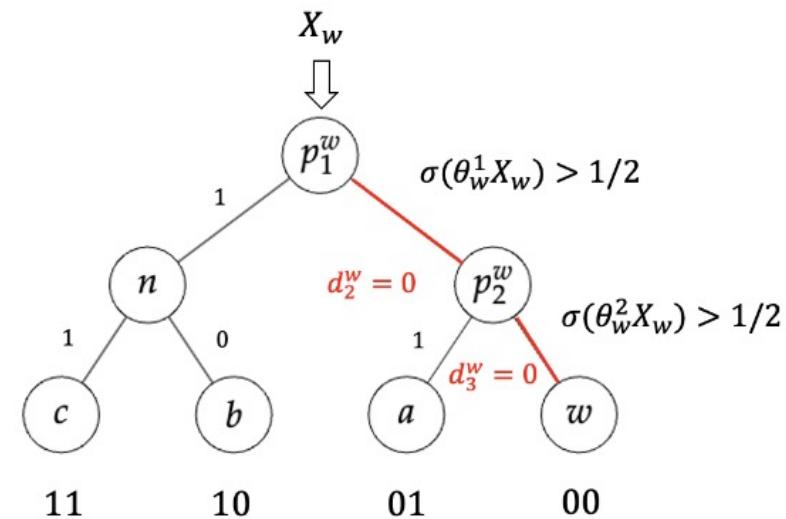
CBOW: Continuous Bag-of-Words

Hierarchical Softmax: a method to improve performance of vec2word models

Biased Walk on Huffman Tree

Input the information of word W, we try to output W by walk on the corresponding Huffman Tree of word set.

$\left\{ \begin{array}{ll} \sigma(\theta_w^1 X_w) > 1/2 & \text{Go Right} \\ \text{ELSE:} & \text{Go Left} \end{array} \right.$





Trials on Incremental Learning



It's costly to rebuild Huffman Tree and retrain model when adding new datas.....

Incremental Huffman Tree

M. Nilufar and A. Abhari, "Incremental text clustering algorithm for cloud-based data management in scientific research papers," in 2022 Annual Modeling and Simulation Conference (ANNSIM), 2022, pp. 778–789

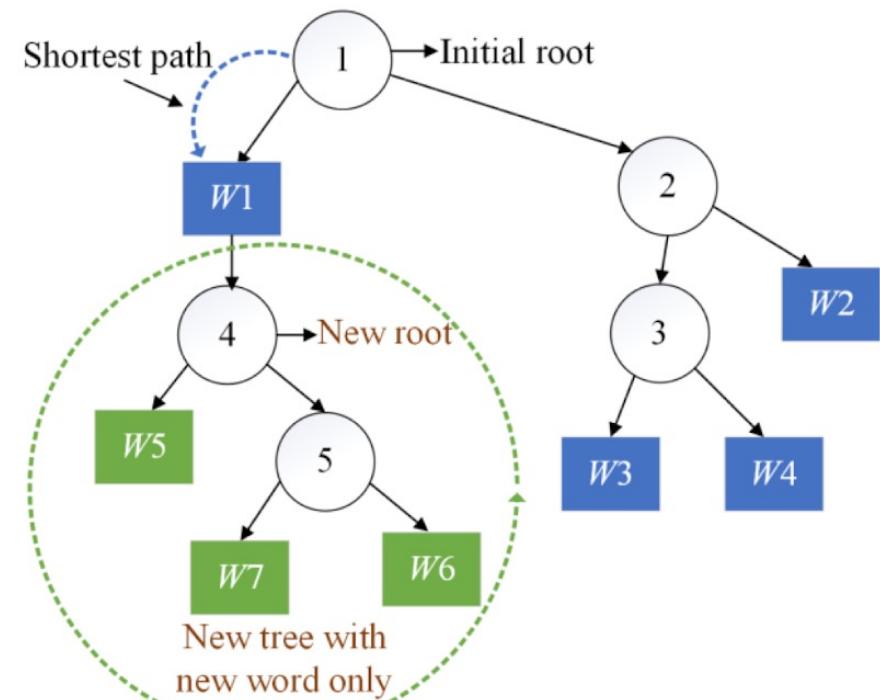
L. Tian, X. Wen, Z. Song et al., "An online word vector generation method based on incremental huffman tree merging," Tehnički vjesnik, vol. 28, no. 1, pp. 52–57, 2021.i

Algorithm 2 Incremental Huffman Tree

Input: previous Huffman Tree T_p , new dataset

Output: updated "Huffman Tree" T_u

- 1: **for** word in new dataset and not in previous Huffman Tree **do**
 - 2: add word into new word set
 - 3: **end for**
 - 4: build a new Huffman Tree T_n on new word set
 - 5: **Merge:** find the shortest path of T_p and make its leaf node n_s the root of T_n
 - 6: update the Huffman Code of leaf nodes in T_n by adding the code of n_s as prefix
-



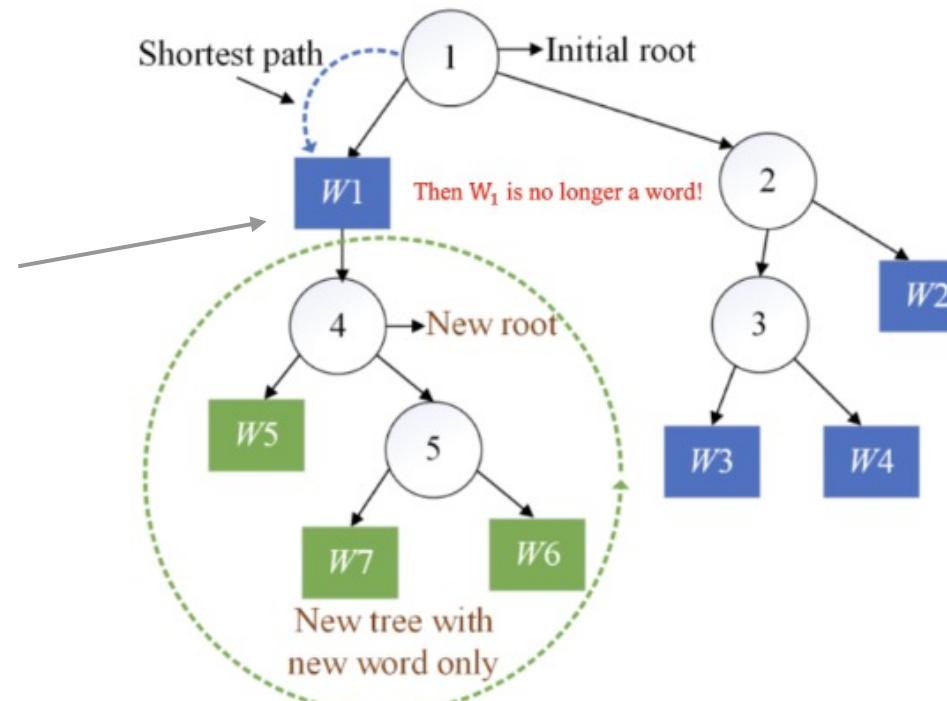
Some deficiencies we found



Incremental Huffman Tree has several drawbacks....

Problem 1. *The accuracy of the model will decrease with this training method.*

A frequently used word
being removed !



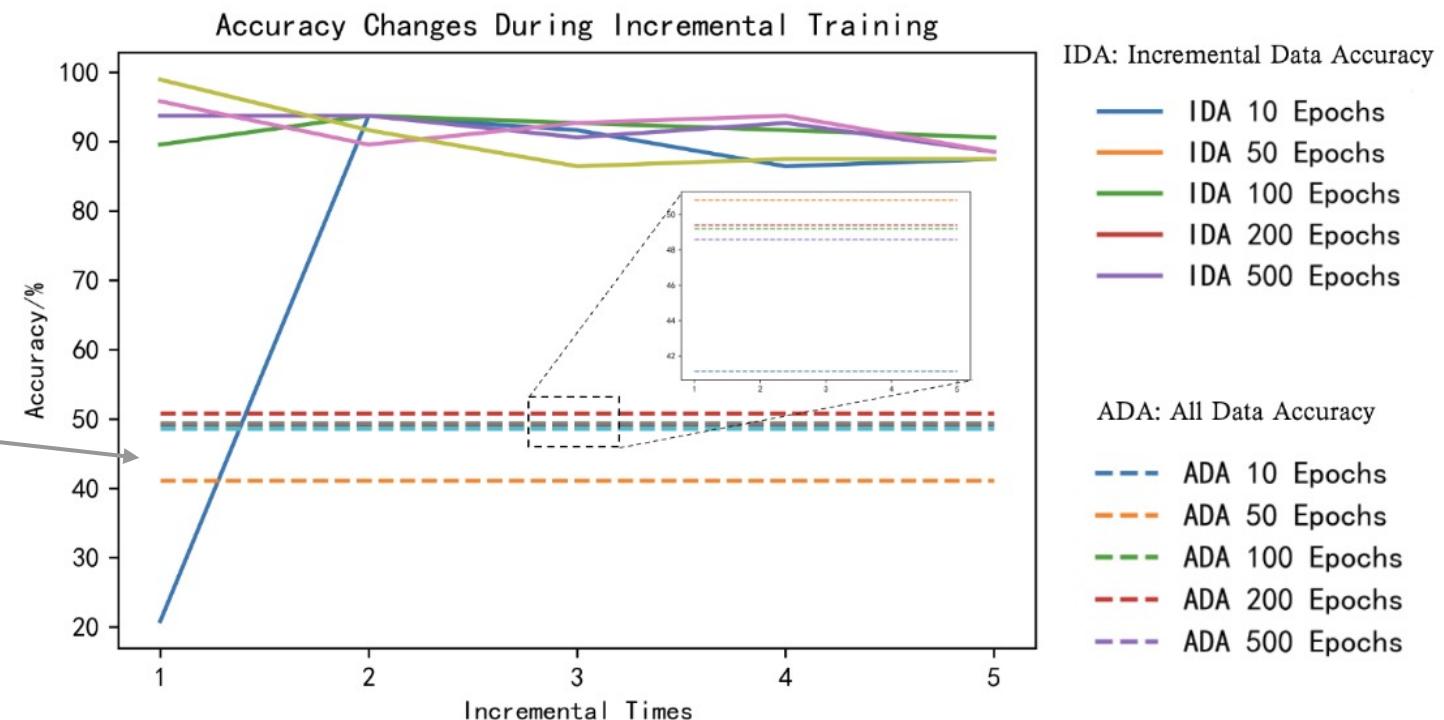
Some deficiencies we found



Incremental Huffman Tree has several drawbacks....

Problem 2. *This method can't really implement incremental learning.*

Bad Accuracy on the whole dataset !

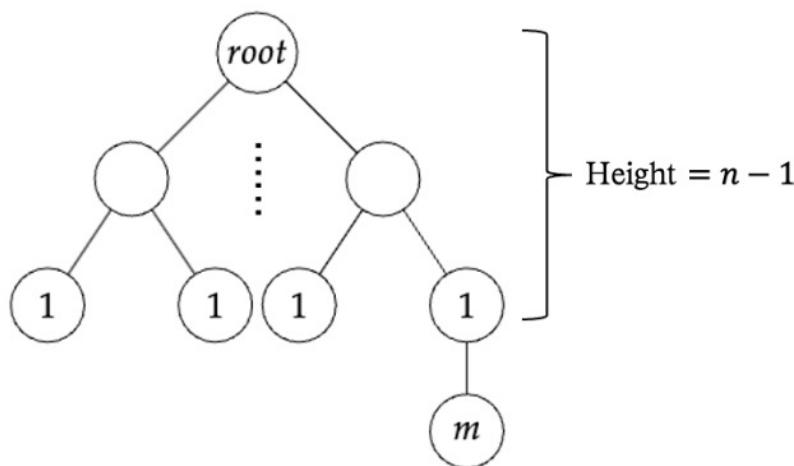


Some deficiencies we found

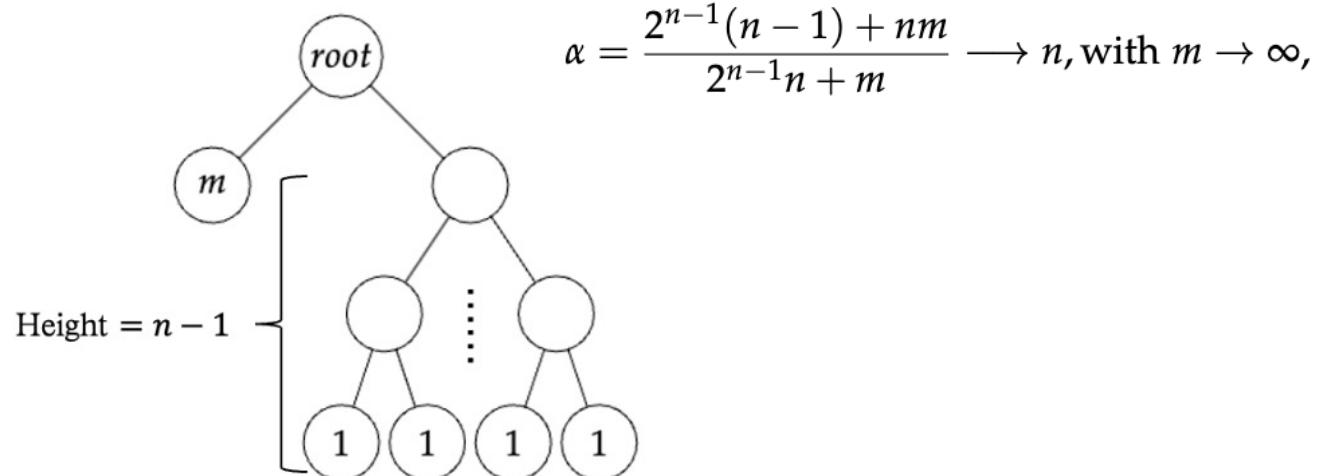


Incremental Huffman Tree has several drawbacks....

Problem 3. Incremental Huffman Tree's code length could be very bad, as data set becoming very large, which also means Incremental Huffman Tree has large height.



Incremental Method



Naive Huffman



Our Refinement: PIWA Algorithm

How about changing incremental to adaptive ?

Algorithm 3 PIWA:Partial Incremental With Adaptive Huffman

Input: previous Huffman Tree T_p , new dataset

Output: updated Huffman Tree T_u

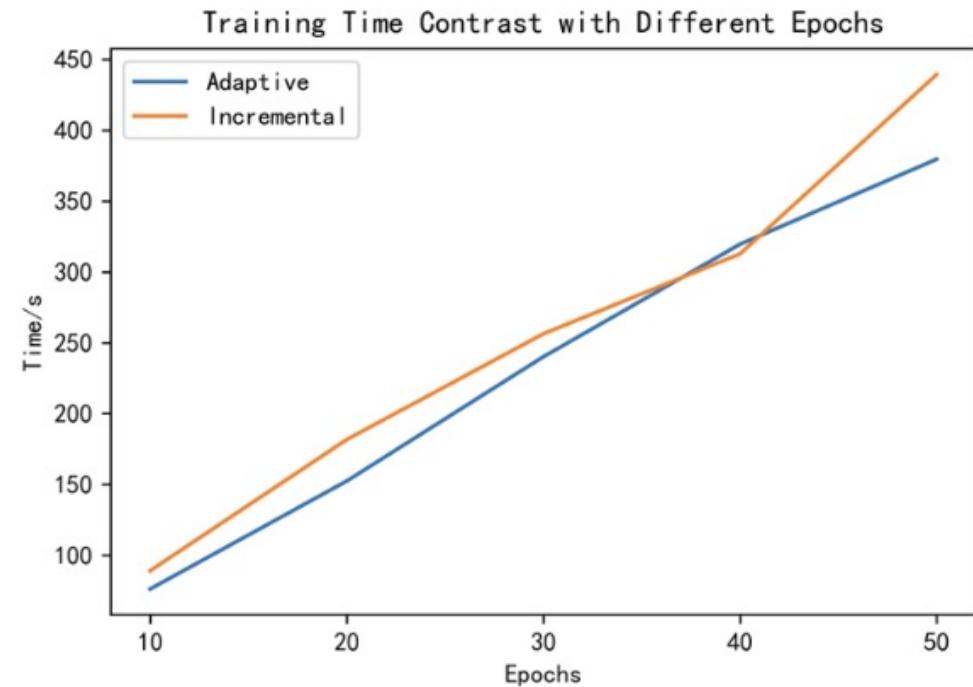
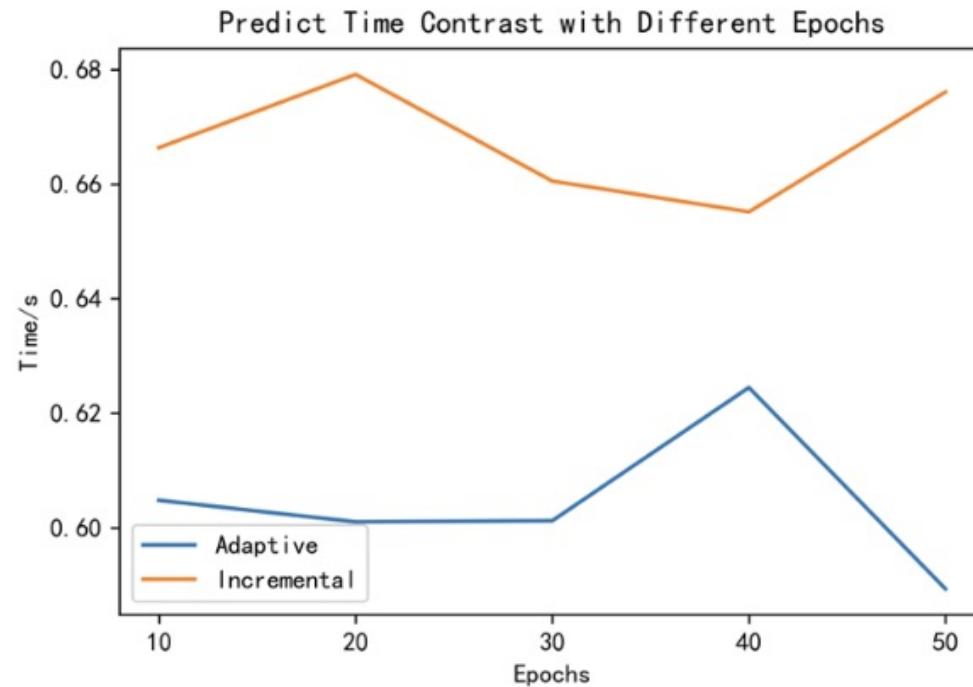
- 1: **for** word in new dataset **do**
 - 2: use Adaptive Huffman Tree algorithm to update the tree
 - 3: **end for**
 - 4: $dataset \leftarrow old\ dataset \cup new\ dataset$
 - 5: Retrain the model on $dataset$
-

“ ”





PIWA: Training and Predicting Time



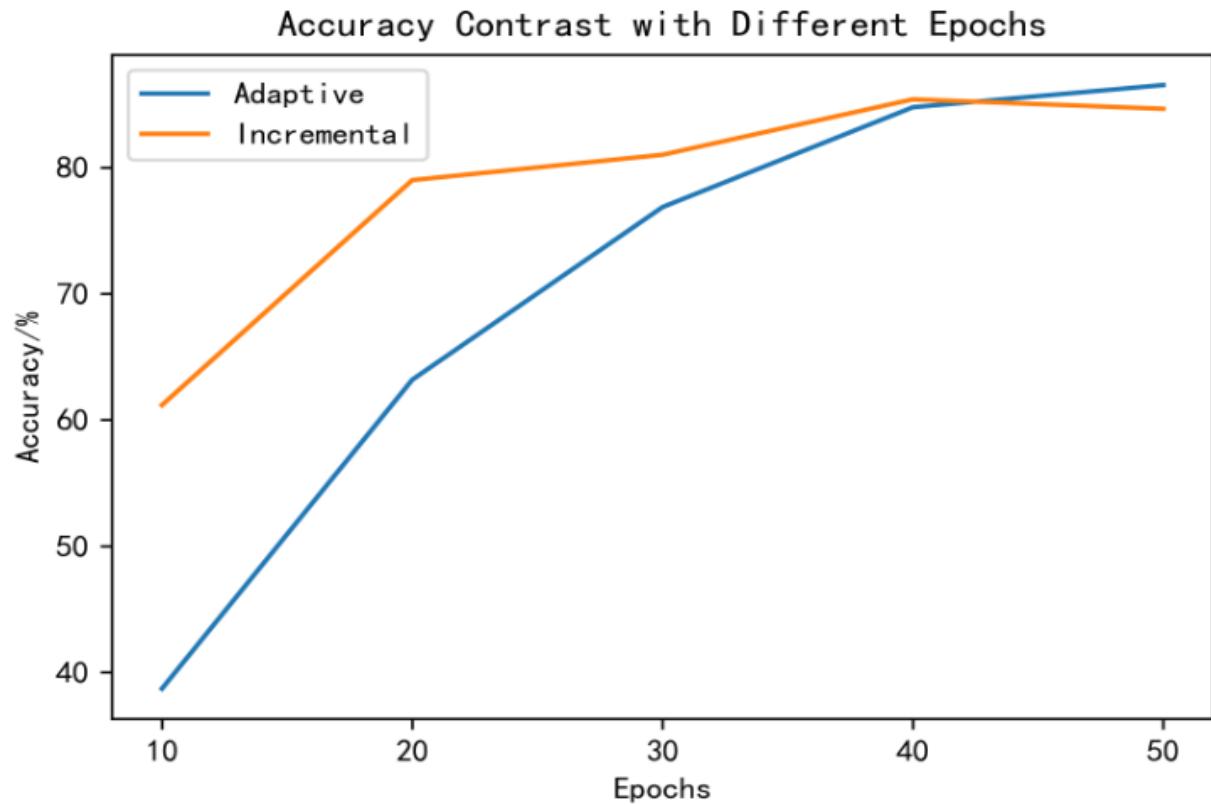
- predicting time is mainly related to the average tree height, PIWA has smaller tree height
- training time of the PIWA increases more steadily with the increase of the epoch, while the Incremental method has a change in slope.



Observations

- With the increase of epoch, the accuracy of Incremental method increases gently.
- When epoch=50, it is overtaken by Adaptive method.
- incremental method is verified to reduce accuracy, though having high accuracy at begining.

Our PIWA is Better!





Adaptive Huffman Code With Buffer

- We just implemented the process of encode and analyzed its performance. The process of decoder can be implemented in the future to make the Adaptive Huffman Code With Buffer complete.
- To truly implement Incremental Learning, we may have to modify the whole structure of the hierarchical softmax model.

Modification on PIWA

- Combine the research on improving the performance of Adaptive Huffman Tree with PIWA.
- To truly implement Incremental Learning, we may have to modify the whole structure of the hierarchical softmax model.



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Thanks For
Listening

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