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MACHINE
    M36
SEES
    C35
VARIABLES
    MULTISETS
    LINKS
INVARIANTS
    inv1 : MULTISETS \subseteq TYPES \times N \times SYMBOLS \times N
            : LINKS ⊆ TYPES × N × TYPES × N
EVENTS
    INITIALISATION ≜
    STATUS
      ordinary
    BEGIN
              : MULTISETS = \{(t1 \mapsto 1 \mapsto a \mapsto 2), (t1 \mapsto 1 \mapsto t_2 \mapsto 1), (t1 \mapsto 1 \mapsto t_3 \mapsto 1), (t1 \mapsto 1 \mapsto s \mapsto 1), (t3 \mapsto 1 \mapsto a \mapsto 1)\}
     act2 : LINKS = \{(t1 \mapsto 1 \mapsto t4 \mapsto 1), (t1 \mapsto 1 \mapsto t5 \mapsto 1), (t2 \mapsto 1 \mapsto t4 \mapsto 1), (t2 \mapsto 1 \mapsto t5 \mapsto 1), (t0 \mapsto 1 \mapsto t3 \mapsto 1)\}
    STATUS
     ordinary
    ANY
     multiset
     cell_no
    WHERE
     grd1
                    multiset ⊆ MULTISETS
      grd2
                    cell_no ∈ N
      grd3
                    multiset(t1 \mapsto cell_no \mapsto a)=2
              .
      grd4
                    multiset(t1 \mapsto cell_no \mapsto t_3)>0
    THEN
                    MULTISETS = (MULTISETS U
                     (t1 \mapsto cell\_no \mapsto a \mapsto (multiset(t1 \mapsto cell\_no \mapsto a) - 1)),
                     (t1 \mapsto cell\_no \mapsto t\_3 \mapsto (multiset(t1 \mapsto cell\_no \mapsto t\_3) - 1))
      act1
                     (t1 \mapsto cell\_no \mapsto a \mapsto (multiset(t1 \mapsto cell\_no \mapsto a))),
                     (t1 \mapsto cell\_no \mapsto t\_3 \mapsto (multiset(t1 \mapsto cell\_no \mapsto t\_3)))
                   LINKS = LINKS \cup {(t1 \mapsto 1 \mapsto t2 \mapsto 1)}
     act2
    END
    STATUS
     ordinary
    ANY
     multiset
     cell no
    WHERE
      grd1
                    multiset \subseteq MULTISETS
      grd2
                    cell_no ∈ N
      grd3
                    multiset(t1 \rightarrow cell_no \rightarrow a)=2
      grd4
                    multiset(t1 \rightarrow cell_no \rightarrow t_2)>0
    THEN
                    MULTISETS = (MULTISETS U
                     (t1 \mapsto cell_no \mapsto a \mapsto (multiset(t1 \mapsto cell_no \mapsto a) - 1)),
                     (t1 \mapsto cell\_no \mapsto t\_2 \mapsto (multiset(t1 \mapsto cell\_no \mapsto t\_2) - 1))
                    })
      act1
                     (t1 \mapsto cell \ no \mapsto a \mapsto (multiset(t1 \mapsto cell \ no \mapsto a))),
                     (t1 \mapsto cell\_no \mapsto t\_2 \mapsto (multiset(t1 \mapsto cell\_no \mapsto t\_2)))
      act2 : LINKS = LINKS \cup {(t1 \mapsto 1 \mapsto t3 \mapsto 1)}
    END
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STATUS
  ordinary
ANY
 multiset
  cell_no
  link
WHERE
                multiset ⊆ MULTISETS
  grd1
                cell no ∈ N
  grd2
  grd3
                multiset(t1 \mapsto cell_no \mapsto s)=1
                multiset(t1 \mapsto cell_no \mapsto t_2)=1
  grd4
                 multiset(t1 \mapsto cell_no \mapsto t_3)=0
  grd5
           :
  grd6
                 link ⊆ LINKS
                link(t1 \rightarrow 1 \rightarrow t2)=1
  grd7
THEN
                 MULTISETS = ( MULTISETS U
                 (t1 \mapsto cell\_no \mapsto s \mapsto (multiset(t1 \mapsto cell\_no \mapsto s) - 1)),
                 (t1 \mapsto cell\_no \mapsto tt\_3 \mapsto 1),
                 (t2 \mapsto 1 \mapsto a \mapsto 1)
  act1
                 })
                 (t1 \mapsto cell\_no \mapsto s \mapsto (multiset(t1 \mapsto cell\_no \mapsto s)))
END
T1_strateg2_R2 ≜
STATUS
 ordinary
ANY
 multiset
  cell_no
 link
WHERE
  grd1
                multiset ⊆ MULTISETS
  grd2
                cell_no ∈ N
  grd3
                multiset(t1 \mapsto cell_no \mapsto s)=1
  grd4
                multiset(t1 \mapsto cell_no \mapsto t_3)=1
                multiset(t1 \mapsto cell_no \mapsto t_2)=0
  grd5
  grd7
           :
                link ⊆ LINKS
  grd6
                link(t1 \rightarrow 1 \rightarrow t3)=1
THEN
                 MULTISETS = (MULTISETS U
                 (\texttt{t1} \; \mapsto \; \texttt{cell\_no} \; \mapsto \; \; \texttt{s} \; \mapsto \; (\texttt{multiset}(\texttt{t1} \; \mapsto \; \texttt{cell\_no} \; \mapsto \; \texttt{s}) \; - \; \texttt{1})) \, ,
                 (t1 \mapsto cell_{no} \mapsto tt_{2} \mapsto 1),
                 (t3 \mapsto 1 \mapsto a \mapsto 1)
  act1
                 })
                 (t1 \mapsto cell \ no \mapsto s \mapsto (multiset(t1 \mapsto cell \ no \mapsto s)))
                 }
END
T1_strateg3_R1 ≜
STATUS
 ordinary
ANY
 multiset
 cell_no
WHERE
  grd1
                multiset ⊆ MULTISETS
  grd2
          : cell_no ∈ N
                multiset(t1 → cell_no → a)=1
  grd3
           :
  grd4
                 multiset(t1 \rightarrow cell_no \rightarrow s)=0
  grd5
                multiset(t1 \Rightarrow cell_no \Rightarrow t_2)=1
 grd6
                multiset(t1 \mapsto cell_no \mapsto t_3)=0
THEN
  act1
                MULTISETS ≔ ( MULTISETS ∪
                 {
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(t1 \mapsto cell\_no \mapsto a \mapsto (multiset(t1 \mapsto cell\_no \mapsto a) - 1))
                 })
                 (t1 \mapsto cell\_no \mapsto a \mapsto (multiset(t1 \mapsto cell\_no \mapsto a)))
          : LINKS = LINKS \ \{(t1 \mapsto 1 \mapsto t2 \mapsto 1)\}
  act2
END
T1_strateg3_R2 ≜
STATUS
  ordinary
ANY
 multiset
 cell_no
WHERE
 grd1
                 multiset ⊆ MULTISETS
  grd2
                cell_no ∈ N
  grd3
                 multiset(t1 \rightarrow cell_no \rightarrow a)=1
  grd4
                 multiset(t1 \mapsto cell_no \mapsto s)=0
                 multiset(t1 \Rightarrow cell_no \Rightarrow t_3)=1
  grd5
  grd6
                 multiset(t1 \Rightarrow cell_no \Rightarrow t_2)=0
THEN
                 MULTISETS = (MULTISETS U
                 (t1 \mapsto cell_{no} \mapsto a \mapsto (multiset(t1 \mapsto cell_{no} \mapsto a) - 1))
                 })
  act1
                 (t1 \mapsto cell\_no \mapsto a \mapsto (multiset(t1 \mapsto cell\_no \mapsto a)))
                LINKS = LINKS \ \{(t1 \mapsto 1 \mapsto t3 \mapsto 1)\}
  act2
END
T1_strateg4_R1 ≜
STATUS
 ordinary
ANY
 multiset
 cell_no
WHERE
                 multiset ⊆ MULTISETS
  grd1
  grd2
                 cell_no ∈ N
                 multiset(t1 \Rightarrow cell\_no \Rightarrow a)=0
  grd3
  grd4
                 multiset(t1 \Rightarrow cell_no \Rightarrow tt_2)>0
THEN
                 \texttt{MULTISETS} \; \coloneqq \; \big( \; \; \texttt{MULTISETS} \; \; \upsilon
                 (t1 \mapsto cell\_no \mapsto tt\_2 \mapsto (multiset(t1 \mapsto cell\_no \mapsto tt\_2) - 1)),
                 (t1 \mapsto cell_no \mapsto s \mapsto 1),
                 (t1 \mapsto cell\_no \mapsto t\_2 \mapsto 1)
  act1
                 })
                 (t1 \mapsto cell\_no \mapsto tt\_2 \mapsto (multiset(t1 \mapsto cell\_no \mapsto tt\_2)))
END
T1_strateg4_R2 ≜
STATUS
 ordinary
ANY
 multiset
 cell_no
WHERE
 grd1
                 multiset ⊆ MULTISETS
  grd2
                 cell_no ∈ N
                 multiset(t1 \mapsto cell_no \mapsto a)=0
  grd3
           :
  grd4
                 multiset(t1 \rightarrow cell_no \rightarrow tt_3)=1
THEN
  act1
                MULTISETS ≔ ( MULTISETS ∪
                 {
```

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(t1 \mapsto cell_no \mapsto tt_3 \mapsto (multiset(t1 \mapsto cell_no \mapsto tt_3) - 1)),
                (t1 \mapsto cell_no \mapsto s \mapsto 1),
                (t1 \mapsto cell_no \mapsto t_3 \mapsto 1)
               })
                (t1 \mapsto cell\_no \mapsto tt\_3 \mapsto (multiset(t1 \mapsto cell\_no \mapsto tt\_3)))
END
T2 ≜
STATUS
 ordinary
ANY
 multiset
 cell_no
WHERE
 grd1
               multiset ⊆ MULTISETS
 grd2
                cell_no ∈ N
               multiset(t2 → cell_no → a)=1
 grd3
THEN
               MULTISETS = (MULTISETS U
                (t2 \mapsto cell\_no \mapsto a \mapsto (multiset(t2 \mapsto cell\_no \mapsto a) - 1)),
                (t4 \mapsto cell_no \mapsto a \mapsto 1),
                (t5 \mapsto cell_no \mapsto a \mapsto 1)
 act1
                })
                (t2 \mapsto cell\_no \mapsto a \mapsto (multiset(t2 \mapsto cell\_no \mapsto a)))
END
T3_R1 ≜
STATUS
 ordinary
ANY
 multiset
 cell no
WHERE
 grd1
               multiset ⊆ MULTISETS
          :
 grd2
               cell_no ∈ N
               multiset(t3 \mapsto cell_no \mapsto a)=1
 grd3
THEN
               MULTISETS = (MULTISETS U
                (t3 \mapsto cell_no \mapsto a \mapsto (multiset(t3 \mapsto cell_no \mapsto a) - 1)),
                (t0 \mapsto cell_no \mapsto a \mapsto 1)
 act1
               })
                (t3 \mapsto cell\_no \mapsto a \mapsto (multiset(t3 \mapsto cell\_no \mapsto a)))
END
T4 ≜
STATUS
 ordinary
ANY
 multiset
 cell_no
WHERE
 grd1
               multiset ⊆ MULTISETS
 grd2
         : cell_no ∈ N
 grd3
         : multiset(t4 → cell_no → a)=1
THEN
  act1
               MULTISETS ≔ ( MULTISETS ∪
                (t4 \mapsto cell_no \mapsto a \mapsto (multiset(t4 \mapsto cell_no \mapsto a) - 1)),
                (t1 \mapsto cell_no \mapsto a \mapsto 1)
                })
```

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{
  (t4 → cell_no → a → (multiset(t4 → cell_no → a)))
}
END
T5 ≜
STATUS
 ordinary
ANY
 multiset
 cell_no
WHERE
 grd1 : multiset ⊆ MULTISETS
 grd2 : cell_no ∈ N
 grd3 : multiset(t5 → cell_no → a)=1
THEN
             MULTISETS = (MULTISETS U
             (t5 \mapsto cell\_no \mapsto a \mapsto (multiset(t5 \mapsto cell\_no \mapsto a) - 1)),
             (t1 \mapsto cell\_no \mapsto a \mapsto 1)
 act1 : })
             (t5 → cell_no → a → (multiset(t5 → cell_no → a)))
}
END
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END