

In the following subsections, the proposed algorithm is compared against the centralized (MPCOPF) algorithm in terms of resultant optimal control variables, optimality gap in objective function and computational performance. Secondly, the resultant control variables are tested for ACOPF feasibility against OpenDSS. Section -A describes the comparison over a 5 time-period horizon with an additional focus on describing the workflow of the MPDOPF algorithm. Section -B describes the comparison over a 10 time-period horizon to test for the scalability of the MPDOPF algorithm.

#### A. Simulation Results

Table I represents a comparison between MPCOPF and MPDOPF in their problem scope, results and computational performance.

##### 1) Biggest Subproblem vs Computational Performance:

This first section of the table, 'Biggest subproblem' provides specifics of the 'computational bottleneck' encountered by either algorithm during its course. As established in ??, the bottleneck represents the OPF subproblem which is computationally the most intensive, and thus is a key indicator of the expected time the algorithm will take to complete.

TABLE I: Comparative analyses between MPCOPF and MPDOPF - 5 time-period horizon

| Metric                           | MPCOPF  | MPDOPF  |
|----------------------------------|---------|---------|
| Biggest subproblem               |         |         |
| Decision variables               | 3150    | 1320    |
| Linear constraints               | 5831    | 2451    |
| Nonlinear constraints            | 635     | 265     |
| Simulation results               |         |         |
| Substation power cost (\$)       | 576.31  | 576.30  |
| Substation real power (kW)       | 4308.28 | 4308.14 |
| Line loss (kW)                   | 75.99   | 76.12   |
| Substation reactive power (kVAR) | 574.18  | 656.24  |
| PV reactive power (kVAR)         | 116.92  | 160.64  |
| Battery reactive power (kVAR)    | 202.73  | 76.01   |
| Computation                      |         |         |
| Number of Iterations             | -       | 5       |
| Total Simulation Time (s)        | 521.25  | 49.87   |

Further, here the

TABLE II: ACOPF feasibility analyses - 5 time-period horizon

| Metric                           | MPDOPF  | OpenDSS |
|----------------------------------|---------|---------|
| Full horizon                     |         |         |
| Substation real power (kW)       | 4308.14 | 4308.35 |
| Line loss (kW)                   | 76.12   | 76.09   |
| Substation reactive power (kVAR) | 656.24  | 652.49  |
| Max. all-time discrepancy        |         |         |
| Voltage (pu)                     |         | 0.0002  |
| Line loss (kW)                   |         | 0.0139  |
| Substation power (kW)            |         | 0.3431  |

Boundary Variable Plots are too tall, make them slightly shorter, like 25% of the page only.

#### B. Scalability Analysis

To demonstrate the effectiveness of the proposed algorithm over a bigger horizon to demonstrate scalability, simulations were run for a 10 time-period horizon. Figure 4 shows

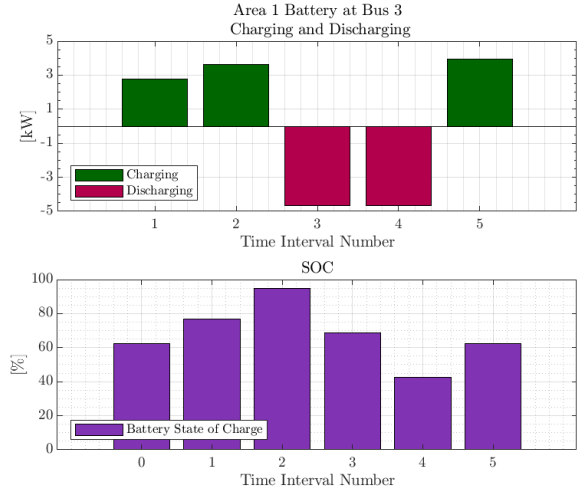


Fig. 1: Charging-Discharging and SOC graphs for Battery at Bus 3 located in Area 1 obtained by MPDOPF

the forecasted profiles for load, solar irradiance and cost of substation power over the horizon.

1) *Comparison between MPCOPF and MPDOPF:* In this section, comparative analyses are carried out between MPCOPF and MPDOPF considering 10-hour time steps with 20% PV penetration and 30% battery penetration.

TABLE III: Comparative analyses between MPCOPF and MPDOPF - 10 time-period horizon

| Metric                           | MPCOPF  | MPDOPF  |
|----------------------------------|---------|---------|
| Biggest subproblem               |         |         |
| Decision variables               | 6300    | 2640    |
| Linear constraints               | 11636   | 4891    |
| Nonlinear constraints            | 1270    | 530     |
| Simulation results               |         |         |
| Substation power cost (\$)       | 1197.87 | 1197.87 |
| Substation real power (kW)       | 8544.28 | 8544.04 |
| Line loss (kW)                   | 148.67  | 148.94  |
| Substation reactive power (kVAR) | 1092.39 | 1252.03 |
| PV reactive power (kVAR)         | 222.59  | 139.81  |
| Battery reactive power (kVAR)    | 388.52  | 310.94  |
| Computation                      |         |         |
| Number of Iterations             | -       | 5       |
| Total Simulation Time (s)        | 4620.73 | 358.69  |

Further, here the

TABLE IV: ACOPF feasibility analyses - 10 time-period horizon

| Metric                           | MPDOPF  | OpenDSS |
|----------------------------------|---------|---------|
| Full horizon                     |         |         |
| Substation real power (kW)       | 8544.04 | 8544.40 |
| Line loss (kW)                   | 148.94  | 148.87  |
| Substation reactive power (kVAR) | 1252.03 | 1243.36 |
| Max. all-time discrepancy        |         |         |
| Voltage (pu)                     |         | 0.0002  |
| Line loss (kW)                   |         | 0.0132  |
| Substation power (kW)            |         | 0.4002  |

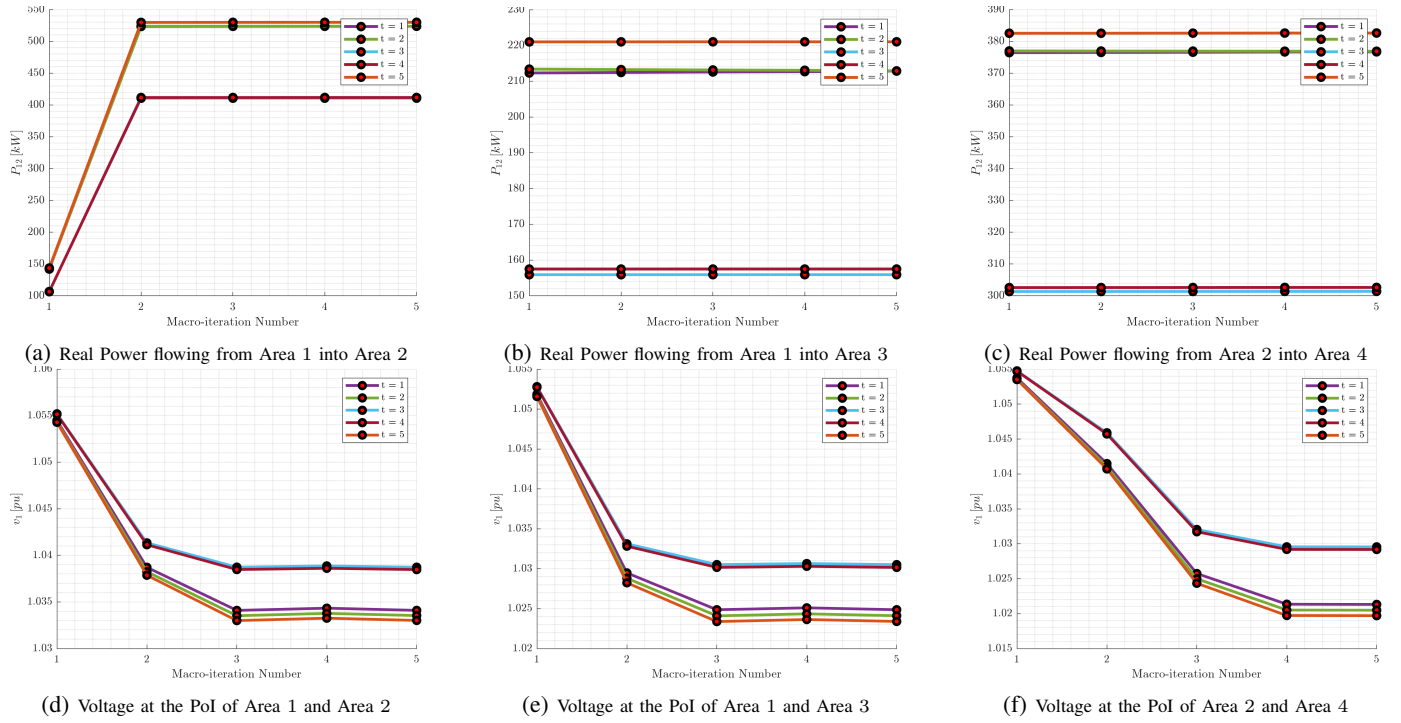


Fig. 2: Convergence of Boundary variables with every iteration. Each plot represents a particular variable exchanged between a pair of connected areas. Each line graph within a plot represents a particular time period.

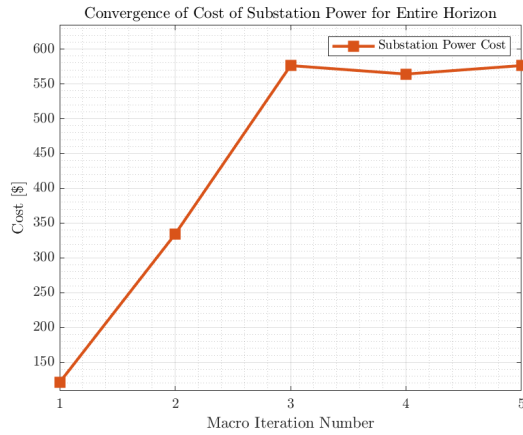


Fig. 3: Convergence of Objective Function Value with each MPDOPF iteration

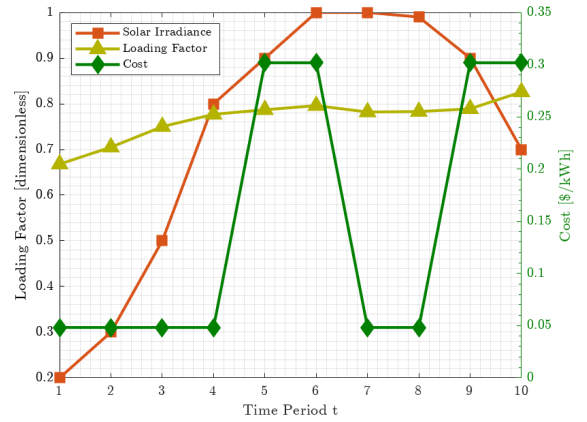


Fig. 4: Forecasts for Demand Power, Irradiance and Cost of Substation Power over a 10 Hour Horizon

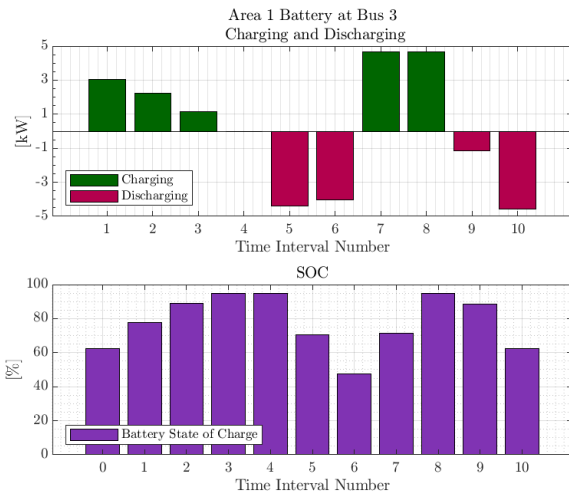


Fig. 5: Charging-Discharging and SOC graphs for Battery at Bus 3 located in Area 1 obtained via MPDOPF