AI1110 Assignment 1

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EE22BTECH11215

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Question: 10.13.2.12 Sushma tosses a coin 3 times and gets tail each time. Do you think that the outcome of next toss will be a tail? Give reasons. Solution: As the coin is tossed 3 times and gets a tail each time but it is not necessary that 4th time will be a tail. It may be either tail or head in any further toss.

Let X be the random variable for the occarance of tail.

(i) In this binomial distribution, n = 3.

$$\Pr(X = r) = {^{n}C_{r}}p^{r}q^{n-r} \tag{1}$$

where,

$$X \in \{0, 1, 2, 3\}$$
 (2)

$$p = q = \frac{1}{2}$$

$$\Pr(X=3) = {}^{3}C_{3} \left(\frac{1}{2}\right)^{3} \left(\frac{1}{2}\right)^{0} = \frac{1}{8}$$
 (3)

(ii) In this binomial distribution, n = 4.

$$\Pr(X = r) = {^{n}C_{r}}p^{r}q^{n-r} \tag{4}$$

where,

$$X \in \{0, 1, 2, 3, 4\}$$
 (5)

$$p = q = \frac{1}{2}$$

$$\Pr(X=4) = {}^{4}C_{4} \left(\frac{1}{2}\right)^{4} \left(\frac{1}{2}\right)^{0} = \frac{1}{16}$$
 (6)

Comparing from the both cases, Probability of fourth tail on fourth toss = Probability of three tails till third $toss \times \frac{1}{2} = \frac{1}{8} \times \frac{1}{2} = \frac{1}{16}$. Probability of head on fourth toss for first time = Probability of three tails till third $toss \times \frac{1}{2} = \frac{1}{8} \times \frac{1}{2} = \frac{1}{16}$. Clearly, Probability of head and tail on fourth toss for first three tosses being tails is the same = $\frac{1}{16}$. Probability of Head = Tail = $\frac{1}{2}$ in every single case. Hence, the given statement is false.