

Loggerhead PVA

NRES 421/621

Spring 2020

PVA for loggerhead turtles!

This PVA example shows the use of demographic data in projecting a population into the future. By the time we meet on Tuesday, April 3 be sure that this model is running on your laptop (in InsightMaker) because we will be exploring the model more fully in class together, and we will use this PVA to do some management-relevant **scenario testing**. Also make sure you have run through the Excel exercise- see below!

Constructing a demographic (matrix) model data for loggerhead turtles

If you would like more background information on loggerhead turtles, visit these websites:

USFWS site

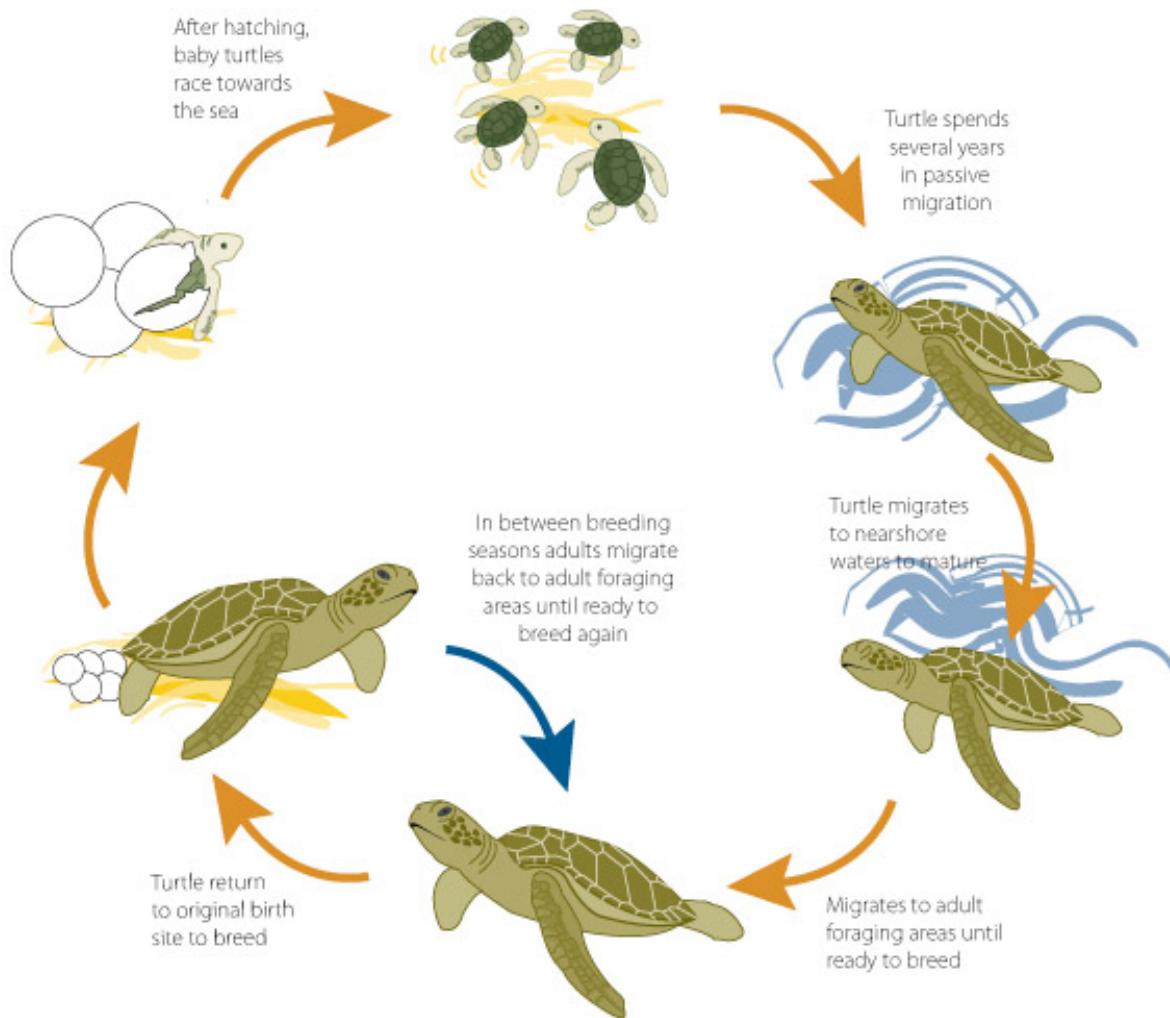
NMFS site

Texas site

Background

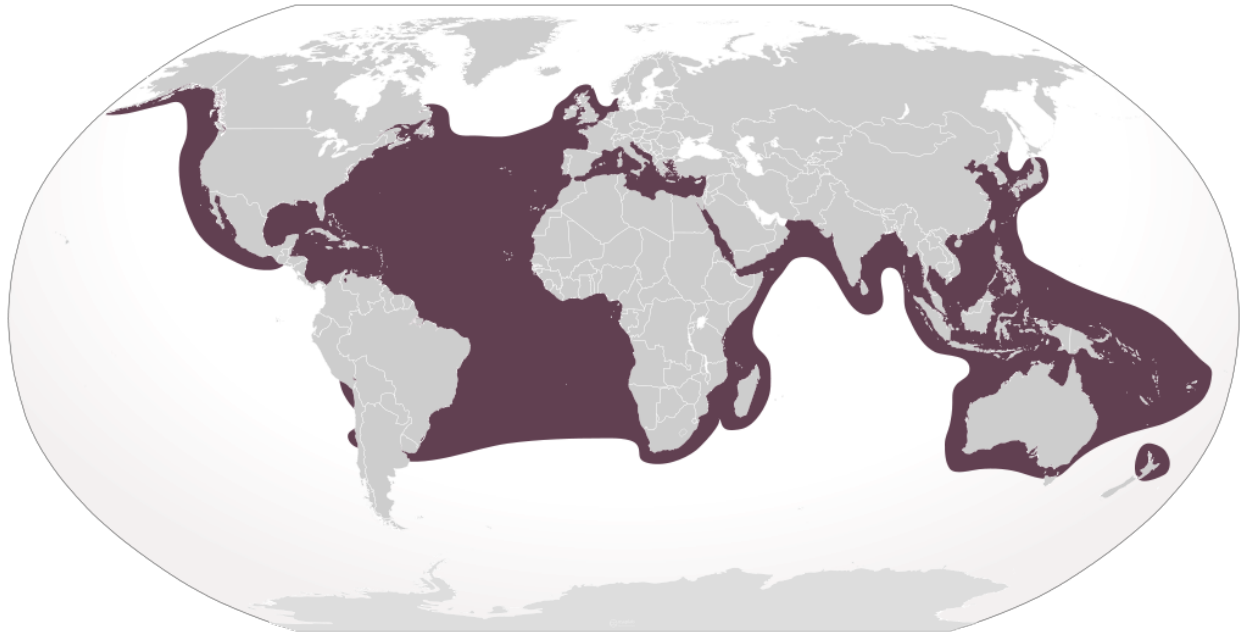


The loggerhead sea turtle, *C. caretta*, is a large marine turtle with a nearly global distribution. Nesting areas in the USA occur along the Atlantic coast from New Jersey to Texas, although individuals may be observed along the Pacific coast and in Hawaii.



The species has been federally listed as ‘threatened’ since 1978. When a species is listed, the Endangered Species Act (ESA) requires that a recovery plan be drafted whose goal is to eventually remove the species from the list.

Loggerheads are listed as “Threatened” under the IUCN Red List.



Threats

Biologists have identified two key types of threats facing loggerheads: alteration of nesting beaches and bycatch from commercial fisheries.

1. Threats to nesting beaches



Adult females lay their eggs (ca. three nests every 2-3 years, up to 190 eggs/nest) on sandy beaches between April and September. Eggs incubate under the sand for about 2 months, and juveniles make a mad dash for the water upon hatching.

Because beaches are popular sites for human recreation and development, arriving female turtles and hatchlings face risks including

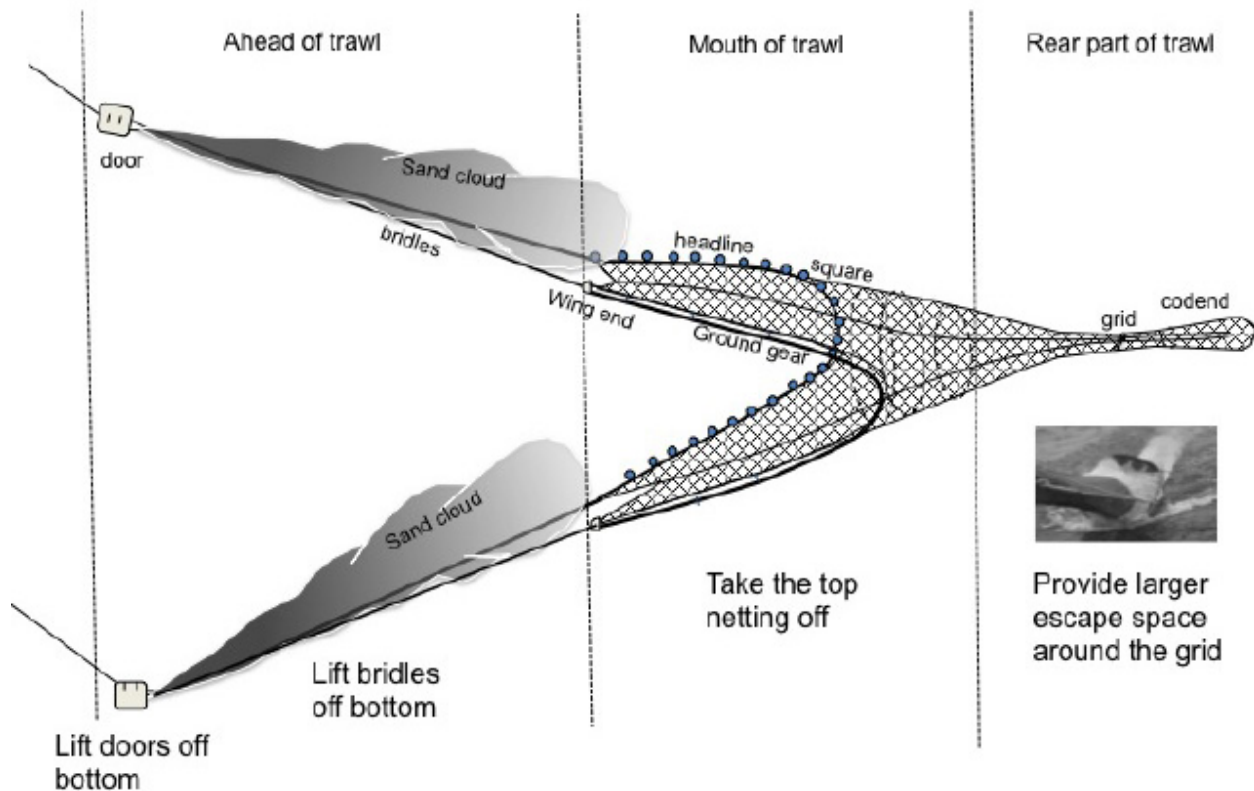
- *poaching* (eggs or adults)
- *beach erosion* or beach fortification to prevent erosion

- *artificial lighting*
- *recreational vehicles*
- ... and many others.

2. Incidental mortality due to marine fisheries

Once hatchlings reach the ocean, they face different threats as they slowly develop to maturity.

- Juveniles (after the sargassum-feeding stage) feed in coastal seagrass mats which are also frequented by shrimp boats and other inshore trawling vessels. Hence *accidental capture* (“bycatch”) and subsequent drowning in the nets and traps used by these vessels is common.



- In addition to these primary threats, sea-going juveniles and adults face mortality due to *bycatch* in longline, hook-and-line, and trap fisheries targeting tuna and other species.

3. Additional threats

- During cold temperatures turtles may go dormant, burying themselves in muddy bays and estuaries. While dormant they can be killed by periodic *dredging* to maintain bays and waterways.
- Human-produced debris (styrofoam peanuts, plastic bags, tar balls, and balloons) may cause *entanglement*, stranding, and drowning.
- Shallow swimming turtles may also collide with *boat propellers*.
- Toxins (*pesticides and heavy metals*) and oil spills may harm turtle physiology and decrease fecundity, but their impact has not been quantified.
- Finally, although rare in the US, *illegal harvest* of eggs as well as subadults and adults for meat, may occur frequently in the coastal Caribbean (Panama, Honduras). Turtle eggs are occasionally seen in open-air markets in Panama.

Step 1: a size-structured model

The loggerhead is a long-lived species – sexual maturity often doesn't occur until animals are almost 30 years of age! The life cycle of the loggerhead is best described by distinct **stage classes** defined by body size (carapace length).

Once turtle life-stages with similar vital rates have been identified, three pieces of data (collectively called *transition rates*) must be collected to construct the stage-structured model:

1. fraction of turtles surviving each year but not advancing to the next larger size-class (often just called 'survival');
2. fraction of turtles surviving each year and advancing to the next larger size-class (often called 'growth'); and
3. average number of hatchlings successfully produced by females of each size-class per year, discounted by the probability of surviving each year (often called 'fecundity').

Step 2: parameterize the model

Transition rates for turtles and other species are often estimated on the basis of *capture-mark-recapture* (CMR) data.

Here are some relevant parameters, from this paper:

Transition from stage 1-2 (hatchling to small juvenile): 0.675

Transition from stage 2-3 (small to large juvenile): 0.047

Transition from stage 3-4 (large juvenile to subadult): 0.019

Transition from stage 4-5 (subadult to adult): 0.061

Transition from stage 2-2 (stay small juvenile): 0.703

Transition from stage 3-3 (stay large juvenile): 0.657

Transition from stage 4-4 (stay subadult): 0.682

Transition from stage 5-5 (stay adult): 0.809

Transition from stage 4-1 (reproduction by subadults): 4.67

Transition from stage 5-1 (reproduction by adults): 61.90

For this model we will assume no stochasticity or uncertainty in any of these parameters.

Step 3: spatial structure

We are not modeling spatial structure, so we can skip this one!

Step 4: simulate!

We can project the loggerhead population into the future using *matrix multiplication*!

We can do this using any number of tools- including R, Excel, or Insightmaker.

See the end of this lecture for a review of matrix population models and how they work.

Since you probably are most familiar with Excel, let's do it in Excel first! Or if you'd like to do it in R instead, I've provided some code to get you started! You can download the R code [here](#)

Population projection in Excel

You can load the base Excel model [here](#)

Build the baseline loggerhead projection matrix

- Your initial spreadsheet should look something like this:

Loggerhead projection matrix (see website for instructions)							
This year							
Next year	H	SJ	LJ	SAd	Ad		[n]0
H	0	0	0	4.665	61.896		2000
SJ	0.675	0.703	0	0	0		500
LJ	0	0.047	0.657	0	0		300
SAd	0	0	0.019	0.682	0		300
Ad	0	0	0	0.061	0.809		20

- Note that the transition rates are already provided for you in the spreadsheet – in the form of a transition matrix!
- NOTE: Wherever a transition is not possible, e.g., from hatchlings to large juveniles, you will see a zero in the transition matrix.

In R, your projection matrix should look like this!

specify projection matrix!

```
projection_matrix <- matrix(
  c(
    0,      0,      0,      4.665,    61.896,
    0.675, 0.703, 0,      0,      0,
    0,      0.047, 0.657, 0,      0,
    0,      0,      0.019, 0.682, 0,
    0,      0,      0,      0.061, 0.809
  )
  ,nrow=5,ncol=5,byrow=T
)

stagenames <- c("Hatchling","Small Juv","Large Juv","Subadult","Adult")
rownames(projection_matrix) <- stagenames
colnames(projection_matrix) <- stagenames
projection_matrix
```

```
##           Hatchling Small Juv Large Juv Subadult Adult
## Hatchling    0.000    0.000    0.000    4.665 61.896
## Small Juv    0.675    0.703    0.000    0.000 0.000
## Large Juv    0.000    0.047    0.657    0.000 0.000
## Subadult     0.000    0.000    0.019    0.682 0.000
## Adult        0.000    0.000    0.000    0.061 0.809
```

Forecast the population into the future in Excel

The projection matrix can be used to project future loggerhead population size assuming the transition probabilities (the F_i , S_i , and G_i) do not change over time.

Let's use the following initial densities in our model!

- 2000 size-class 1 (Hatchlings)
- 500 size-class 2 (Sm. juveniles)
- 300 size-class 3 (Lg. juveniles)
- 300 size-class 4 (Subadults)
- 20 size-class 5 (Adults)

Here's how it looks in R:

```
Abundance_year0 <- c(2000,500,300,300,20) # vector of initial abundances
Abundance_year0
```

```
## [1] 2000 500 300 300 20
```

So your EXCEL file should look something like the one below:

Loggerhead projection matrix (see website for instructions)						
This year						
Next year	H	SJ	LJ	SAd	Ad	[n]0
H	0	0	0	4.665	61.896	2000
SJ	0.675	0.703	0	0	0	500
LJ	0	0.047	0.657	0	0	300
SAd	0	0	0.019	0.682	0	300
Ad	0	0	0	0.061	0.809	20
Year	Hatchling	Sm. Juve	Lg. Juven	Subadult	Adults	[n]total
0	2000	500	300	300	20	3120
1	0					
2						
3						
4						
5						
6						
7						
8						
9						
10						
11						
12						
13						
14						
15						
16						
17						
18						
19						

Using the 'size-distribution vector', we can project the population size of each size-class next year using the matrix formula: $\mathbf{N}_{t+1} = \mathbf{A} \cdot \mathbf{N}_t$. (remember to see below for a refresher of matrix multiplication).

This formula calculates the size distribution next year (i.e., in year $t + 1$) based on the projection matrix \mathbf{A} and the size distribution this year \mathbf{N}_t .

For example, to calculate the first row of $[n]_t + 1$, the number of hatchlings:

$$\text{hatchlings in year 1} = 2000x_0 + 500x_0 + 300x_0 + 300x_{4.665} + 20x_{61.896} = 2637.42$$

We systematically multiply each entry of the first row of the transition matrix $[A]$ by the entries in column $[n]_0$ and sum up these values. The first entry in row 1 is multiplied by the first entry of the column vector. The second entry of row 1 is multiplied by the second entry of the column vector, and so forth, until all 5 entries of row 1 have been accounted for. Let's do this together!

Q: Using actual numbers as for hatchlings above, write out the equation for calculating the number of small juveniles (sm juv) in year 1 based on \mathbf{A} and \mathbf{N}_0 :

Number of small juveniles in year 1 =

Now we can enter formulas in Excel to calculate the stage distribution vector for year 1.

For example, our formula for computing the number of hatchlings in year 1 might look something like this:

$$= B\$4*B12 + C\$4*C12 + D\$4*D12 + E\$4*E12 + F\$4*F12$$

And the projected number of small juveniles (SJ) in year 1 might look like this:

$$= B\$5*B12 + C\$5*C12 + D\$5*D12 + E\$5*E12 + F\$5*F12$$

Q: What is the formula for the projected number of large juveniles in year 1?

Finally, create an additional formula in cells H12-H13 which calculates the total population size in a year (the sum of all size-classes):

In Excel, this will look something like this:

$$=SUM(B12:F12)$$

You should note two things about the formulas:

1. The references to the rows of the $[A]$ matrix should be absolute, i.e., have a '\$' in front of the row number. This is because when we drag these formulas down, we want them to continue to refer to the correct row of the $[A]$ matrix.
2. The references to the size distribution vector should *not* be absolute (should not contain the '\$').

Q: Why? (Hint: what are we going to do with this model?)

ADDITIONAL NOTE: If your data are in different columns and rows than described above, you will not be able to copy the above formulas exactly, as they will not be referring to the proper cells in your file. So make sure your formulas are correct for your particular EXCEL file.

Q: Use your $[A]$ matrix and skills in EXCEL to project the loggerhead population 100 years in the future. This will require dragging formulas down. This is equivalent to iterating (i.e., repeating) the matrix multiplication process 100 times.

Your results should look similar to this (which was done in R):

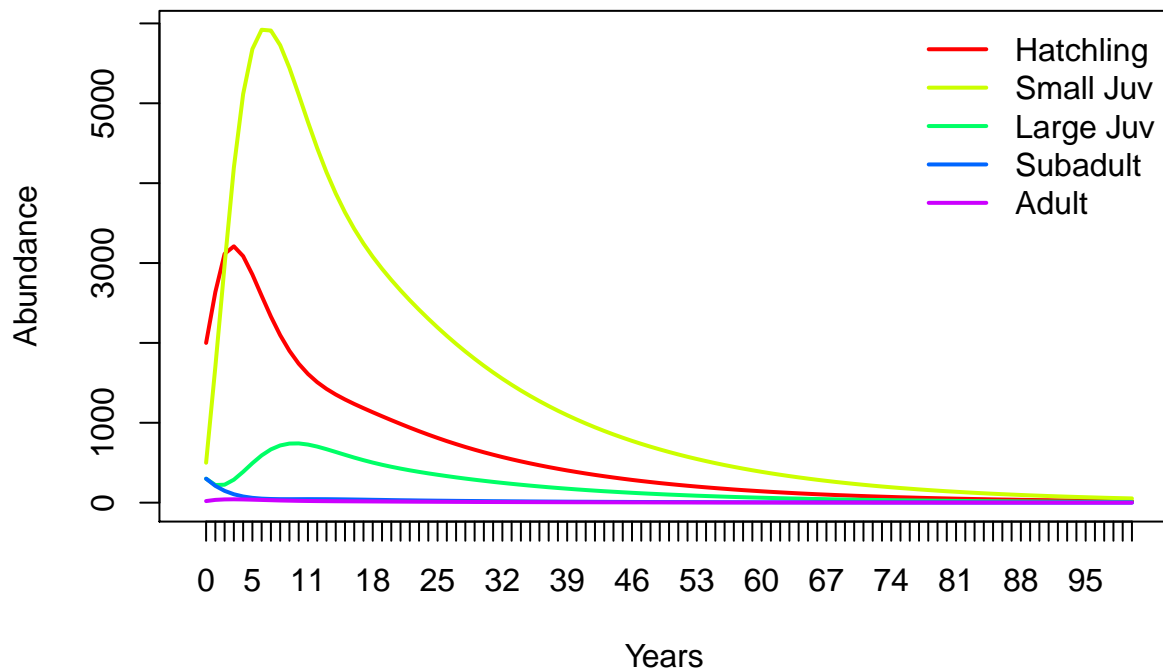
```

# Run the matrix projection model!

nYears <- 100                                # set the number of years to project
TMat <- projection_matrix                     # define the projection matrix
InitAbund <- Abundance_year0                 # define the initial abundance

## NOTE: the code below can be re-used without modification:
allYears <- matrix(0,nrow=nrow(TMat),ncol=nYears+1) # build a storage array for all abundances!
allYears[,1] <- InitAbund # set the year 0 abundance
for(t in 2:(nYears+1)){ # loop through all years
  allYears[,t] <- TMat %*% allYears[,t-1]
}
plot(1,1,pch="",ylim=c(0,max(allYears)),xlim=c(0,nYears+1),xlab="Years",ylab="Abundance",xaxt="n") # s
cols <- rainbow(5) # set up colors to use
for(s in 1:5){
  points(allYears[s,],col=cols[s],type="l",lwd=2) # plot out each life stage abundance, one at a ti
}
axis(1,at=seq(1,nYears+1),labels = seq(0,nYears)) # label the axis
legend("topright",col=cols,lwd=rep(2,3),legend=rownames(TMat),bty="n") # put a legend on the plot

```



Q: Is this model *deterministic* or *stochastic*?

Projecting the loggerhead population in InsightMaker

First, clone the baseline loggerhead PVA model here.

Hit “Simulate”. Make sure that the model results look the same as the above figure! If not, make sure the parameters are correct!

NOTE: here we use the term “survival” to refer to surviving and staying in the same stage class, and “growth” to refer to surviving and moving on to the next life stage.

Look over the model, and make sure that you understand the inner workings!

Group exercise (in class!): loggerhead management

Working in groups of 2-3, investigate four management scenarios for the loggerhead turtle population:

1. Improve fecundity (labeled “Sub Fecundity” and “Adult Fecundity” in the IM model) via *nest-site protection*!
 - Improve fecundity to 1.5X the current value
 - Double fecundity (2X the current value)
2. Improve hatchling survival (labeled “hatchling growth” in the IM model) via *nest monitoring*
 - Improve *to* 90%
 - Improve *to* 100%
3. Improve large juvenile survival (labeled “Lg Juv Surv” in the IM model) using *Turtle Excluder Devices (TEDs)*
 - Increase by 15% (add 0.15 to the existing juvenile survival)
 - Increase by 25% (add 0.25 to the existing juvenile survival)
4. Improve adult/subadult survival (labeled “Sub Surv” and “Adult Surv” in IM) by *restricting longline fisheries*.
 - Increase by 5% (add 0.05 to the existing subadult and adult survival)
 - Increase by 10% (add 0.1 to the existing subadult and adult survival)

For each scenario, consider:

- The short-term outlook (4-6 years out)
- The long-term outlook (100 years out)

Please write down your responses to the following questions::

Question 3.1: What is your management recommendation for this population? Why?

Question 3.2: In the base model, why does the population always seem to grow during the first few years of the simulation, even if it ultimately declines?



Figure 1: turtle excluder device

References

- Mills, L. S., S. G. Hayes, C. Baldwin, M. J. Wisdom, J. Michael, J. Citta, D. J. Mattson, and K. Murphy. 1996. Factors Leading to Different Viability Predictions for a Grizzly Bear Data Set. *Conservation Biology* 10 (3), 863-873. doi: 10.1046/j.1523-1739.1996.10030863.x
- Morris, W. F. and D. F. Doak. 2002. *Quantitative conservation biology: Theory and practice of population viability analysis*. Sinauer, Sunderland, MA.
- Morris, W. F., D. F. Doak, M. Groom, P. Kareiva, J Fieberg, L. Gerber, P. Murphy, D. Thomson. 1999. *A practical handbook for population viability analysis*. The Nature Conservancy, Wash., DC.

REVIEW: matrix population models:

We can present yearly fecundity and survival probabilities compactly in a **projection matrix** $[A]$ which we use to project the population size year to year.

We all remember the finite-population-growth equation:

$$N_{t+1} = \lambda \cdot N_t \quad (\text{Eq. 1}),$$

where N is abundance (as always), t is time, often in years but could be any time units, and λ is the multiplicative growth rate over the time period $t \rightarrow t + 1$

The matrix population growth equation looks pretty much the same!

$$\mathbf{N}_{t+1} = \mathbf{A} \cdot \mathbf{N}_t \quad (\text{Eq. 2}),$$

where \mathbf{N} is a **vector** of abundances (abundance for all stages), and \mathbf{A} is the **transition matrix**, which we have seen before.

We can be more explicit about this if we re-write the above equation this way:

$$\begin{bmatrix} N_1 \\ N_2 \\ N_3 \end{bmatrix}_{t+1} = \begin{bmatrix} 0 & F_2 & F_3 \\ P_{1 \rightarrow 2} & P_{2 \rightarrow 2} & 0 \\ 0 & P_{2 \rightarrow 3} & P_{3 \rightarrow 3} \end{bmatrix} \cdot \begin{bmatrix} N_1 \\ N_2 \\ N_3 \end{bmatrix}_t \quad (\text{Eq. 3})$$

Where $P_{1 \rightarrow 2}$ is the probability of advancing from stage 1 to 2, and F_2 is the **fecundity** of stage 2.

There are three important types of transitions.

- F_i = Fecundities, or the number of new turtles (hatchlings) produced by an average individual of size-class i per year. This is the top row of the transition matrix.
- S_i = Stage Survival, or fraction of size i turtles surviving and staying in the same size-class per year. These are the diagonal elements of the matrix
- G_i = fraction of size i turtles surviving and growing to size-class $i + 1$ per year. These are the subdiagonal elements of the matrix.

NOTE: *fecundity is NOT the same thing as birth rate, b* . What's the difference?

Birth rate, b_t , is the *per-capita rate of offspring production* for stage t

Fecundity, F_t , is the *per-capita rate by which an individual of stage t contributes new offspring to the population at time $t + 1$* . Sounds pretty similar, right? What's the difference??

Fecundity also takes into account the survival rate from t to $t + 1$!! For an adult of stage t to contribute to the next generation, *it must both survive and reproduce!*.

$$F_t = P_{1 \rightarrow 2} \cdot b_{t+1} \quad (\text{Eq. 4})$$

There is a lot we can do with matrix population models. The most obvious one is *projection*:

Projection:

We have already seen the projection equation (Eq. 2, above). Here is how we can implement this in R:

```
Year1 <- projection_matrix %*% Abundance_year0 # matrix multiplication!
```

Let's try it!

First, let's build a *projection matrix*:

```
projection_matrix <- matrix(
  c(
    0,      1.2,  3.1,
    0.4,    0,    0,
    0,      0.75, 0
  ),
  ,nrow=3,ncol=3,byrow=T
)

projection_matrix
```

```
##      [,1] [,2] [,3]
## [1,]  0.0 1.20 3.1
## [2,]  0.4 0.00 0.0
## [3,]  0.0 0.75 0.0
```

Next, let's build an initial abundance vector:

```
Abundance_year0 <- c(1000,0,0)
Abundance_year0
```

```
## [1] 1000    0    0
```

Now we can run the code for real!

```
Year1 <- projection_matrix %*% Abundance_year0 # matrix multiplication!
Year1
```

```
##      [,1]
## [1,]    0
## [2,]  400
## [3,]    0
```

Now we have 300 individuals in stage 2!

Let's project one more year:

```
Year2 <- projection_matrix %*% Year1 # matrix multiplication!
Year2
```

```
##      [,1]
## [1,]  480
## [2,]    0
## [3,]  300
```

Here is some R code to project many years into the future!

```
nYears <- 20 # set the number of years to project
TMat <- projection_matrix # define the projection matrix
InitAbund <- Abundance_year0 # define the initial abundance

## NOTE: the code below can be re-used without modification:
allYears <- matrix(0,nrow=nrow(TMat),ncol=nYears+1) # build a storage array for all abundances!
allYears[,1] <- InitAbund # set the year 0 abundance
for(t in 2:(nYears+1)){ # loop through all years
  allYears[,t] <- TMat %*% allYears[,t-1]
}
plot(1,1,pch="",ylim=c(0,max(allYears)),xlim=c(0,nYears+1),xlab="Years",ylab="Abundance",xaxt="n") # s
cols <- rainbow(3) # set up colors to use
for(s in 1:3){
  points(allYears[s,],col=cols[s],type="l",lwd=2) # plot out each life stage abundance, one at a ti
}
axis(1,at=seq(1,nYears+1),labels = seq(0,nYears)) # label the axis
legend("topleft",col=cols,lwd=rep(2,3),legend=paste("Stage ",seq(1:nrow(TMat)))) # put a legend on the
```

