

## Powerful Series of Power Series (Lecture Assignment)

Complete this assignment and submit it to Gradescope by 4:00pm on your class day. You can print this sheet, or write on your own paper. Contact us if internet connections or other issues require alternate arrangements.

Find a power series representation, and its radius of convergence, for the following functions:

1.  $f(x) = \frac{1}{8+x^3}$ . *Hint: rewrite  $f(x)$  to match the formula of the sum of a geometric series.*

$$\begin{aligned}
 &= \frac{1}{8} \cdot \frac{1}{1 - (-\frac{x^3}{8})} \\
 &= \sum_{n=0}^{\infty} \frac{1}{8} \left(-\frac{x^3}{8}\right)^n
 \end{aligned}
 \quad
 \begin{aligned}
 &\left| \frac{x^3}{8} \right| < 1 \\
 &|x| < 2 \\
 &R = 2
 \end{aligned}$$

2.  $g(x) = \frac{x^2}{8+x^3}$

$$\begin{aligned}
 &= \frac{x^2}{8} \cdot \frac{1}{1 - (-\frac{x^3}{8})} \\
 &= \sum_{n=0}^{\infty} \frac{x^2}{8} \left(-\frac{x^3}{8}\right)^n
 \end{aligned}
 \quad
 \begin{aligned}
 &\left| \frac{x^3}{8} \right| < 1 \\
 &|x| < 2 \\
 &R = 2
 \end{aligned}$$

3.  $g'(x) = \frac{16x - x^4}{(8+x^3)^2} \Rightarrow 16x + 2x^4 - 3x^7$

$$\begin{aligned}
 g(x) &= \frac{x^2}{8+x^3} \\
 &= \text{see} \\
 &= \sum_{n=0}^{\infty} \frac{x^2}{8} \left(-\frac{x^3}{8}\right)^n \rightarrow R = 2
 \end{aligned}$$

One-Minute Questions: Write a sentence for each.

- A. What's one mathematical question you have after watching the videos?

Not from videos, but still unclear  
on distinction between geometric & power series.

- B. What's one interesting thing you learned from the book or videos?

I didn't know that you could  
integrate/differentiate power series