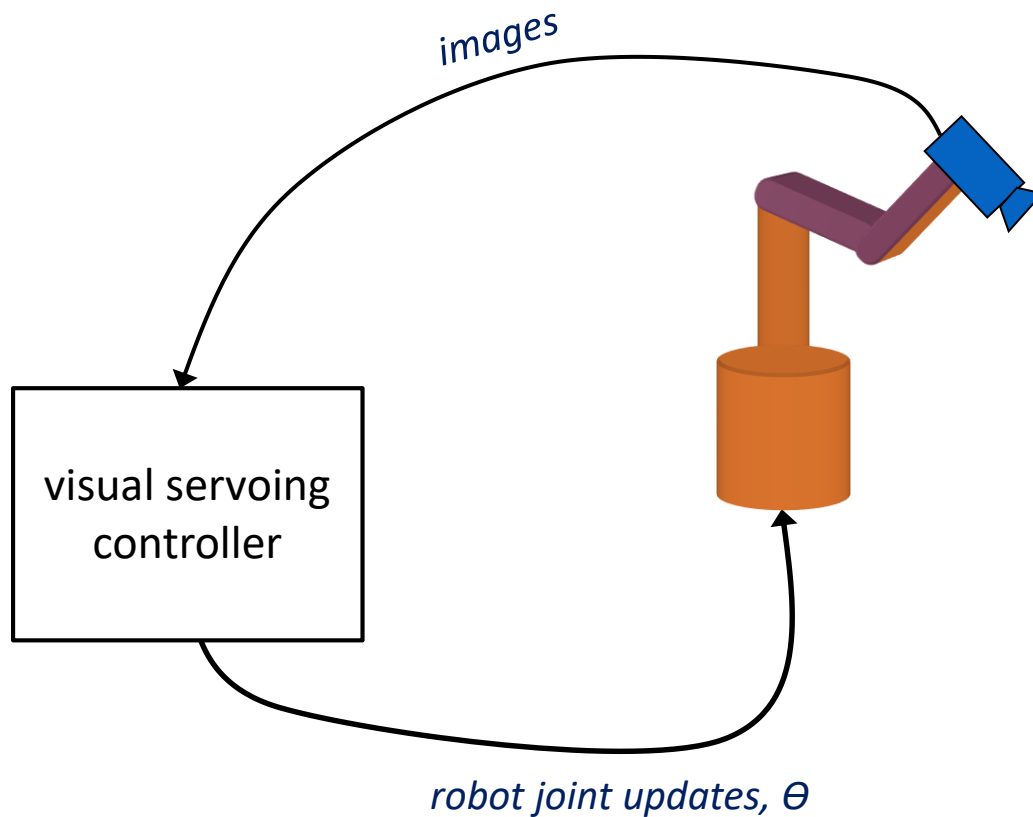


Visual servoing (VS) control uses real-time camera images as feedback.

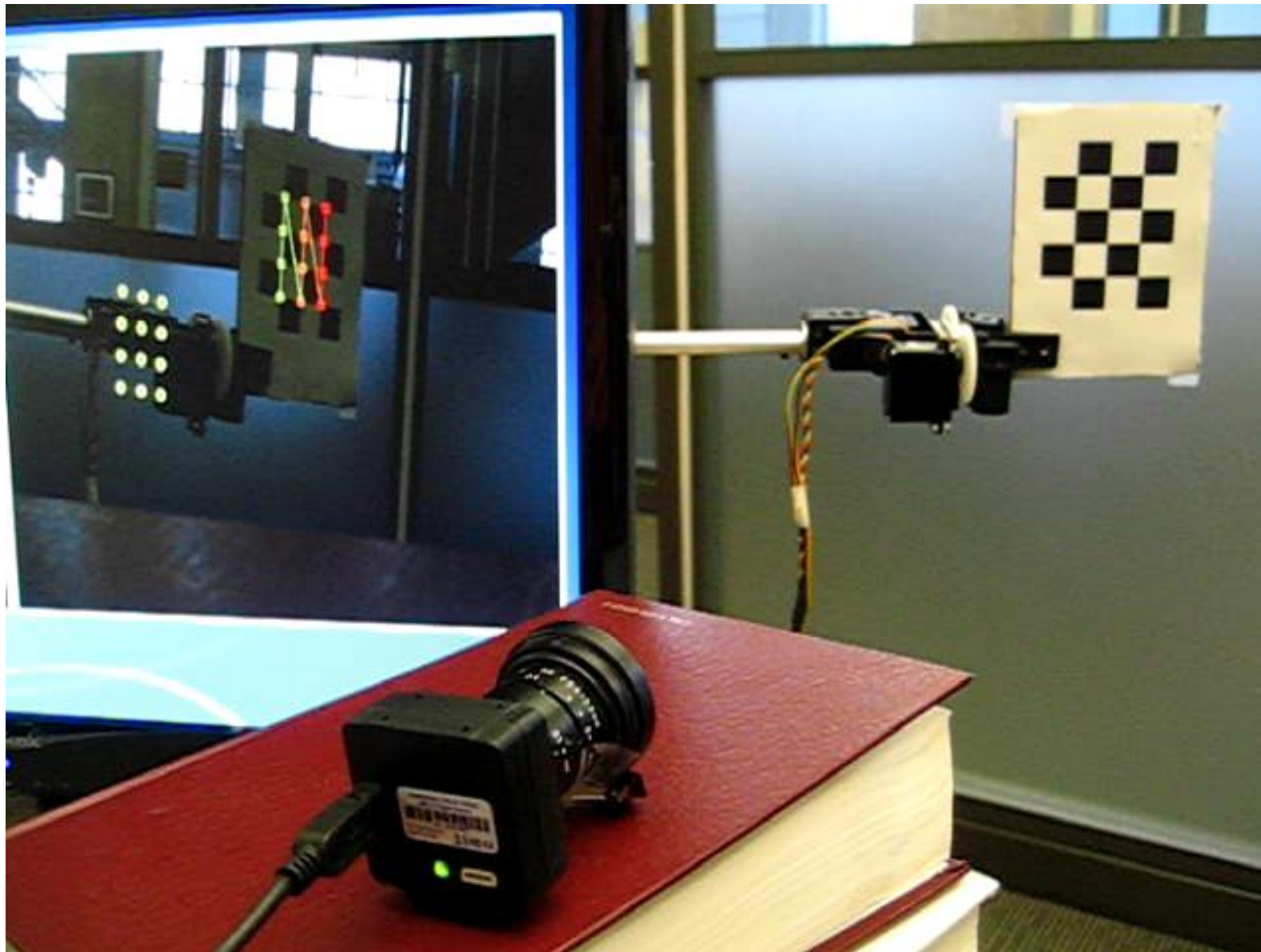


*Learns mapping from  
image space to robot  
joint space.*

*Camera calibration  
not needed.*

*Robot model not  
needed.*

desired locations  
of checkboard  
corners in image



real-time object  
detection of  
checkerboard  
corners

non eye-in-hand example *[VIDEO]*

Mathematical details:

$$V = J(\theta)\dot{\theta}$$

where  $V$  = Cartesian velocity vector of robot end-effector

$J$  = Jacobian matrix

$\theta$  = robot joint angles .

Rigidly attach a camera onto end-effector:

$$\dot{e} = J'(\theta)\dot{\theta}$$

where  $e$  = vector of image features (generally the feature error)

$J'$  = image Jacobian matrix .

*$J'$  units: change in pixels / change in axis (rad or m or PSI)*

$$\dot{\Theta} = J'(\Theta)^{-1} \dot{e}$$

To obtain exponential feature error decrease, desire:

$$\dot{e} = -\lambda e, \text{ where } \lambda > 0.$$

Visual servoing iteratively **updates the commanded robot joint vector**  $\Theta$ :

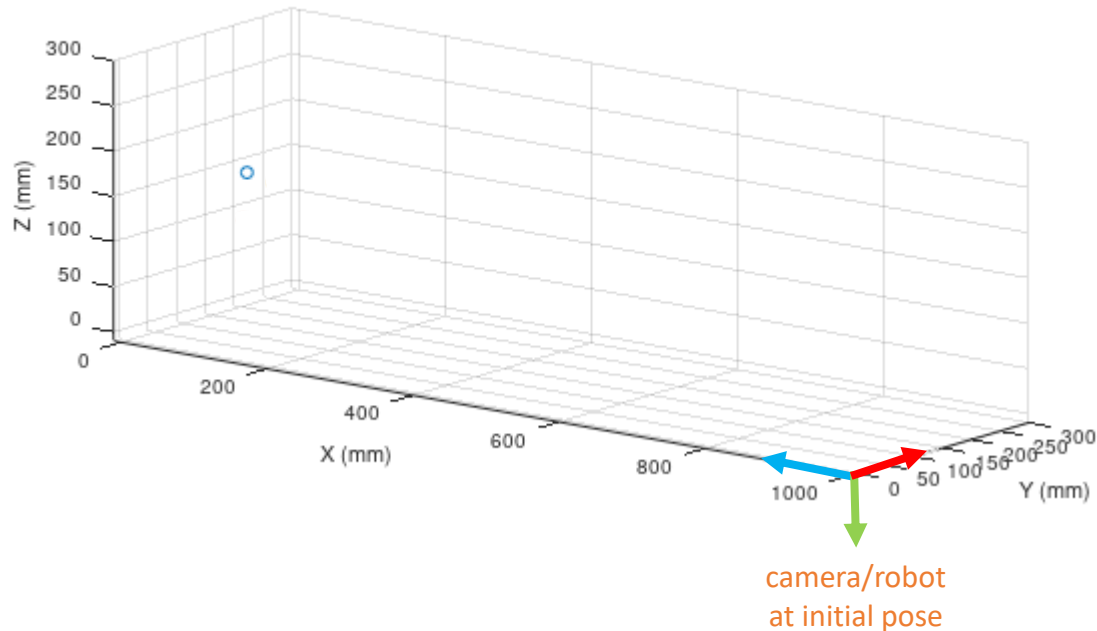
$$\Theta_k = \Theta_{k-1} - \lambda J'(\Theta)^{-1} e_k.$$

*updated robot axes = previous robot axes + correction term*

# EXAMPLE: 2-DOF visual servoing

one-point physical target locations (w.r.t. XYZ world coordinate frame in mm):

**P1 = (110, 69.904, 178.923)**



2-DOF “flying robot”: D435 camera that can move along Y & Z (only)

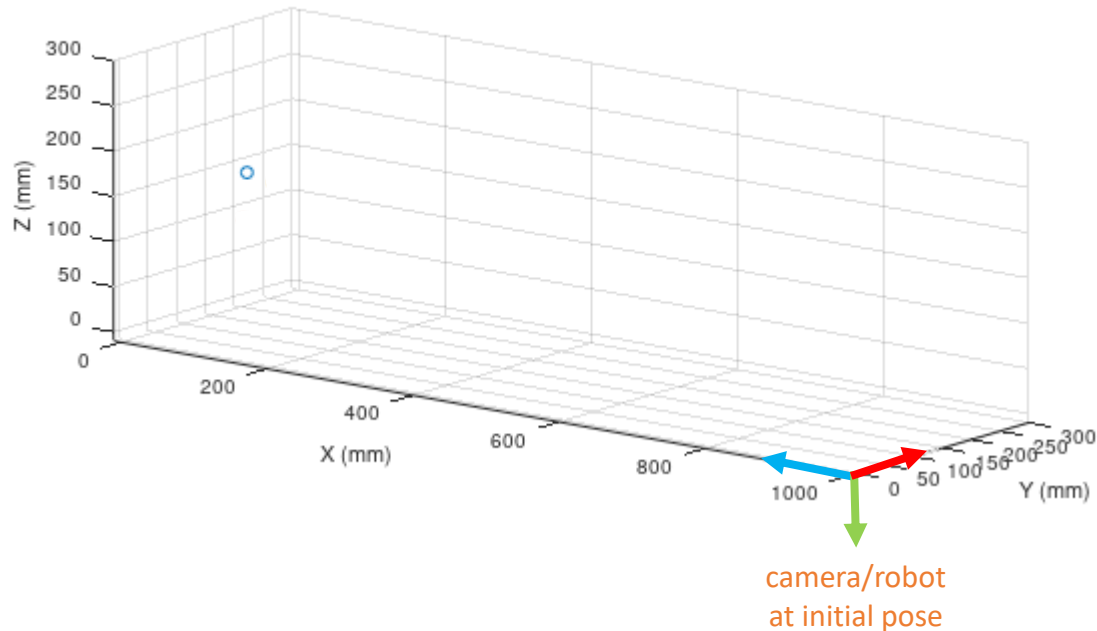


**Task:** implement visual servoing method to actuate the 2 robot axes so that the single target point coincides with the center pixel location (640,360) in image space.

# EXAMPLE: 2-DOF visual servoing

one-point physical target locations (w.r.t. XYZ world coordinate frame in mm):

**P1 = (110, 69.904, 178.923)**

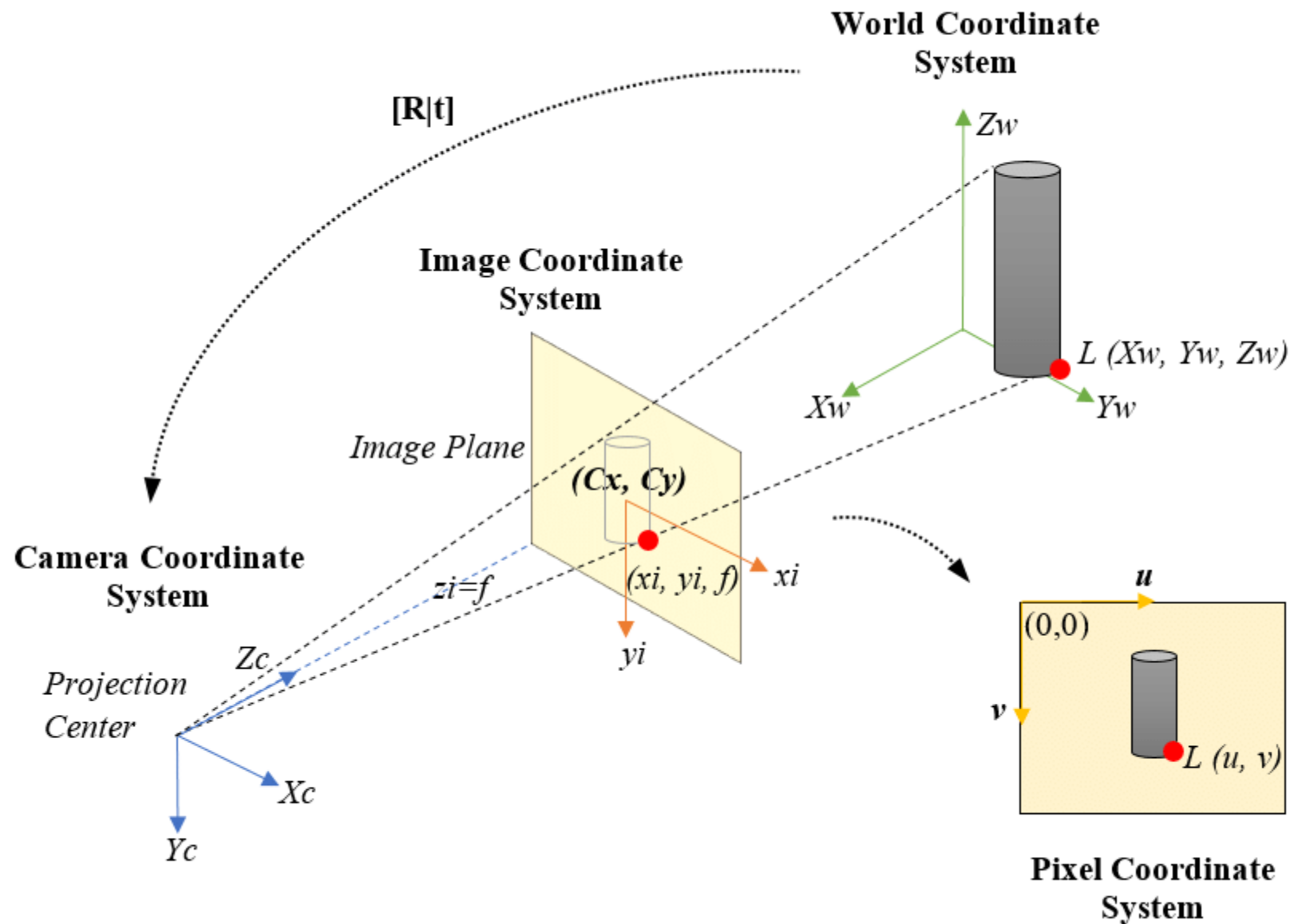


2-DOF “flying robot”: D435 camera that can move along Y & Z (only)



**Task:** implement visual servoing method to actuate the 2 robot axes so that the single target point coincides with the center pixel location (640,360) in image space.

*From inspection, require: robot (Y,Z) = (69.904,178.923)*



pinhole worksheet.xlsx - Excel

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	A	B	C	D	E	F	G	H	I	J	K
1	Compute (xc,yc):										
2	xp	yp	z (mm)	cx	cy	f	size	f/size			
3	861	161	737	640	360	1.88E-03	1.40E-06	1.3429E+03			
4											
5	xc	yc									
6	121	-109									
7											
8											
9											
10											
11	Compute (xp,yp):										
12	xp	yp	z (mm)	cx	cy	f	size	f/size			
13	745	90	890	640	360	1.88E-03	1.40E-06	1.3429E+03			
14											
15	xc	yc									
16	70	-179									
17											
18											
19											
20											
21											
22											
23											
24											
25											

Sheet1

Ready 100%



## EXAMPLE: 2-DOF visual servoing (continued)

Initial pixel coordinates of P1 can be computed as: (745,90).

Calculate image Jacobian numerically by perturbing each axis separately and noting change in image space of P1.

Perturb from  $Y = 0$  to  $Y = +3$  mm. New P1 pixel coordinates are: (741,90).

Return to initial pose.

Perturb from  $Z = 0$  to  $Z = -3$  mm. New P1 pixel coordinates are: (745,86).

Form image Jacobian matrix (once):

$$\begin{aligned} J' &= [dx_p/dY \ dx_p/dZ; \ dy_p/dY \ dy_p/dZ] \quad 2 \times 2 \text{ matrix} \\ &= [(741-745)/3 \ (745-745)/(-3); \ (90-90)/3 \ (86-90)/(-3)] \\ &= [-4/3 \ 0; \ 0 \ 4/3] \end{aligned}$$

Take inverse:

$$\text{inv}(J') = [-0.75 \ 0; \ 0 \ 0.75]$$

Update 2-DOF robot axes via VS (set  $\lambda = 1$ ):

$$[Y_{\text{new}}; Z_{\text{new}}] = [Y_{\text{prev}}; Z_{\text{prev}}] - \text{inv}(J') * [745 - 640; 90 - 360]$$

*image error vector, e:  
actual – desired pixel coordinates*

$$= [0; 0] - \text{inv}(J') * [745 - 640; 90 - 360]$$

$$= [78.75 \text{ mm}; 202.5 \text{ mm}]$$

→ corresponds to P1 pixel coordinates of (633,355)

## Additional VS iterations:

$$[Y_{\text{new}}; Z_{\text{new}}] = [78.75; 202.5] - \text{inv}(J') * [627 - 640; 396 - 360]$$

$$= [65.75 \text{ mm}; 166.5 \text{ mm}]$$

→ corresponds to P1 pixel coordinates of (646,341)

$$[Y_{\text{new}}; Z_{\text{new}}] = [65.75; 166.5] - \text{inv}(J') * [646 - 640; 341 - 360]$$

$$= [59.75 \text{ mm}; 185.5 \text{ mm}]$$

→ corresponds to P1 pixel coordinates of (655,370)

$$[Y_{\text{new}}; Z_{\text{new}}] = [59.75; 185.5] - \text{inv}(J') * [655 - 640; 370 - 360]$$

$$= [74.75 \text{ mm}; 175.5 \text{ mm}]$$

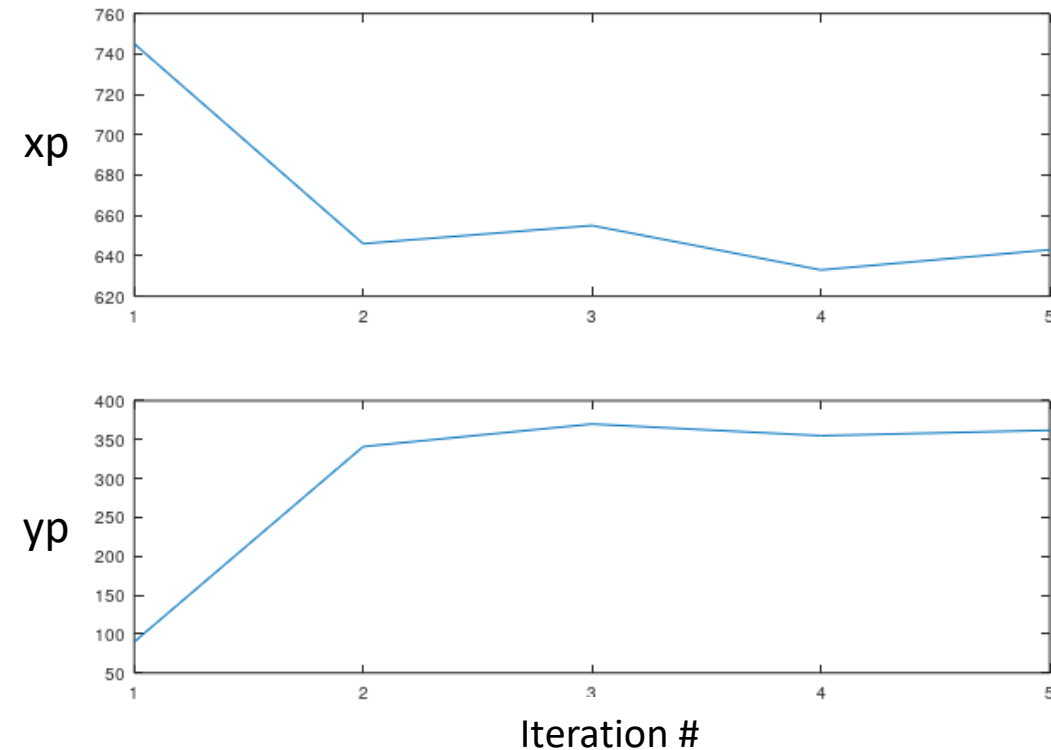
→ corresponds to P1 pixel coordinates of (633,355)

$$[Y_{\text{new}}; Z_{\text{new}}] = [74.75; 175.5] - \text{inv}(J') * [633 - 640; 355 - 360]$$

$$= [67.75 \text{ mm}; 180.5 \text{ mm}]$$

*compare to known solution of (Y,Z) = (69.904,178.923)*

→ corresponds to P1 pixel coordinates of (643,362)



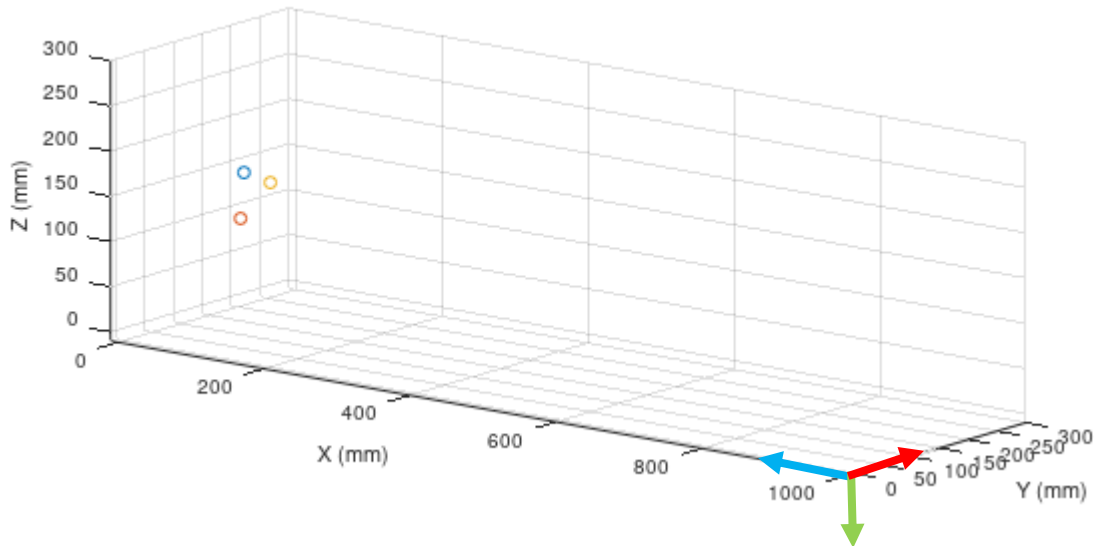
three-point physical target locations (w.r.t. XYZ world coordinate frame in mm):

**P1 = (110, 69.904, 178.923)**

**P2 = (110, 63.923, 129.282)**

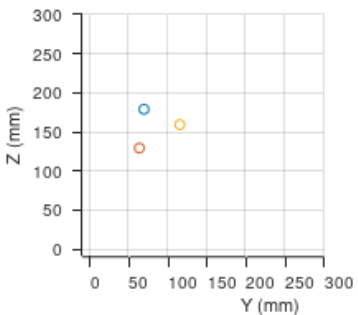
**P3 = (110, 115.885, 159.282)**

three-point target in XYZ coordinate frame



camera/robot  
at initial pose

three-point target in XYZ coordinate frame



4-DOF “flying robot”: D435 camera that can move along X, Y, & Z and can rotate about  $z_c$

**Initial robot pose:** XYZ = (1000, 0, 0) and  $z_c$  is parallel to -X and  $x_c$  is parallel to +Y (see figure at left)



**Task:** implement method to actuate the 4 robot axes so that the three target points coincide with the desired pixel locations in image space (below).

