

Вариант № 1.

1. $4xdx - 3ydy = 3x^2ydy - 2xy^2dx$
2. $y' = \frac{y^2}{x^2} + 4\frac{y}{x} + 2$
3. $y' = \frac{x+2y-3}{2x-2}$
4. $y' - \frac{y}{x} = x^2, y(1) = 0$
5. $y' + xy = (1+x)e^{-x}y^2, y(0) = 1$
6. $3x^2e^ydx + (x^3e^y - 1)dy = 0$

7. $y'''x \ln x = y''$
8. $4y^3y'' = y^4 - 1;$
 $y(0) = \sqrt{2}; y'(0) = 1/(2\sqrt{2})$
9. $y''' + 3y'' + 2y' = 1 - x^2$
10. $y''' - 4y'' + 5y' - 2y = (16 - 12x)e^{-x}$
11. $y'' + 2y' = 4e^x(\sin x + \cos x)$
12. $y'' - 2y' = 2\cos 2x$

Вариант № 2.

1. $\sqrt{4+y^2}dx - ydy = x^2ydy$
2. $xy' = \frac{3y^3 + 2yx^2}{2y^2 + x^2}$
3. $y' = \frac{x+y-2}{2x-2}$
4. $y' - y \operatorname{ctg} x = 2x \sin x, y(\frac{\pi}{2}) = 0$
5. $xy' + y = 2y^2 \ln x, y(1) = 1/2$

6. $(3x^2 + \frac{2}{y} \cos \frac{2x}{y})dx - \frac{2x}{y^2} \cos \frac{2x}{y} dy = 0$
7. $xy''' + y'' = 1$
8. $y'' = 128y^3; y(0) = 1; y'(0) = 8$
9. $y''' - y'' = 6x^2 + 3x$
10. $y''' - 3y'' + 2y' = (1 - 2x)e^x$
11. $y'' - 4y' + 4y = -e^{2x} \sin 6x$
12. $y'' + y = 2 \sin x - 6 \cos x = 2e^x$

Вариант № 3.

1. $6xdx - 6ydy = 2x^2ydy - 3xy^2dx$
2. $y' = \frac{x+y}{x-y}$
3. $y' = \frac{3y-x-4}{3x+3}$
4. $y' + y \cos x = \frac{1}{2} \sin 2x, y(0) = 0$
5. $2(xy' + y) = xy^2, y(1) = 2$
6. $(3x^2 + 4y^2)dx + (8xy + e^y)dy = 0$

7. $2xy''' = y''$
8. $y^3y'' + 64 = 0; y(0) = 4; y'(0) = 2$
9. $y''' - y' = x^2 + x$
10. $y''' - y'' - y' + y = (3x + 7)e^{2x}$
11. $y'' + 2y' = -2e^x(\sin x + \cos x)$
12. $y''' - y' = 2e^x + \cos x$

Вариант № 4.

1. $\sqrt{3+y^2}dx - ydy = x^2 ydy$
2. $xy' = \sqrt{x^2 + y^2} + y$
3. $y' = \frac{2y-2}{x+y-2}$
4. $y' + y \operatorname{tg} x = \cos^2 x, y(\frac{\pi}{4}) = \frac{1}{2}$
5. $y' + 4x^3 y = 4(1+x^3)e^{-4x} y^2, y(0) = 1$
6. $(2x-1-\frac{y}{x^2})dx - (2y-\frac{1}{x})dy = 0$
7. $xy''' + y'' = x+1$
8. $y'' + 2 \sin y \cos^3 y = 0; y(0) = 0; y'(0) = 1$
9. $y^{\text{IV}} - 3y''' + 3y'' - y' = 2x$
10. $y''' - 2y'' + y' = (2x+5)e^{2x}$
11. $y'' + y = 2 \cos 7x + 3 \sin 7x$
12. $y'' - 3y' = 2 \operatorname{ch} 3x$

Вариант № 5.

1. $x\sqrt{3+y^2}dx + y\sqrt{2+x^2}dy = 0$
2. $2y' = \frac{y^2}{x^2} + 6\frac{y}{x} + 3$
3. $y' = \frac{x+y-2}{3x-y-2}$
4. $y' - \frac{y}{x+2} = x^2 + 2x, y(-1) = \frac{3}{2}$
5. $xy' - y = -y^2(\ln x + 2) \ln x, y(1) = 1$
6. $(y^2 + y \sec^2 x)dx + (2xy + \operatorname{tg} x)dy = 0$
7. $\operatorname{tg} x y'' - y' + \frac{1}{\sin x} = 0$
8. $y'' = 32 \sin^3 y \cos y; y(1) = \pi/2; y'(1) = 4$
9. $y^{\text{IV}} - y''' = 5(x+2)^2$
10. $y''' - 3y'' + 4y = (18x-21)e^{-x}$
11. $y'' + 2y' + 5y = -\sin 2x$
12. $y'' + 4y = -8 \sin 2x + 32 \cos 2x + 4e^{2x}$

Вариант № 6.

1. $x\sqrt{1+y^2} + yy'\sqrt{1+x^2} = 0$
2. $xy' = \frac{3y^3 + 4yx^2}{2y^2 + 2x^2}$
3. $y' = \frac{2x+y-3}{x-1}$
4. $y' - \frac{1}{x+1}y = e^x(x+1), y(0) = 1$
5. $2(y' + xy) = (1+x)e^{-x}y^2, y(0) = 2$
6. $(3x^2y + 2y + 3)dx + (x^3 + 2x + 3y^2)dy = 0$
7. $x^2 y'' + xy' = 1$
8. $y'' = 98y^3; y(1) = 1; y'(1) = 7$
9. $y^{\text{IV}} - 2y''' + y'' = 2x(1-x)$
10. $y''' - 5y'' + 8y' - 4y = (2x-5)e^x$
11. $y'' - y' + 8y = e^x(5 \sin x - 3 \cos x)$
12. $y''' - y' = 10 \sin x + 6 \cos x + 4e^x$

Вариант № 7.

1. $(e^{2x} + 5)dy + ye^{2x}dx = 0$
2. $y' = \frac{x+2y}{2x-y}$
3. $y' = \frac{x+7y-8}{9x-y-8}$
4. $y' - \frac{y}{x} = x \sin x, y(\frac{\pi}{2}) = 1$
5. $3(xy' + y) = y^2 \ln x, y(1) = 3$
6. $\left(\frac{x}{\sqrt{x^2+y^2}} + \frac{1}{x} + \frac{1}{y}\right)dx + \left(\frac{y}{\sqrt{x^2+y^2}} + \frac{1}{y} - \frac{x}{y^2}\right)dy = 0$
7. $y''' \operatorname{ctg} 2x + 2y'' = 0$
8. $y^3 y'' + 49 = 0; y(3) = -7; y'(3) = -1$
9. $y^{\text{IV}} + y''' + y'' = x^2 + x - 1$
10. $y''' - 4y'' + 4y' = (x-1)e^x$
11. $y'' + 2y' = e^x(\sin x + \cos x)$
12. $y'' - 4y' = 16 \operatorname{ch} 4x$

Вариант № 8.

$$1. 6xdx - 6ydy = 3x^2 ydy - 2xy^2 dx$$

$$2. xy' = 2\sqrt{x^2 + y^2} + y$$

$$3. y' = \frac{x + 3y + 4}{3x - 6}$$

$$4. y' + \frac{y}{x} = \sin x, \quad y(\pi) = \frac{1}{\pi}$$

$$5. 2y' + y \cos x = y^{-1} \cos x (1 + \sin x), \quad y(0) = 1$$

$$6. [\sin 2x - 2 \cos(x + y)]dx - 2 \cos(x + y)dy = 0$$

$$7. x^3 y''' + x^2 y'' = 1$$

$$8. 4y^3 y'' = 16y^4 - 1; \quad y(0) = \sqrt{2}/2; \quad y'(0) = 1/\sqrt{2}$$

$$9. y^V - y^{IV} = 2x + 3$$

$$10. y''' + 2y'' + y' = (18x + 21)e^{2x}$$

$$11. y'' - 4y' + 4y = e^{2x} \sin 3x$$

$$12. y'' + 9y = -18 \sin 3x - 18e^{3x}$$

Вариант № 9.

$$1. x\sqrt{5 + y^2} dx + y\sqrt{4 + x^2} dy = 0$$

$$2. 3y' = \frac{y^2}{x^2} + 8\frac{y}{x} + 4$$

$$3. y' = \frac{3y + 3}{2x + y - 1}$$

$$4. y' + \frac{y}{2x} = x^2, \quad y(1) = 1$$

$$5. y' + 4x^3 y = 4y^2 e^{4x} (1 - x^3), \quad y(0) = -1$$

$$6. (xy^2 + x/y^2)dx + (x^2 y - x^2/y^3)dy = 0$$

$$7. y''' \operatorname{tg} x = 2y''$$

$$8. y'' + 8 \sin y \cos^3 y = 0; \quad y(0) = 0; \quad y'(0) = 2$$

$$9. 3y^{IV} + y''' = 6x - 1$$

$$10. y''' - 3y' - 2y = 4x e^x$$

$$11. y'' + 6y' + 13y = e^{-3x} \cos 4x$$

$$12. y''' - 4y' = 24e^{2x} - 4 \cos 2x + 8 \sin 2x$$

Вариант № 10.

$$1. y(4 + e^x)dy - e^x dx = 0$$

$$2. xy' = \frac{3y^3 + 6yx^2}{2y^2 + 3x^2}$$

$$3. y' = \frac{x + 2y - 3}{4x - y - 3}$$

$$4. y' + \frac{2x}{1 + x^2} y = \frac{2x^2}{1 + x^2}, \quad y(0) = \frac{2}{3}$$

$$5. 3y' + 2xy = 2xy^{-2} e^{-2x^2}, \quad y(0) = -1$$

$$6. \left(\frac{1}{x^2} + \frac{3y^2}{x^4}\right)dx - \frac{2y}{x^3} dy = 0$$

$$7. y''' \operatorname{cth} 2x = 2y''$$

$$8. y'' = 72y^3; \quad y(2) = 1; \quad y'(2) = 6$$

$$9. y^{IV} + 2y''' + y'' = 4x^2$$

$$10. y''' - 3y' - 2y = -4x e^x$$

$$11. y'' + y = 2 \cos 3x - 3 \sin 3x$$

$$12. y'' - 5y' = 50 \operatorname{ch} 5x$$

Вариант № 11.

$$1. \sqrt{4 - x^2} y' + xy^2 + x = 0$$

$$2. y' = \frac{x^2 + xy - y^2}{x^2 - 2xy}$$

$$3. y' = \frac{x - 2y + 3}{-2x - 2}$$

$$4. y' - \frac{2x - 5}{x^2} y = 5, \quad y(2) = 4$$

$$5. 2xy' - 3y = -(5x^2 + 3)y^3, \quad y(1) = 1/\sqrt{2}$$

$$6. \left(\frac{x}{\sqrt{x^2 + y^2}} + y\right)dx + \left(x + \frac{y}{\sqrt{x^2 + y^2}}\right)dy = 0$$

$$7. x^4 y'' + x^3 y' = 1$$

$$8. y^3 y'' + 36 = 0; \quad y(0) = 3; \quad y'(0) = 2$$

$$9. y''' + y'' = 5x^2 - 1$$

$$10. y''' - 3y' + 2y = (4x + 9)e^{2x}$$

$$11. y'' + 2y' + 5y = -2 \sin x$$

$$12. y'' + 16y = 16 \cos 4x - 16e^{4x}$$

Вариант № 12.

$$1. 2xdx - 2ydy = x^2 y dy - 2xy^2 dx$$

$$2. xy' = \sqrt{2x^2 + y^2} + y$$

$$3. y' = \frac{x + 8y - 9}{10x - y - 9}$$

$$4. y' + \frac{y}{x} = \frac{x+1}{x} e^x, \quad y(1) = e$$

$$5. 3xy' + 5y = (4x - 5)y^4, \quad y(1) = 1$$

$$6. \frac{y}{x^2} \cos \frac{y}{x} dx - \left(\frac{1}{x} \cos \frac{y}{x} + 2y \right) dy = 0$$

$$7. xy''' + 2y'' = 0$$

$$8. y'' = 18 \sin^3 y \cos y; \quad y(1) = \pi/2; \quad y'(1) = 3$$

$$9. y^{IV} + 4y''' + 4y'' = x - x^2$$

$$10. y''' + 4y'' + 5y' + 2y = (12x + 16)e^x$$

$$11. y'' - 4y' + 8y = e^x (-3 \sin x + 4 \cos x)$$

$$12. y''' - 9y' = -9e^{3x} - 9 \cos 3x + 18 \sin 3x$$

Вариант № 13.

$$1. x\sqrt{4+y^2} dx + y\sqrt{1+x^2} dy = 0$$

$$2. 2y' = \frac{y^2}{x^2} + 6\frac{y}{x} + 6$$

$$3. y' = \frac{2x + 3y - 5}{5x - 5}$$

$$4. y' - \frac{y}{x} = -2 \frac{\ln x}{x}, \quad y(1) = 1$$

$$5. 2y' + 3y \cos x = e^{2x} (2 + 3 \cos x) y^{-1}, \quad y(0) = 1$$

$$6. \frac{1+xy}{x^2 y} dx + \frac{1-xy}{xy^2} dy = 0$$

$$7. (1+x^2)y'' + 2xy' = x^3$$

$$8. 4y^3 y'' = y^4 - 16; \quad y(0) = 2\sqrt{2}; \quad y'(0) = 1/\sqrt{2}$$

$$9. 7y''' - y'' = 12x$$

$$10. y''' - y'' - 2y' = (6x - 11)e^{-x}$$

$$11. y'' + 2y' = 10e^x (\sin x + \cos x)$$

$$12. y'' - y' = 2 \operatorname{ch} x$$

Вариант № 14.

$$1. (e^x + 8)dy - ye^x dx = 0$$

$$2. xy' = \frac{3y^3 + 8yx^2}{2y^2 + 4x^2}$$

$$3. y' = \frac{4y - 8}{3x + 2y - 7}$$

$$4. y' - \frac{y}{x} = \frac{-12}{x^3}, \quad y(1) = 4$$

$$5. 3(xy' + y) = xy^2, \quad y(1) = 3$$

$$6. \frac{dx}{y} - \frac{x+y^2}{y^2} dy = 0$$

$$7. x^5 y''' + x^4 y'' = 1$$

$$8. y'' = 50y^3; \quad y(3) = 1; \quad y'(3) = 5$$

$$9. y''' + 3y'' + 2y' = 3x^2 + 2x$$

$$10. y''' + y'' - 2y' = (6x + 5)e^x$$

$$11. y'' - 4y' + 4y = e^{2x} \sin 5x$$

$$12. y'' + 25y = 20 \cos 5x - 10 \sin 5x + 50e^{5x}$$

Вариант № 15.

$$1. \sqrt{5+y^2} + y'y\sqrt{1-x^2} = 0$$

$$2. y' = \frac{x^2 + 2xy - y^2}{2x^2 - 2xy}$$

$$5. y' - y = 2xy^2, y(0) = 1/2$$

$$6. \frac{y}{x} dx - \frac{xy+1}{x} dy = 0$$

$$7. xy''' - y'' + 1/x = 0$$

$$8. y^3 y'' + 25 = 0; y(2) = -5; y'(2) = -1$$

$$3. y' = \frac{x+3y-4}{5x-y-4}$$

$$4. y' + \frac{2y}{x} = x^3, y(1) = -5/6$$

$$9. y''' - y' = 3x^2 - 2x + 1$$

$$10. y''' + 4y'' + 4y' = (9x+15)e^x$$

$$11. y'' + y = 2\cos 5x + 3\sin 5x$$

$$12. y''' - 16y' = 48e^{4x} + 64\cos 4x - 64\sin 4x$$

Вариант № 16.

$$1. 6x dx - 2y dy = yx^2 dy - 3xy^2 dx$$

$$2. xy' = 3\sqrt{x^2 + y^2} + y$$

$$3. y' = \frac{y-2x+3}{x-1}$$

$$4. y' + \frac{y}{x} = 3x, y(1) = 1$$

$$5. 2xy' - 3y = -(20x^2 + 12)y^3, y(1) = 1/2\sqrt{2}$$

$$6. \left(xe^x + \frac{y}{x^2}\right) dx - \frac{1}{x} dy = 0$$

$$7. xy''' + y'' + x = 0$$

$$8. y'' + 18\sin y \cos^3 y = 0; y(0) = 0; y'(0) = 3$$

$$9. y''' - y'' = 4x^2 - 3x + 2$$

$$10. y''' - 3y'' - y' + 3y = (4-8x)e^x$$

$$11. y'' + 2y' + 5y = -17\sin 2x$$

$$12. y'' + 2y' = 2\operatorname{sh} 2x$$

Вариант № 17.

$$1. y \ln y + xy' = 0$$

$$2. 2y' = \frac{y^2}{x^2} + 8\frac{y}{x} + 8$$

$$3. y' = \frac{x+2y-3}{x-1}$$

$$4. y' - \frac{2xy}{1+x^2} = 1+x^2, y(1) = 3$$

$$5. y' + 2xy = 2x^3 y^3, y(0) = \sqrt{2}$$

$$6. (10xy - \frac{1}{\sin y}) dx + (5x^2 + \frac{x \cos y}{\sin^2 y} - y^2 \sin y^3) dy = 0$$

$$7. \operatorname{th} x y^{\text{IV}} = y'''$$

$$8. y'' = 8\sin^3 y \cos y; y(1) = \pi/2; y'(1) = 2$$

$$9. y^{\text{IV}} - 3y''' + 3y'' - y' = x - 3$$

$$10. y''' - y'' - 4y' + 4y = (7-6x)e^x$$

$$11. y'' + 6y' + 13y = e^{-3x} \cos x$$

$$12. y'' + 36y = 24 \sin 6x - 12 \cos 6x + 36e^{6x}$$

Вариант № 18.

$$1. (1+e^x)y' = ye^x$$

$$2. xy' = \frac{3y^3 + 10yx^2}{2y^2 + 5x^2}$$

$$3. y' = \frac{3x+2y-1}{x+1}$$

$$4. y' + \frac{1-2x}{x^2} y = 1, y(1) = 1$$

$$5. xy' + y = y^2 \ln x, y(1) = 1$$

$$6. \left(\frac{y}{x^2 + y^2} + e^x\right) dx - \frac{xdy}{x^2 + y^2} = 0$$

$$7. xy''' + y'' = \sqrt{x}$$

$$8. y'' = 32y^3; y(4) = 1; y'(4) = 4$$

$$9. y^{\text{IV}} + 2y''' + y'' = 12x^2 - 6x$$

$$10. y''' + 3y'' + 2y' = (1-2x)e^{-x}$$

$$11. y'' - 4y' + 8y = e^x (3\sin x + 5\cos x)$$

$$12. y''' - 25y' = 25(\sin 5x + \cos 5x) - 50e^{5x}$$

Вариант № 19.

1. $\sqrt{1-x^2}y' + xy^2 + x = 0$
2. $y' = \frac{x^2 + 3xy - y^2}{3x^2 - 2xy}$
3. $y' = \frac{5y+5}{4x+3y-1}$
4. $y' + \frac{3y}{x} = \frac{2}{x^3}, y(1) = 1$
5. $2y' + 3y \cos x = (8 + 12 \cos x)e^{2x}y^{-1}, y(0) = 2$
6. $e^y dx + (\cos y + xe^y)dy = 0$
7. $y''' \operatorname{tg} x = y'' + 1$
8. $y^3 y'' + 16 = 0; y(1) = 2; y'(1) = 2$
9. $y''' - 4y'' = 32 - 384x^2$
10. $y''' - 5y'' + 7y' - 3y = (20 - 16x)e^{-x}$
11. $y'' + 2y' = 6e^x (\sin x + \cos x)$
12. $y'' + 3y' = 2sh3x$

Вариант № 20.

1. $6xdx - 2ydy = 2yx^2 dy - 3xy^2 dx$
2. $xy' = 3\sqrt{2x^2 + y^2} + y$
3. $y' = \frac{x+4y-5}{6x-y-5}$
4. $y' + 2xy = -2x^3, y(1) = e^{-1}$
5. $4y' + x^3 y = (8 + x^3)e^{-2x}y^2, y(0) = 1$
6. $(y^3 + \cos x)dx + (3xy^2 + e^y)dy = 0$
7. $y''' \operatorname{tg} 5x = 5y''$
8. $y'' + 32 \sin y \cos^3 y = 0; y(0) = 0; y'(0) = 4$
9. $y^{IV} + 2y''' + y'' = 2 - 3x^2$
10. $y''' - 4y'' + 3y' = -4xe^x$
11. $y'' - 4y' + 4y = -e^{2x} \sin 4x$
12. $y'' + 49y = 14 \sin 7x + 7 \cos 7x - 98e^{7x}$

Вариант № 21.

1. $y(1 + \ln y) + xy' = 0$
2. $y' = \frac{y^2}{x^2} + 8\frac{y}{x} + 12$
3. $y' = \frac{x+y+2}{x+1}$
4. $y' + \frac{xy}{2(1-x^2)} = \frac{x}{2}, y(0) = 2/3$
5. $8xy' - 12y = -(5x^2 + 3)y^3, y(1) = \sqrt{2}$
6. $xe^{y^2} dx + (x^2 ye^{y^2} + \operatorname{tg}^2 y)dy = 0$
7. $y''' \operatorname{tg} 7x = 7y''$
8. $y'' = 50 \sin^3 y \cos y; y(1) = \pi/2; y'(1) = 5$
9. $y''' + y'' = 49 - 24x^2$
10. $y''' - 5y'' + 3y' + 9y = (32x - 32)e^{-x}$
11. $y'' + 6y' + 13y = e^{-3x} \cos 5x$
12. $y''' - 36y' = 36e^{6x} - 72(\cos 6x + \sin 6x)$

Вариант № 22.

1. $(3 + e^x)yy' = e^x$
2. $xy' = \frac{3y^3 + 12yx^2}{2y^2 + 6x^2}$
3. $y' = \frac{2x+y-3}{4x-4}$
4. $y' + xy = -x^3, y(0) = 3$
5. $2(y' + y) = xy^2, y(0) = 2$
6. $(5xy^2 - x^3)dx + (5x^2 y - y)dy = 0$
7. $x^3 y''' + x^2 y'' = \sqrt{x}$
8. $y'' = 18y^3; y(1) = 1; y'(1) = 3$
9. $y''' - 2y'' = 3x^2 + x - 4$
10. $y''' - 6y'' + 9y' = 4xe^x$
11. $y'' + y = -3 \sin 7x + 2 \cos 7x$
12. $y'' + 4y' = 16sh4x$

Вариант № 23.

$$1. \sqrt{3+y^2} + \sqrt{1-x^2} yy' = 0$$

$$2. y' = \frac{x^2 + xy - 3y^2}{x^2 - 4xy}$$

$$3. y' = \frac{2x + y - 3}{2x - 2}$$

$$4. y' - \frac{2y}{x+1} = e^x (x+1)^2, y(0) = 1$$

$$5. y' + xy = (x-1)e^x y^2, y(0) = 1$$

$$6. [\cos(x+y^2) + \sin x] dx + 2y \cos(x+y^2) dy = 0$$

$$7. \operatorname{cth} x y'' - y' + \frac{1}{\operatorname{ch} x} = 0$$

$$8. y^3 y'' + 9 = 0; y(1) = 1; y'(1) = 3$$

$$9. y''' - 13y'' + 12y' = x - 1$$

$$10. y''' - 7y'' + 15y' - 9y = (8x - 12)e^x$$

$$11. y'' + 2y' + 5y = -\cos x$$

$$12. y'' + 64y = 16 \sin 8x - 16 \cos 8x - 64e^{8x}$$

Вариант № 24.

$$1. xdx - ydy = yx^2 dy - xy^2 dx$$

$$2. xy' = 2\sqrt{3x^2 + y^2} + y$$

$$3. y' = \frac{y}{2x + 2y - 2}$$

$$4. y' + 2xy = xe^{-x^2} \sin x, y(0) = 1$$

$$5. 2y' - 3y \cos x = -e^{-2x} (2 + 3 \cos x) y^{-1}, y(0) = 1$$

$$6. (x^2 - 4xy - 2y^2) dx + (y^2 - 4xy - 2x^2) dy = 0$$

$$7. (x+1)y''' + y'' = (x+1)$$

$$8. y^3 y'' = 4(y^4 - 1); y(0) = \sqrt{2}; y'(0) = \sqrt{2}$$

$$9. y^{IV} + y''' = x$$

$$10. y''' - y'' - 5y' - 3y = -(8x + 4)e^x$$

$$11. y'' - 4y' + 8y = e^x (2 \sin x - \cos x)$$

$$12. y''' - 49y' = 14e^{7x} - 49(\cos 7x + \sin 7x)$$

Вариант № 25.

$$1. y'y \sqrt{\frac{1-x^2}{1-y^2}} + 1 = 0$$

$$2. 4y' = \frac{y^2}{x^2} + 10 \frac{y}{x} + 5$$

$$3. y' = \frac{x + 5y - 6}{7x - y - 6}$$

$$4. y' - \frac{2y}{x+1} = (x+1)^3, y(0) = 1/2$$

$$5. y' - y = xy^2, y(0) = 1$$

$$6. (\sin y + y \sin x + \frac{1}{x}) dx + (x \cos y - \cos x + \frac{1}{y}) dy = 0$$

$$7. (1 + \sin x) y''' = \cos x y''$$

$$8. y'' + 50 \sin y \cos^3 y = 0; y(0) = 0; y'(0) = 5$$

$$9. y''' - y'' = 6x + 5$$

$$10. y''' + 5y'' + 7y' + 3y = (16x + 20)e^x$$

$$11. y'' + 2y' = 3e^x (\sin x + \cos x)$$

$$12. y'' + 5y' = 50 \operatorname{sh} 5x$$

Вариант № 26.

$$1. \sqrt{5+y^2} dx + 4(x^2 y + y) dy = 0$$

$$2. xy' = \frac{3y^3 + 14yx^2}{2y^2 + 7x^2}$$

$$3. y' = \frac{x + y - 4}{x - 2}$$

$$4. y' - y \cos x = -\sin 2x, y(0) = 3$$

$$5. 2(xy' + y) = y^2 \ln x, y(1) = 2$$

$$6. (1 + \frac{1}{y} e^{x/y}) dx + (1 - \frac{x}{y^2} e^{x/y}) dy = 0$$

$$7. (1 + x^2) y'' + 2xy' = 12x^3$$

$$8. y'' = 8y^3; y(0) = 1; y'(0) = 2$$

$$9. y''' + 3y'' + 2y' = x^2 + 2x + 3$$

$$10. y''' - 2y'' - 3y' = (8x - 14)e^{-x}$$

$$11. y'' - 4y' + 4y = e^{2x} \sin 4x$$

$$12. y'' + 81y = 9 \sin 9x + 3 \cos 9x + 162 e^{9x}$$

Вариант № 27.

1. $(1 + e^x)yy' = e^x$
2. $y' = \frac{x^2 + xy - 5y^2}{x^2 - 6xy}$
3. $y' = \frac{2x + y - 1}{2x - 2}$
4. $y' - 4xy = -4x^3, y(0) = -1/2$
5. $y' + y = xy^2, y(0) = 1$
6. $\frac{(x - y)dx + (x + y)dy}{x^2 + y^2} = 0$
7. $-xy''' + 2y'' = \frac{2}{x^2}$
8. $y^3 y'' + 4 = 0; y(0) = -1; y'(0) = -2$
9. $y''' - 5y'' + 6y' = (1 - x)^2$
10. $y''' + 2y'' - 3y' = (8x + 6)e^x$
11. $y'' + 6y' + 13y = e^{-3x} \cos 8x$
12. $y''' - 64y' = 128 \cos 8x - 64e^{8x}$

Вариант № 28.

1. $\sqrt{2 + y^2} dx + 3(x^2 y + y) dy = 0$
2. $xy' = 4\sqrt{x^2 + y^2} + y$
3. $y' = \frac{3y - 2x + 1}{3x + 3}$
4. $y' - \frac{y}{x} = -\frac{\ln x}{x}, y(1) = 1$
5. $2(y' + xy) = (x - 1)e^x y^2, y(0) = 2$
6. $2(3xy^2 + 2x^3) dx + 3(2x^2 y + y^2) dy = 0$
7. $\operatorname{cth} x y'' + y' = \operatorname{ch} x$
8. $y'' = 2 \sin^3 y \cos y; y(1) = \pi/2; y'(1) = 1$
9. $y''' - 13y'' + 12y' = 18x^2 - 39$
10. $y''' + 6y'' + 9y' = (16x + 24)e^x$
11. $y'' + 2y' + 5y = 10 \cos x$
12. $y'' + y' = 2 \operatorname{sh} x$

Вариант № 29.

1. $2x dx - y dy = x^2 y dy - xy^2 dx$
2. $3y' = \frac{y^2}{x^2} + 10 \frac{y}{x} + 10$
3. $y' = \frac{6y - 6}{5x + 4y - 9}$
4. $y' - 3x^2 y = x^2(1 + x^3)/3, y(0) = 0$
5. $2(y' + xy) = (x - 1)e^x y^2, y(0) = 2$
6. $(3x^3 + 6x^2 y + 3xy^2) dx + (2x^3 + 3x^2 y) dy = 0$
7. $x^4 y'' + x^3 y' = 4$
8. $y^3 y'' + 1 = 0; y(1) = -1; y'(1) = -1$
9. $y^{IV} - 6y''' + 9y'' = 3x - 1$
10. $y''' - y'' - 9y' + 9y = (12 - 16x)e^x$
11. $y'' + y = 2 \cos 4x + 3 \sin 4x$
12. $y'' + 100y = 20 \sin 10x - 30 \cos 10x - 200e^{10x}$

Вариант № 30.

1. $\sqrt{2 - x^2} y' + 2xy^2 + 2x = 0$
2. $xy' = 4\sqrt{2x^2 + y^2} + y$
3. $y' = \frac{x + 6y - 7}{8x - y - 7}$
4. $y' - y \cos x = \sin 2x, y(0) = -1$
5. $xy' + y = xy^2, y(1) = 1$
6. $x dx + y dy + (x dy - y dx)/(x^2 + y^2) = 0$
7. $y'' + \frac{2x}{1 + x^2} y' = 2x$
8. $y'' = 2y^3; y(-1) = 1; y'(-1) = 1$
9. $y^{IV} + y''' = 12x + 6$
10. $y''' + 4y'' + 3y' = 4(1 - x)e^{-x}$
11. $y'' - 4y' + 4y = e^{2x} \sin 6x$
12. $y''' - 81y' = 162e^{9x} + 81 \sin 9x$