

Standard normal/Gaussian distribution

```
In[ ]:= Clear[f, x, σ]
f = Exp[-0.5 x^2 / σ^2]
Refine[ $\frac{1}{\text{Sqrt}[2 \pi] \sigma}$  Integrate[f, {x, -∞, +∞}], {σ > 0}]

Out[ ]:=  $e^{-\frac{0.5 x^2}{\sigma^2}}$ 

Out[ ]:= 1.
```

General FWHM as function of σ :

$$\text{FWHM} = 2\text{Sqrt}[2\text{Log}[2]] \sigma$$


```
Clear[f, x, σ, f0, sols]

(* start with standard Gaussian profile *)
f = Exp[-0.5 x^2 / σ^2]

(* get points where fwhm will be calculated *)
sols = Solve[f == 1 / 2, x];

(* points are equidistant from origin *)
2 sols[[2, 1, 2]]
fwhm = 2 Sqrt[2 Log[2]] σ // N
```

Out[62]= $e^{-\frac{0.5 x^2}{\sigma^2}}$

 **Solve:** Inverse functions are being used by Solve, so some solutions may not be found; use Reduce for complete solution information.

Out[64]= 2.35482 σ

Out[65]= 2.35482 σ

Spotsize FWHM as function of W0:

$$\text{FWHM} = 2 \sqrt{\text{Log}[2]} \sigma$$

```
In[ ]:= Clear[f, x, σ, f0, a, W0]
a = Exp[-x^2 / W0^2]
(Solve[a == 1 / 2, x] // Normal) /. {c1 -> 0}
fwhm = 2 Sqrt[Log[2]] σ // N
```

Out[]:= $e^{-\frac{x^2}{W0^2}}$

Out[]:= $\left\{ \left\{ x \rightarrow -W0 \sqrt{\text{Log}[2]} \right\}, \left\{ x \rightarrow W0 \sqrt{\text{Log}[2]} \right\} \right\}$

Out[]:= 1.66511 σ


Intensity FWHM vs Field FWHM:


$$I_{\text{FWHM}}/E_{\text{FWHM}} = 1/\sqrt{2}$$

$$E_{\text{FWHM}} = 2 \sqrt{2 \text{Log}[2]} \sigma E$$

$$I_{\text{FWHM}} = 2 \sqrt{\text{Log}[2]} \sigma E$$

```
Clear[fE, fI, f0, x, σ, fwhm]
fI = Exp[-0.5 x^2 / σ^2];
fE = Sqrt[fI];
Solve[fI == 1 / 2, x] [[2, 1, 2]] / Solve[fE == 1 / 2, x] [[2, 1, 2]]
1 / Sqrt[2] // N
```

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Out[]:= 0.707107

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```
In[80]:= Clear[fE, fI, f0, x, σ, fwhm, Efwhm, Ifwhm]
Efwhm = 2 Sqrt[2 Log[2]] σ
Ifwhm = Efwhm / Sqrt[2]
```

Out[81]= $2 \sigma \sqrt{2 \text{Log}[2]}$

Out[82]= $2 \sigma \sqrt{\text{Log}[2]}$