COMP226

Assignment 1

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These slides **a1_slides.pdf** are an **abridged** (shortened) version of the main handout **a1_wsheet.pdf**.

Limit Order Books

Continuous Assessment Number	1 (of 2)	
Weighting	15%	
Assignment Circulated	Sunday 26 February 2023	
Deadline	21:00 Tuesday 14 March 2023	
Submission Mode	CodeGrade assignment on Canvas	
Learning Outcomes Assessed	Have an understanding of market microstructure and its impact on trading.	

	Assignment	compute quantities based on the limit order book
	Marking Criteria	Pre-deadline visible CodeGrade tests of correctness of 6 functions (70%); Post-deadline CodeGrade tests of correctness for 4 "extra" functions (30%)
1	Submission necessary in order to satisfy module requirements	No
ı	Expected time	Roughly 8-12 hours

Reconstruct a limit order book from order messages:

Goal of

taken

Pre vs. post deadline tests

- 70% of marks are available via visible pre-deadline tests on CodeGrade for 6 functions. If your code passes all the tests you get the full 70% for this part of the assignment
- You can submit as many times as you want, and use the CodeGrade feedback to improve your mark for this part
- 30% of marks are for passing post-deadline tests for 4
 extra functions but these marks are only available if
 you got all 70% for the pre-deadline tests

Code/data zip handout

- Download comp226_a1.zip
- Unzip comp226_a1.zip
- This will yield a directory called comp226_a1

```
comp226 al
common.R
■■■ input
   ■■■ book 1.csv
   ■■■ book 2.csv
   ■■■ book 3.csv
   empty.txt
   message a.txt
   ■■■ message ar.txt
   ■■■ message_arc.txt
   ■■■ message ex add.txt
   message ex cross.txt
   message ex reduce.txt
   message ex same price.txt
main.R
■■■ output
   ■■■ book 1-message a.out
   ■■■ book 1-message ar.out
   ■■■ book 1-message arc.out
  ■■■ book 2-message a.out
  ■■■ book 2-message ar.out
■ ■ book 2-message arc.out
 book 3-message a.out
   book 3-message ar.out
   ■■■ book 3-message arc.out
■■■ template.R
2 directories, 23 files
```

The contents are explained on the next slide..

Code/data zip handout

- main.R: the script that you should call, examples below (do not edit it)
- common.R: provides a range of fully implemented functions (do not edit it)
- **template.R**: **code template** that contains 10 empty functions that you need to complete
- input: subdirectory that contains two types of input files, initial book files and message files
- output: subdirectory that contains sample output that allows you to check your code implementations

Ex: using main.R with template.R

```
$ Rscript main.R template.R input/book_1.csv input/empty.txt
$ask
   oid price size
1   a   105   100

$bid
   oid price size
1   b   95   100

Total volume:
Best prices:
Mid-price:
Spread:
```

input/book_1.csv is the initial book, input/empty.txt is the
message file (empty in this case)

main.R

```
options(warn=-1)
args <- commandArgs(trailingOnly = TRUE); nargs = length(args)
log <- (nargs == 4) # TRUE is there are exactly 4 arguments
arg format <- "<--log> <solution path> <book path> <messages path>"
if (nargs < 3 | nargs > 4) # check that there are 3 or 4 arguments
    stop(paste("main.R has 3 required arguments and 1 optional flag:", arg format))
if (nargs == 4 && args[1] != "--log") # if 4 check that --log is the first
    stop(paste("Bad arguments format, expected:", arg format))
solution path <- args[nargs-2]
book path <- args[nargs-1]
messages path <- args[nargs]
if (!all(file.exists(c(solution path, book path, messages path))))
    stop("File does not exist at path provided.")
source(solution path); source("common.R") # source common.R from pwd
book <- book.load(book path)
book <- book.reconstruct(data.load(messages path), init=book, log=log)
book.summarise(book)
```

main.R

- checks the command line arguments are ok
- assigns them to variables
- sources common.R and the file at solution_path
- loads an initial book
- reconstructs the book according to the messages
- prints out the book
- prints out the book stats

Rscript from Rstudio

Rscript main.R template.R input/book_1.csv input/empty.txt

- In R studio, you can call Rscript from the "terminal" tab (as opposed to the "console")
- On Windows, use Rscript.exe not Rscript:

Rscript.exe main.R template.R input/book_1.csv input/empty.txt

70%: 6 functions to implement

Order book stats:

```
1. book.total_volume <- function(book) [5%]</pre>
```

```
2. book.best_prices <- function(book) [5%]</pre>
```

```
3. book.midprice <- function(book) [5%]</pre>
```

```
4. book.spread <- function(book) [5%]</pre>
```

Reconstructing the limit order book:

```
5. book.reduce <- function(book, message) [15%]</pre>
```

```
6. book.add <- function(book, message) [35%]</pre>
```

input/book_1.csv

```
oid,side,price,size
a,S,105,100
b,B,95,100
```

oid	side	price	size
а	S	105	100
b	В	95	100

- oid (order id) is used to process (partial) cancellations of orders that arise in "reduce" messages
- side: 'B' for a buy/bid; 'S' for a sell/ask order
- price and size are self-explanatory

Order book stats

- book.total_volumes should return a list with named elements, bid and ask where bid (ask) should be the total volume in the bid (ask) book
- book.best_prices should return a list with two named elements, bid and ask where bid (ask) should be the best bid (ask) price
- book.midprice should return the midprice
- book.spread should return the spread

The functions can be tested with an empty message file (you do not need to have implemented book.add or book.reduce)

Expected output

```
$ Rscript main.R solution.R input/book_1.csv input/empty.txt
Sask
 oid price size
1 a 105 100
$bid
 oid price size
1 b 95 100
Total volume: 100 100
Best prices: 95 105
Mid-price: 100
Spread: 10
```

book.add and book.reduce

For the 5th and 6th functions, book.add and book.reduce, you need to understand the format of messages...

Message format

- message files contain one message per line (terminated by a single linefeed character, '\n')
- each message is a series of fields separated by spaces
- two types of messages: "Add" and "Reduce" messages.
- Here's an example, which contains an "Add" message followed by a "Reduce" message:

```
A c S 97 36
R a 50
```

Add messages

'A' oid side price size

- 'A': fixed string that identifies this as an "Add" message
- oid: "order id" used by subsequent "Reduce" messages
- side: 'B' for a bid, 'S' for an ask
- price: limit price of this order
- size: size of this order

Reduce messages

'R' oid size

- 'R': fixed string identifying this as a "Reduce" message
- oid: "order id" identifies the order to be reduced
- size: amount by which to reduce the size of the order (not the new size of the order); if size is equal to or greater than the existing size of the order, the order is removed from the book

Processing messages

- "Reduce" messages affect at most one existing limit order
- "Add" messages either:
 - add a single row to the book (orders at the same price are stored separately to preserve "oid"s)
 - cross the spread and then (partially) remove any number of orders on the other side of the book (and may result in a new limit order of unmatched volume)
- Example message files are split into cases that include crosses and those that don't to help you develop your code incrementally and test it on inputs of differing difficulty

Ex: initial book

```
$ Rscript main.R solution.R input/book_1.csv input/empty.txt
Sask
 oid price size
1 a 105 100
$bid
 oid price size
1 b 95 100
Total volume: 100 100
Best prices: 95 105
Mid-price: 100
Spread: 10
```

Ex: processing a reduce message

```
$ cat input/message_ex_reduce.txt
R a 50
```

```
$ Rscript main.R solution.R input/book_1.csv input/message_ex_reduce.txt
$ask
   oid price size
1   a  105   50

$bid
   oid price size
1   b   95   100

Total volume: 100   50
Best prices: 95   105
Mid-price: 100
Spread: 10
```

Ex: Non-crossing add message

```
$ cat input/message_ex_add.txt
A c S 97 36
```

```
$ Rscript main.R solution.R input/book 1.csv input/message ex add.txt
Šask
 oid price size
2 a 105 100
1 c 97 36
$bid
 oid price size
1 b 95 100
Total volume: 100 136
Best prices: 95 97
Mid-price: 96
Spread: 2
```

Ex: crossing add message

```
$ cat input/message_ex_cross.txt
A c B 106 101
```

```
$ Rscript main.R solution.R input/book_1.csv input/message_ex_cross.txt
$ask
[1] oid    price size
<0 rows> (or 0-length row.names)

$bid
    oid price size
1    c    106    1
2    b    95    100

Total volume: 101 0
Best prices: 106 NA
Mid-price: NA
Spread: NA
```

9 longer sample output files

	messages_a	messages_ar	messages_arc
book_1			
book_2			
book_3			

```
output

book_1-message_a.out

book_1-message_ar.out

book_1-message_ar.out

book_2-message_a.out

book_2-message_ar.out

book_2-message_ar.out

book_3-message_ar.out

book_3-message_ar.out

book_3-message_ar.out

odirectories, 9 files
```

Ex: two orders at the same price

Recall initial book:

```
$ Rscript main.R solution.R input/book_1.csv input/empty.txt
$ask
 oid price size
1 a 105 100
$bid
  oid price size
1 b 95 100
Total volume: 100 100
Best prices: 95 105
Mid-price: 100
Spread: 10
```

Ex: message_same_price.txt

```
$ Rscript main.R solution.R input/book_1.csv input/message_ex_same_price.txt
$ask
    oid price size
2    j   105   132
1    a   105   100

$bid
    oid price size
1    b   95   100
2    k   95   71

Total volume: 171   232
Best prices: 95   105
Mid-price: 100
Spread: 10
```

Earlier messages closer to the top of the book

Price-time precedence

- Orders are executed according to price time precedence
- Best price first, but when two orders have the same price, the earlier one is executed first
- We provide book.sort that respects price-time precedence
- It relies on the fact that the order ids increase as follows:

where < is indicating "comes before" in the message files

book.sort (in common.R)

```
book.sort <- function(book, sort bid=T, sort ask=T) {</pre>
    if (sort ask && nrow(book$ask) >= 1) {
        book$ask <- book$ask[order(book$ask$price,
                                    nchar(book$ask$oid).
                                    book$ask$oid.
                                    decreasing=F),]
        row.names(book$ask) <- 1:nrow(book$ask)</pre>
    if (sort bid && nrow(book$bid) >= 1) {
        book$bid <- book$bid[order(-book$bid$price,
                                    nchar(book$bid$oid),
                                    book$bid$oid.
                                    decreasing=F),]
        row.names(book$bid) <- 1:nrow(book$bid)
    book
```

You are welcome (and encouraged) to use book.sort

Example output

```
$ask
 oid price size
  a 105 100
  0 104 292
  r 102 194
  k 99 71
 q 98 166
 m 98 88
  j 97 132
 n 96 375
Shid
 oid price size
1 b 95 100
  1 95 29
 p 94 87
 g 91 102
Total volume: 318 1418
Best prices: 95 96
Mid-price: 95.5
Spread: 1
```

The rownames are now: 1,2,... starting from the best prices

book.summarise

```
book.summarise <- function(book, with stats=T) {
    if (nrow(book$ask) > 0)
        book$ask <- book$ask[nrow(book$ask):1.]
    book$ask <- book$ask[, c("oid", "price", "size")]
    book$bid <- book$bid[, c("oid", "price", "size")]
    print(book)
    if (with stats) {
        clean <- function(x) { ifelse(is.infinite(x), NA, x) }</pre>
        total volumes <- book.total volumes(book)
        best prices <- lapply(book.best prices(book), clean)</pre>
        midprice <- clean(book.midprice(book))</pre>
        spread <- clean(book.spread(book))
        cat("Total volume:", total volumes$bid, total volumes$ask, "\n")
        cat("Best prices:", best prices$bid, best prices$ask, "\n")
        cat("Mid-price:", midprice, "\n")
        cat("Spread:", spread, "\n")
```

Hints

For book.spread and book.midprice a nice implementation would use book.best_prices, which you should then implement first.

Turn on logging to help with debugging

Rscript main.R --log solution.R input/book_1.csv input/message_arc.txt

Then book.reconstruct uses book.summarise at every step

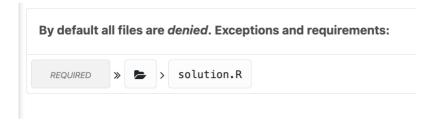
Remember to use stringsAsFactors=FALSE (e.g. for creating data.frames)

Hint for book.add & book.reduce

A possible way to implement book.add and book.reduce that makes use of the different example message files is the following:

- Do a partial implementation of book.add for messages that do not cross, and check your implementation with message_a.txt.
- 2. Implement book.reduce fully. Check combined (partial) implementation of book.add and book.reduce with message_ar.txt and book_3.csv (only this combination with message_ar.txt has no crosses).
- 3. Complete book.add implementation. Check crosses using message_arc.txt and any initial book, or with message_ar.txt and book_1.csv or book_2.csv

Submit only "solution.R"



Plagiarism / collusion

Warning

- Do not show your work to other students or search for solutions online.
- Automatic plagiarism/collusion detection is in place, and suspected cases are passed on to the academic integrity officer.
- Students found to have plagiarized or colluded get 0, with further sanctions such as termination of studies for repeat offences.

4 "extra" functions to implement

Final 30% is only available if CodeGrade gives you full marks (70%) for the pre-deadline tests.

Only focus on the extra problems once you have achieved this.

You can get marks for any one of these independently:

- 1. book.extral <- function(book,size) [6%]</pre>
- 2. book.extra2 <- function(book,size) [6%]</pre>
- 3. book.extra3 <- function(book) [6%]</pre>
- 4. book.extra4 <- function(book,k) [12%]</pre>

Using CodeGrade to improve

After you submit the tests for the first 6 functions are run. After a short while you get:

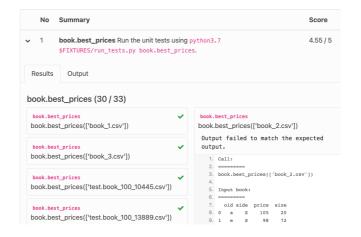
- 1. a provisional mark is visible;
- 2. to **see any tests that you failed**, with details of the inputs, the expected, and the received output.

To illustrate, I edited the correct solution so that book.best_prices give the wrong answer 10% of the time at random, and submitted this as a test student:

Example: Order book stats

Oı	Order book stats			Options • 89 %	
	No	Summary	Score	Pass	
>	1	<pre>book.best_prices Run the unit tests using python3.7 \$FIXTURES/run_tests.py book.best_prices.</pre>	4.55 / 5	~	
>	2	book.spread Run the unit tests using python3.7 \$FIXTURES/run_tests.py book.spread.	3.79 / 5	~	
>	3	<pre>book.midprice Run the unit tests using python3.7 \$FIXTURES/run_tests.py book.midprice.</pre>	4.55 / 5	~	
>	4	book.total_volumes Run the unit tests using python3.7 \$FIXTURES/run_tests.py book.total_volumes.	5/5	~	

Example: book.best_prices



```
book.best_prices(['book_2.csv'])
Output failed to match the expected
output.
   1. Call:
   2. =======
   3. book.best prices(['book 2.csv'])
```

105 20

95 100

22

98 72

7. oid side price size 8. 0 a S

9. 1 e S

11. 3 b B

10. 2 d S 104

book.best_prices

4. 5. Input book: 6 ======

12. 13. Expected: 14. ====== 15. \$ask 16. [1] 98 17. 18. \$bid 19. [1] 95 20. 21. Got: 22. ==== 23. [1] "Hello"

Example: correct order book stats

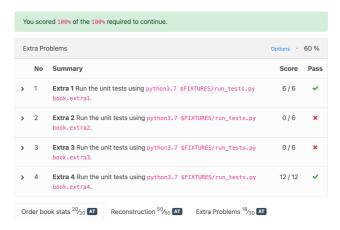
0	Order book stats		Options • 1	Options • 100 %	
	No	Summary	Score	Pass	
>	1	<pre>book.best_prices Run the unit tests using python3.7 \$FIXTURES/run_tests.py book.best_prices.</pre>	5/5	~	
>	2	<pre>book.spread Run the unit tests using python3.7 \$FIXTURES/run_tests.py book.spread.</pre>	5/5	~	
>	3	<pre>book.midprice Run the unit tests using python3.7 \$FIXTURES/run_tests.py book.midprice.</pre>	5/5	~	
>	4	book.total_volumes Run the unit tests using python3.7 \$FIXTURES/run_tests.py book.total_volumes.	5/5	~	

Example test for book.add



Tests for extra functions

Similar test output for extra functions, provided that you got the first 6 functions totally correct, **but only after the deadline**:



Tests

- First few tests in each category use book_{1,2,3}.csv.
- Many tests use more complicated csv files, and while the data is visible in CodeGrade, we do not give you the csv file.
- Some tests are randomly generated (needed to disincentivise hardcoding).

This means that you may experience a small amount of variance in the mark you see when you resubmit the same wrong code (correct code will get full marks every time).

Submit to CodeGrade for help

- we can see test results, which helps us to help you;
- we can enter comments directly on submitted source code: