

~\Documents\documents_general\structured_courses\math564\evaluations\projects
p05\pathtime.m

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1 function [f,g]=pathtime(x,par)
2
3 % parse the input data
4 % n is the number of sinusoid coefficients for x and for y
5 % w,z are the decision variable weights
6 % v is the velocity map array (rows are y, cols are x)
7 % A,B are the (x,y) coordinates of the beginning and ending points
8 n=length(x)/2;
9 w=x(1:n);
10 z=x(n+1:end);
11 v=par.v;
12 [my,mx]=size(v);
13 A=par.A;
14 B=par.B;
15
16 % construct a piecewise linear path approximation for computation
17 % xx,yy are the x and y coordinates along the path on [0,1]x[0,1]
18 % s is the variable that parametrically defines the path
19 s=linspace(0,1,1000)';
20 xx=(1-s)*A(1)+s*B(1);
21 yy=(1-s)*A(2)+s*B(2);
22 for k=1:n % you can do this without a loop
23     S=sin(k*pi*s);
24     xx=xx+w(k)*S;
25     yy=yy+z(k)*S;
26 end
27
28 % xxr,yyr are the coordinates of the midpoint of each line segment
29 % in the velocity array index units. Any points outside of the array
30 % are set at the boundary using max/min functions.
31 xxm=1+xx*(mx-1);
32 yym=1+yy*(my-1);
33 xxm=(xxm(2:end)+xxm(1:end-1))/2;
34 yym=(yyym(2:end)+yyym(1:end-1))/2;
35 xxm=max(min(xxm,mx),1);
36 yym=max(min(yym,my),1);
37
38 % compute the travel time. dist is the distance on [0,1]x[0,1]
39 % between line segment end points -- summed. vel is the velocity
40 % at the midpoint interpolated from array data. f is travel time.
41 dist=sqrt(diff(xx).^2+diff(yy).^2);
42 vel=interp2(v,xxm,yyym);
43 f=sum(dist./vel);
44
45 % compute the gradient by approximation
46 if nargout>1
47     del=sqrt(eps);
48     g=zeros(2*n,1);
49     for j=1:2*n
50         y=x;
51         y(j)=y(j)+del;
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52         df=pathtime(y,par);
53         g(j)=(df-f)/del;
54     end
55 end
56
57 return
```