

# EE 521 Power System Analysis and EE 523 Power System Stability and Control Algorithms

## Preamble and Control Inputs

```
systemName =  
"ieee11-caseThree-"
```

```
powerFlowMethod =  
"NRPF"
```

## Read CDF file and store the data in neat MATLAB tables: busData and branchData.

```
busData = 11x18 table
```

...

	bus	busName	loadFlowArea	lossZone	busType	vFinal
1	1	"Bus 1 HV"	1	1	3	1.0300
2	2	"Bus 2 HV"	1	1	0	1.0100
3	3	"Bus 3 HV"	2	1	0	1.0300
4	4	"Bus 4 HV"	2	1	0	1.0100
5	5	"Bus 5 HV"	1	1	0	1.0200
6	6	"Bus 6 LV"	1	1	0	1.0120
7	7	"Bus 7 ZV"	1	1	0	1.0210
8	8	"Bus 8 TV"	3	1	0	1.0100
9	9	"Bus 9 LV"	2	1	0	1.0020
10	10	"Bus 10 LV"	2	1	0	1.0010
11	11	"Bus 11 LV"	2	1	0	1.0150

```
branchData = 10x15 table
```

...

	i	j	loadFlowArea	lossZone	ckt	type	R
1	1	5	1	1	1	0	0
2	2	6	1	1	1	0	0
3	3	11	2	1	1	0	0
4	4	10	2	1	1	0	0
5	5	6	1	1	1	0	0.0025
6	6	7	1	1	1	0	0.0010
7	7	8	1	1	1	0	0.0037
8	8	9	2	1	1	0	0.0055
9	9	10	2	1	1	0	0.0010
10	10	11	2	1	1	0	0.0025

N = 11  
numBranch = 10

Extract  $Y_{Bus}$ , Adjacency List  $E$  from the branchData table.

ybusTable = 11×11 table

	1	2	3	4	5
1 1	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i
2 2	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
3 3	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i
4 4	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i
5 5	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	3.9604 -99.5701i
6 6	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	-3.9604 +39.6040i
7 7	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
8 8	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
9 9	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
10 10	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i
11 11	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i

Run Newton Raphson Power Flow and obtain a steady state snapshot of the system variables  $P_i, Q_i, V_i, \delta_i \forall$  buses  $i \in [1, N], i \in \mathbb{N}$

Iteration Number 1 Jacobian:  
JTable = 20×20 table

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.3989	0	0	0	-60.3989	0
2 \$P_3\$	0	60.8939	0	0	0	0
3 \$P_4\$	0	0	60.1657	0	0	0
4 \$P_5\$	0	0	0	102.3984	-40.2170	0
5 \$P_6\$	-60.3989	0	0	-39.7473	200.6702	-100.5240
6 \$P_7\$	0	0	0	0	-99.5758	126.9689
7 \$P_8\$	0	0	0	0	0	-27.1258
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.1657	0	0	0
10 \$P_{11}\$	0	-60.8939	0	0	0	0
11 \$Q_2\$	2.4204	0	0	0	-2.4204	0
12 \$Q_3\$	0	2.4494	0	0	0	0
13 \$Q_4\$	0	0	2.4377	0	0	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
14 \$Q_5\$	0	0	0	-4.0424	1.6500	0
15 \$Q_6\$	2.4204	0	0	6.3465	-14.0310	5.2642
16 \$Q_7\$	0	0	0	0	14.7457	-16.1386
17 \$Q_8\$	0	0	0	0	0	4.0635
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	2.4377	0	0	0
20 \$Q_{11}\$	0	2.4494	0	0	0	0

Iteration Number 2 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	38.1877	0	0	0	-38.1877	0
2 \$P_3\$	0	8.9792	0	0	0	0
3 \$P_4\$	0	0	7.6318	0	0	0
4 \$P_5\$	0	0	0	87.5629	-29.8789	0
5 \$P_6\$	-38.1877	0	0	-28.8854	126.8167	-59.7435
6 \$P_7\$	0	0	0	0	-57.9441	69.7455
7 \$P_8\$	0	0	0	0	0	-11.4375
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-7.6318	0	0	0
10 \$P_{11}\$	0	-8.9792	0	0	0	0
11 \$Q_2\$	5.0718	0	0	0	-5.0718	0
12 \$Q_3\$	0	1.5173	0	0	0	0
13 \$Q_4\$	0	0	1.2967	0	0	0
14 \$Q_5\$	0	0	0	-4.3102	-2.0291	0
15 \$Q_6\$	5.0718	0	0	7.9055	-9.8645	-3.1128
16 \$Q_7\$	0	0	0	0	14.8816	-14.2264
17 \$Q_8\$	0	0	0	0	0	2.9810
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	1.2967	0	0	0
20 \$Q_{11}\$	0	1.5173	0	0	0	0

Iteration Number 3 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	78.4372	0	0	0	-78.4372	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	65.0761	0	0	0	0
3 \$P_4\$	0	0	72.6642	0	0	0
4 \$P_5\$	0	0	0	115.0481	-48.9592	0
5 \$P_6\$	-78.4372	0	0	-47.6987	260.6417	-134.5059
6 \$P_7\$	0	0	0	0	-132.4269	170.5106
7 \$P_8\$	0	0	0	0	0	-37.6205
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-72.6642	0	0	0
10 \$P_{11}\$	0	-65.0761	0	0	0	0
11 \$Q_2\$	5.3958	0	0	0	-5.3958	0
12 \$Q_3\$	0	14.6921	0	0	0	0
13 \$Q_4\$	0	0	14.9692	0	0	0
14 \$Q_5\$	0	0	0	-4.9957	-1.4698	0
15 \$Q_6\$	5.3958	0	0	11.1356	-19.4832	2.9518
16 \$Q_7\$	0	0	0	0	23.7414	-25.2155
17 \$Q_8\$	0	0	0	0	0	6.1025
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	14.9692	0	0	0
20 \$Q_{11}\$	0	14.6921	0	0	0	0

Iteration Number 4 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.8149	0	0	0	-60.8149	0
2 \$P_3\$	0	48.3427	0	0	0	0
3 \$P_4\$	0	0	47.3917	0	0	0
4 \$P_5\$	0	0	0	103.6065	-40.9387	0
5 \$P_6\$	-60.8149	0	0	-39.6409	202.4846	-102.0288
6 \$P_7\$	0	0	0	0	-99.5520	126.3970
7 \$P_8\$	0	0	0	0	0	-26.2116
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-47.3917	0	0	0
10 \$P_{11}\$	0	-48.3427	0	0	0	0
11 \$Q_2\$	6.4324	0	0	0	-6.4324	0
12 \$Q_3\$	0	8.3519	0	0	0	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
13 \$Q_4\$	0	0	8.3153	0	0	0
14 \$Q_5\$	0	0	0	-4.3067	-2.4602	0
15 \$Q_6\$	6.4324	0	0	10.5182	-14.6457	-2.3048
16 \$Q_7\$	0	0	0	0	22.4629	-21.9538
17 \$Q_8\$	0	0	0	0	0	5.8192
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	8.3153	0	0	0
20 \$Q_{11}\$	0	8.3519	0	0	0	0

Iteration Number 5 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	57.9353	0	0	0	-57.9353	0
2 \$P_3\$	0	57.1683	0	0	0	0
3 \$P_4\$	0	0	54.7002	0	0	0
4 \$P_5\$	0	0	0	101.6541	-39.6051	0
5 \$P_6\$	-57.9353	0	0	-38.2573	193.5509	-97.3583
6 \$P_7\$	0	0	0	0	-94.6278	120.7135
7 \$P_8\$	0	0	0	0	0	-25.3213
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-54.7002	0	0	0
10 \$P_{11}\$	0	-57.1683	0	0	0	0
11 \$Q_2\$	6.9631	0	0	0	-6.9631	0
12 \$Q_3\$	0	6.7927	0	0	0	0
13 \$Q_4\$	0	0	6.6685	0	0	0
14 \$Q_5\$	0	0	0	-4.0560	-2.8459	0
15 \$Q_6\$	6.9631	0	0	10.6321	-13.5424	-4.0529
16 \$Q_7\$	0	0	0	0	23.2515	-22.0050
17 \$Q_8\$	0	0	0	0	0	6.3914
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	6.6685	0	0	0
20 \$Q_{11}\$	0	6.7927	0	0	0	0

Iteration Number 6 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.9375	0	0	0	-60.9375	0
2 \$P_3\$	0	62.1710	0	0	0	0
3 \$P_4\$	0	0	60.1199	0	0	0
4 \$P_5\$	0	0	0	103.6850	-41.0133	0
5 \$P_6\$	-60.9375	0	0	-39.6503	203.4097	-102.8219
6 \$P_7\$	0	0	0	0	-100.0673	128.0324
7 \$P_8\$	0	0	0	0	0	-27.1910
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.1199	0	0	0
10 \$P_{11}\$	0	-62.1710	0	0	0	0
11 \$Q_2\$	6.9882	0	0	0	-6.9882	0
12 \$Q_3\$	0	7.1865	0	0	0	0
13 \$Q_4\$	0	0	6.9849	0	0	0
14 \$Q_5\$	0	0	0	-4.1280	-2.7816	0
15 \$Q_6\$	6.9882	0	0	10.8480	-14.2075	-3.6287
16 \$Q_7\$	0	0	0	0	23.9176	-22.8102
17 \$Q_8\$	0	0	0	0	0	6.6276
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	6.9849	0	0	0
20 \$Q_{11}\$	0	7.1865	0	0	0	0

Iteration Number 7 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.9049	0	0	0	-60.9049	0
2 \$P_3\$	0	62.3526	0	0	0	0
3 \$P_4\$	0	0	60.2614	0	0	0
4 \$P_5\$	0	0	0	103.6630	-40.9984	0
5 \$P_6\$	-60.9049	0	0	-39.6341	203.3114	-102.7723
6 \$P_7\$	0	0	0	0	-100.0124	127.9735
7 \$P_8\$	0	0	0	0	0	-27.1844
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.2614	0	0	0
10 \$P_{11}\$	0	-62.3526	0	0	0	0
11 \$Q_2\$	7	0	0	0	-7	0

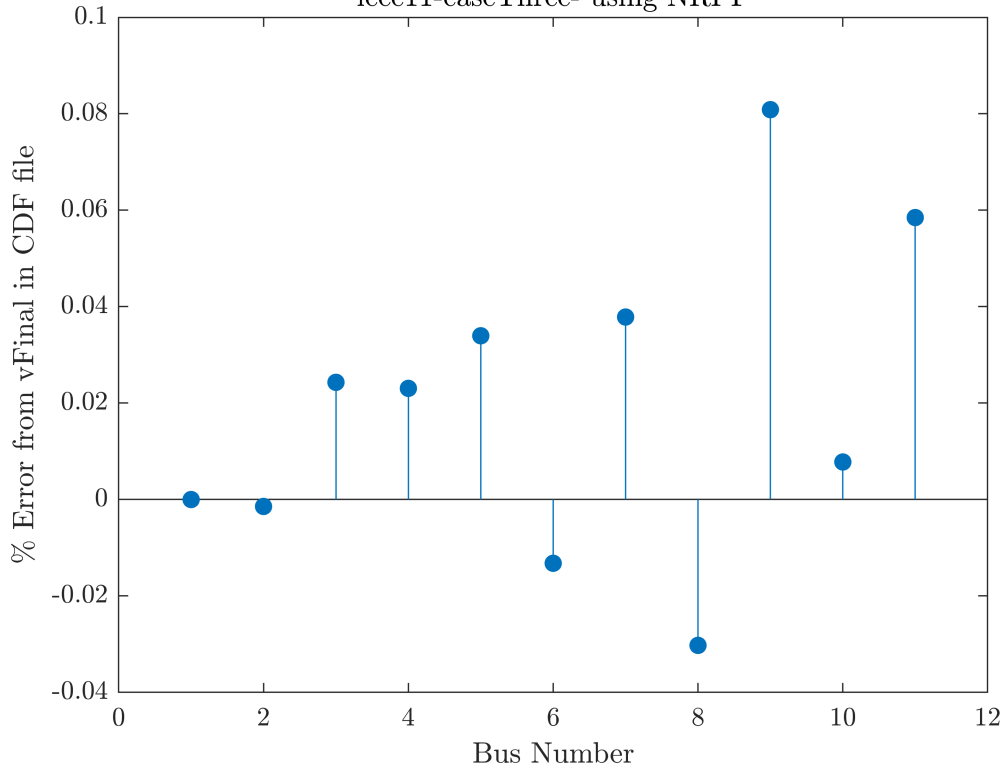
	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
12 \$Q_3\$	0	7.1900	0	0	0	0
13 \$Q_4\$	0	0	7	0	0	0
14 \$Q_5\$	0	0	0	-4.1232	-2.7895	0
15 \$Q_6\$	7	0	0	10.8527	-14.1923	-3.6604
16 \$Q_7\$	0	0	0	0	23.9389	-22.8180
17 \$Q_8\$	0	0	0	0	0	6.6400
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	7	0	0	0
20 \$Q_{11}\$	0	7.1900	0	0	0	0

Convergence using NRPF achieved in 7 iterations.  
resultTable = 11x4 table

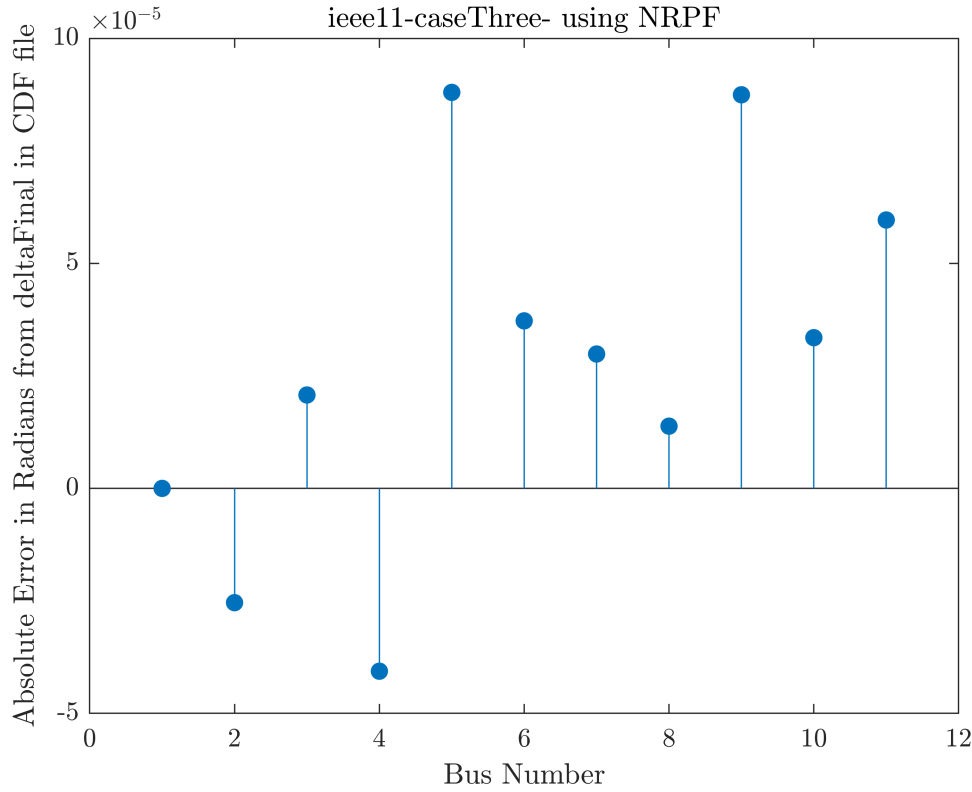
	P	Q	V	delta
1 \$Bus_1\$	6.9127	0.9766	1.0300	0
2 \$Bus_2\$	7	0.2870	1.0100	-0.1630
3 \$Bus_3\$	7.1900	1.3190	1.0303	-0.3319
4 \$Bus_4\$	7	0.9600	1.0102	-0.5076
5 \$Bus_5\$	-0	0	1.0203	-0.1099
6 \$Bus_6\$	-0	0	1.0119	-0.2775
7 \$Bus_7\$	-9.6700	-1	1.0214	-0.4127
8 \$Bus_8\$	0	0	1.0097	-0.5526
9 \$Bus_9\$	-17.6701	-1	1.0028	-0.7644
10 \$Bus_{10}\$	0.0001	0	1.0011	-0.6232
11 \$Bus_{11}\$	0	0	1.0156	-0.4467

Compare obtained snapshot values of  $V_i$  and  $\delta_i$  against the ones given in the CDF file.

Obtained Solution vs Given Solution in CDF file for Voltages of  
ieee11-caseThree- using NRPF



Obtained Solution vs Given Solution in CDF file for Voltage Angles of  
ieee11-caseThree- using NRPF



## Economic Dispatch and Optimal Power Flow Calculations:

Elapsed time is 1.796283 seconds.



## Have a nice day!

In case you encounter a Java Heap Memory error, delete the above gif, or go to Preferences -> General -> Java Heap Memory and increase the allocated size.