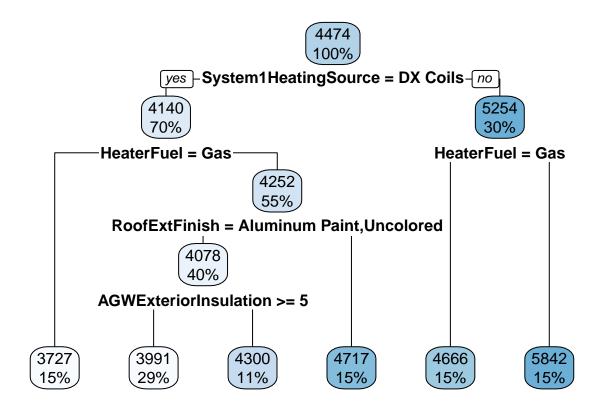
## Regression Tress for RET Project Rev.1 (Response Variable - kWh/year)

07/05/2023

```
#Importing necessary libraries
library(rpart)
library(rpart.plot)
library(ggplot2)
library(readxl)
#Importing the updated spreadsheet
df <- read_xlsx("C:/Users/jaiva/OneDrive/Documents/RET - Cost Output.xlsx")</pre>
#Defining the categorical variables as factors
RoofExtFinish <- as.factor(df$RoofExtFinish)</pre>
AGWExtFinish <- as.factor(df$AGWExtFinish)
GlassCategory <- as.factor(df$GlassCategory)</pre>
GlassTypeEmissivity <- as.factor(df$GlassTypeEmissivity)</pre>
FrameType <- as.factor(df$FrameType)</pre>
System1HeatingSource <- as.factor(df$System1HeatingSource)</pre>
System1SystemType <- as.factor(df$System1SystemType)</pre>
SupplyFans <- as.factor(df$SupplyFans)</pre>
HeaterFuel <- as.factor(df$HeaterFuel)</pre>
HeaterType <- as.factor(df$HeaterType)</pre>
model1 <- rpart(formula = kWhperyear ~.,</pre>
                 data = df,
                 method ='anova')
##Plotting the initial fitted tree
rpart.plot(model1)
```



## summary(model1)

```
## Call:
## rpart(formula = kWhperyear ~ ., data = df, method = "anova")
##
##
             CP nsplit rel error
## 1 0.49440119
                     0 1.0000000 1.0183826 0.16747418
                     1 0.5055988 0.5344511 0.10308917
## 2 0.19665421
## 3 0.07309843
                     2 0.3089446 0.3386701 0.06985099
## 4 0.01464606
                     4 0.1627477 0.1964131 0.04910081
## 5 0.01000000
                     5 0.1481017 0.1817688 0.04885274
##
## Variable importance
##
     System1HeatingSource
                                      HeaterFuel
                                                           RoofExtFinish
##
                                                                        8
## RoofExteriorInsulation
                                AGWAdlInsulation
                                                              HeaterType
##
##
        System1SystemType
                               RoofAdlInsulation
                                                   AGWExteriorInsulation
##
                                                3
##
                                      complexity param=0.4944012
## Node number 1: 80 observations,
##
     mean=4474.154, MSE=527589
     left son=2 (56 obs) right son=3 (24 obs)
##
##
     Primary splits:
         System1HeatingSource splits as LR,
                                                improve=0.4944012, (0 missing)
##
```

```
splits as LRRL, improve=0.1982518, (0 missing)
##
         RoofExtFinish
##
         AGWExtFinish
                              splits as RRLL, improve=0.1982518, (0 missing)
                              splits as
##
         FrameType
                                         LRLR, improve=0.1982518, (0 missing)
##
                              splits as LRR, improve=0.1982518, (0 missing)
         SupplyFans
##
## Node number 2: 56 observations,
                                      complexity param=0.07309843
     mean=4139.805, MSE=168782.1
##
     left son=4 (12 obs) right son=5 (44 obs)
##
##
     Primary splits:
##
                                                        improve=0.27546600, (0 missing)
         HeaterFuel
                                splits as RL,
##
         RoofExteriorInsulation < 2
                                          to the right, improve=0.06898060, (0 missing)
                                                        improve=0.04764771, (0 missing)
##
         HeaterType
                                splits as RL,
##
         AGWAdlInsulation
                                < 17
                                         to the left,
                                                        improve=0.03616048, (0 missing)
##
         RoofExtFinish
                                                        improve=0.03012129, (0 missing)
                                splits as LRRL,
##
## Node number 3: 24 observations,
                                      complexity param=0.1966542
##
     mean=5254.3, MSE=495336.3
##
     left son=6 (12 obs) right son=7 (12 obs)
##
     Primary splits:
##
         HeaterFuel
                               splits as RL,
                                                       improve=0.69819640, (0 missing)
##
         GlassTypeThickness
                               < 0.1875 to the right, improve=0.04019332, (0 missing)
##
         GlassTypeSpacing
                               < 0.375 to the right, improve=0.04019332, (0 missing)
         AGWExteriorInsulation < 15.75 to the right, improve=0.03341331, (0 missing)
##
##
         AGWExtFinish
                               splits as RL--,
                                                       improve=0.02313160, (0 missing)
##
## Node number 4: 12 observations
##
     mean=3726.917, MSE=63431.46
##
## Node number 5: 44 observations,
                                      complexity param=0.07309843
     mean=4252.411, MSE=138340.3
##
##
     left son=10 (32 obs) right son=11 (12 obs)
##
     Primary splits:
##
         RoofExtFinish
                                splits as LRRL,
                                                        improve=0.5859889, (0 missing)
##
         AGWExtFinish
                                                        improve=0.5859889, (0 missing)
                                splits as RRLL,
##
         FrameType
                                splits as
                                           LRLR,
                                                        improve=0.5859889, (0 missing)
##
                                                        improve=0.5859889, (0 missing)
         SupplyFans
                                splits as LRR,
##
         RoofExteriorInsulation < 2
                                         to the right, improve=0.3689811, (0 missing)
##
     Surrogate splits:
##
         RoofExteriorInsulation < 5
                                         to the right, agree=0.886, adj=0.583, (0 split)
##
         AGWAdlInsulation
                                         to the left, agree=0.864, adj=0.500, (0 split)
                                < 12
##
         System1SystemType
                                                        agree=0.864, adj=0.500, (0 split)
                                splits as RL,
                                                        agree=0.864, adj=0.500, (0 split)
##
         HeaterType
                                splits as RL,
         RoofAdlInsulation
                                         to the right, agree=0.841, adj=0.417, (0 split)
##
                                < 1.5
##
## Node number 6: 12 observations
     mean=4666.217, MSE=184247.1
##
##
## Node number 7: 12 observations
##
     mean=5842.383, MSE=114741.4
##
## Node number 10: 32 observations,
                                       complexity param=0.01464606
    mean=4078.056, MSE=37632.89
##
##
     left son=20 (23 obs) right son=21 (9 obs)
##
    Primary splits:
```

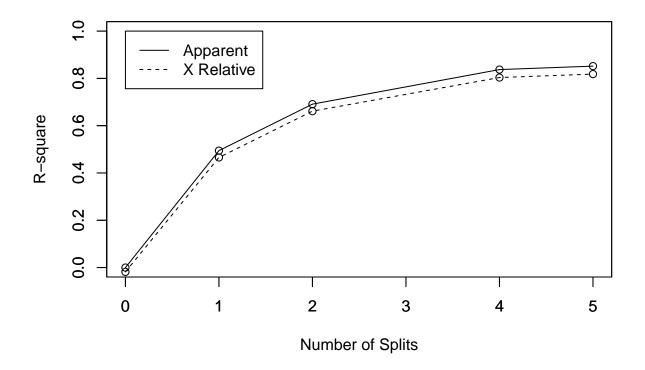
```
to the right, improve=0.5133211, (0 missing)
##
         AGWExteriorInsulation < 5
##
         GlassTypeSpacing
                                < 0.125 to the right, improve=0.2290074, (0 missing)
                                                       improve=0.2290074, (0 missing)
##
         GlassCategory
                                splits as LLRL,
##
         AGWAdlInsulation
                                < 5
                                         to the right, improve=0.1784729, (0 missing)
                                         to the right, improve=0.1022451, (0 missing)
##
         CeilingsBattInsulation < 20
##
## Node number 11: 12 observations
     mean=4717.358, MSE=109651.8
##
##
## Node number 20: 23 observations
##
     mean=3991.113, MSE=10308.62
##
## Node number 21: 9 observations
    mean=4300.244, MSE=38776.21
#Plotting the cp for the initial fitted tree
plotcp(model1)
```

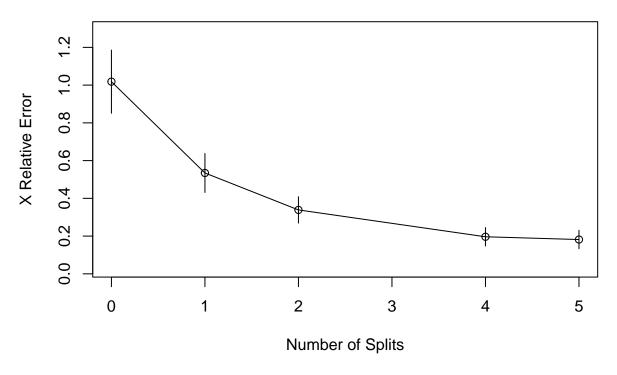
## size of tree 2 3 1 5 6 1.0 X-val Relative Error 0.8 9.0 0.4 0.2 0.0 Inf 0.31 0.12 0.033 0.012 ср

```
##Plotting the r-square value of the initial fitted tree
rsq.rpart(model1)
```

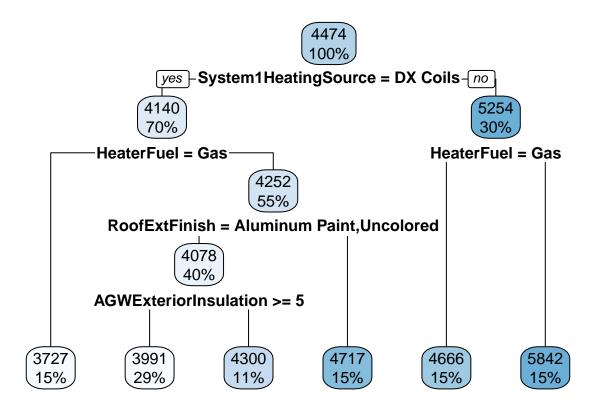
```
##
## Regression tree:
## rpart(formula = kWhperyear ~ ., data = df, method = "anova")
##
## Variables actually used in tree construction:
## [1] AGWExteriorInsulation HeaterFuel RoofExtFinish
```

```
## [4] System1HeatingSource
##
## Root node error: 42207122/80 = 527589
##
## n= 80
##
           CP nsplit rel error xerror
##
                       1.00000 1.01838 0.167474
## 1 0.494401
## 2 0.196654
                       0.50560 0.53445 0.103089
                   1
## 3 0.073098
                       0.30894 0.33867 0.069851
                   2
                       0.16275 0.19641 0.049101
## 4 0.014646
## 5 0.010000
                       0.14810 0.18177 0.048853
```



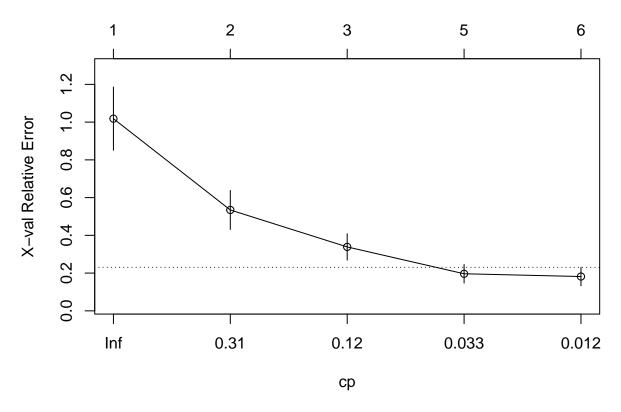


```
#Pruning the tree using minimum cp parameter
pruned.tree <- prune(model1, cp = model1$cptable[which.min(model1$cptable[,"xerror"]),"CP"])</pre>
printcp(pruned.tree)
##
## Regression tree:
## rpart(formula = kWhperyear ~ ., data = df, method = "anova")
##
## Variables actually used in tree construction:
## [1] AGWExteriorInsulation HeaterFuel
                                                    RoofExtFinish
## [4] System1HeatingSource
##
## Root node error: 42207122/80 = 527589
##
## n= 80
##
##
           CP nsplit rel error xerror
                                            xstd
## 1 0.494401
                   0
                       1.00000 1.01838 0.167474
## 2 0.196654
                   1
                       0.50560 0.53445 0.103089
## 3 0.073098
                       0.30894 0.33867 0.069851
## 4 0.014646
                   4
                       0.16275 0.19641 0.049101
## 5 0.010000
                   5
                       0.14810 0.18177 0.048853
#Plotting the pruned tree
rpart.plot(pruned.tree)
```



#The pruned tree is same as the initially fitted tree
plotcp(pruned.tree)





## pruned.tree

```
## n= 80
##
## node), split, n, deviance, yval
##
        * denotes terminal node
##
##
   1) root 80 42207120.0 4474.154
##
     2) System1HeatingSource=DX Coils 56 9451800.0 4139.805
       4) HeaterFuel=Gas 12
##
                            761177.5 3726.917 *
##
       5) HeaterFuel=Electricity 44 6086973.0 4252.411
        10) RoofExtFinish=Aluminum Paint, Uncolored 32 1204252.0 4078.056
##
##
          20) AGWExteriorInsulation>=5 23
                                          237098.3 3991.113 *
##
          21) AGWExteriorInsulation< 5 9
                                         348985.9 4300.244 *
##
        ##
     3) System1HeatingSource=Electric Resistance 24 11888070.0 5254.300
       6) HeaterFuel=Gas 12 2210965.0 4666.217 *
##
##
       7) HeaterFuel=Electricity 12 1376897.0 5842.383 *
```