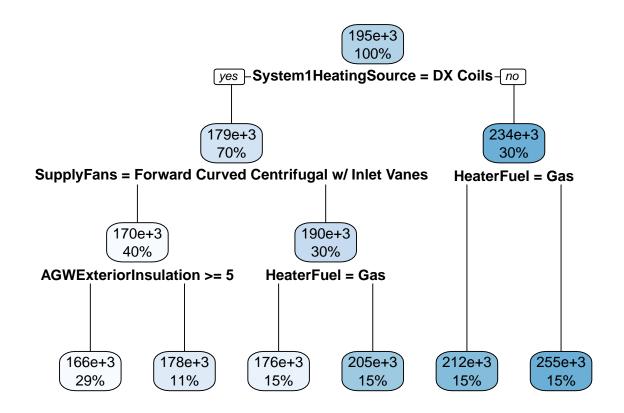
## Regression Trees for RET Project Rev.1 (Response variable - GWP)

### 07/05/2023

```
#Importing the necessary libraries
library(rpart)
library(rpart.plot)
##Reading the updated spreadsheet
dfgwp <- readxl::read_xlsx("C:/Users/jaiva/OneDrive/Documents/RET - GWP Output.xlsx")</pre>
##Defining the categorical variables
RoofExtFinish <- as.factor(dfgwp$RoofExtFinish)</pre>
AGWExtFinish <- as.factor(dfgwp$AGWExtFinish)
GlassCategory <- as.factor(dfgwp$GlassCategory)</pre>
GlassTypeEmissivity <- as.factor(dfgwp$GlassTypeEmissivity)</pre>
FrameType <- as.factor(dfgwp$FrameType)</pre>
System1HeatingSource <- as.factor(dfgwp$System1HeatingSource)</pre>
System1SystemType <- as.factor(dfgwp$System1SystemType)</pre>
SupplyFans <- as.factor(dfgwp$SupplyFans)</pre>
HeaterFuel <- as.factor(dfgwp$HeaterFuel)</pre>
HeaterType <- as.factor(dfgwp$HeaterType)</pre>
model2 <- rpart(formula = GWP~.,</pre>
                 data = dfgwp,
                 method = 'anova',)
##Fitting the initial tree
rpart.plot(model2)
```



### summary(model2)

```
## Call:
## rpart(formula = GWP ~ ., data = dfgwp, method = "anova")
##
##
             CP nsplit rel error
                                     xerror
                     0 1.0000000 1.0322501 0.18041872
## 1 0.55412275
## 2 0.11824492
                     1 0.4458773 0.4715404 0.10623933
## 3 0.06579178
                     2 0.3276323 0.4174949 0.08872683
                     3 0.2618406 0.3550122 0.07976947
## 4 0.05826506
## 5 0.01085387
                     4 0.2035755 0.2455157 0.05483341
                     5 0.1927216 0.2456111 0.05483084
## 6 0.01000000
##
## Variable importance
##
     System1HeatingSource
                                       HeaterFuel
                                                               SupplyFans
##
## RoofExteriorInsulation
                                 {\tt AGWAdlInsulation}
                                                        RoofAdlInsulation
##
##
        System1SystemType
                            AGWExteriorInsulation
##
##
## Node number 1: 80 observations,
                                       complexity param=0.5541227
     mean=195012.5, MSE=1.145662e+09
##
     left son=2 (56 obs) right son=3 (24 obs)
##
     Primary splits:
##
```

```
##
         System1HeatingSource splits as LR,
                                                improve=0.5541227, (0 missing)
##
         RoofExtFinish
                              splits as LRRL, improve=0.3778275, (0 missing)
##
         AGWExtFinish
                              splits as RRLL, improve=0.3778275, (0 missing)
                              splits as LRLR, improve=0.3778275, (0 missing)
##
         FrameType
         SupplyFans
##
                              splits as LRR, improve=0.3778275, (0 missing)
##
## Node number 2: 56 observations,
                                       complexity param=0.06579178
     mean=178517.9, MSE=3.512497e+08
##
##
     left son=4 (32 obs) right son=5 (24 obs)
##
     Primary splits:
##
         SupplyFans
                          splits as
                                     LRR,
                                                  improve=0.3065592, (0 missing)
##
         RoofExtFinish
                                                  improve=0.3065592, (0 missing)
                          splits as
                                     LRRL,
                          splits as
##
         AGWExtFinish
                                     RRLL,
                                                  improve=0.3065592, (0 missing)
                                                  improve=0.3065592, (0 missing)
##
         FrameType
                          splits as
                                    LRLR,
##
         AGWAdlInsulation < 17
                                                  improve=0.2152182, (0 missing)
                                   to the left,
##
     Surrogate splits:
##
         RoofExteriorInsulation < 5</pre>
                                          to the right, agree=0.911, adj=0.792, (0 split)
##
         AGWAdlInsulation
                                 < 12
                                          to the left, agree=0.893, adj=0.750, (0 split)
##
         RoofAdlInsulation
                                          to the right, agree=0.804, adj=0.542, (0 split)
                                 < 20
##
         System1SystemType
                                 splits as RL,
                                                        agree=0.786, adj=0.500, (0 split)
##
         HeaterFuel
                                 splits as LR,
                                                        agree=0.786, adj=0.500, (0 split)
##
## Node number 3: 24 observations,
                                       complexity param=0.1182449
     mean=233500, MSE=8.831667e+08
##
     left son=6 (12 obs) right son=7 (12 obs)
##
##
     Primary splits:
##
         HeaterFuel
                                 splits as RL,
                                                        improve=0.51129930, (0 missing)
         {\tt GlassTypeThickness}
                                 < 0.1875 to the right, improve=0.04662043, (0 missing)
##
                                 < 0.375 to the right, improve=0.04662043, (0 missing)
##
         GlassTypeSpacing
                                                        improve=0.03963798, (0 missing)
##
         GlassTypeEmissivity
                                 splits as LR,
##
         CeilingsBattInsulation < 10.5
                                        to the left, improve=0.03635906, (0 missing)
##
##
  Node number 4: 32 observations,
                                       complexity param=0.01085387
     mean=169531.2, MSE=6.043652e+07
##
##
     left son=8 (23 obs) right son=9 (9 obs)
##
     Primary splits:
##
         AGWExteriorInsulation < 5
                                          to the right, improve=0.51437750, (0 missing)
##
         GlassCategory
                                                        improve=0.24897530, (0 missing)
                                 splits as LLRL,
##
         GlassTypeSpacing
                                 < 0.125 to the right, improve=0.24897530, (0 missing)
##
                                 < 5
                                          to the right, improve=0.18374240, (0 missing)
         AGWAdlInsulation
##
         RoofExteriorInsulation < 32.5
                                          to the left, improve=0.09816278, (0 missing)
##
                                       complexity param=0.05826506
## Node number 5: 24 observations,
     mean=190500, MSE=4.8775e+08
##
     left son=10 (12 obs) right son=11 (12 obs)
##
##
     Primary splits:
##
         HeaterFuel
                                 splits as RL,
                                                        improve=0.45619060, (0 missing)
##
         CeilingsBattInsulation < 10.5
                                                        improve=0.11790250, (0 missing)
                                          to the left,
##
         AGWAdlInsulation
                                 < 16
                                          to the left,
                                                        improve=0.04464947, (0 missing)
                                          to the right, improve=0.03418475, (0 missing)
##
         RoofExteriorInsulation < 2
##
         RoofAdlInsulation
                                          to the right, improve=0.03012700, (0 missing)
                                 < 9.5
##
## Node number 6: 12 observations
     mean=212250, MSE=3.708542e+08
```

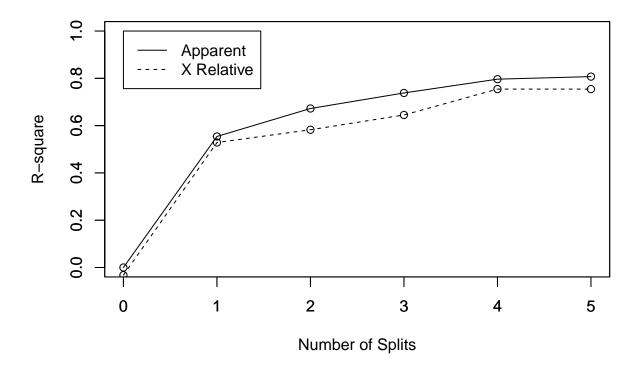
```
##
## Node number 7: 12 observations
     mean=254750, MSE=4.923542e+08
##
##
## Node number 8: 23 observations
     mean=166043.5, MSE=1.725898e+07
##
##
## Node number 9: 9 observations
##
     mean=178444.4, MSE=6.024691e+07
##
## Node number 10: 12 observations
     mean=175583.3, MSE=2.120764e+08
##
##
## Node number 11: 12 observations
     mean=205416.7, MSE=3.184097e+08
plotcp(model2)
```

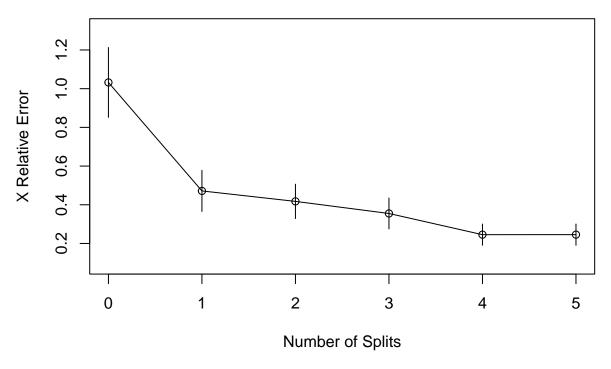
### size of tree 2 3 1 5 6 X-val Relative Error 1.0 0.8 9.0 0.4 0.2 0.26 Inf 0.088 0.062 0.025 0.01 ср

# #Plotting the r-squared value for initial fitted tree for GWP as response rsq.rpart(model2)

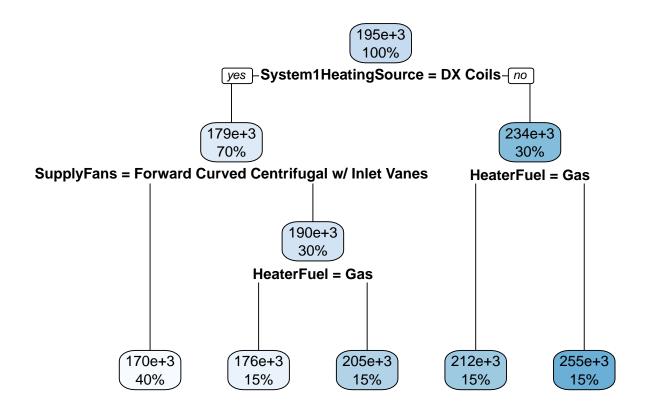
```
##
## Regression tree:
## rpart(formula = GWP ~ ., data = dfgwp, method = "anova")
##
## Variables actually used in tree construction:
## [1] AGWExteriorInsulation HeaterFuel SupplyFans
```

```
## [4] System1HeatingSource
##
## Root node error: 9.1653e+10/80 = 1145662344
##
## n= 80
##
           CP nsplit rel error xerror
##
                       1.00000 1.03225 0.180419
## 1 0.554123
## 2 0.118245
                   1
                       0.44588 0.47154 0.106239
                       0.32763 0.41749 0.088727
## 3 0.065792
                   2
## 4 0.058265
                       0.26184 0.35501 0.079769
## 5 0.010854
                       0.20358 0.24552 0.054833
## 6 0.010000
                       0.19272 0.24561 0.054831
```





```
#Pruning the initial tree
pruned.tree2 <- prune(model2, cp = model2$cptable[which.min(model2$cptable[,"xerror"]),"CP"])</pre>
printcp(pruned.tree2)
##
## Regression tree:
## rpart(formula = GWP ~ ., data = dfgwp, method = "anova")
##
## Variables actually used in tree construction:
## [1] HeaterFuel
                                                  System1HeatingSource
                             SupplyFans
##
## Root node error: 9.1653e+10/80 = 1145662344
##
## n = 80
##
##
           CP nsplit rel error xerror
## 1 0.554123
                   0
                       1.00000 1.03225 0.180419
## 2 0.118245
                       0.44588 0.47154 0.106239
                   1
## 3 0.065792
                   2
                       0.32763 0.41749 0.088727
## 4 0.058265
                   3
                       0.26184 0.35501 0.079769
## 5 0.010854
                   4
                       0.20358 0.24552 0.054833
#Plotting the pruned tree
rpart.plot(pruned.tree2)
```



```
#The pruned tree is same as the initially fitted tree
printcp(pruned.tree2)
```

```
##
## Regression tree:
## rpart(formula = GWP ~ ., data = dfgwp, method = "anova")
## Variables actually used in tree construction:
## [1] HeaterFuel
                                                 System1HeatingSource
                            SupplyFans
##
## Root node error: 9.1653e+10/80 = 1145662344
## n= 80
##
           CP nsplit rel error xerror
##
## 1 0.554123
                   0 1.00000 1.03225 0.180419
                       0.44588 0.47154 0.106239
## 2 0.118245
                   1
## 3 0.065792
                   2 0.32763 0.41749 0.088727
## 4 0.058265
                   3
                       0.26184 0.35501 0.079769
## 5 0.010854
                       0.20358 0.24552 0.054833
pruned.tree2
## n=80
```

## node), split, n, deviance, yval

\* denotes terminal node

```
##
##
  1) root 80 91652990000 195012.5
     2) System1HeatingSource=DX Coils 56 19669980000 178517.9
##
##
       4) SupplyFans=Forward Curved Centrifugal w/ Inlet Vanes 32 1933969000 169531.2 *
       5) SupplyFans=Two-Speed, Variable 24 11706000000 190500.0
##
        10) HeaterFuel=Gas 12 2544917000 175583.3 *
##
##
        3) System1HeatingSource=Electric Resistance 24 21196000000 233500.0
##
       6) HeaterFuel=Gas 12 4450250000 212250.0 *
##
       7) HeaterFuel=Electricity 12 5908250000 254750.0 *
##
```