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$$(1) \quad \dot{k}(t) = A(v(t)k(t))^\alpha (u(t)h(t))^{1-\alpha} - c(t)$$

$$(2) \quad \dot{h}(t) = B((1-v(t))k(t))^\eta ((1-u(t))h(t))^{1-\eta}$$

$$\frac{\dot{k}}{k} = \frac{A v^\alpha k^{\alpha-1} (u h)^{1-\alpha} - c}{k}$$

$$\hat{k} = A v^\alpha u^{1-\alpha} \left( \frac{k}{h} \right)^{\alpha-1} - \chi$$

$$(3) \quad \frac{x_1}{\frac{vk}{uh}} =$$

$$\hat{k} = A x_1^\alpha \frac{uh}{k} - \chi$$

$$(4)$$

$$\hat{h} = B \left[ (1-v) \frac{k}{h} \right]^\eta (1-u)^{1-\eta}$$

$$(5)$$

$$\frac{x_2}{\frac{(1-v)k}{(1-u)h}} =$$

$$\hat{h} = B x_2^\eta (1-u)$$

$$(6)$$

$$H = e^{-\rho t} \frac{c^{1-\sigma}}{1-\sigma} + \gamma_1 (A(vk)^\alpha (uh)^{1-\alpha} - c) + \gamma_2 B[(1-v)k]^\eta [(1-u)h]^{1-\eta}$$

$$(7)$$

$$\frac{\partial H}{\partial c! = 0} \frac{\partial H}{\partial v! = 0} \frac{\partial H}{\partial k! = -\gamma_1} \frac{\partial H}{\partial u! = 0} \frac{\partial H}{\partial h! = -\gamma_2} = 0$$

$$(8)$$

$$\gamma_1 = e^{-\rho t} c^{-\sigma}$$

$$(9)$$

$$\frac{\partial \gamma_1}{\partial t} = \dot{\gamma}_1$$

$$(10)$$

$$\dot{\gamma}_1 = \frac{-e^{-\rho t} \rho c^{-\sigma} - e^{-\rho t} c^{-\sigma-1} \sigma \dot{c}}{e^{-\rho t} c^{-\sigma-1} \sigma \dot{c}}$$

$$(11)$$

$$\dot{\gamma}_1 = -e^{-\rho t} c^{-\sigma} (\rho + \sigma \hat{c}) = -\gamma_1 (\rho + \sigma \hat{c})$$

$$(12)$$

$$\hat{\gamma}_1 = -\rho - \sigma \hat{c}$$

$$(13)$$

$$\gamma_1 A \alpha v^{\alpha-1} k^\alpha (uh)^{1-\alpha} - \gamma_2 B \eta (1-v)^{\eta-1} k^\eta [(1-u)h]^{1-\eta} = 0$$

$$(14)$$

$$\gamma_1 A \alpha v^{\alpha-1} k^\alpha (uh)^{1-\alpha} = \gamma_2 B \eta (1-v)^{\eta-1} k^\eta [(1-u)h]^{1-\eta}$$

$$(15)$$

$$\frac{\gamma_2}{\gamma_1} = \frac{A \alpha v^{\alpha-1} k^\alpha (uh)^{1-\alpha}}{B \eta (1-v)^{\eta-1} k^\eta [(1-u)h]^{1-\eta}}$$

$$(16)$$

$$= \frac{A \alpha \left( \frac{vk}{uh} \right)^{\alpha-1}}{B \eta \left( \frac{(1-v)k}{(1-u)h} \right)^{\eta-1}} = \frac{A \alpha x_1^{\alpha-1}}{B \eta x_2^{\eta-1}}$$

$$\gamma_2 = \gamma_1 \frac{A \alpha \left( \frac{vk}{uh} \right)^{\alpha-1}}{B \eta \left( \frac{(1-v)k}{(1-u)h} \right)^{\eta-1}} \iff \gamma_1 = \gamma_2 \frac{B \eta \left( \frac{(1-v)k}{(1-u)h} \right)^{\eta-1}}{A \alpha \left( \frac{vk}{uh} \right)^{\alpha-1}}$$