

Sumthing Clever

1. Which of the following series converge? Prove your answer.

(a) $\sum_{n=1}^{\infty} \left(\frac{1}{n+2} - \frac{1}{n+1} \right)$

(b) $\sum_{n=2}^{\infty} \frac{n}{\ln(n)}$

(c) $\sum_{n=1}^{\infty} \left(\frac{\cos(2\pi n)(n+1)}{n^2} - \frac{1}{n^2} \right)$

(d) $\sum_{n=3}^{\infty} (-1)^{n+1} \frac{2^n}{3^{n+2}}$

(e) $\sum_{n=1}^{\infty} \frac{2^n + 3^n}{6^n}$

(f) $\sum_{k=5}^{\infty} \frac{k^2}{k^2 - 1}$