

Name: Razin Sufian

ID: 22301219

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Lab Assignment 03

Code Explanation

Task 1:

First task is the implementation of merge sort which gives $n \log n$ running time in sorting an array.

Here we used two functions. One to divide the array in small ~~pieces~~ pieces (merge sort). Here by doing recursive call we break the array in small pieces then ~~there two every~~ ~~sort~~ pieces are merged into a single sorted array by merge function.

Task 2:

in this task we found out the max number by ~~dividing~~ the same dividing method we use in merge sort. but here we don't combine the small pieces; we just compare it and keep the max value and return the maximum one after the full iteration by comparing all the numbers. So, here we don't need any merge function

task 3:

here we are given an array, we have to check for every elements how many small numbers are there of that specific number from the right. and this to the count.

There is already $O(n^2)$ solution given in the question. I am presenting a $O(n \log n)$ solution.

Solution:-

1. First I sorted the array
using merge-sort
→ sorted-array

2.

the I ran a loop in to
the give array. ~~find that~~

~~sum each number~~

let it is i .

It will find i in the
sorted array using binary
search; and the returned
index number of it will
add to the count.

basically

$$\text{count} += \text{len}(array) - (\text{len}(array) - \text{indx})$$

Ex:

② 7 4 1 5 6 8 3

1 ^{ind=1} ② 3 4 5 6 7 8

$$9 - (9 - 1) \\ = 1 = \text{ind}$$

→ pop after founding each
count. So: ~~is~~ for 7 the
arrays will be

Task 4:

In this task from the given array we have to find the maximum possible of

$$A[i] + A[j] \quad ; \quad 1 \leq i < j \leq N$$

Steps:

First I converted the array into tuple which contains the square of it and the 2nd element contains the index number. Then I sorted the array using the 1st element of the tuple using merged sort.

Ex:

-5 -2 -6 -7 -1 8 2

top = (25, 0), (4, 1), (36, 2),
(49, 3), (1, 4), (64, 5)
(4, 6)

top = (1, 4), (4, 1), (4, 6), ~~(36, 2)~~.
(25, 0), (36, 2), (49, 3),
(64, 5)

Then create two pointers i and j

i = 0

j = len(arr) - 1

while $i < j$:

if $[j] [i] \geq i$:

$j = i$

it means if the index of
a maximum squared value is
less than or equal to i
then we move on to the
next maximum squared value.

as ~~to~~ $i > j$:

the saving the maximum each
time .

it's running time is $O(n \log n)$

Task 5

~~it~~ \rightarrow

$task$ is the

implementation of Quick sort

Here we use two function.

one for determining the area
of partition (start, end)

and other will create the
partition.

in partition we consider
the utmost element as the
pivot. All the elements to
its left is smaller and
to its right is greater
than the pivot.

by recursively doing the partition
we get the sorted array, which
running time is $O(n \log n)$,
but worst case, (if array
is sorted) ; time is $O(n^2)$

Task 6:

here we are just finding
the index number of an
element using partition.

here the same code as
quick sort ~~but there we~~
~~don't swap~~

Steps:

find the index of K

1. choose a pivot elem from the list

2. Partition the list

3. if the pivot's position is K , return pivot

4. if K is less than the pivot's position recursively apply the method to the left sub array

5. If k is greater than
than the pivot then doing
for recursion to the right