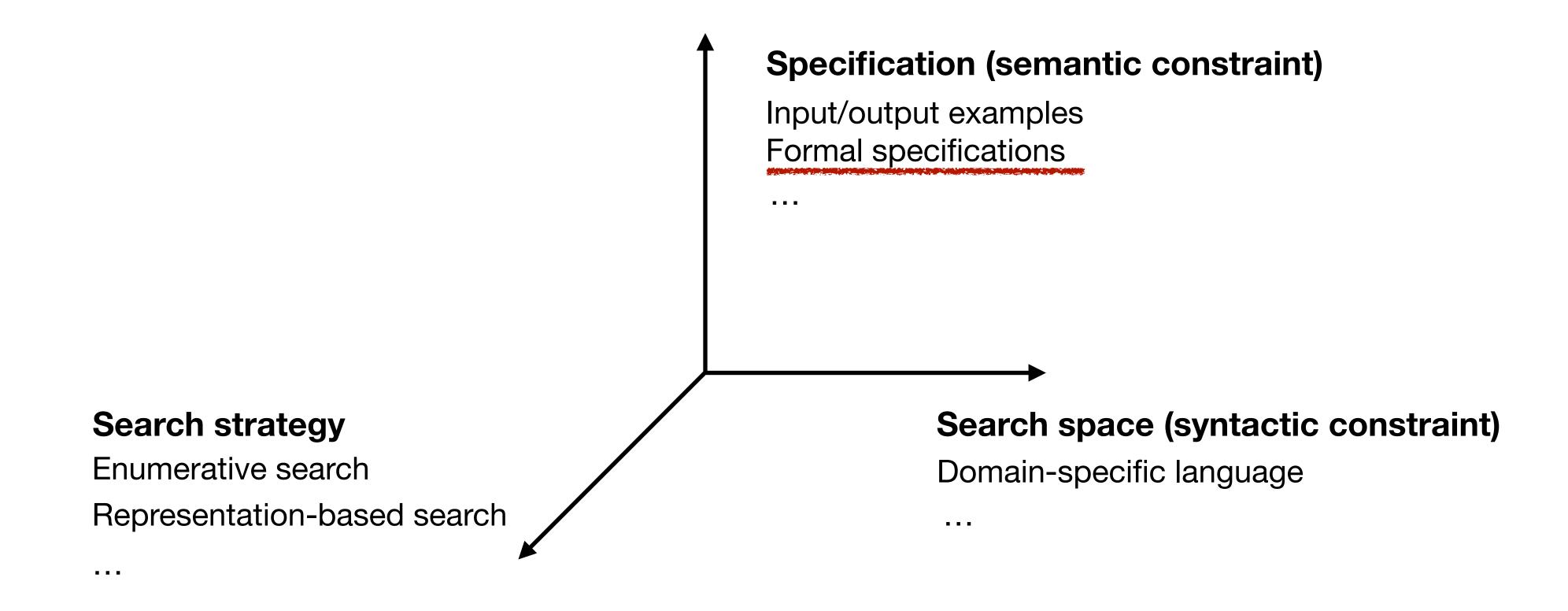
Advanced Software Security

7. Program Synthesis and Verification

Kihong Heo



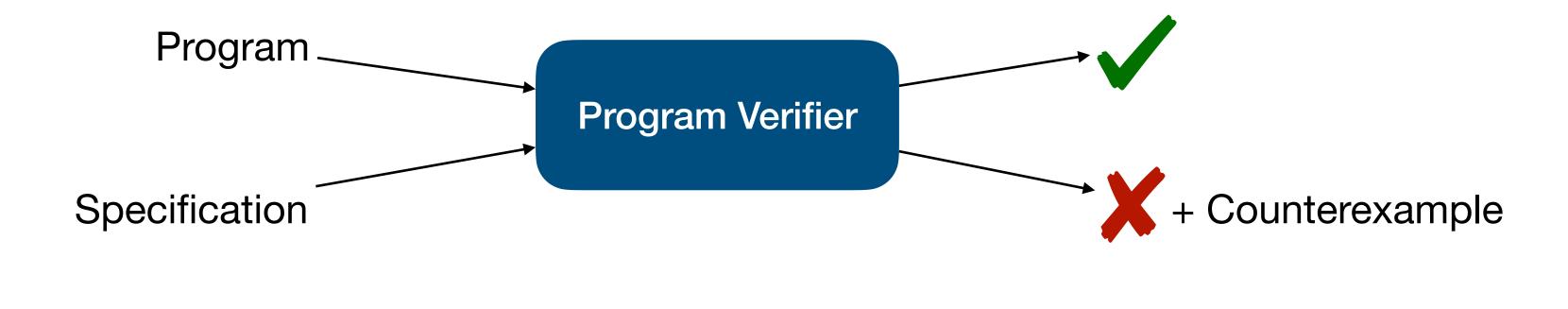
Dimensions in Program Synthesis



Functional Synthesis

- Goal: find a function that satisfies a formal specification (i.e., logical formula)
 - Pre-condition: a predicate that all valid inputs to a function must satisfy
 - Post-condition: a post-condition that all outputs must satisfy
- Question: how can make a functional synthesizer using an inductive synthesizer?

(Hint)



Example

Specification

Find a function f(x) where $\forall x, y . f(x, y) \ge x \land f(x, y) \ge y \land (f(x, y) = x \lor f(x, y) = y)$

Grammar

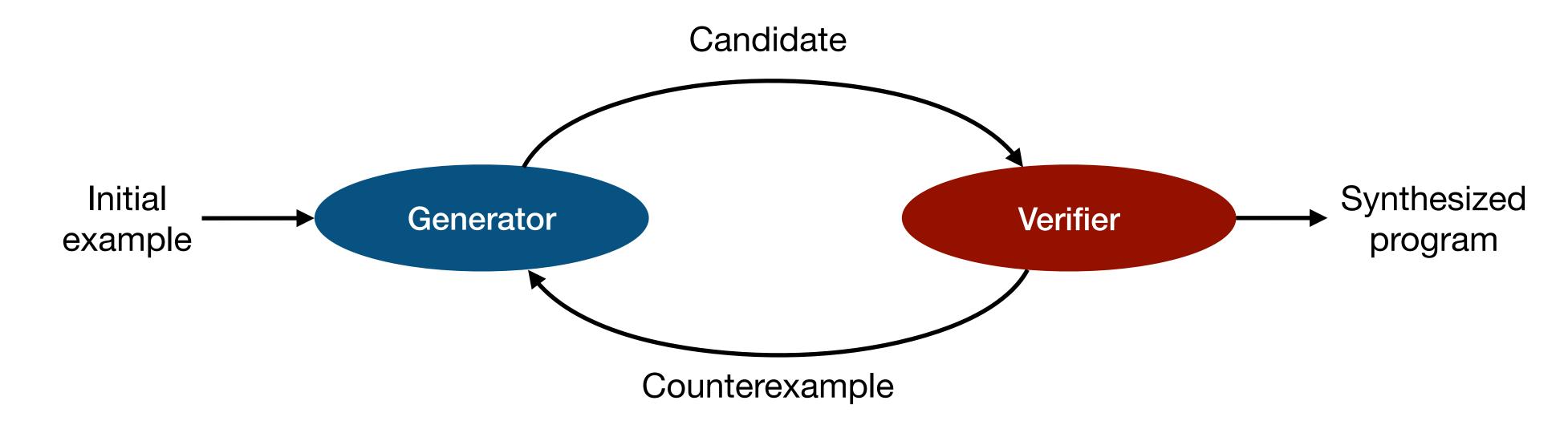
$$S \to x \mid y \mid S + S \mid S - S \mid$$
 if $B \mid S \mid S$
$$B \to S \leq S \mid S = S$$

Example

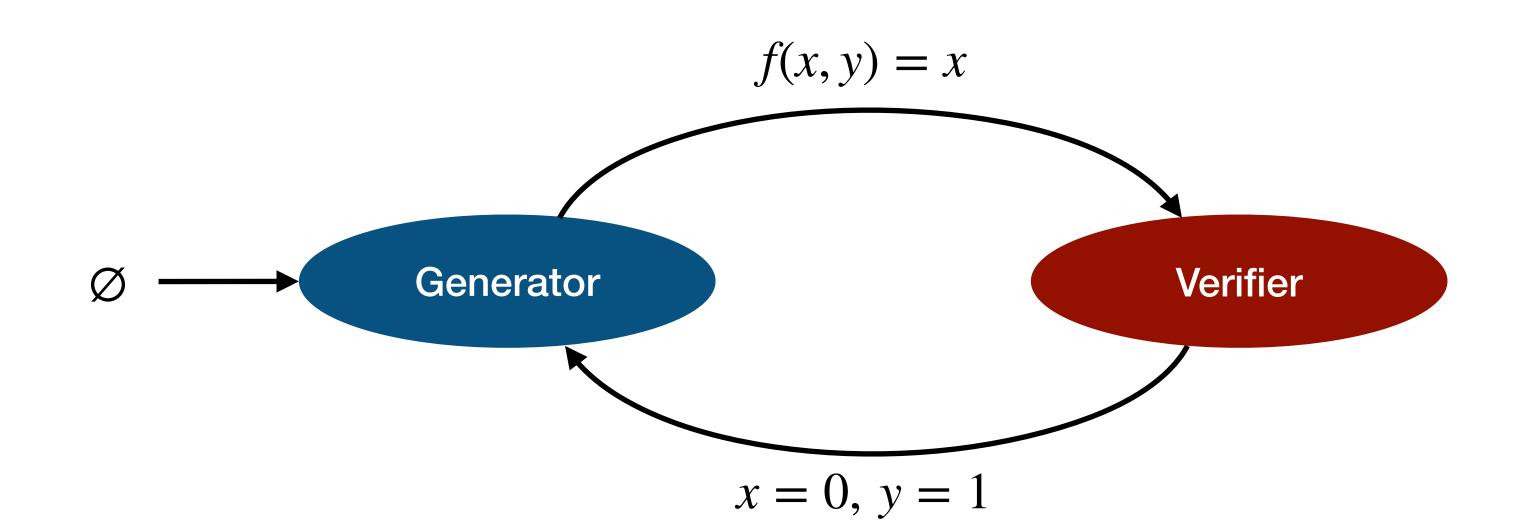
$$if(x >= y) x y$$

CEGIS

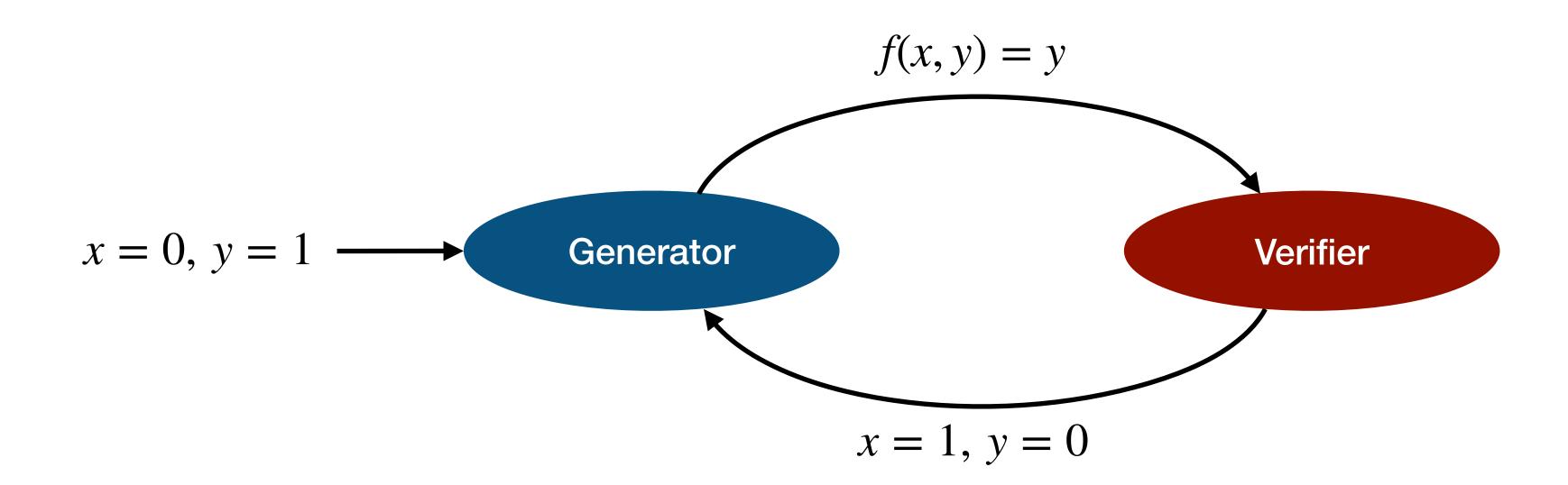
- CounterExample-Guided Inductive Synthesis
- A framework that enables us to use inductive synthesizers for functional synthesis
 - Generator: generate a candidate program (inductive synthesizer)
 - Verifier: check whether the candidate satisfies the specification (program verifier)



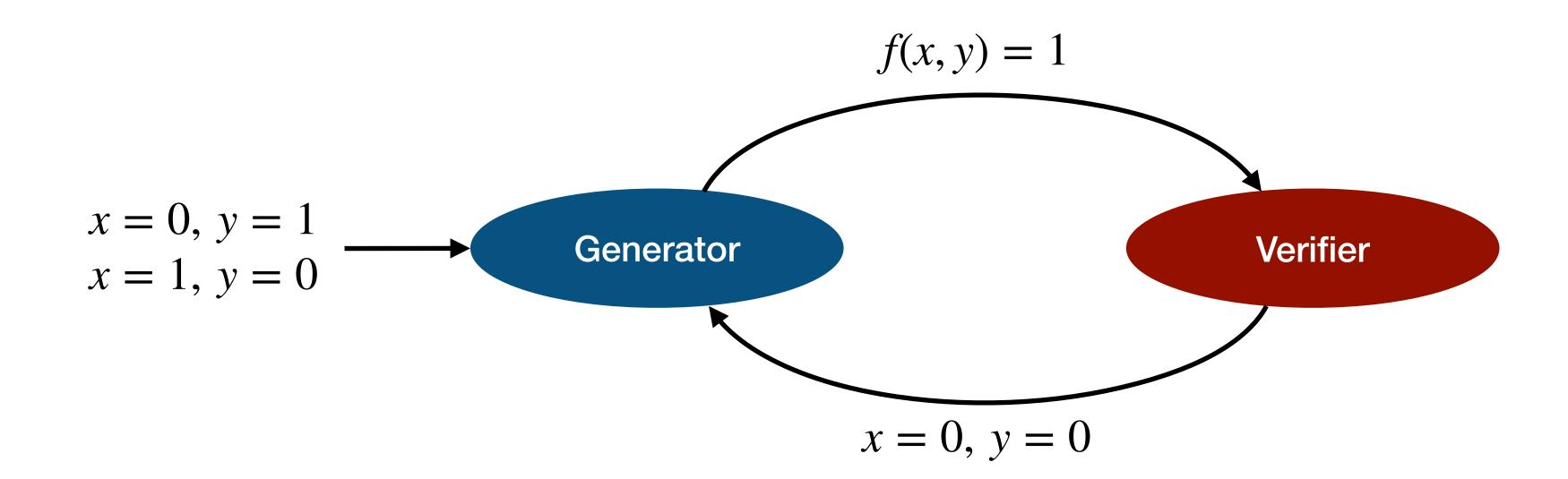
Specification



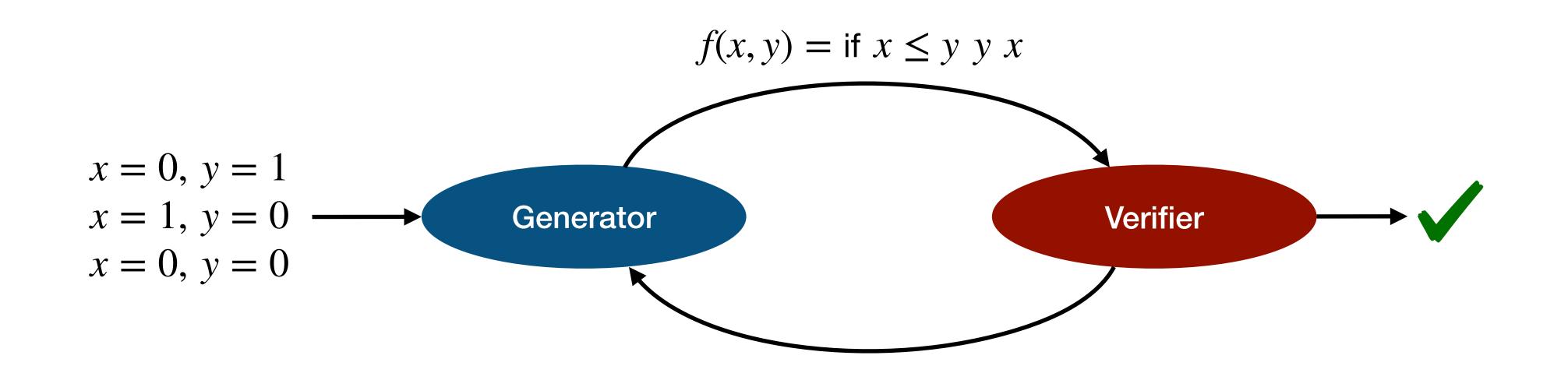
Specification



Specification



Specification



Program Verification via Theorem Proving

- Program verification: check whether a program satisfies a specification or not
- Theorem: "This program satisfies the specification"
- Proving: the correctness is verified if the theorem is proved
 - Otherwise, a counterexample is given
- Automated theorem provers: Z3, CVC, etc
- Interactive theorem provers (proof assistant): Coq, Isabelle/HOL, etc

A Real-World Usage of Theorem Provers

- 1. N students take IS593.
- 2. Each student will pick up and present one paper among M papers in the list provided by Prof. H.
- 3. Each student has different preferences on papers.
 - (1) Each student has a ranking in his/her mind
 - (2) If a student is assigned to the rank-1 paper, +5 happy pts
 - (3) rank-2: +3 pts, rank-3: +1 pts, otherwise: 0 pts
- 4. Prof. H. is so kind that he wants to maximize the sum of happiness of all students.

How to solve this problem?
What is the assignment that makes everybody happy?

Solving

- $x_{ij} \in \{0, 1\}$: student *i* is assigned to paper *j*
- $w_{ij} \in \{0,1,3,5\}$: happy points of student i on paper j

$$\forall i \,. \, \sum_{j=0}^{m-1} x_{ij} = 1 \qquad \qquad \forall j \,. \,\, 0 \le \sum_{i=0}^{n-1} x_{ij} \le 1$$

(One paper per student)

(Maximum one student per paper)

Goal: find x that maximizes $\sum_{i=0}^{n-1} \sum_{j=0}^{m-1} x_{ij} w_{ij}$

Dragon Ball Z3

- A Wish-granting Theorem Prover for Everyone (in our class)
 - Used to assign papers to you folks
 - A reference code for Z3
- Open-source: https://github.com/prosyslab-classroom/dragon-ball-z3

