



WASHINGTON STATE
UNIVERSITY

MPOPF Simulation and OpenDSS Validation

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Washington State University

strLoadShape = 'New Loadshape.LoadShape npts =8 interval = 1 mult = [0.705 0.75 0.777 0.787 0.796 0.782 0.783 0.789]'

strLoadShapePV = 'New Loadshape.LoadShapePV npts =8 interval = 1 mult = [0.3 0.5 0.8 0.9 1 1 0.99 0.9]'

MPDOPF Verified for $T = 8, PV = 10\%, Batt = 15\%$

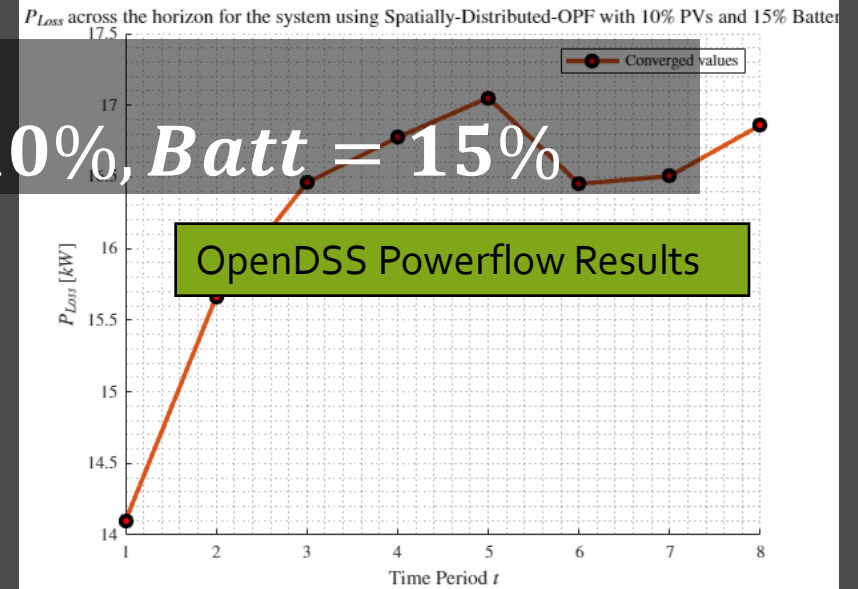
MPDOPF Simulation Results

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01. Machine ID: ETRL204-ARYAN  
02. Horizon Duration: 8  
03. Nature of Simulation: Spatially-Distributed-OPF with 4 Areas.  
04. GED Configuration: pv_10_batt_15  
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Hour: Full 8 Hour Horizon

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01. Horizon Line Loss: 129.87 kW  
02. Horizon Total Substation Power: 7081.55 kW + 1415.56 kVAr  
03. Horizon Total Load: 7175.76 kW + 3948.23 kVAr  
04. Horizon Total Generation: 223.61 kW + 2791.98 kVAr  
05. Horizon Total PV Generation: 223.61 kW + 45.49 kVAr  
06. Horizon Total Battery Generation: -0.00 kW + -53.51 kVAr  
07. Horizon Total Static Capacitor Reactive Power Generation: 2800.00 kVAr  
08. Horizon Total Substation Power Cost: $239.48  
09. Horizon Total SCD Observed: 0.00 kW  
10. Horizon-end Battery Energy Deviation from Reference: 0.00 kWh  
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11. Number of Macro-Iterations: 5  
12. Simulation Time: 769.62 s  
13. Time to solve with sequential (non-parallel) computation: 740.73 s  
14. Time to solve if OPF computation parallelized: 468.59 s
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Hour: Full 8 Hour Horizon

```
Horizon Line Loss: 129.8017 kW  
Horizon Total Substation Power: 7081.9146 kW + 1408.5741 kVAr  
Horizon Total Load: 7175.7623 kW + 3948.234 kVAr  
Horizon Total Generation: 223.6076 kW + 2791.9764 kVAr  
Horizon Total PV Generation: 223.6058 kW + 45.487 kVAr  
Horizon Total Battery Generation: 0.0017449 kW + -53.5106 kVAr  
Horizon Total Static Capacitor Reactive Power Generation: 2800 kVAr  
Horizon Substation Power Cost: $ 239.4947  
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```

Horizon Period (hourly time-steps): 8 h

GED Penetration: 10% PVs + 15% Batteries

Maximum All Time Voltage Discrepancy: 0.000149 pu

Maximum All Time Line Loss Discrepancy: 0.011397 kW

Maximum All Time Substation Borrowed Real Power Discrepancy: 0.13449 kW

Maximum All Time Substation Borrowed Reactive Power Discrepancy: 0.95273 kVAr

strLoadShape = 'New Loadshape.LoadShape npts =8 interval = 1 mult = [0.705 0.75 0.777 0.787 0.796 0.782 0.783 0.789]'

strLoadShapePV = 'New Loadshape.LoadShapePV npts =8 interval = 1 mult = [0.3 0.5 0.8 0.9 1 1 0.99 0.9]'

MPCOPF Verified for $T = 8, PV = 10\%, Batt = 15\%$

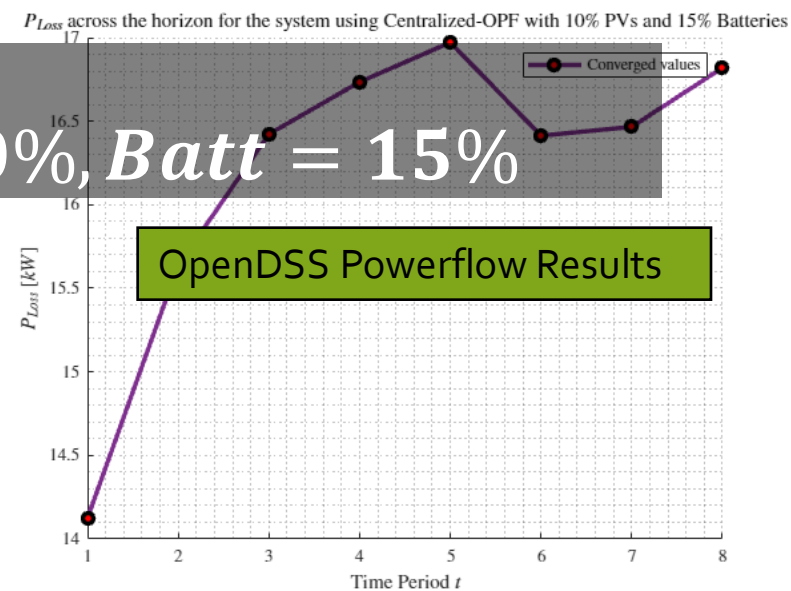
MPCOPF Simulation Results

```
-----
01. Machine ID: ETRL204-ARYAN
02. Horizon Duration: 8
03. Nature of Simulation: Centralized-OPF
04. GED Configuration: pv_10_batt_15
-----
```

Hour: Full 8 Hour Horizon

```
01. Horizon Line Loss: 129.59 kW
02. Horizon Total Substation Power: 7081.84 kW + 1285.80 kVAr
03. Horizon Total Load: 7175.76 kW + 3948.23 kVAr
04. Horizon Total Generation: 223.51 kW + 2922.02 kVAr
05. Horizon Total PV Generation: 223.61 kW + 128.23 kVAr
06. Horizon Total Battery Generation: -0.10 kW + -6.22 kVAr
07. Horizon Total Static Capacitor Reactive Power Generation: 2800.00 kVAr
08. Horizon Total Substation Power Cost: $239.51
09. Horizon Total SCD Observed: -0.00 kW
10. Horizon-end Battery Energy Deviation from Reference: 0.00 kWh
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11. Number of Macro-Iterations: 1
12. Simulation Time: 1872.15 s
13. Time to solve with sequential (non-parallel) computation: 1191.35 s
14. Time to solve if OPF computation parallelized: 1191.35 s
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```



Hour: Full 8 Hour Horizon

```
Horizon Line Loss: 129.5051 kW
Horizon Total Substation Power: 7081.7363 kW + 1277.9781 kVAr
Horizon Total Load: 7175.7623 kW + 3948.234 kVAr
Horizon Total Generation: 223.5079 kW + 2922.011 kVAr
Horizon Total PV Generation: 223.6058 kW + 128.2327 kVAr
Horizon Total Battery Generation: -0.097902 kW + -6.2217 kVAr
Horizon Total Static Capacitor Reactive Power Generation: 2800 kVAr
Horizon Substation Power Cost: $ 239.5056
```

Horizon Period (hourly time-steps): 8 h

GED Penetration: 10% PVs + 15% Batteries

Maximum All Time Voltage Discrepancy: 8.8485e-05 pu

Maximum All Time Line Loss Discrepancy: 0.013391 kW

Maximum All Time Substation Borrowed Real Power Discrepancy: 0.072875 kW

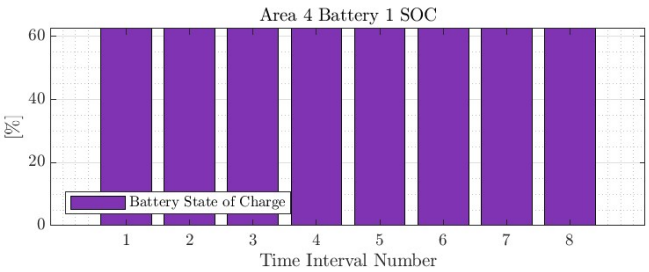
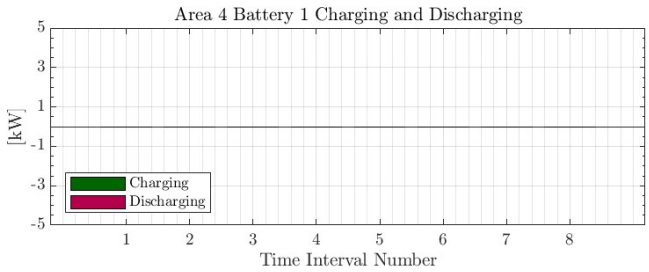
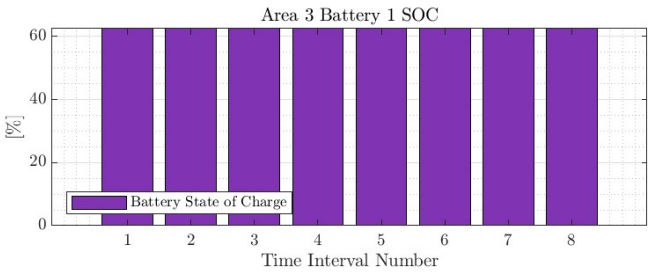
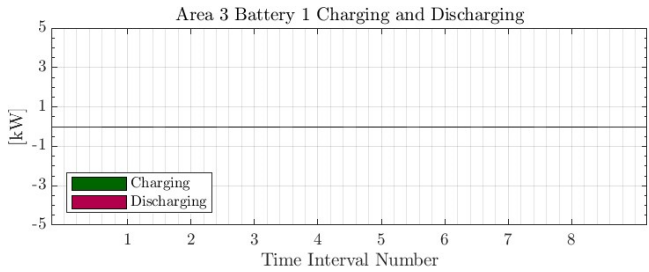
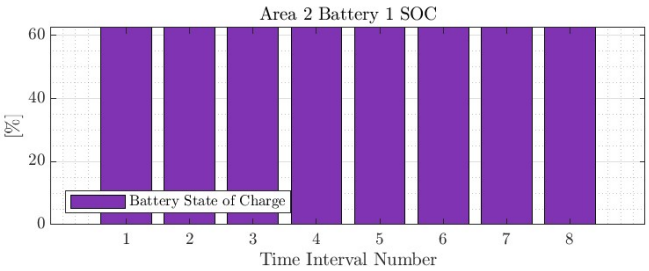
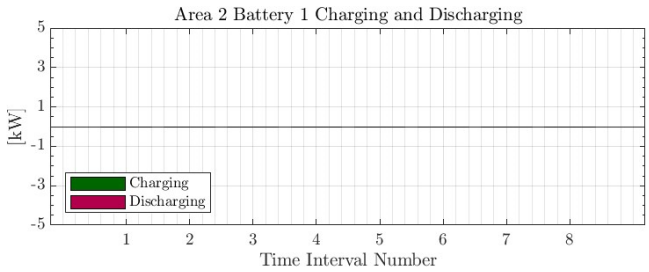
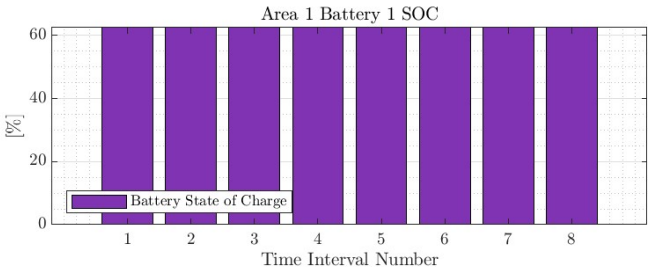
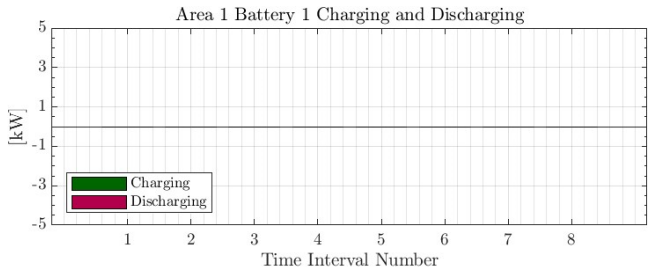
Maximum All Time Substation Borrowed Reactive Power Discrepancy: 1.0043 kVAr

strLoadShape = 'New Loadshape.LoadShape npts =8 interval = 1 mult = [0.705 0.75 0.777 0.787 0.796 0.782 0.783 0.789]'

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1, 5, 6, 8 in
COPF values

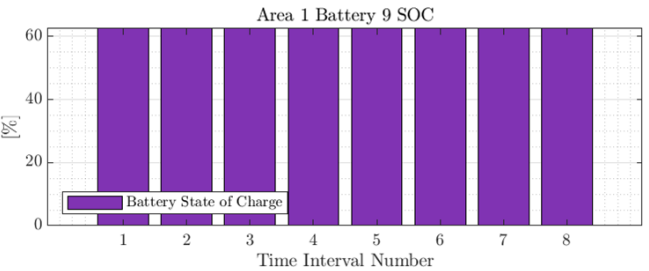
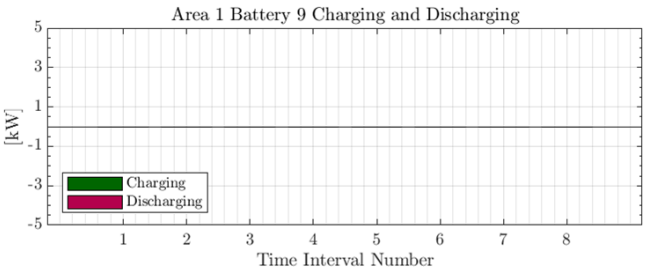
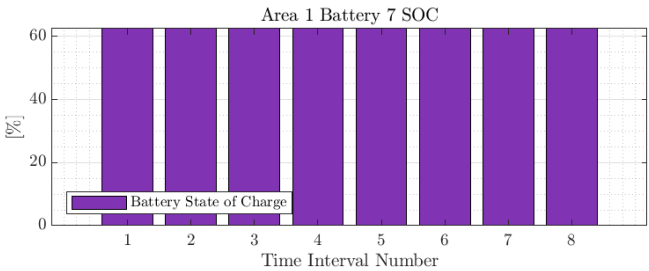
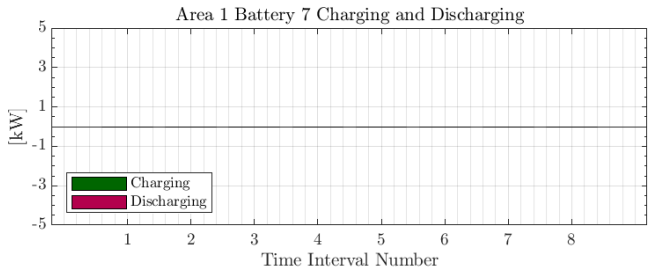
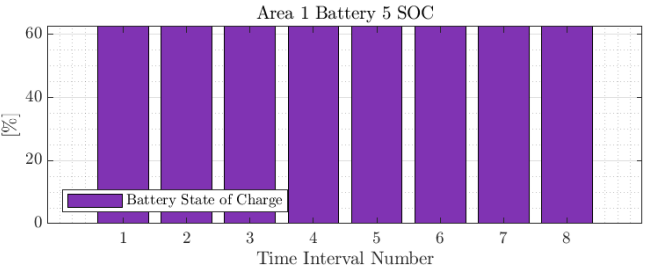
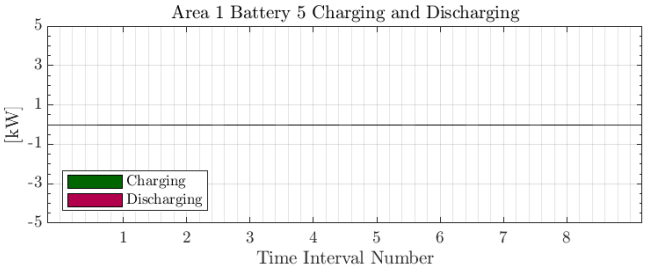
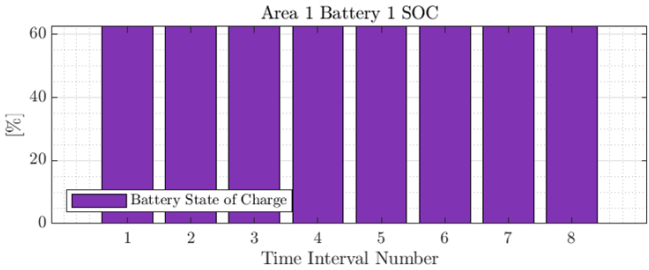
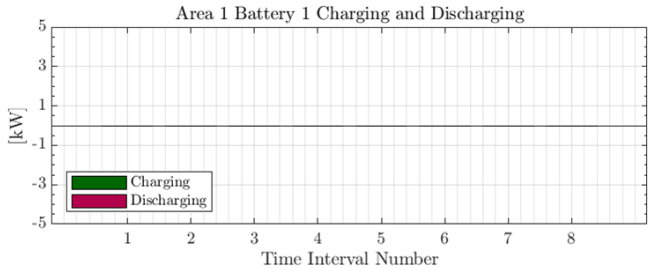
MPDOPF Verified for $T = 8, PV = 10\%, Batt = 15\%$



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MP-COPF Verified for $T = 8, PV = 10\%, Batt = 15\%$

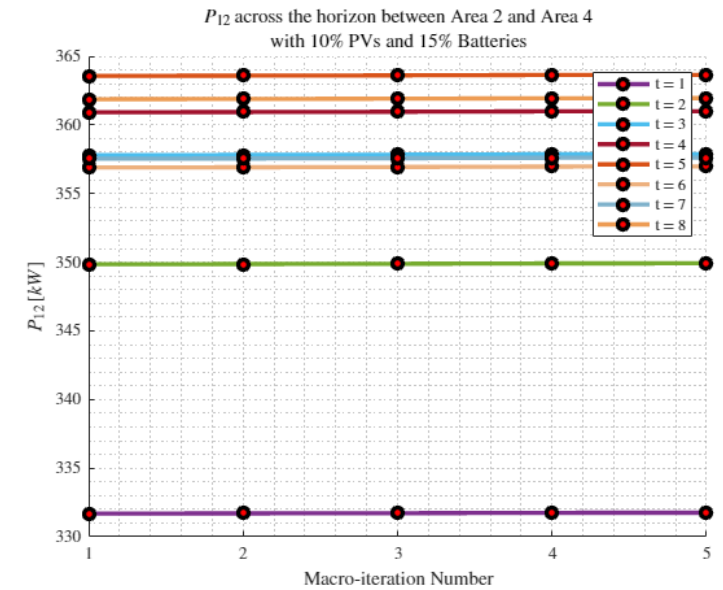
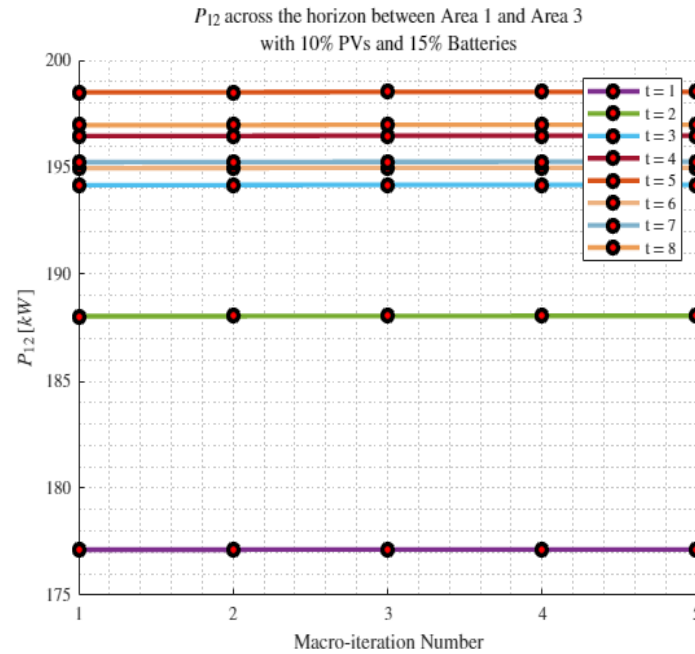
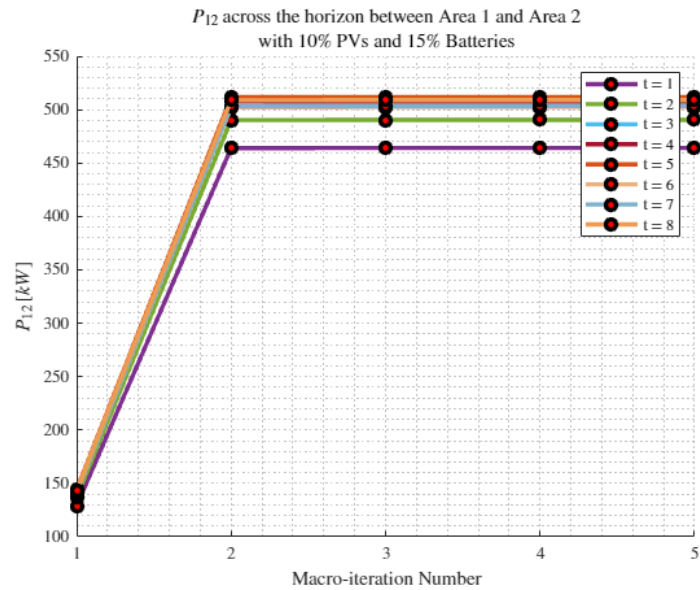


strLoadShape = 'New Loadshape.LoadShape npts =8 interval = 1 mult = [0.705 0.75 0.777 0.787 0.796 0.782 0.783 0.789]'

strLoadShapePV = 'New Loadshape.LoadShapePV npts =8 interval = 1 mult = [0.3 0.5 0.8 0.9 1 1 0.99 0.9]'

MPDOPF Verified for $T = 8$, $PV = 10\%$, $Batt = 15\%$

Boundary Complex Powers



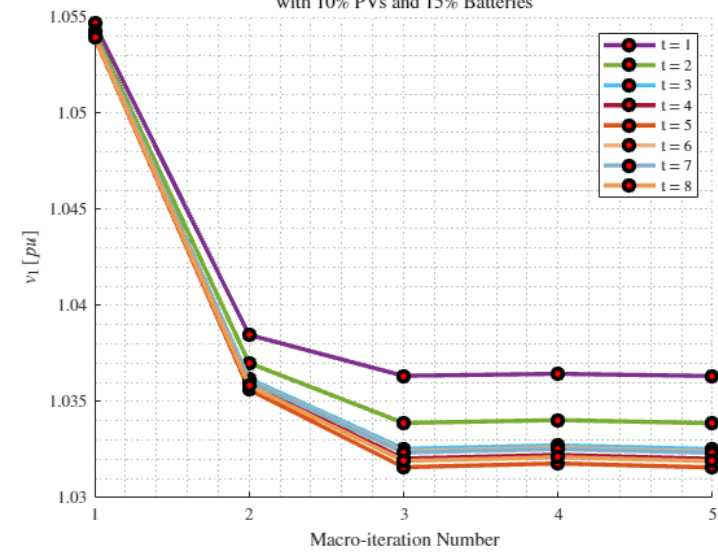
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strLoadShapePV = 'New Loadshape.LoadShapePV npts =8 interval = 1 mult = [0.3 0.5 0.8 0.9 1 1 0.99 0.9]'

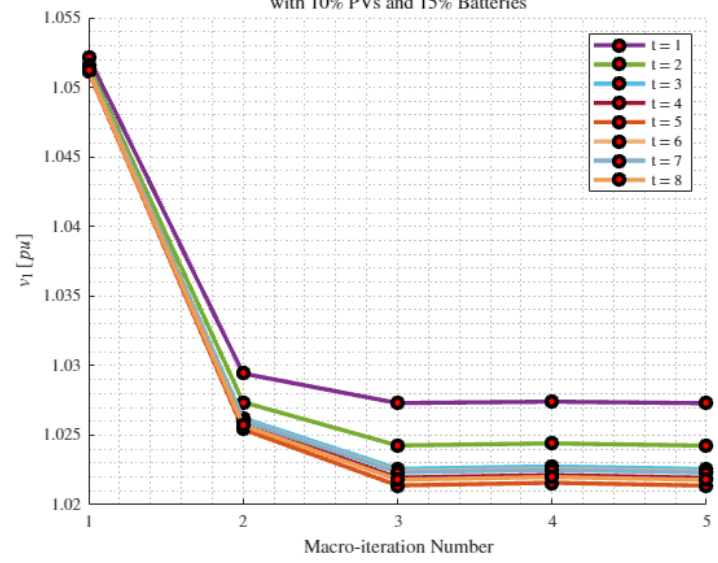
MPDOPF Verified for $T = 8, PV = 10\%, Batt = 15\%$

Boundary Voltages

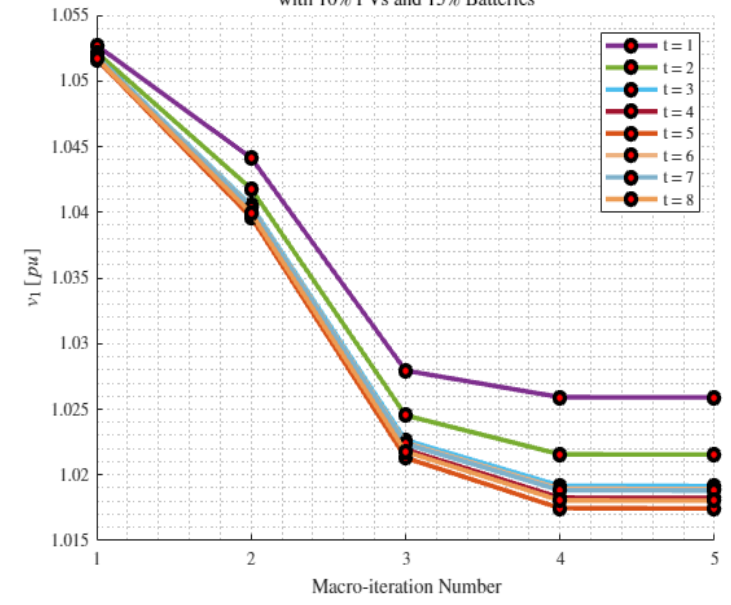
v_1 across the horizon between Area 1 and Area 2
with 10% PVs and 15% Batteries



v_1 across the horizon between Area 1 and Area 3
with 10% PVs and 15% Batteries



v_1 across the horizon between Area 2 and Area 4
with 10% PVs and 15% Batteries



strLoadShape = 'New Loadshape.LoadShape npts =10 interval = 1 mult = [0.668 0.705 0.75 0.777 0.787 0.796 0.782 0.783 0.789 0.826]'

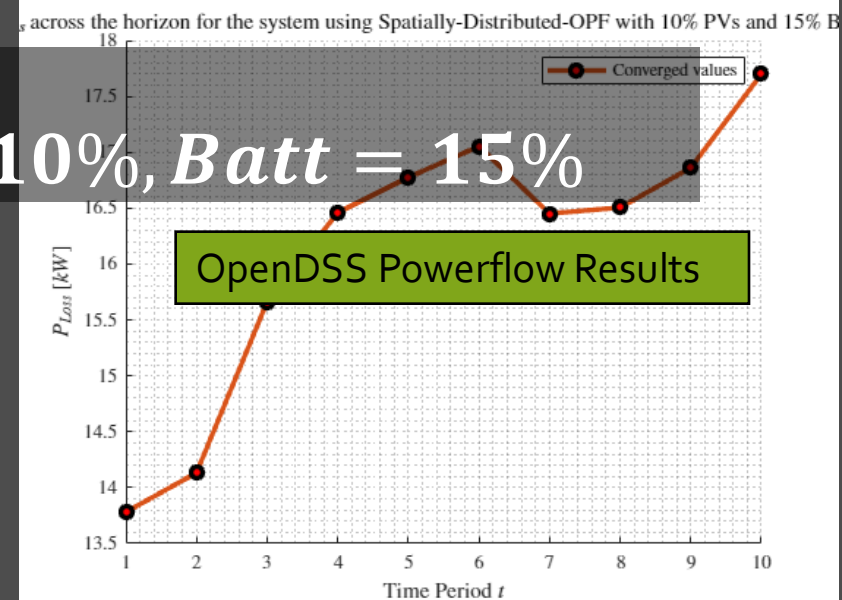
strLoadShapePV = 'New Loadshape.LoadShapePV npts =10 interval = 1 mult = [0.2 0.3 0.5 0.8 0.9 1 1 0.99 0.9 0.7]'

MPDOPF Verified for $T = 10$, $PV = 10\%$, $Batt = 15\%$

MPDOPF Simulation Results

```
-----
01. Machine ID: ETRL204-ARYAN
02. Horizon Duration: 10
03. Nature of Simulation: Spatially-Distributed-OPF with 4 Areas.
04. GED Configuration: pv_10_batt_15
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```

```
-----
Hour: Full 10 Hour Horizon
01. Horizon Line Loss: 161.38 kW
02. Horizon Total Substation Power: 8822.85 kW + 1739.65 kVAr
03. Horizon Total Load: 8913.58 kW + 4904.41 kVAr
04. Horizon Total Generation: 251.37 kW + 3487.00 kVAr
05. Horizon Total PV Generation: 255.10 kW + 55.46 kVAr
06. Horizon Total Battery Generation: -3.73 kW + -68.46 kVAr
07. Horizon Total Static Capacitor Reactive Power Generation: 3500.00 kVAr
08. Horizon Total Substation Power Cost: $284.48
09. Horizon Total SCD Observed: -0.00 kW
10. Horizon-end Battery Energy Deviation from Reference: 0.00 kWh
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11. Number of Macro-Iterations: 5
12. Simulation Time: 3942.82 s
13. Time to solve with sequential (non-parallel) computation: 3903.53 s
14. Time to solve if OPF computation parallelized: 3485.18 s
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Hour: Full 10 Hour Horizon
Horizon Line Loss: 161.5011 kW
Horizon Total Substation Power: 8830.6928 kW + 1731.3489 kVAr
Horizon Total Load: 8913.5786 kW + 4904.412 kVAr
Horizon Total Generation: 244.3731 kW + 3486.9955 kVAr
Horizon Total PV Generation: 248.1008 kW + 55.4602 kVAr
Horizon Total Battery Generation: -3.7278 kW + -68.4647 kVAr
Horizon Total Static Capacitor Reactive Power Generation: 3500 kVAr
Horizon Substation Power Cost: $ 284.716
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Horizon Period (hourly time-steps): 10 h
GED Penetration: 10% PVs + 15% Batteries
Maximum All Time Voltage Discrepancy: 0.00030211 pu
Maximum All Time Line Loss Discrepancy: 0.23144 kW
Maximum All Time Substation Borrowed Real Power Discrepancy: 8.7069 kW
Maximum All Time Substation Borrowed Reactive Power Discrepancy: 0.973 kVAr
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```


strLoadShape = 'New Loadshape.LoadShape npts =10 interval = 1 mult = [0.668 0.705 0.75 0.777 0.787 0.796 0.782 0.783 0.789 0.826]'

strLoadShapePV = 'New Loadshape.LoadShapePV npts =10 interval = 1 mult = [0.2 0.3 0.5 0.8 0.9 1 1 0.99 0.9 0.7]'

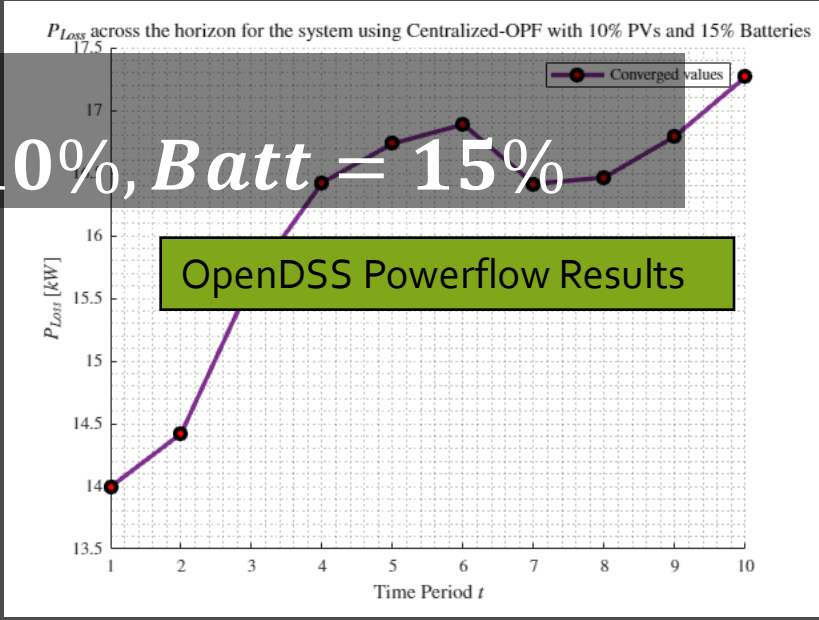
MPCOPF Verified for $T = 10, PV = 10\%, Batt = 15\%$

MPCOPF Simulation Results

- 01. Machine ID: ETRL204-ARYAN
- 02. Horizon Duration: 10
- 03. Nature of Simulation: Centralized-OPF
- 04. GED Configuration: pv_10_batt_15

```
-----
Hour: Full 10 Hour Horizon
01. Horizon Line Loss: 161.03 kW
02. Horizon Total Substation Power: 8824.15 kW + 1586.67 kVar
03. Horizon Total Load: 8913.58 kW + 4904.41 kVar
04. Horizon Total Generation: 250.46 kW + 3640.31 kVar
05. Horizon Total PV Generation: 255.10 kW + 151.88 kVar
06. Horizon Total Battery Generation: -4.64 kW + -11.57 kVar
07. Horizon Total Static Capacitor Reactive Power Generation: 3500.00 kVar
08. Horizon Total Substation Power Cost: $284.71
09. Horizon Total SCD Observed: -0.10 kW
10. Horizon-end Battery Energy Deviation from Reference: 0.00 kWh
-----
11. Number of Macro-Iterations: 1
12. Simulation Time: 10125.58 s
13. Time to solve with sequential (non-parallel) computation: 10100.61 s
14. Time to solve if OPF computation parallelized: 10100.61 s
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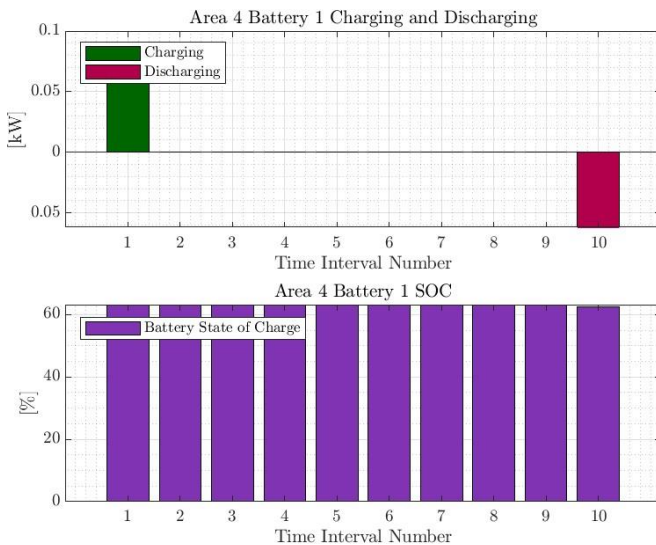
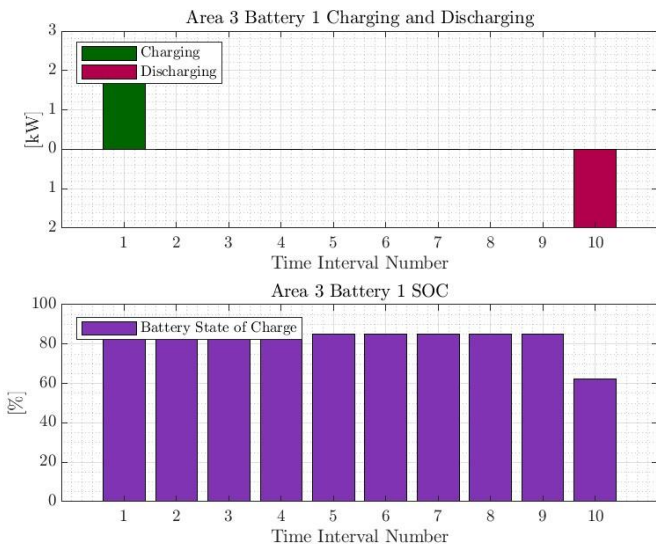
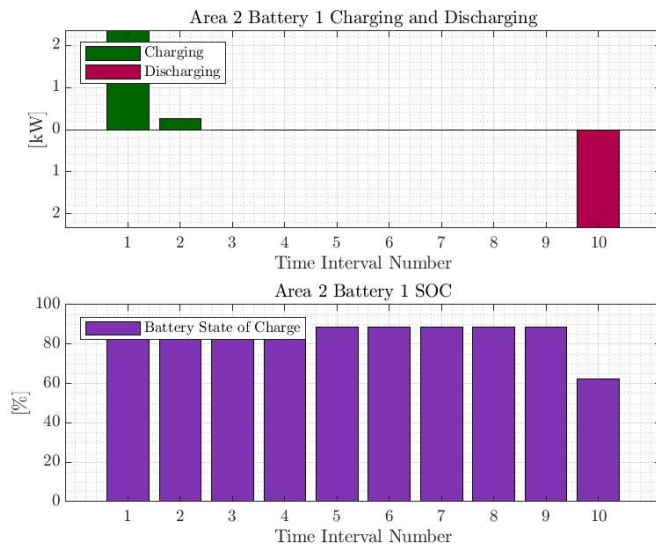
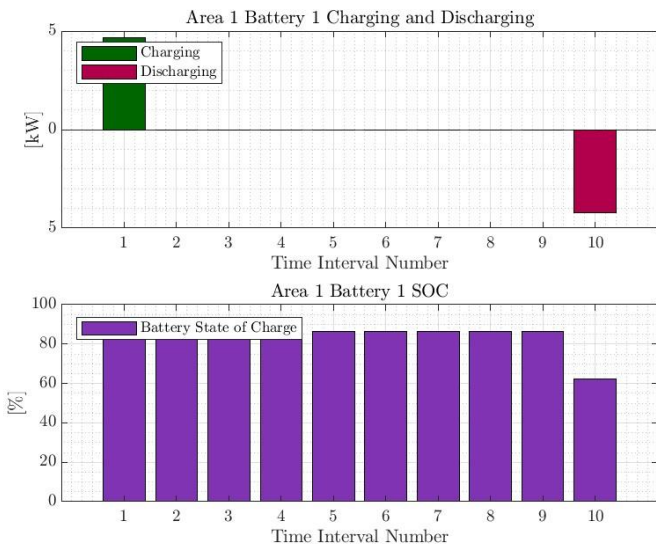
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Hour: Full 10 Hour Horizon
Horizon Line Loss: 161.0605 kW
Horizon Total Substation Power: 8829.266 kW + 1577.1768 kVar
Horizon Total Load: 8913.5786 kW + 4904.412 kVar
Horizon Total Generation: 245.3898 kW + 3640.299 kVar
Horizon Total PV Generation: 248.0943 kW + 151.8789 kVar
Horizon Total Battery Generation: -2.7045 kW + -11.5799 kVar
Horizon Total Static Capacitor Reactive Power Generation: 3500 kVar
Horizon Substation Power Cost: $ 284.8622
-----
Horizon Period (hourly time-steps): 10 h
GED Penetration: 10% PVs + 15% Batteries
Maximum All Time Voltage Discrepancy: 0.00015989 pu
Maximum All Time Line Loss Discrepancy: 0.19634 kW
Maximum All Time Substation Borrowed Real Power Discrepancy: 7.2355 kW
Maximum All Time Substation Borrowed Reactive Power Discrepancy: 1.0955 kVar
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```



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strLoadShapePV = 'New Loadshape.LoadShapePV npts =10 interval = 1 mult = [0.2 0.3 0.5 0.8 0.9 1 1 0.99 0.9 0.7]'

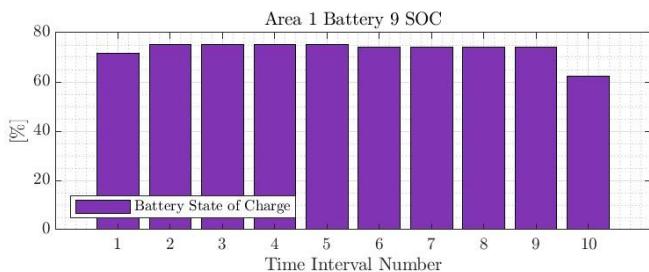
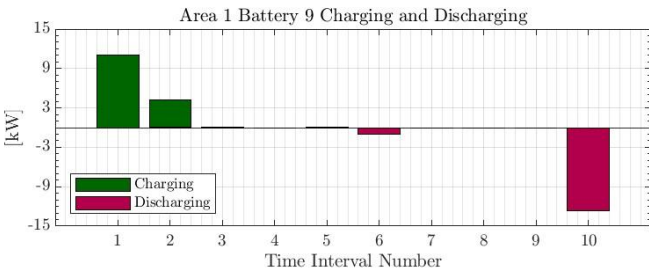
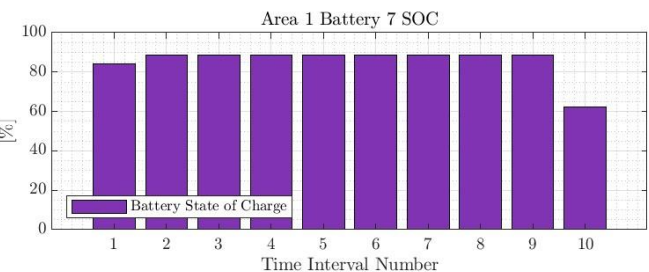
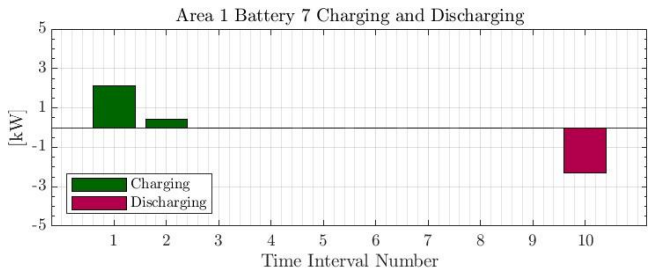
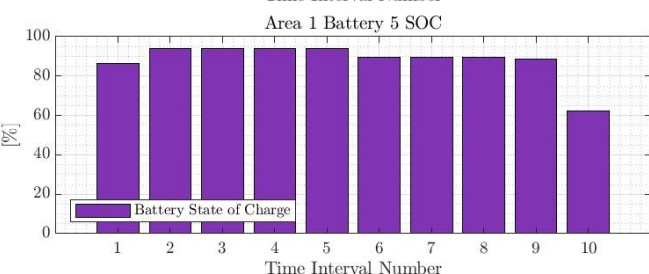
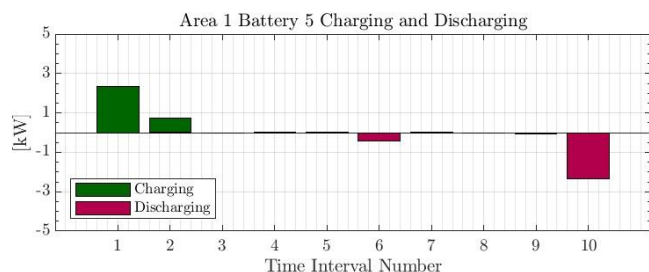
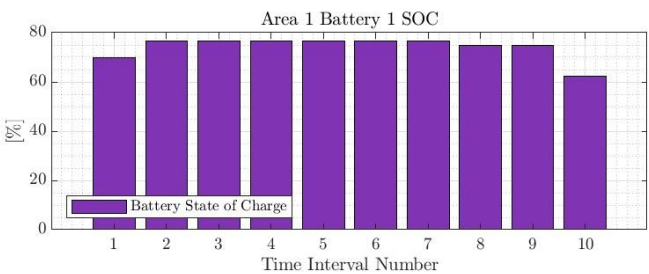
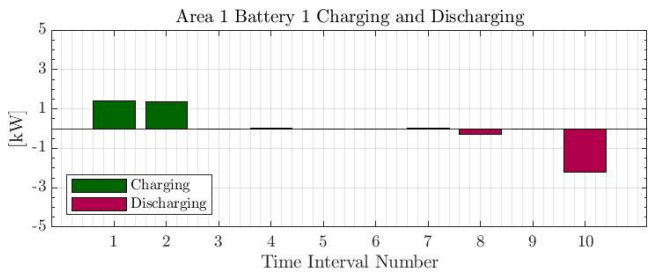
MPDOPF Verified for $T = 10, PV = 10\%, Batt = 15\%$



strLoadShape = 'New Loadshape.LoadShape npts =10 interval = 1 mult = [0.668 0.705 0.75 0.777 0.787 0.796 0.782 0.783 0.789 0.826]'

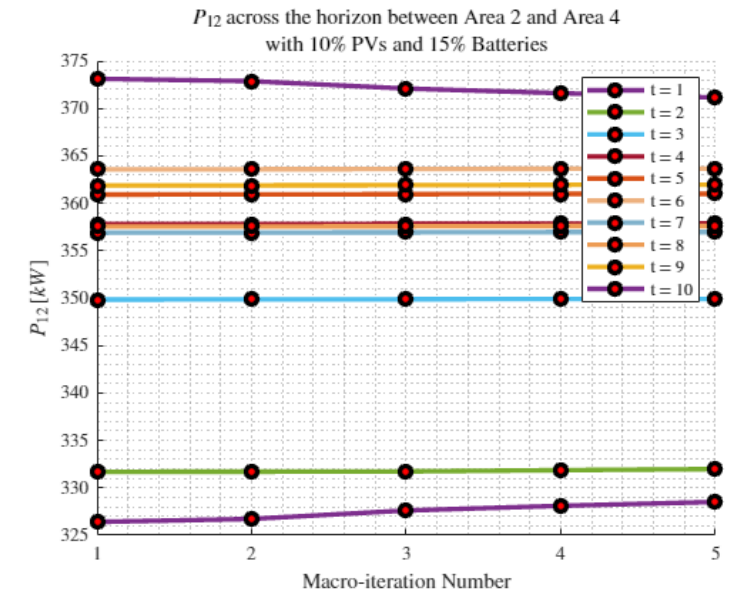
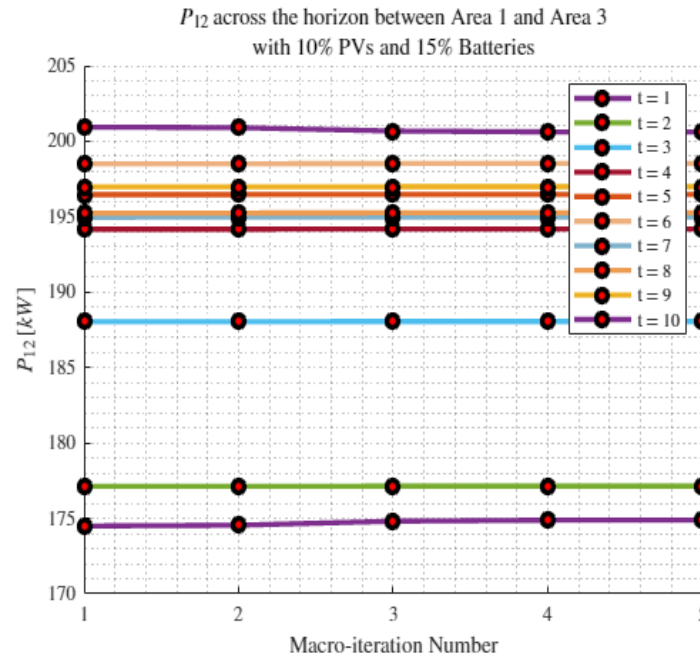
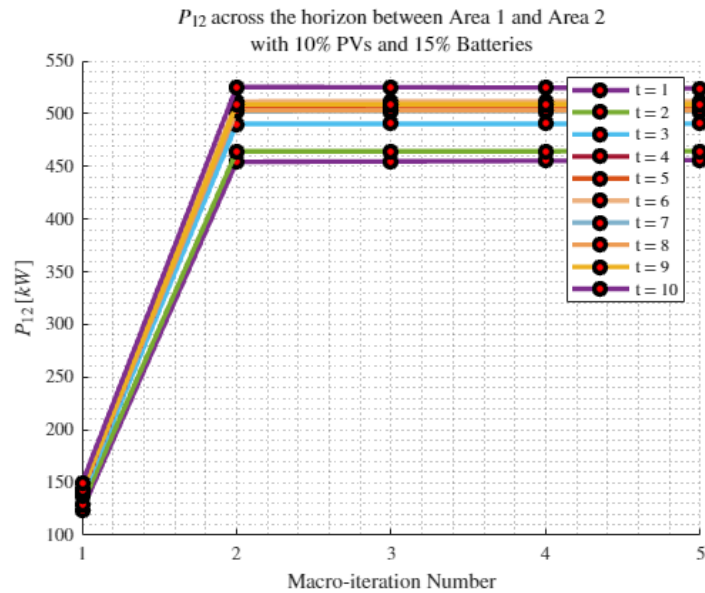
strLoadShapePV = 'New Loadshape.LoadShapePV npts =10 interval = 1 mult = [0.2 0.3 0.5 0.8 0.9 1 1 0.99 0.9 0.7]'

MPCOPF Verified for $T = 10, PV = 10\%, Batt = 15\%$



MPDOPF Verified for $T = 10, PV = 10\%, Batt = 15\%$

Boundary Complex Powers



MPDOPF Verified for $T = 10, PV = 10\%, Batt = 15\%$

Boundary Voltages

