

EE 521 Power System Analysis and EE 523 Power System Stability and Control Algorithms

Preamble and Control Inputs

```
tic;
addpath functions\
systemName = "ieee11"
powerFlowMethod = "NRPF"
useSparseDSA = false;
includeOPFScenarios = false;
showOPFFormulae = false;
showOPFValues = false;
numIterations = 50; %I don't wait for the system to converge,
printPowerFlowConvergenceMessages = false;
% neither do I care if the system converges earlier.
toleranceLimit = 1e-3; %mean of absolute values of
% corrections should be less than this for convergence to be achieved.
displayRawData = true;
displayYBus = true;
displayTables = true; %show busData, branchData, ybus,
% basically data structures which are not the final output.
printJacobians = true ; %Print Jacobians during NRPF iterations? Does not work if displayTables
printMismatches = false; %Print Mismatches during NRPF iterations? Does not work if displayTables
printCorrections = false;
disableTaps = false; %Disable Tap-changers when computing YBus?
showPlots = true;
displayResults = true;
reducedBranchColumnsCDFReading = true;
showImages = true; %might add iteration specific images later.
verboseCDFReading = false; %Will give a verbose output when reading CDF files.
MVAb = 100; %Currently the same for all systems in database.
```

```
folder_rawData = "rawData/"; %location of CDF .txt file for the system
file_rawData = strcat(folder_rawData, systemName, "cdf.txt"); %Exact location of CDF .txt file
folder_processedData = "processedData/";
% Should configure it to be read from the CDF file later.
latex_interpreter %for LaTeX typesetting in plots
```

Read CDF file and store the data in neat MATLAB tables: busData and branchData.

```
[busData, branchData, N, numBranch] = ...
    readCDF(file_rawData, reducedBranchColumnsCDFReading, verboseCDFReading);
if displayTables && displayRawData
    displayRawDataAsTables(busData, branchData, N, numBranch);
end
```

Extract Y_{Bus} , Adjacency List E from the branchData table.

```
if useSparseDSA
    [nnzYBus, NYBus] = makeSparseYBus(busData, branchData, displayTables, displayYBus); %#ok
else
    [ybus, BMatrix, ~, ~, ~, E] = ybusGenerator(busData, branchData);
    ybusTable = array2table(ybus, VariableNames=[string(1:N)], RowNames=[string(1:N)]);

end

if ~useSparseDSA && displayTables && displayYBus
    display(ybusTable);
end
```

Run Newton Raphson Power Flow and obtain a steady state snapshot of the system variables $P_i, Q_i, V_i, \delta_i \forall$ buses $i \in [1, N], i \in \mathbb{N}$

```
[PSpecified, QSpecified, V, delta, ...
    listOfPQBuses, listOfPVBuses, nPQ, nPV, ...
    listOfNonSlackBuses] = initializeVectors(busData, N, MVAb);

if useSparseDSA
    doTheSparseThing(PSpecified, QSpecified, V, delta, nnzYBus, NYBus, busData); %#ok
else
    if contains(systemName, 'caseThree')
        resultsFromCaseTwo = load("processedData\ieee11-caseTwoResults");
        resultsFromCaseTwo = resultsFromCaseTwo.resultTable;
        wiggle = 0.35; %minimum 0.35 value for good result
        V = V*(1-wiggle) + wiggle*resultsFromCaseTwo.V;
        delta = delta*(1-wiggle) + wiggle*resultsFromCaseTwo.delta;
    end
    [P, Q, V, delta] = solveForPowerFlow(PSpecified, QSpecified, V, delta, ybus, BMatrix, E, N);

    resultTable = displayPowerFlowResults(N, P, Q, V, delta, displayResults);
    if contains(systemName, 'caseTwo')
        save("processedData\ieee11-caseTwoResults", "resultTable");
    end
end
```

Compare obtained snapshot values of V_i and δ_i against the ones given in the CDF file.

```
plotPowerFlowResults(showPlots, useSparseDSA, V, busData, systemName, powerFlowMethod, delta);
```

Economic Dispatch and Optimal Power Flow Calculations:

```
if includeOPFScenarios && strcmp(systemName, 'ieee14') && ~useSparseDSA
    runOPFScenarios(busData, P, Q, V, delta, N, ybus, BMatrix, E, nPQ, nPV, listOfPQBuses, list
```

```
toc;
```

Have a nice day!

In case you encounter a Java Heap Memory error, delete the above gif, or go to Preferences -> General -> Java Heap Memory and increase the allocated size.

EE 521 Power System Analysis and EE 523 Power System Stability and Control Algorithms

Preamble and Control Inputs

```
systemName =  
"ieee11"  
  
powerFlowMethod =  
"NRPF"
```

Read CDF file and store the data in neat MATLAB tables: **busData** and **branchData**.

```
busData = 11x18 table
```

...

	bus	busName	loadFlowArea	lossZone	busType	vFinal
1	1	"Bus 1 HV"	1	1	3	1.0300
2	2	"Bus 2 HV"	1	1	2	1.0100
3	3	"Bus 3 HV"	2	1	2	1.0300
4	4	"Bus 4 HV"	2	1	2	1.0100
5	5	"Bus 5 HV"	1	1	0	1.0060
6	6	"Bus 6 LV"	1	1	0	0.9780
7	7	"Bus 7 ZV"	1	1	0	0.9610
8	8	"Bus 8 TV"	3	1	0	0.9490
9	9	"Bus 9 LV"	2	1	0	0.9710
10	10	"Bus 10 LV"	2	1	0	0.9840
11	11	"Bus 11 LV"	2	1	0	1.0080

```
branchData = 10x15 table
```

...

	i	j	loadFlowArea	lossZone	ckt	type	R
1	1	5	1	1	1	0	0
2	2	6	1	1	1	0	0
3	3	11	2	1	1	0	0
4	4	10	2	1	1	0	0
5	5	6	1	1	1	0	0.0025
6	6	7	1	1	1	0	0.0010
7	7	8	1	1	1	0	0.0055
8	8	9	2	1	1	0	0.0055
9	9	10	2	1	1	0	0.0010
10	10	11	2	1	1	0	0.0025

N = 11
numBranch = 10

Extract Y_{Bus} , Adjacency List E from the branchData table.

ybusTable = 11×11 table

	1	2	3	4	5
1 1	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i
2 2	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
3 3	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i
4 4	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i
5 5	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	3.9604 -99.5701i
6 6	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	-3.9604 +39.6040i
7 7	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
8 8	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
9 9	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
10 10	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i
11 11	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i

Run Newton Raphson Power Flow and obtain a steady state snapshot of the system variables $P_i, Q_i, V_i, \delta_i \forall$ buses $i \in [1, N], i \in \mathbb{N}$

Iteration Number 1 Jacobian:

JTable = 17×17 table

	δ_2	δ_3	δ_4	δ_5	δ_6	δ_7
1 P_2	60.5879	0	0	0	-60.5879	0
2 P_3	0	61.7876	0	0	0	0
3 P_4	0	0	60.5879	0	0	0
4 P_5	0	0	0	101.3916	-39.6040	0
5 P_6	-60.5879	0	0	-39.6040	199.2017	-99.0099
6 P_7	0	0	0	0	-99.0099	117.0117
7 P_8	0	0	0	0	0	-18.0018
8 P_9	0	0	0	0	0	0
9 P_{10}	0	0	-60.5879	0	0	0
10 P_{11}	0	-61.7876	0	0	0	0
11 Q_5	0	0	0	-3.9604	3.9604	0
12 Q_6	-0	0	0	3.9604	-13.8614	9.9010
13 Q_7	0	0	0	0	9.9010	-11.7012

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
14 \$Q_8\$	0	0	0	0	0	1.8002
15 \$Q_9\$	0	0	0	0	0	0
16 \$Q_{10}\$	0	0	-0	0	0	0
17 \$Q_{11}\$	0	-0	0	0	0	0

Iteration Number 2 Jacobian:

JTable = 17×17 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	62.4416	0	0	0	-62.4416	0
2 \$P_3\$	0	64.1116	0	0	0	0
3 \$P_4\$	0	0	62.9589	0	0	0
4 \$P_5\$	0	0	0	106.8334	-42.8853	0
5 \$P_6\$	-62.4416	0	0	-41.5654	211.8705	-107.8634
6 \$P_7\$	0	0	0	0	-105.0023	125.0538
7 \$P_8\$	0	0	0	0	0	-19.2736
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-62.9589	0	0	0
10 \$P_{11}\$	0	-64.1116	0	0	0	0
11 \$Q_5\$	0	0	0	-4.0096	-2.3765	0
12 \$Q_6\$	7.2464	0	0	10.8216	-14.4060	-3.6620
13 \$Q_7\$	0	0	0	0	24.9486	-23.0256
14 \$Q_8\$	0	0	0	0	0	5.8554
15 \$Q_9\$	0	0	0	0	0	0
16 \$Q_{10}\$	0	0	7.3065	0	0	0
17 \$Q_{11}\$	0	7.4943	0	0	0	0

Iteration Number 3 Jacobian:

JTable = 17×17 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.1939	0	0	0	-59.1939	0
2 \$P_3\$	0	62.0471	0	0	0	0
3 \$P_4\$	0	0	59.5177	0	0	0
4 \$P_5\$	0	0	0	101.3844	-39.4132	0
5 \$P_6\$	-59.1939	0	0	-38.0634	192.0894	-94.8321
6 \$P_7\$	0	0	0	0	-92.1279	108.8595
7 \$P_8\$	0	0	0	0	0	-15.9653

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-59.5177	0	0	0
10 \$P_{11}\$	0	-62.0471	0	0	0	0
11 \$Q_5\$	0	0	0	-4.0635	-2.8751	0
12 \$Q_6\$	6.9933	0	0	10.6227	-13.4428	-4.1732
13 \$Q_7\$	0	0	0	0	22.8692	-20.6724
14 \$Q_8\$	0	0	0	0	0	5.4665
15 \$Q_9\$	0	0	0	0	0	0
16 \$Q_{10}\$	0	0	6.9950	0	0	0
17 \$Q_{11}\$	0	7.1920	0	0	0	0

Iteration Number 4 Jacobian:

JTable = 17×17 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	58.8549	0	0	0	-58.8549	0
2 \$P_3\$	0	61.8842	0	0	0	0
3 \$P_4\$	0	0	59.1799	0	0	0
4 \$P_5\$	0	0	0	100.8691	-39.0748	0
5 \$P_6\$	-58.8549	0	0	-37.7096	190.0235	-93.4590
6 \$P_7\$	0	0	0	0	-90.7375	107.0731
7 \$P_8\$	0	0	0	0	0	-15.5496
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-59.1799	0	0	0
10 \$P_{11}\$	0	-61.8842	0	0	0	0
11 \$Q_5\$	0	0	0	-4.0129	-2.9865	0
12 \$Q_6\$	6.9997	0	0	10.6650	-13.2670	-4.3977
13 \$Q_7\$	0	0	0	0	22.8173	-20.4812
14 \$Q_8\$	0	0	0	0	0	5.5247
15 \$Q_9\$	0	0	0	0	0	0
16 \$Q_{10}\$	0	0	6.9998	0	0	0
17 \$Q_{11}\$	0	7.1900	0	0	0	0

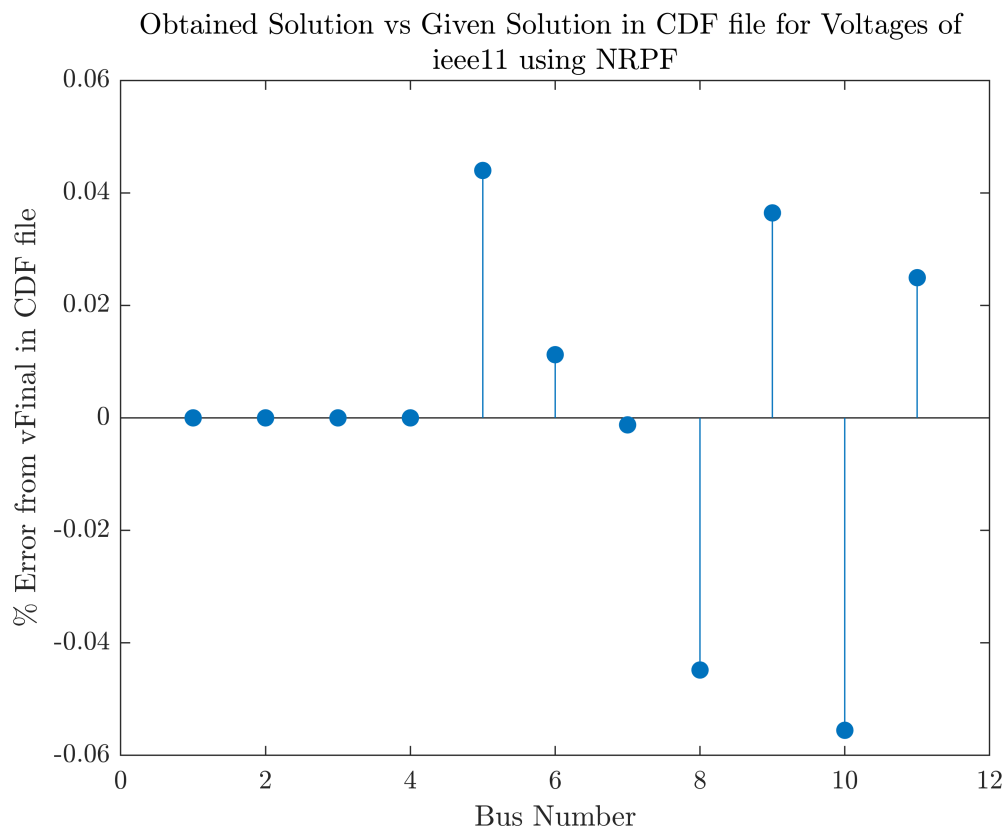
Convergence using NRPF achieved in 4 iterations.

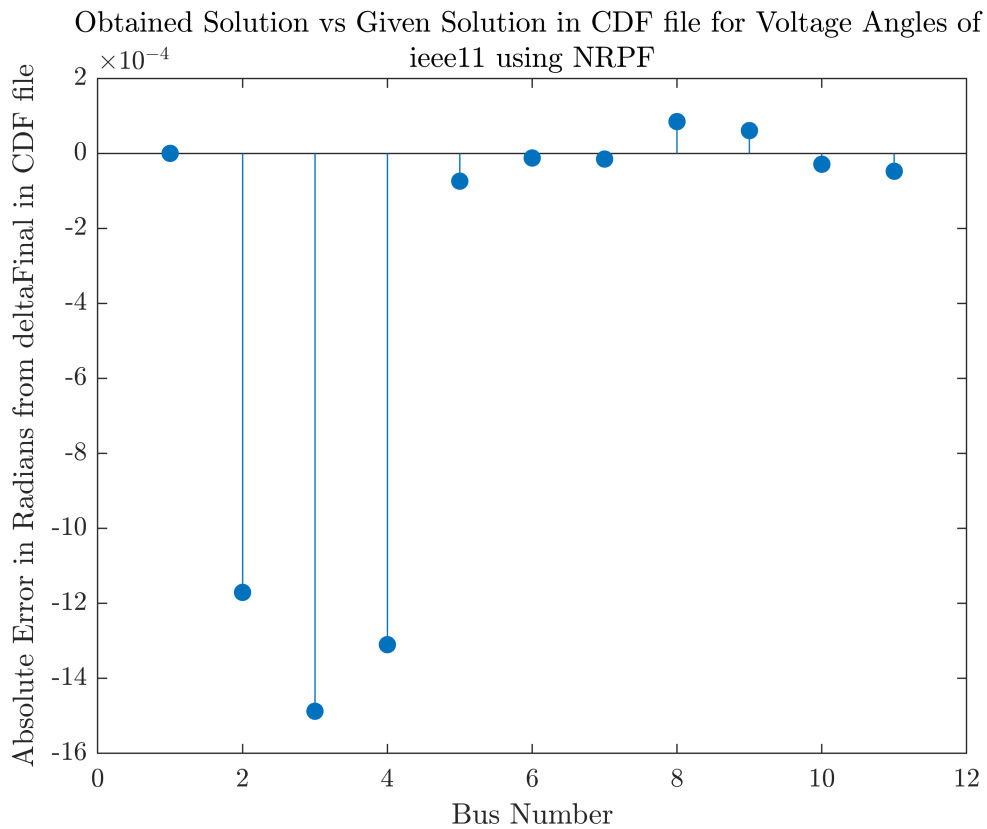
resultTable = 11×4 table

	P	Q	V	delta
1 \$Bus_1\$	6.9995	1.8469	1.0300	0
2 \$Bus_2\$	6.9997	2.3389	1.0100	-0.1705

	P	Q	V	delta
3 \$Bus_3\$	7.1900	1.7571	1.0300	-0.4727
4 \$Bus_4\$	6.9998	2.0139	1.0100	-0.6506
5 \$Bus_5\$	-0.0009	0.0003	1.0064	-0.1128
6 \$Bus_6\$	-0.0023	0.0010	0.9781	-0.2889
7 \$Bus_7\$	-9.6703	-0.9983	0.9610	-0.4356
8 \$Bus_8\$	0.0003	0.0022	0.9486	-0.6778
9 \$Bus_9\$	-17.6648	-0.9988	0.9714	-0.9152
10 \$Bus_10\$	-0.0009	0.0007	0.9835	-0.7683
11 \$Bus_11\$	-0.0001	0.0001	1.0083	-0.5884

Compare obtained snapshot values of V_i and δ_i against the ones given in the CDF file.





Economic Dispatch and Optimal Power Flow Calculations:

Elapsed time is 1.376304 seconds.

Have a nice day!

In case you encounter a Java Heap Memory error, delete the above gif, or go to Preferences->General->Java Heap Memory and increase the allocated size.

EE 521 Power System Analysis and EE 523 Power System Stability and Control Algorithms

Preamble and Control Inputs

```
systemName =  
"ieee11"  
  
powerFlowMethod =  
"Fast Decoupled NRPF"
```

Read CDF file and store the data in neat MATLAB tables: **busData** and **branchData**.

```
busData = 11x18 table
```

...

	bus	busName	loadFlowArea	lossZone	busType	vFinal
1	1	"Bus 1 HV"	1	1	3	1.0300
2	2	"Bus 2 HV"	1	1	2	1.0100
3	3	"Bus 3 HV"	2	1	2	1.0300
4	4	"Bus 4 HV"	2	1	2	1.0100
5	5	"Bus 5 HV"	1	1	0	1.0060
6	6	"Bus 6 LV"	1	1	0	0.9780
7	7	"Bus 7 ZV"	1	1	0	0.9610
8	8	"Bus 8 TV"	3	1	0	0.9490
9	9	"Bus 9 LV"	2	1	0	0.9710
10	10	"Bus 10 LV"	2	1	0	0.9840
11	11	"Bus 11 LV"	2	1	0	1.0080

```
branchData = 10x15 table
```

...

	i	j	loadFlowArea	lossZone	ckt	type	R
1	1	5	1	1	1	0	0
2	2	6	1	1	1	0	0
3	3	11	2	1	1	0	0
4	4	10	2	1	1	0	0
5	5	6	1	1	1	0	0.0025
6	6	7	1	1	1	0	0.0010
7	7	8	1	1	1	0	0.0055
8	8	9	2	1	1	0	0.0055
9	9	10	2	1	1	0	0.0010
10	10	11	2	1	1	0	0.0025

N = 11
numBranch = 10

Extract Y_{Bus} , Adjacency List E from the branchData table.

ybusTable = 11×11 table

	1	2	3	4	5
1 1	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i
2 2	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
3 3	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i
4 4	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i
5 5	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	3.9604 -99.5701i
6 6	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	-3.9604 +39.6040i
7 7	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
8 8	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
9 9	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
10 10	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i
11 11	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i

Run Newton Raphson Power Flow and obtain a steady state snapshot of the system variables $P_i, Q_i, V_i, \delta_i \forall$ buses $i \in [1, N], i \in \mathbb{N}$

Iteration Number 1 Jacobian J11:
J11Table = 10×10 table

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.5879	0	0	0	-60.5879	0
2 \$P_3\$	0	61.7876	0	0	0	0
3 \$P_4\$	0	0	60.5879	0	0	0
4 \$P_5\$	0	0	0	101.8314	-40	0
5 \$P_6\$	-60.5879	0	0	-40	200.6491	-100
6 \$P_7\$	0	0	0	0	-100	122.5843
7 \$P_8\$	0	0	0	0	0	-18.1818
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.5879	0	0	0
10 \$P_{11}\$	0	-61.7876	0	0	0	0

Iteration Number 1 Jacobians:
J22Table = 7×7 table

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	98.0700	2.6691	0	0
2 \$Q_6\$	-2.6691	199.6509	9.6758	0
3 \$Q_7\$	0	-9.6758	119.5336	0.9156
4 \$Q_8\$	0	0	-0.9156	36.4006
5 \$Q_9\$	0	0	0	-1.1135
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 2 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.3141	0	0	0	-60.7189	0
2 \$P_3\$	0	62.3014	0	0	0	0
3 \$P_4\$	0	0	59.9979	0	0	0
4 \$P_5\$	0	0	0	104.0569	-40.8771	0
5 \$P_6\$	-60.7189	0	0	-40.8771	201.4831	-100.1002
6 \$P_7\$	0	0	0	0	-100.1002	121.4679
7 \$P_8\$	0	0	0	0	0	-18.3333
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.4006	0	0	0
10 \$P_{11}\$	0	-62.7256	0	0	0	0

Iteration Number 2 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	104.0890	5.2546	0	0
2 \$Q_6\$	-5.2546	200.7991	12.2541	0
3 \$Q_7\$	0	-12.2541	119.2798	2.8758
4 \$Q_8\$	0	0	-2.8758	37.8586
5 \$Q_9\$	0	0	0	-3.0141
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 3 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.3472	0	0	0	-60.7475	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	62.2490	0	0	0	0
3 \$P_4\$	0	0	60.2359	0	0	0
4 \$P_5\$	0	0	0	103.8189	-40.8578	0
5 \$P_6\$	-60.7475	0	0	-40.8578	200.9119	-100.0309
6 \$P_7\$	0	0	0	0	-100.0309	120.6333
7 \$P_8\$	0	0	0	0	0	-18.1160
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.6283	0	0	0
10 \$P_{11}\$	0	-62.6447	0	0	0	0

Iteration Number 3 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	103.9159	6.2959	0	0
2 \$Q_6\$	-6.2959	201.5133	13.2413	0
3 \$Q_7\$	0	-13.2413	119.2940	3.5434
4 \$Q_8\$	0	0	-3.5434	36.9668
5 \$Q_9\$	0	0	0	-3.5277
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 4 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.2266	0	0	0	-60.6285	0
2 \$P_3\$	0	62.3337	0	0	0	0
3 \$P_4\$	0	0	60.1280	0	0	0
4 \$P_5\$	0	0	0	103.4944	-40.7363	0
5 \$P_6\$	-60.6285	0	0	-40.7363	199.8126	-99.4471
6 \$P_7\$	0	0	0	0	-99.4471	119.5230
7 \$P_8\$	0	0	0	0	0	-17.8883
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.5275	0	0	0
10 \$P_{11}\$	0	-62.7432	0	0	0	0

Iteration Number 4 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	103.7460	6.6942	0	0
2 \$Q_6\$	-6.6942	200.8864	13.6182	0
3 \$Q_7\$	0	-13.6182	118.4077	3.8240
4 \$Q_8\$	0	0	-3.8240	36.2420
5 \$Q_9\$	0	0	0	-3.7792
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 5 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.0596	0	0	0	-60.4631	0
2 \$P_3\$	0	62.2855	0	0	0	0
3 \$P_4\$	0	0	60.0921	0	0	0
4 \$P_5\$	0	0	0	103.1760	-40.5700	0
5 \$P_6\$	-60.4631	0	0	-40.5700	198.6490	-98.7362
6 \$P_7\$	0	0	0	0	-98.7362	118.4582
7 \$P_8\$	0	0	0	0	0	-17.6965
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.4955	0	0	0
10 \$P_{11}\$	0	-62.6960	0	0	0	0

Iteration Number 5 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	103.4619	6.8323	0	0
2 \$Q_6\$	-6.8323	199.7971	13.7453	0
3 \$Q_7\$	0	-13.7453	117.2997	3.9255
4 \$Q_8\$	0	0	-3.9255	35.7639
5 \$Q_9\$	0	0	0	-3.8720
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 6 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.8900	0	0	0	-60.2951	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	62.2742	0	0	0	0
3 \$P_4\$	0	0	59.9676	0	0	0
4 \$P_5\$	0	0	0	102.8990	-40.4034	0
5 \$P_6\$	-60.2951	0	0	-40.4034	197.5940	-98.0666
6 \$P_7\$	0	0	0	0	-98.0666	117.5266
7 \$P_8\$	0	0	0	0	0	-17.5231
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.3720	0	0	0
10 \$P_{11}\$	0	-62.6867	0	0	0	0

Iteration Number 6 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	103.1740	6.8791	0	0
2 \$Q_6\$	-6.8791	198.6139	13.7861	0
3 \$Q_7\$	0	-13.7861	116.3147	3.9608
4 \$Q_8\$	0	0	-3.9608	35.2898
5 \$Q_9\$	0	0	0	-3.9109
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 7 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.7425	0	0	0	-60.1491	0
2 \$P_3\$	0	62.2192	0	0	0	0
3 \$P_4\$	0	0	59.8926	0	0	0
4 \$P_5\$	0	0	0	102.6631	-40.2560	0
5 \$P_6\$	-60.1491	0	0	-40.2560	196.6758	-97.4659
6 \$P_7\$	0	0	0	0	-97.4659	116.7314
7 \$P_8\$	0	0	0	0	0	-17.3876
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.2988	0	0	0
10 \$P_{11}\$	0	-62.6320	0	0	0	0

Iteration Number 7 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	102.8985	6.8979	0	0
2 \$Q_6\$	-6.8979	197.6053	13.7969	0
3 \$Q_7\$	0	-13.7969	115.3650	3.9776
4 \$Q_8\$	0	0	-3.9776	34.9996
5 \$Q_9\$	0	0	0	-3.9276
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 8 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.6076	0	0	0	-60.0154	0
2 \$P_3\$	0	62.1891	0	0	0	0
3 \$P_4\$	0	0	59.7921	0	0	0
4 \$P_5\$	0	0	0	102.4619	-40.1253	0
5 \$P_6\$	-60.0154	0	0	-40.1253	195.8881	-96.9574
6 \$P_7\$	0	0	0	0	-96.9574	116.0614
7 \$P_8\$	0	0	0	0	0	-17.2681
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.1988	0	0	0
10 \$P_{11}\$	0	-62.6027	0	0	0	0

Iteration Number 8 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	102.6754	6.9052	0	0
2 \$Q_6\$	-6.9052	196.6376	13.8012	0
3 \$Q_7\$	0	-13.8012	114.6379	3.9845
4 \$Q_8\$	0	0	-3.9845	34.6974
5 \$Q_9\$	0	0	0	-3.9375
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 9 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.4997	0	0	0	-59.9085	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	62.1453	0	0	0	0
3 \$P_4\$	0	0	59.7226	0	0	0
4 \$P_5\$	0	0	0	102.2901	-40.0162	0
5 \$P_6\$	-59.9085	0	0	-40.0162	195.2256	-96.5210
6 \$P_7\$	0	0	0	0	-96.5210	115.4918
7 \$P_8\$	0	0	0	0	0	-17.1705
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.1303	0	0	0
10 \$P_{11}\$	0	-62.5590	0	0	0	0

Iteration Number 9 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	102.4608	6.9105	0	0
2 \$Q_6\$	-6.9105	195.9012	13.8004	0
3 \$Q_7\$	0	-13.8004	113.9477	3.9901
4 \$Q_8\$	0	0	-3.9901	34.4887
5 \$Q_9\$	0	0	0	-3.9437
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 10 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.4016	0	0	0	-59.8112	0
2 \$P_3\$	0	62.1164	0	0	0	0
3 \$P_4\$	0	0	59.6469	0	0	0
4 \$P_5\$	0	0	0	102.1462	-39.9216	0
5 \$P_6\$	-59.8112	0	0	-39.9216	194.6586	-96.1542
6 \$P_7\$	0	0	0	0	-96.1542	115.0121
7 \$P_8\$	0	0	0	0	0	-17.0853
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.0550	0	0	0
10 \$P_{11}\$	0	-62.5306	0	0	0	0

Iteration Number 10 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	102.3009	6.9131	0	0
2 \$Q_6\$	-6.9131	195.1972	13.8011	0
3 \$Q_7\$	0	-13.8011	113.4258	3.9933
4 \$Q_8\$	0	0	-3.9933	34.2776
5 \$Q_9\$	0	0	0	-3.9488
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 11 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.3238	0	0	0	-59.7343	0
2 \$P_3\$	0	62.0836	0	0	0	0
3 \$P_4\$	0	0	59.5897	0	0	0
4 \$P_5\$	0	0	0	102.0226	-39.8431	0
5 \$P_6\$	-59.7343	0	0	-39.8431	194.1833	-95.8411
6 \$P_7\$	0	0	0	0	-95.8411	114.6027
7 \$P_8\$	0	0	0	0	0	-17.0138
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-59.9985	0	0	0
10 \$P_{11}\$	0	-62.4980	0	0	0	0

Iteration Number 11 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	102.1454	6.9162	0	0
2 \$Q_6\$	-6.9162	194.6686	13.7997	0
3 \$Q_7\$	0	-13.7997	112.9327	3.9966
4 \$Q_8\$	0	0	-3.9966	34.1205
5 \$Q_9\$	0	0	0	-3.9527
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 12 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.2532	0	0	0	-59.6643	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	62.0596	0	0	0	0
3 \$P_4\$	0	0	59.5330	0	0	0
4 \$P_5\$	0	0	0	101.9194	-39.7752	0
5 \$P_6\$	-59.6643	0	0	-39.7752	193.7751	-95.5766
6 \$P_7\$	0	0	0	0	-95.5766	114.2564
7 \$P_8\$	0	0	0	0	0	-16.9519
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-59.9422	0	0	0
10 \$P_{11}\$	0	-62.4742	0	0	0	0

Iteration Number 12 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	102.0306	6.9180	0	0
2 \$Q_6\$	-6.9180	194.1650	13.8000	0
3 \$Q_7\$	0	-13.8000	112.5544	3.9988
4 \$Q_8\$	0	0	-3.9988	33.9683
5 \$Q_9\$	0	0	0	-3.9562
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 13 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.1968	0	0	0	-59.6084	0
2 \$P_3\$	0	62.0351	0	0	0	0
3 \$P_4\$	0	0	59.4878	0	0	0
4 \$P_5\$	0	0	0	101.8303	-39.7184	0
5 \$P_6\$	-59.6084	0	0	-39.7184	193.4316	-95.3506
6 \$P_7\$	0	0	0	0	-95.3506	113.9599
7 \$P_8\$	0	0	0	0	0	-16.8994
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-59.8975	0	0	0
10 \$P_{11}\$	0	-62.4499	0	0	0	0

Iteration Number 13 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	101.9193	6.9201	0	0
2 \$Q_6\$	-6.9201	193.7815	13.7990	0
3 \$Q_7\$	0	-13.7990	112.2009	4.0011
4 \$Q_8\$	0	0	-4.0011	33.8496
5 \$Q_9\$	0	0	0	-3.9591
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 14 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.1458	0	0	0	-59.5579	0
2 \$P_3\$	0	62.0160	0	0	0	0
3 \$P_4\$	0	0	59.4451	0	0	0
4 \$P_5\$	0	0	0	101.7556	-39.6694	0
5 \$P_6\$	-59.5579	0	0	-39.6694	193.1358	-95.1586
6 \$P_7\$	0	0	0	0	-95.1586	113.7080
7 \$P_8\$	0	0	0	0	0	-16.8540
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-59.8552	0	0	0
10 \$P_{11}\$	0	-62.4310	0	0	0	0

Iteration Number 14 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	101.8359	6.9215	0	0
2 \$Q_6\$	-6.9215	193.4205	13.7991	0
3 \$Q_7\$	0	-13.7991	111.9240	4.0027
4 \$Q_8\$	0	0	-4.0027	33.7385
5 \$Q_9\$	0	0	0	-3.9616
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 15 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.1045	0	0	0	-59.5170	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	61.9976	0	0	0	0
3 \$P_4\$	0	0	59.4101	0	0	0
4 \$P_5\$	0	0	0	101.6910	-39.6281	0
5 \$P_6\$	-59.5170	0	0	-39.6281	192.8858	-94.9943
6 \$P_7\$	0	0	0	0	-94.9943	113.4918
7 \$P_8\$	0	0	0	0	0	-16.8153
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-59.8205	0	0	0
10 \$P_{11}\$	0	-62.4128	0	0	0	0

Iteration Number 15 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	101.7561	6.9231	0	0
2 \$Q_6\$	-6.9231	193.1396	13.7985	0
3 \$Q_7\$	0	-13.7985	111.6690	4.0043
4 \$Q_8\$	0	0	-4.0043	33.6491
5 \$Q_9\$	0	0	0	-3.9637
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

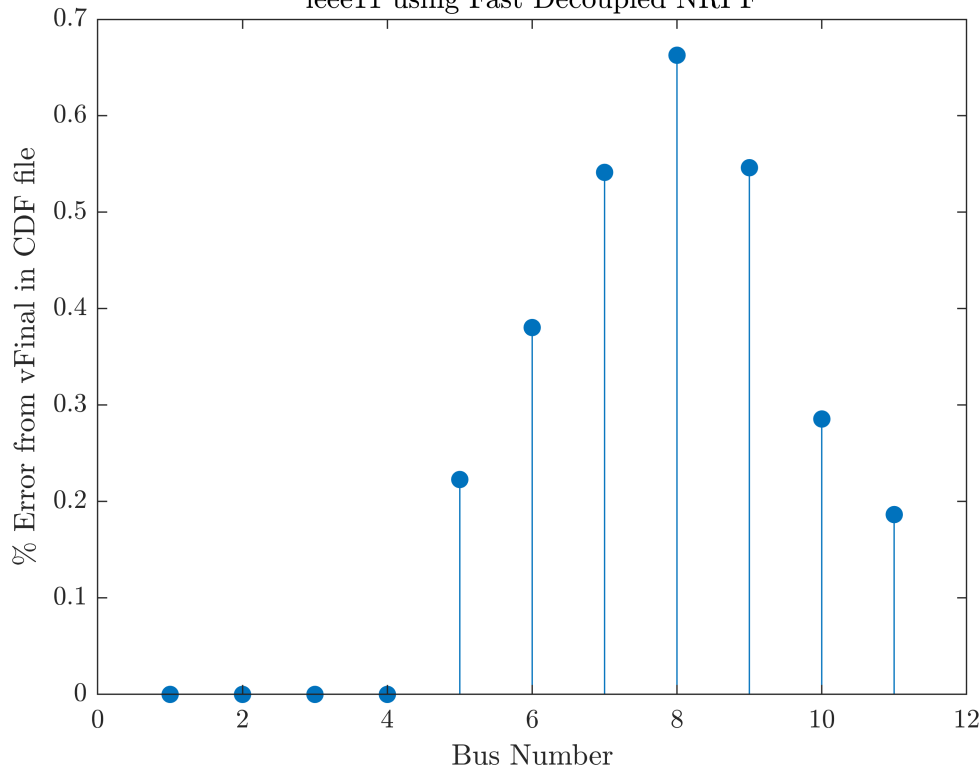
Convergence using Fast Decoupled NRPF achieved in 15 iterations.

resultTable = 11×4 table

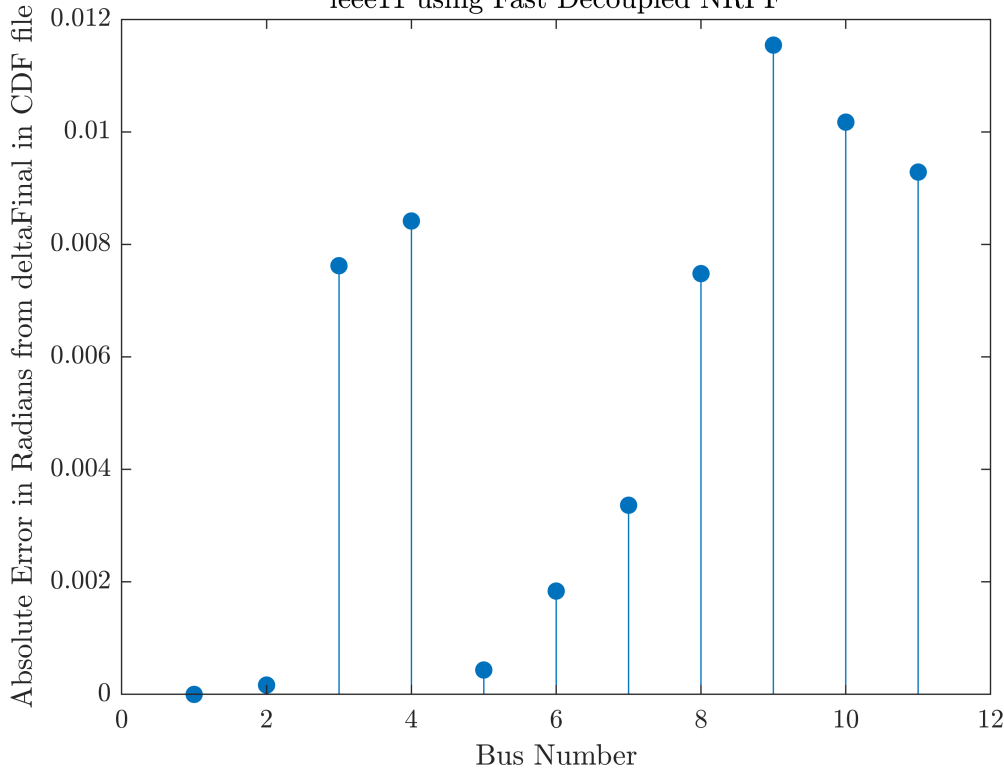
	P	Q	V	delta
1 \$Bus_1\$	6.9841	1.7193	1.0300	0
2 \$Bus_2\$	6.9999	2.0898	1.0100	-0.1691
3 \$Bus_3\$	7.1894	1.6439	1.0300	-0.4636
4 \$Bus_4\$	6.9993	1.7842	1.0100	-0.6408
5 \$Bus_5\$	-0.0001	0.0332	1.0082	-0.1123
6 \$Bus_6\$	-0.0001	0.1289	0.9817	-0.2870
7 \$Bus_7\$	-9.6684	-0.9079	0.9662	-0.4323
8 \$Bus_8\$	0.0002	0.0375	0.9553	-0.6704
9 \$Bus_9\$	-17.6618	-0.9235	0.9763	-0.9037
10 \$Bus_{10}\$	-0.0020	0.1126	0.9868	-0.7581
11 \$Bus_{11}\$	-0.0005	0.0279	1.0099	-0.5791

Compare obtained snapshot values of V_i and δ_i against the ones given in the CDF file.

Obtained Solution vs Given Solution in CDF file for Voltages of
ieee11 using Fast Decoupled NRPF



Obtained Solution vs Given Solution in CDF file for Voltage Angles of
ieee11 using Fast Decoupled NRPF



Economic Dispatch and Optimal Power Flow Calculations:

Elapsed time is 3.608046 seconds.

Have a nice day!

In case you encounter a Java Heap Memory error, delete the above gif, or go to Preferences -> General -> Java Heap Memory and increase the allocated size.

EE 521 Power System Analysis and EE 523 Power System Stability and Control Algorithms

Preamble and Control Inputs

```
systemName =  
"ieee11-caseTwo-"  
  
powerFlowMethod =  
"NRPF"
```

Read CDF file and store the data in neat MATLAB tables: busData and branchData.

```
busData = 11x18 table
```

...

	bus	busName	loadFlowArea	lossZone	busType	vFinal
1	1	"Bus 1 HV"	1	1	3	1.0300
2	2	"Bus 2 HV"	1	1	2	1.0100
3	3	"Bus 3 HV"	2	1	2	1.0300
4	4	"Bus 4 HV"	2	1	2	1.0100
5	5	"Bus 5 HV"	1	1	0	1.0200
6	6	"Bus 6 LV"	1	1	0	1.0120
7	7	"Bus 7 ZV"	1	1	0	1.0210
8	8	"Bus 8 TV"	3	1	0	1.0100
9	9	"Bus 9 LV"	2	1	0	1.0020
10	10	"Bus 10 LV"	2	1	0	1.0010
11	11	"Bus 11 LV"	2	1	0	1.0150

```
branchData = 10x15 table
```

...

	i	j	loadFlowArea	lossZone	ckt	type	R
1	1	5	1	1	1	0	0
2	2	6	1	1	1	0	0
3	3	11	2	1	1	0	0
4	4	10	2	1	1	0	0
5	5	6	1	1	1	0	0.0025
6	6	7	1	1	1	0	0.0010
7	7	8	1	1	1	0	0.0037
8	8	9	2	1	1	0	0.0055
9	9	10	2	1	1	0	0.0010
10	10	11	2	1	1	0	0.0025

N = 11
numBranch = 10

Extract Y_{Bus} , Adjacency List E from the branchData table.

ybusTable = 11×11 table

	1	2	3	4	5
1 1	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i
2 2	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
3 3	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i
4 4	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i
5 5	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	3.9604 -99.5701i
6 6	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	-3.9604 +39.6040i
7 7	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
8 8	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
9 9	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
10 10	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i
11 11	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i

Run Newton Raphson Power Flow and obtain a steady state snapshot of the system variables $P_i, Q_i, V_i, \delta_i \forall$ buses $i \in [1, N], i \in \mathbb{N}$

Iteration Number 1 Jacobian:

JTable = 17×17 table

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.5879	0	0	0	-60.5879	0
2 \$P_3\$	0	61.7876	0	0	0	0
3 \$P_4\$	0	0	60.5879	0	0	0
4 \$P_5\$	0	0	0	101.3916	-39.6040	0
5 \$P_6\$	-60.5879	0	0	-39.6040	199.2017	-99.0099
6 \$P_7\$	0	0	0	0	-99.0099	126.0097
7 \$P_8\$	0	0	0	0	0	-26.9998
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.5879	0	0	0
10 \$P_{11}\$	0	-61.7876	0	0	0	0
11 \$Q_5\$	0	0	0	-3.9604	3.9604	0
12 \$Q_6\$	-0	0	0	3.9604	-13.8614	9.9010
13 \$Q_7\$	0	0	0	0	9.9010	-12.6032

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
14 \$Q_8\$	0	0	0	0	0	2.7022
15 \$Q_9\$	0	0	0	0	0	0
16 \$Q_{10}\$	0	0	-0	0	0	0
17 \$Q_{11}\$	0	-0	0	0	0	0

Iteration Number 2 Jacobian:

JTable = 17×17 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	64.3143	0	0	0	-64.3143	0
2 \$P_3\$	0	64.4459	0	0	0	0
3 \$P_4\$	0	0	63.7632	0	0	0
4 \$P_5\$	0	0	0	109.4332	-44.7054	0
5 \$P_6\$	-64.3143	0	0	-43.3132	224.7675	-117.1400
6 \$P_7\$	0	0	0	0	-113.9729	147.1125
7 \$P_8\$	0	0	0	0	0	-32.2870
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-63.7632	0	0	0
10 \$P_{11}\$	0	-64.4459	0	0	0	0
11 \$Q_5\$	0	0	0	-3.9040	-2.5600	0
12 \$Q_6\$	7.4638	0	0	11.3619	-14.5457	-4.2799
13 \$Q_7\$	0	0	0	0	27.3912	-26.4053
14 \$Q_8\$	0	0	0	0	0	7.5339
15 \$Q_9\$	0	0	0	0	0	0
16 \$Q_{10}\$	0	0	7.3998	0	0	0
17 \$Q_{11}\$	0	7.5334	0	0	0	0

Iteration Number 3 Jacobian:

JTable = 17×17 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	61.1546	0	0	0	-61.1546	0
2 \$P_3\$	0	62.4514	0	0	0	0
3 \$P_4\$	0	0	60.4908	0	0	0
4 \$P_5\$	0	0	0	104.0460	-41.2510	0
5 \$P_6\$	-61.1546	0	0	-39.8939	204.8646	-103.8161
6 \$P_7\$	0	0	0	0	-101.0427	129.3982
7 \$P_8\$	0	0	0	0	0	-27.5832

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.4908	0	0	0
10 \$P_{11}\$	0	-62.4514	0	0	0	0
11 \$Q_5\$	0	0	0	-4.1447	-2.7286	0
12 \$Q_6\$	7.0047	0	0	10.8431	-14.2238	-3.6240
13 \$Q_7\$	0	0	0	0	24.1099	-23.0510
14 \$Q_8\$	0	0	0	0	0	6.6574
15 \$Q_9\$	0	0	0	0	0	0
16 \$Q_{10}\$	0	0	7.0010	0	0	0
17 \$Q_{11}\$	0	7.1934	0	0	0	0

Iteration Number 4 Jacobian:

JTable = 17×17 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.9063	0	0	0	-60.9063	0
2 \$P_3\$	0	62.3224	0	0	0	0
3 \$P_4\$	0	0	60.2338	0	0	0
4 \$P_5\$	0	0	0	103.6639	-40.9989	0
5 \$P_6\$	-60.9063	0	0	-39.6348	203.3142	-102.7731
6 \$P_7\$	0	0	0	0	-100.0132	127.9725
7 \$P_8\$	0	0	0	0	0	-27.1827
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.2338	0	0	0
10 \$P_{11}\$	0	-62.3224	0	0	0	0
11 \$Q_5\$	0	0	0	-4.1236	-2.7890	0
12 \$Q_6\$	6.9999	0	0	10.8523	-14.1924	-3.6598
13 \$Q_7\$	0	0	0	0	23.9384	-22.8184
14 \$Q_8\$	0	0	0	0	0	6.6388
15 \$Q_9\$	0	0	0	0	0	0
16 \$Q_{10}\$	0	0	6.9999	0	0	0
17 \$Q_{11}\$	0	7.1900	0	0	0	0

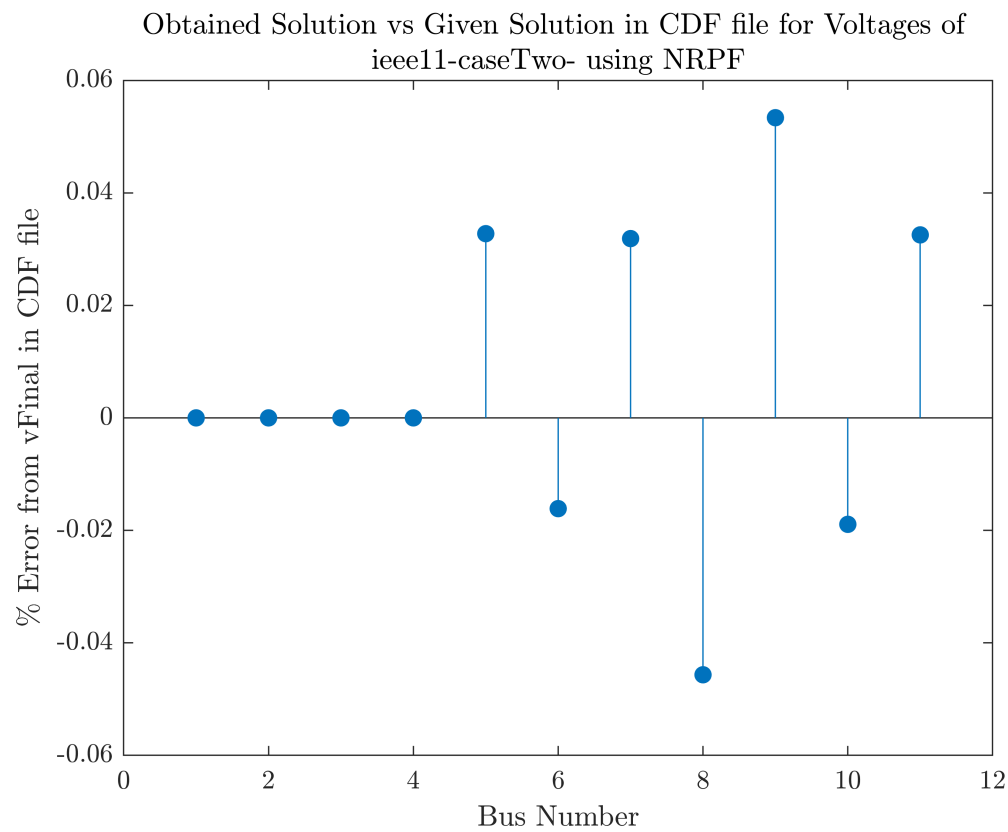
Convergence using NRPF achieved in 4 iterations.

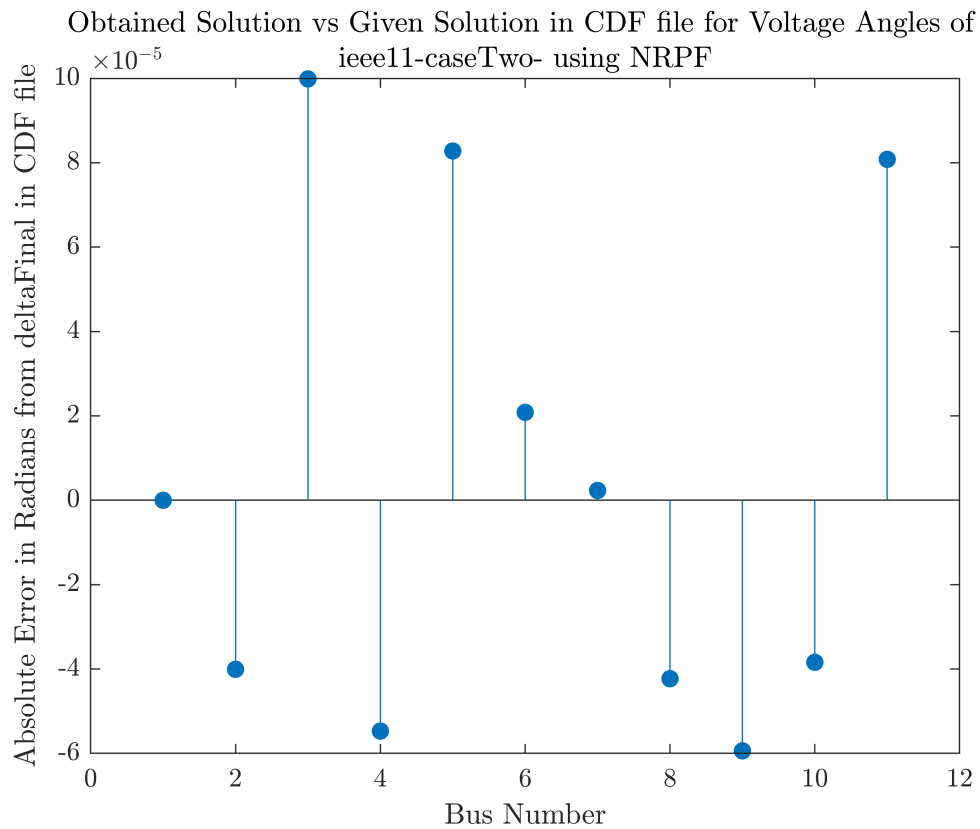
resultTable = 11×4 table

	P	Q	V	delta
1 \$Bus_1\$	6.9125	0.9763	1.0300	0
2 \$Bus_2\$	6.9999	0.2874	1.0100	-0.1631

	P	Q	V	delta
3 \$Bus_3\$	7.1900	1.3188	1.0300	-0.3319
4 \$Bus_4\$	6.9999	0.9600	1.0100	-0.5076
5 \$Bus_5\$	-0.0003	0.0001	1.0203	-0.1099
6 \$Bus_6\$	0.0001	0.0004	1.0118	-0.2775
7 \$Bus_7\$	-9.6704	-0.9992	1.0213	-0.4128
8 \$Bus_8\$	-0.0002	0.0006	1.0095	-0.5526
9 \$Bus_9\$	-17.6690	-0.9991	1.0025	-0.7645
10 \$Bus_10\$	0.0003	0.0005	1.0008	-0.6233
11 \$Bus_11\$	0	0.0001	1.0153	-0.4467

Compare obtained snapshot values of V_i and δ_i against the ones given in the CDF file.





Economic Dispatch and Optimal Power Flow Calculations:

Elapsed time is 1.369501 seconds.

Have a nice day!

In case you encounter a Java Heap Memory error, delete the above gif, or go to Preferences->General->Java Heap Memory and increase the allocated size.

EE 521 Power System Analysis and EE 523 Power System Stability and Control Algorithms

Preamble and Control Inputs

```
systemName =  
"ieee11-caseTwo-"  
  
powerFlowMethod =  
"Fast Decoupled NRPF"
```

Read CDF file and store the data in neat MATLAB tables: busData and branchData.

```
busData = 11x18 table
```

...

	bus	busName	loadFlowArea	lossZone	busType	vFinal
1	1	"Bus 1 HV"	1	1	3	1.0300
2	2	"Bus 2 HV"	1	1	2	1.0100
3	3	"Bus 3 HV"	2	1	2	1.0300
4	4	"Bus 4 HV"	2	1	2	1.0100
5	5	"Bus 5 HV"	1	1	0	1.0200
6	6	"Bus 6 LV"	1	1	0	1.0120
7	7	"Bus 7 ZV"	1	1	0	1.0210
8	8	"Bus 8 TV"	3	1	0	1.0100
9	9	"Bus 9 LV"	2	1	0	1.0020
10	10	"Bus 10 LV"	2	1	0	1.0010
11	11	"Bus 11 LV"	2	1	0	1.0150

```
branchData = 10x15 table
```

...

	i	j	loadFlowArea	lossZone	ckt	type	R
1	1	5	1	1	1	0	0
2	2	6	1	1	1	0	0
3	3	11	2	1	1	0	0
4	4	10	2	1	1	0	0
5	5	6	1	1	1	0	0.0025
6	6	7	1	1	1	0	0.0010
7	7	8	1	1	1	0	0.0037
8	8	9	2	1	1	0	0.0055
9	9	10	2	1	1	0	0.0010
10	10	11	2	1	1	0	0.0025

N = 11
numBranch = 10

Extract Y_{Bus} , Adjacency List E from the branchData table.

ybusTable = 11×11 table

...

	1	2	3	4	5
1 1	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i
2 2	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
3 3	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i
4 4	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i
5 5	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	3.9604 -99.5701i
6 6	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	-3.9604 +39.6040i
7 7	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
8 8	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
9 9	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
10 10	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i
11 11	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i

Run Newton Raphson Power Flow and obtain a steady state snapshot of the system variables $P_i, Q_i, V_i, \delta_i \forall$ buses $i \in [1, N], i \in \mathbb{N}$

Iteration Number 1 Jacobian J11:
J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.5879	0	0	0	-60.5879	0
2 \$P_3\$	0	61.7876	0	0	0	0
3 \$P_4\$	0	0	60.5879	0	0	0
4 \$P_5\$	0	0	0	101.8314	-40	0
5 \$P_6\$	-60.5879	0	0	-40	200.6491	-100
6 \$P_7\$	0	0	0	0	-100	135.8652
7 \$P_8\$	0	0	0	0	0	-27.2702
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.5879	0	0	0
10 \$P_{11}\$	0	-61.7876	0	0	0	0

Iteration Number 1 Jacobians:
J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	98.0708	2.0941	0	0
2 \$Q_6\$	-2.0941	199.5635	9.0994	0
3 \$Q_7\$	0	-9.0994	128.5016	0.9525
4 \$Q_8\$	0	0	-0.9525	45.4849
5 \$Q_9\$	0	0	0	-1.1567
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 2 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.2894	0	0	0	-60.6941	0
2 \$P_3\$	0	62.3028	0	0	0	0
3 \$P_4\$	0	0	59.9808	0	0	0
4 \$P_5\$	0	0	0	104.0408	-40.8609	0
5 \$P_6\$	-60.6941	0	0	-40.8609	203.2130	-101.7909
6 \$P_7\$	0	0	0	0	-101.7909	137.4177
7 \$P_8\$	0	0	0	0	0	-27.9890
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.3834	0	0	0
10 \$P_{11}\$	0	-62.7270	0	0	0	0

Iteration Number 2 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	104.0396	4.5396	0	0
2 \$Q_6\$	-4.5396	198.6628	11.7357	0
3 \$Q_7\$	0	-11.7357	134.7113	2.6985
4 \$Q_8\$	0	0	-2.6985	46.6301
5 \$Q_9\$	0	0	0	-2.8769
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 3 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.9105	0	0	0	-61.3150	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	62.2260	0	0	0	0
3 \$P_4\$	0	0	60.3452	0	0	0
4 \$P_5\$	0	0	0	104.2781	-41.2433	0
5 \$P_6\$	-61.3150	0	0	-41.2433	205.0155	-103.0160
6 \$P_7\$	0	0	0	0	-103.0160	138.4018
7 \$P_8\$	0	0	0	0	0	-28.1841
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.7415	0	0	0
10 \$P_{11}\$	0	-62.6246	0	0	0	0

Iteration Number 3 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	103.4945	5.8580	0	0
2 \$Q_6\$	-5.8580	204.9811	12.8914	0
3 \$Q_7\$	0	-12.8914	134.4874	3.4004
4 \$Q_8\$	0	0	-3.4004	47.5039
5 \$Q_9\$	0	0	0	-3.4165
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 4 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.8587	0	0	0	-61.2568	0
2 \$P_3\$	0	62.3773	0	0	0	0
3 \$P_4\$	0	0	60.2610	0	0	0
4 \$P_5\$	0	0	0	104.4303	-41.3345	0
5 \$P_6\$	-61.2568	0	0	-41.3345	205.2871	-103.5625
6 \$P_7\$	0	0	0	0	-103.5625	138.9251
7 \$P_8\$	0	0	0	0	0	-28.2756
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.6601	0	0	0
10 \$P_{11}\$	0	-62.7876	0	0	0	0

Iteration Number 4 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	104.6030	6.4381	0	0
2 \$Q_6\$	-6.4381	203.7895	13.5491	0
3 \$Q_7\$	0	-13.5491	137.3028	3.6932
4 \$Q_8\$	0	0	-3.6932	46.9533
5 \$Q_9\$	0	0	0	-3.6930
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 5 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	61.0604	0	0	0	-61.4620	0
2 \$P_3\$	0	62.3300	0	0	0	0
3 \$P_4\$	0	0	60.3712	0	0	0
4 \$P_5\$	0	0	0	104.3333	-41.4135	0
5 \$P_6\$	-61.4620	0	0	-41.4135	205.5974	-103.7414
6 \$P_7\$	0	0	0	0	-103.7414	138.9472
7 \$P_8\$	0	0	0	0	0	-28.2975
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.7748	0	0	0
10 \$P_{11}\$	0	-62.7403	0	0	0	0

Iteration Number 5 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	104.0624	6.7265	0	0
2 \$Q_6\$	-6.7265	206.1404	13.7638	0
3 \$Q_7\$	0	-13.7638	136.2970	3.8402
4 \$Q_8\$	0	0	-3.8402	47.4083
5 \$Q_9\$	0	0	0	-3.8043
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 6 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.9649	0	0	0	-61.3637	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	62.3848	0	0	0	0
3 \$P_4\$	0	0	60.3029	0	0	0
4 \$P_5\$	0	0	0	104.3467	-41.3964	0
5 \$P_6\$	-61.3637	0	0	-41.3964	205.4568	-103.7942
6 \$P_7\$	0	0	0	0	-103.7942	138.9863
7 \$P_8\$	0	0	0	0	0	-28.2902
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.7058	0	0	0
10 \$P_{11}\$	0	-62.7975	0	0	0	0

Iteration Number 6 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	104.5170	6.8281	0	0
2 \$Q_6\$	-6.8281	204.9243	13.9149	0
3 \$Q_7\$	0	-13.9149	137.4081	3.8840
4 \$Q_8\$	0	0	-3.8840	47.0193
5 \$Q_9\$	0	0	0	-3.8585
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 7 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	61.0420	0	0	0	-61.4429	0
2 \$P_3\$	0	62.3496	0	0	0	0
3 \$P_4\$	0	0	60.3425	0	0	0
4 \$P_5\$	0	0	0	104.2787	-41.4090	0
5 \$P_6\$	-61.4429	0	0	-41.4090	205.4900	-103.7662
6 \$P_7\$	0	0	0	0	-103.7662	138.8764
7 \$P_8\$	0	0	0	0	0	-28.2745
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.7472	0	0	0
10 \$P_{11}\$	0	-62.7618	0	0	0	0

Iteration Number 7 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	104.1661	6.8876	0	0
2 \$Q_6\$	-6.8876	205.9323	13.9354	0
3 \$Q_7\$	0	-13.9354	136.6290	3.9159
4 \$Q_8\$	0	0	-3.9159	47.2326
5 \$Q_9\$	0	0	0	-3.8774
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 8 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.9730	0	0	0	-61.3725	0
2 \$P_3\$	0	62.3707	0	0	0	0
3 \$P_4\$	0	0	60.2986	0	0	0
4 \$P_5\$	0	0	0	104.2812	-41.3851	0
5 \$P_6\$	-61.3725	0	0	-41.3851	205.3435	-103.7307
6 \$P_7\$	0	0	0	0	-103.7307	138.8339
7 \$P_8\$	0	0	0	0	0	-28.2565
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.7027	0	0	0
10 \$P_{11}\$	0	-62.7838	0	0	0	0

Iteration Number 8 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	104.3937	6.9009	0	0
2 \$Q_6\$	-6.9009	205.1290	13.9759	0
3 \$Q_7\$	0	-13.9759	137.1187	3.9198
4 \$Q_8\$	0	0	-3.9198	47.0070
5 \$Q_9\$	0	0	0	-3.8890
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

Iteration Number 9 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	61.0059	0	0	0	-61.4066	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	62.3488	0	0	0	0
3 \$P_4\$	0	0	60.3130	0	0	0
4 \$P_5\$	0	0	0	104.2394	-41.3837	0
5 \$P_6\$	-61.4066	0	0	-41.3837	205.3215	-103.6812
6 \$P_7\$	0	0	0	0	-103.6812	138.7363
7 \$P_8\$	0	0	0	0	0	-28.2386
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.7179	0	0	0
10 \$P_{11}\$	0	-62.7617	0	0	0	0

Iteration Number 9 Jacobians:

J22Table = 7×7 table

...

	\$DeltaVByV_5\$	\$DeltaVByV_6\$	\$DeltaVByV_7\$	\$DeltaVByV_8\$
1 \$Q_5\$	104.1891	6.9154	0	0
2 \$Q_6\$	-6.9154	205.6041	13.9691	0
3 \$Q_7\$	0	-13.9691	136.6367	3.9286
4 \$Q_8\$	0	0	-3.9286	47.1064
5 \$Q_9\$	0	0	0	-3.8918
6 \$Q_{10}\$	0	0	0	0
7 \$Q_{11}\$	0	0	0	0

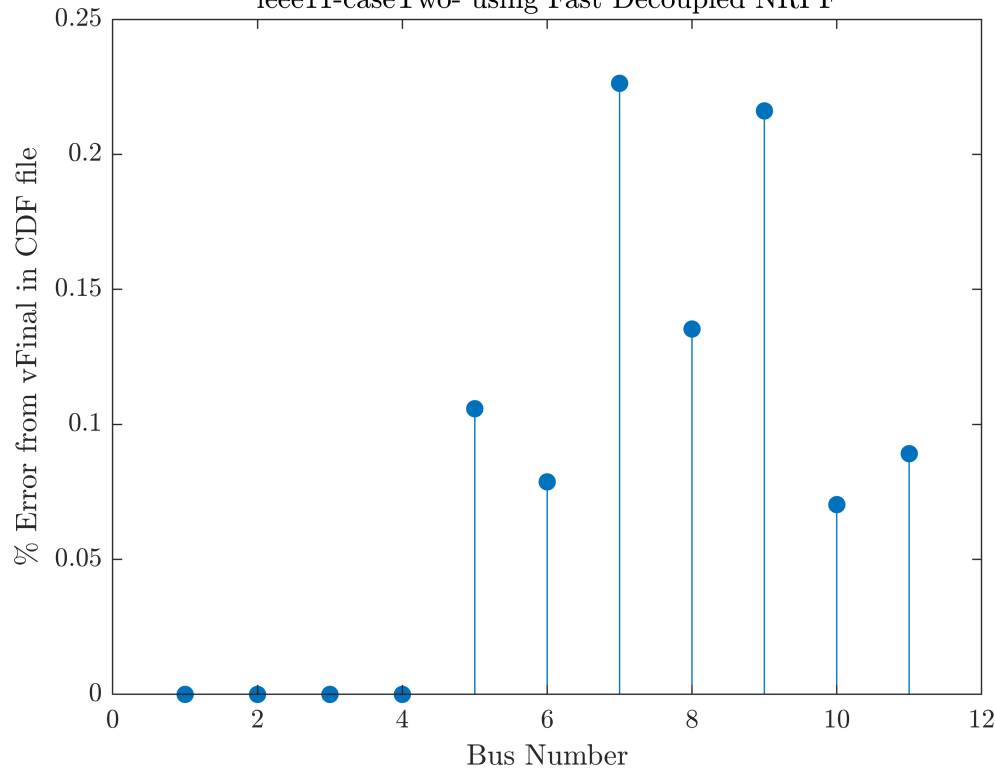
Convergence using Fast Decoupled NRPF achieved in 9 iterations.

resultTable = 11×4 table

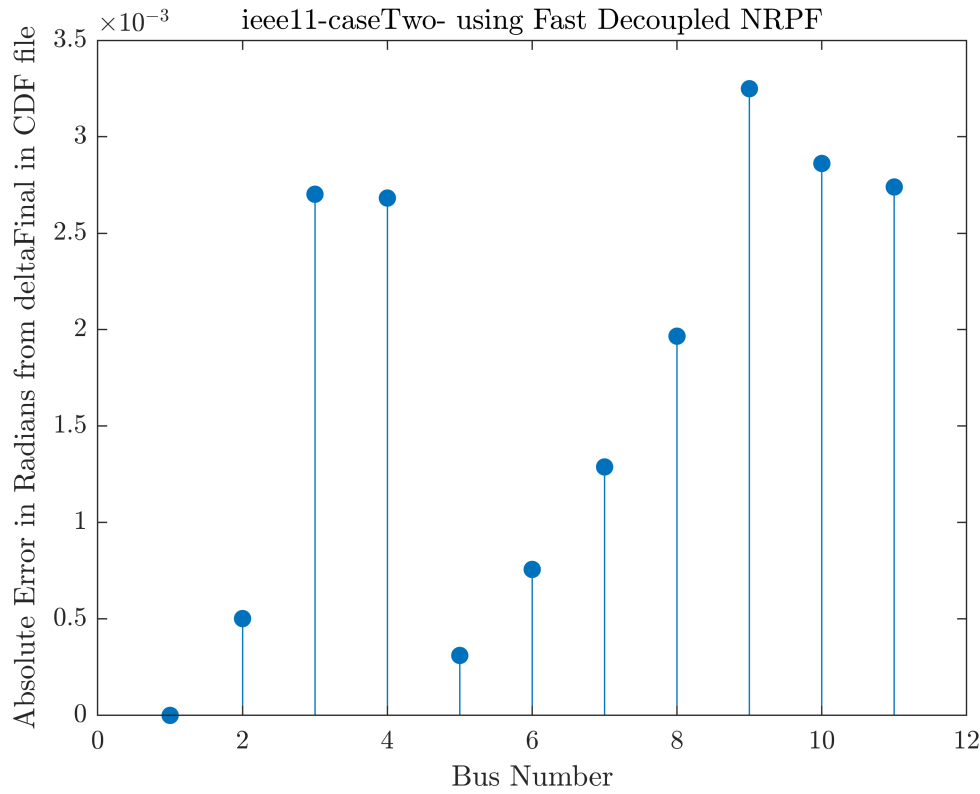
	P	Q	V	delta
1 \$Bus_1\$	6.9017	0.9474	1.0300	0
2 \$Bus_2\$	6.9998	0.1874	1.0100	-0.1625
3 \$Bus_3\$	7.1895	1.2928	1.0300	-0.3293
4 \$Bus_4\$	6.9995	0.8806	1.0100	-0.5049
5 \$Bus_5\$	-0.0001	-0.0239	1.0211	-0.1096
6 \$Bus_6\$	-0.0001	0.1430	1.0128	-0.2768
7 \$Bus_7\$	-9.6661	-1.0495	1.0233	-0.4115
8 \$Bus_8\$	0.0006	0.0417	1.0114	-0.5506
9 \$Bus_9\$	-17.6635	-1.0188	1.0042	-0.7612
10 \$Bus_{10}\$	-0.0014	0.0888	1.0017	-0.6204
11 \$Bus_{11}\$	-0.0003	-0.0111	1.0159	-0.4441

Compare obtained snapshot values of V_i and δ_i against the ones given in the CDF file.

Obtained Solution vs Given Solution in CDF file for Voltages of
ieee11-caseTwo- using Fast Decoupled NRPF



Obtained Solution vs Given Solution in CDF file for Voltage Angles of
ieee11-caseTwo- using Fast Decoupled NRPF



Economic Dispatch and Optimal Power Flow Calculations:

Elapsed time is 2.560879 seconds.

Have a nice day!

In case you encounter a Java Heap Memory error, delete the above gif, or go to Preferences -> General -> Java Heap Memory and increase the allocated size.

EE 521 Power System Analysis and EE 523 Power System Stability and Control Algorithms

Preamble and Control Inputs

```
systemName =  
"ieee11-caseThree-"
```

```
powerFlowMethod =  
"NRPF"
```

Read CDF file and store the data in neat MATLAB tables: busData and branchData.

```
busData = 11x18 table
```

...

	bus	busName	loadFlowArea	lossZone	busType	vFinal
1	1	"Bus 1 HV"	1	1	3	1.0300
2	2	"Bus 2 HV"	1	1	0	1.0100
3	3	"Bus 3 HV"	2	1	0	1.0300
4	4	"Bus 4 HV"	2	1	0	1.0100
5	5	"Bus 5 HV"	1	1	0	1.0200
6	6	"Bus 6 LV"	1	1	0	1.0120
7	7	"Bus 7 ZV"	1	1	0	1.0210
8	8	"Bus 8 TV"	3	1	0	1.0100
9	9	"Bus 9 LV"	2	1	0	1.0020
10	10	"Bus 10 LV"	2	1	0	1.0010
11	11	"Bus 11 LV"	2	1	0	1.0150

```
branchData = 10x15 table
```

...

	i	j	loadFlowArea	lossZone	ckt	type	R
1	1	5	1	1	1	0	0
2	2	6	1	1	1	0	0
3	3	11	2	1	1	0	0
4	4	10	2	1	1	0	0
5	5	6	1	1	1	0	0.0025
6	6	7	1	1	1	0	0.0010
7	7	8	1	1	1	0	0.0037
8	8	9	2	1	1	0	0.0055
9	9	10	2	1	1	0	0.0010
10	10	11	2	1	1	0	0.0025

N = 11
numBranch = 10

Extract Y_{Bus} , Adjacency List E from the branchData table.

ybusTable = 11×11 table

	1	2	3	4	5
1 1	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i
2 2	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
3 3	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i
4 4	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i
5 5	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	3.9604 -99.5701i
6 6	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	-3.9604 +39.6040i
7 7	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
8 8	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
9 9	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
10 10	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i
11 11	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i

Run Newton Raphson Power Flow and obtain a steady state snapshot of the system variables $P_i, Q_i, V_i, \delta_i \forall$ buses $i \in [1, N], i \in \mathbb{N}$

Iteration Number 1 Jacobian:
JTable = 20×20 table

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.3989	0	0	0	-60.3989	0
2 \$P_3\$	0	60.8939	0	0	0	0
3 \$P_4\$	0	0	60.1657	0	0	0
4 \$P_5\$	0	0	0	102.3984	-40.2170	0
5 \$P_6\$	-60.3989	0	0	-39.7473	200.6702	-100.5240
6 \$P_7\$	0	0	0	0	-99.5758	126.9689
7 \$P_8\$	0	0	0	0	0	-27.1258
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.1657	0	0	0
10 \$P_{11}\$	0	-60.8939	0	0	0	0
11 \$Q_2\$	2.4204	0	0	0	-2.4204	0
12 \$Q_3\$	0	2.4494	0	0	0	0
13 \$Q_4\$	0	0	2.4377	0	0	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
14 \$Q_5\$	0	0	0	-4.0424	1.6500	0
15 \$Q_6\$	2.4204	0	0	6.3465	-14.0310	5.2642
16 \$Q_7\$	0	0	0	0	14.7457	-16.1386
17 \$Q_8\$	0	0	0	0	0	4.0635
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	2.4377	0	0	0
20 \$Q_{11}\$	0	2.4494	0	0	0	0

Iteration Number 2 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	38.1877	0	0	0	-38.1877	0
2 \$P_3\$	0	8.9792	0	0	0	0
3 \$P_4\$	0	0	7.6318	0	0	0
4 \$P_5\$	0	0	0	87.5629	-29.8789	0
5 \$P_6\$	-38.1877	0	0	-28.8854	126.8167	-59.7435
6 \$P_7\$	0	0	0	0	-57.9441	69.7455
7 \$P_8\$	0	0	0	0	0	-11.4375
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-7.6318	0	0	0
10 \$P_{11}\$	0	-8.9792	0	0	0	0
11 \$Q_2\$	5.0718	0	0	0	-5.0718	0
12 \$Q_3\$	0	1.5173	0	0	0	0
13 \$Q_4\$	0	0	1.2967	0	0	0
14 \$Q_5\$	0	0	0	-4.3102	-2.0291	0
15 \$Q_6\$	5.0718	0	0	7.9055	-9.8645	-3.1128
16 \$Q_7\$	0	0	0	0	14.8816	-14.2264
17 \$Q_8\$	0	0	0	0	0	2.9810
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	1.2967	0	0	0
20 \$Q_{11}\$	0	1.5173	0	0	0	0

Iteration Number 3 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	78.4372	0	0	0	-78.4372	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
2 \$P_3\$	0	65.0761	0	0	0	0
3 \$P_4\$	0	0	72.6642	0	0	0
4 \$P_5\$	0	0	0	115.0481	-48.9592	0
5 \$P_6\$	-78.4372	0	0	-47.6987	260.6417	-134.5059
6 \$P_7\$	0	0	0	0	-132.4269	170.5106
7 \$P_8\$	0	0	0	0	0	-37.6205
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-72.6642	0	0	0
10 \$P_{11}\$	0	-65.0761	0	0	0	0
11 \$Q_2\$	5.3958	0	0	0	-5.3958	0
12 \$Q_3\$	0	14.6921	0	0	0	0
13 \$Q_4\$	0	0	14.9692	0	0	0
14 \$Q_5\$	0	0	0	-4.9957	-1.4698	0
15 \$Q_6\$	5.3958	0	0	11.1356	-19.4832	2.9518
16 \$Q_7\$	0	0	0	0	23.7414	-25.2155
17 \$Q_8\$	0	0	0	0	0	6.1025
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	14.9692	0	0	0
20 \$Q_{11}\$	0	14.6921	0	0	0	0

Iteration Number 4 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.8149	0	0	0	-60.8149	0
2 \$P_3\$	0	48.3427	0	0	0	0
3 \$P_4\$	0	0	47.3917	0	0	0
4 \$P_5\$	0	0	0	103.6065	-40.9387	0
5 \$P_6\$	-60.8149	0	0	-39.6409	202.4846	-102.0288
6 \$P_7\$	0	0	0	0	-99.5520	126.3970
7 \$P_8\$	0	0	0	0	0	-26.2116
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-47.3917	0	0	0
10 \$P_{11}\$	0	-48.3427	0	0	0	0
11 \$Q_2\$	6.4324	0	0	0	-6.4324	0
12 \$Q_3\$	0	8.3519	0	0	0	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
13 \$Q_4\$	0	0	8.3153	0	0	0
14 \$Q_5\$	0	0	0	-4.3067	-2.4602	0
15 \$Q_6\$	6.4324	0	0	10.5182	-14.6457	-2.3048
16 \$Q_7\$	0	0	0	0	22.4629	-21.9538
17 \$Q_8\$	0	0	0	0	0	5.8192
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	8.3153	0	0	0
20 \$Q_{11}\$	0	8.3519	0	0	0	0

Iteration Number 5 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	57.9353	0	0	0	-57.9353	0
2 \$P_3\$	0	57.1683	0	0	0	0
3 \$P_4\$	0	0	54.7002	0	0	0
4 \$P_5\$	0	0	0	101.6541	-39.6051	0
5 \$P_6\$	-57.9353	0	0	-38.2573	193.5509	-97.3583
6 \$P_7\$	0	0	0	0	-94.6278	120.7135
7 \$P_8\$	0	0	0	0	0	-25.3213
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-54.7002	0	0	0
10 \$P_{11}\$	0	-57.1683	0	0	0	0
11 \$Q_2\$	6.9631	0	0	0	-6.9631	0
12 \$Q_3\$	0	6.7927	0	0	0	0
13 \$Q_4\$	0	0	6.6685	0	0	0
14 \$Q_5\$	0	0	0	-4.0560	-2.8459	0
15 \$Q_6\$	6.9631	0	0	10.6321	-13.5424	-4.0529
16 \$Q_7\$	0	0	0	0	23.2515	-22.0050
17 \$Q_8\$	0	0	0	0	0	6.3914
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	6.6685	0	0	0
20 \$Q_{11}\$	0	6.7927	0	0	0	0

Iteration Number 6 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.9375	0	0	0	-60.9375	0
2 \$P_3\$	0	62.1710	0	0	0	0
3 \$P_4\$	0	0	60.1199	0	0	0
4 \$P_5\$	0	0	0	103.6850	-41.0133	0
5 \$P_6\$	-60.9375	0	0	-39.6503	203.4097	-102.8219
6 \$P_7\$	0	0	0	0	-100.0673	128.0324
7 \$P_8\$	0	0	0	0	0	-27.1910
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.1199	0	0	0
10 \$P_{11}\$	0	-62.1710	0	0	0	0
11 \$Q_2\$	6.9882	0	0	0	-6.9882	0
12 \$Q_3\$	0	7.1865	0	0	0	0
13 \$Q_4\$	0	0	6.9849	0	0	0
14 \$Q_5\$	0	0	0	-4.1280	-2.7816	0
15 \$Q_6\$	6.9882	0	0	10.8480	-14.2075	-3.6287
16 \$Q_7\$	0	0	0	0	23.9176	-22.8102
17 \$Q_8\$	0	0	0	0	0	6.6276
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	6.9849	0	0	0
20 \$Q_{11}\$	0	7.1865	0	0	0	0

Iteration Number 7 Jacobian:

JTable = 20×20 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.9049	0	0	0	-60.9049	0
2 \$P_3\$	0	62.3526	0	0	0	0
3 \$P_4\$	0	0	60.2614	0	0	0
4 \$P_5\$	0	0	0	103.6630	-40.9984	0
5 \$P_6\$	-60.9049	0	0	-39.6341	203.3114	-102.7723
6 \$P_7\$	0	0	0	0	-100.0124	127.9735
7 \$P_8\$	0	0	0	0	0	-27.1844
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.2614	0	0	0
10 \$P_{11}\$	0	-62.3526	0	0	0	0
11 \$Q_2\$	7	0	0	0	-7	0

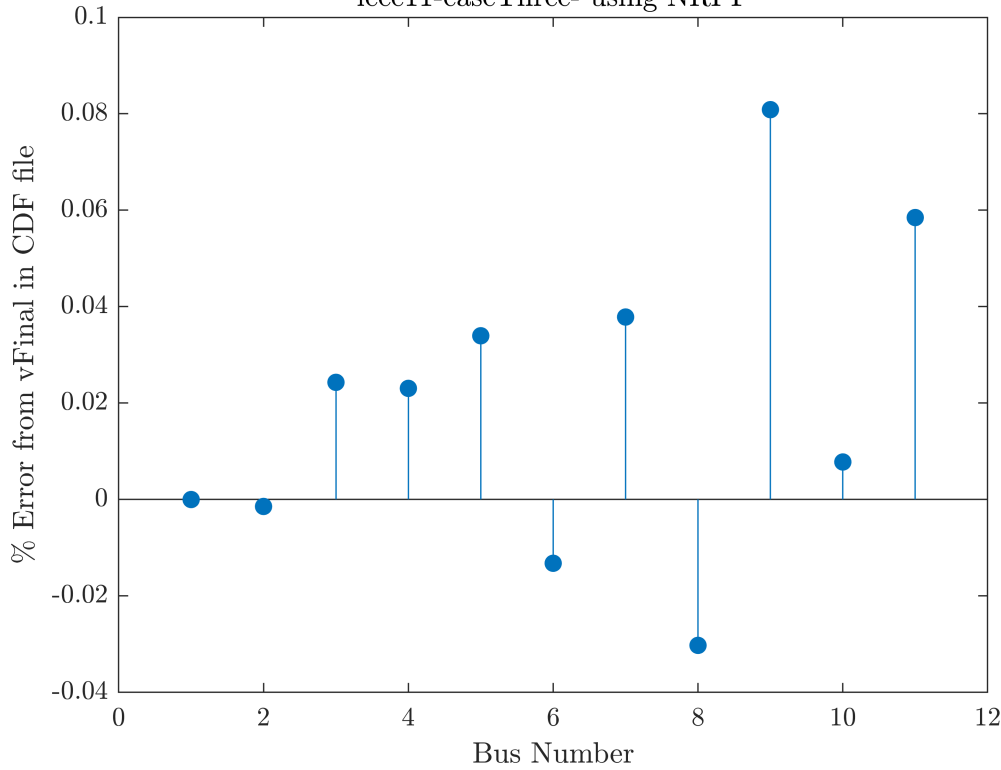
	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
12 \$Q_3\$	0	7.1900	0	0	0	0
13 \$Q_4\$	0	0	7	0	0	0
14 \$Q_5\$	0	0	0	-4.1232	-2.7895	0
15 \$Q_6\$	7	0	0	10.8527	-14.1923	-3.6604
16 \$Q_7\$	0	0	0	0	23.9389	-22.8180
17 \$Q_8\$	0	0	0	0	0	6.6400
18 \$Q_9\$	0	0	0	0	0	0
19 \$Q_{10}\$	0	0	7	0	0	0
20 \$Q_{11}\$	0	7.1900	0	0	0	0

Convergence using NRPF achieved in 7 iterations.
resultTable = 11x4 table

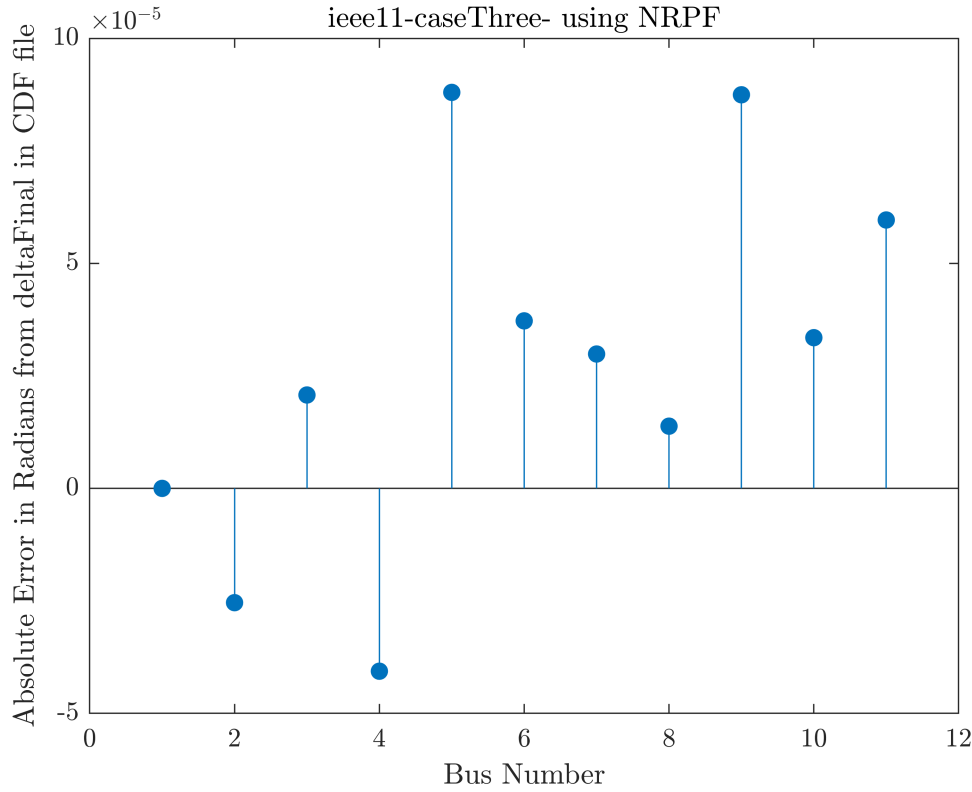
	P	Q	V	delta
1 \$Bus_1\$	6.9127	0.9766	1.0300	0
2 \$Bus_2\$	7	0.2870	1.0100	-0.1630
3 \$Bus_3\$	7.1900	1.3190	1.0303	-0.3319
4 \$Bus_4\$	7	0.9600	1.0102	-0.5076
5 \$Bus_5\$	-0	0	1.0203	-0.1099
6 \$Bus_6\$	-0	0	1.0119	-0.2775
7 \$Bus_7\$	-9.6700	-1	1.0214	-0.4127
8 \$Bus_8\$	0	0	1.0097	-0.5526
9 \$Bus_9\$	-17.6701	-1	1.0028	-0.7644
10 \$Bus_{10}\$	0.0001	0	1.0011	-0.6232
11 \$Bus_{11}\$	0	0	1.0156	-0.4467

Compare obtained snapshot values of V_i and δ_i against the ones given in the CDF file.

Obtained Solution vs Given Solution in CDF file for Voltages of
ieee11-caseThree- using NRPF



Obtained Solution vs Given Solution in CDF file for Voltage Angles of
ieee11-caseThree- using NRPF



Economic Dispatch and Optimal Power Flow Calculations:

Elapsed time is 1.796283 seconds.

Have a nice day!

In case you encounter a Java Heap Memory error, delete the above gif, or go to Preferences -> General -> Java Heap Memory and increase the allocated size.

EE 521 Power System Analysis and EE 523 Power System Stability and Control Algorithms

Preamble and Control Inputs

```
systemName =  
"ieee11-caseThree-"  
  
powerFlowMethod =  
"Fast Decoupled NRPF"
```

Read CDF file and store the data in neat MATLAB tables: busData and branchData.

```
busData = 11x18 table
```

...

	bus	busName	loadFlowArea	lossZone	busType	vFinal
1	1	"Bus 1 HV"	1	1	3	1.0300
2	2	"Bus 2 HV"	1	1	0	1.0100
3	3	"Bus 3 HV"	2	1	0	1.0300
4	4	"Bus 4 HV"	2	1	0	1.0100
5	5	"Bus 5 HV"	1	1	0	1.0200
6	6	"Bus 6 LV"	1	1	0	1.0120
7	7	"Bus 7 ZV"	1	1	0	1.0210
8	8	"Bus 8 TV"	3	1	0	1.0100
9	9	"Bus 9 LV"	2	1	0	1.0020
10	10	"Bus 10 LV"	2	1	0	1.0010
11	11	"Bus 11 LV"	2	1	0	1.0150

```
branchData = 10x15 table
```

...

	i	j	loadFlowArea	lossZone	ckt	type	R
1	1	5	1	1	1	0	0
2	2	6	1	1	1	0	0
3	3	11	2	1	1	0	0
4	4	10	2	1	1	0	0
5	5	6	1	1	1	0	0.0025
6	6	7	1	1	1	0	0.0010
7	7	8	1	1	1	0	0.0037
8	8	9	2	1	1	0	0.0055
9	9	10	2	1	1	0	0.0010
10	10	11	2	1	1	0	0.0025

N = 11
numBranch = 10

Extract Y_{Bus} , Adjacency List E from the branchData table.

ybusTable = 11×11 table

	1	2	3	4	5
1 1	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i
2 2	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
3 3	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i
4 4	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 -59.9880i	0.0000 + 0.0000i
5 5	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	3.9604 -99.5701i
6 6	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i	-3.9604 +39.6040i
7 7	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
8 8	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
9 9	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i
10 10	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i
11 11	0.0000 + 0.0000i	0.0000 + 0.0000i	0.0000 +59.9880i	0.0000 + 0.0000i	0.0000 + 0.0000i

Run Newton Raphson Power Flow and obtain a steady state snapshot of the system variables $P_i, Q_i, V_i, \delta_i \forall$ buses $i \in [1, N], i \in \mathbb{N}$

Iteration Number 1 Jacobian J11:
J11Table = 10×10 table

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.3989	0	0	0	-60.4474	0
2 \$P_3\$	0	60.8939	0	0	0	0
3 \$P_4\$	0	0	60.1657	0	0	0
4 \$P_5\$	0	0	0	102.8444	-40.4516	0
5 \$P_6\$	-60.4474	0	0	-40.4516	202.1296	-101.1638
6 \$P_7\$	0	0	0	0	-101.1638	136.9721
7 \$P_8\$	0	0	0	0	0	-27.5655
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.2150	0	0	0
10 \$P_{11}\$	0	-60.9431	0	0	0	0

Iteration Number 1 Jacobians:
J22Table = 10×10 table

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	60.7750	0	0	0
2 \$Q_3\$	0	61.9899	0	0
3 \$Q_4\$	0	0	61.0087	0
4 \$Q_5\$	0	0	0	100.0669
5 \$Q_6\$	-7.0016	0	0	-3.7653
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0
8 \$Q_9\$	0	0	0	0
9 \$Q_{10}\$	0	0	-7	0
10 \$Q_{11}\$	0	-7.1958	0	0

Iteration Number 2 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	59.9417	0	0	0	-60.3461	0
2 \$P_3\$	0	61.0236	0	0	0	0
3 \$P_4\$	0	0	59.9303	0	0	0
4 \$P_5\$	0	0	0	104.2100	-40.9895	0
5 \$P_6\$	-60.3461	0	0	-40.9895	203.1079	-102.1870
6 \$P_7\$	0	0	0	0	-102.1870	137.6700
7 \$P_8\$	0	0	0	0	0	-28.0876
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.3375	0	0	0
10 \$P_{11}\$	0	-61.4515	0	0	0	0

Iteration Number 2 Jacobians:

J22Table = 10×10 table

...

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	60.5719	0	0	0
2 \$Q_3\$	0	63.8213	0	0
3 \$Q_4\$	0	0	62.4294	0
4 \$Q_5\$	0	0	0	104.4135
5 \$Q_6\$	-6.9894	0	0	-5.4047
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0
8 \$Q_9\$	0	0	0	0

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
9 \$Q_10\$	0	0	-6.9404	0
10 \$Q_11\$	0	-7.1264	0	0

Iteration Number 3 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.2360	0	0	0	-60.6423	0
2 \$P_3\$	0	61.1251	0	0	0	0
3 \$P_4\$	0	0	59.8639	0	0	0
4 \$P_5\$	0	0	0	104.1119	-41.1578	0
5 \$P_6\$	-60.6423	0	0	-41.1578	203.8668	-102.8322
6 \$P_7\$	0	0	0	0	-102.8322	138.0203
7 \$P_8\$	0	0	0	0	0	-28.1478
8 \$P_9\$	0	0	0	0	0	0
9 \$P_10\$	0	0	-60.2622	0	0	0
10 \$P_11\$	0	-61.5384	0	0	0	0

Iteration Number 3 Jacobians:

J22Table = 10×10 table

...

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	59.9946	0	0	0
2 \$Q_3\$	0	63.3770	0	0
3 \$Q_4\$	0	0	61.2930	0
4 \$Q_5\$	0	0	0	103.6666
5 \$Q_6\$	-7.0019	0	0	-6.2605
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0
8 \$Q_9\$	0	0	0	0
9 \$Q_10\$	0	0	-6.9866	0
10 \$Q_11\$	0	-7.1766	0	0

Iteration Number 4 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.5710	0	0	0	-60.9770	0
2 \$P_3\$	0	61.3724	0	0	0	0
3 \$P_4\$	0	0	59.9733	0	0	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
4 \$P_5\$	0	0	0	104.1167	-41.1675	0
5 \$P_6\$	-60.9770	0	0	-41.1675	204.1625	-103.0051
6 \$P_7\$	0	0	0	0	-103.0051	138.0852
7 \$P_8\$	0	0	0	0	0	-28.1384
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.3786	0	0	0
10 \$P_{11}\$	0	-61.7921	0	0	0	0

Iteration Number 4 Jacobians:

J22Table = 10×10 table

...

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	61.3444	0	0	0
2 \$Q_3\$	0	63.8386	0	0
3 \$Q_4\$	0	0	62.2003	0
4 \$Q_5\$	0	0	0	104.3104
5 \$Q_6\$	-7.0096	0	0	-6.6193
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0
8 \$Q_9\$	0	0	0	0
9 \$Q_{10}\$	0	0	-7.0024	0
10 \$Q_{11}\$	0	-7.1927	0	0

Iteration Number 5 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.6605	0	0	0	-61.0635	0
2 \$P_3\$	0	61.4809	0	0	0	0
3 \$P_4\$	0	0	59.9256	0	0	0
4 \$P_5\$	0	0	0	104.0507	-41.2493	0
5 \$P_6\$	-61.0635	0	0	-41.2493	204.3955	-103.1630
6 \$P_7\$	0	0	0	0	-103.1630	138.0736
7 \$P_8\$	0	0	0	0	0	-28.1065
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.3308	0	0	0
10 \$P_{11}\$	0	-61.8998	0	0	0	0

Iteration Number 5 Jacobians:

J22Table = 10×10 table

...

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	60.7739	0	0	0
2 \$Q_3\$	0	64.0589	0	0
3 \$Q_4\$	0	0	61.5943	0
4 \$Q_5\$	0	0	0	103.7586
5 \$Q_6\$	-7.0126	0	0	-6.8074
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0
8 \$Q_9\$	0	0	0	0
9 \$Q_{10}\$	0	0	-7.0095	0
10 \$Q_{11}\$	0	-7.1998	0	0

Iteration Number 6 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.7852	0	0	0	-61.1882	0
2 \$P_3\$	0	61.6054	0	0	0	0
3 \$P_4\$	0	0	59.9462	0	0	0
4 \$P_5\$	0	0	0	104.0855	-41.2253	0
5 \$P_6\$	-61.1882	0	0	-41.2253	204.4326	-103.1526
6 \$P_7\$	0	0	0	0	-103.1526	138.0584
7 \$P_8\$	0	0	0	0	0	-28.0877
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.3531	0	0	0
10 \$P_{11}\$	0	-62.0245	0	0	0	0

Iteration Number 6 Jacobians:

J22Table = 10×10 table

...

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	61.6277	0	0	0
2 \$Q_3\$	0	64.0036	0	0
3 \$Q_4\$	0	0	62.1174	0
4 \$Q_5\$	0	0	0	104.2834
5 \$Q_6\$	-7.0144	0	0	-6.8613
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
8 \$Q_9\$	0	0	0	0
9 \$Q_{10}\$	0	0	-7.0134	0
10 \$Q_{11}\$	0	-7.2037	0	0

Iteration Number 7 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.7754	0	0	0	-61.1769	0
2 \$P_3\$	0	61.6874	0	0	0	0
3 \$P_4\$	0	0	59.8911	0	0	0
4 \$P_5\$	0	0	0	104.0475	-41.2705	0
5 \$P_6\$	-61.1769	0	0	-41.2705	204.5103	-103.2094
6 \$P_7\$	0	0	0	0	-103.2094	138.0317
7 \$P_8\$	0	0	0	0	0	-28.0667
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.2978	0	0	0
10 \$P_{11}\$	0	-62.1058	0	0	0	0

Iteration Number 7 Jacobians:

J22Table = 10×10 table

...

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	61.0467	0	0	0
2 \$Q_3\$	0	64.4136	0	0
3 \$Q_4\$	0	0	61.6455	0
4 \$Q_5\$	0	0	0	103.8416
5 \$Q_6\$	-7.0147	0	0	-6.9075
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0
8 \$Q_9\$	0	0	0	0
9 \$Q_{10}\$	0	0	-7.0145	0
10 \$Q_{11}\$	0	-7.2049	0	0

Iteration Number 8 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.8295	0	0	0	-61.2316	0
2 \$P_3\$	0	61.7379	0	0	0	0

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
3 \$P_4\$	0	0	59.8913	0	0	0
4 \$P_5\$	0	0	0	104.0799	-41.2413	0
5 \$P_6\$	-61.2316	0	0	-41.2413	204.4810	-103.1685
6 \$P_7\$	0	0	0	0	-103.1685	138.0163
7 \$P_8\$	0	0	0	0	0	-28.0597
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.2988	0	0	0
10 \$P_{11}\$	0	-62.1557	0	0	0	0

Iteration Number 8 Jacobians:

J22Table = 10×10 table

...

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	61.6461	0	0	0
2 \$Q_3\$	0	64.1457	0	0
3 \$Q_4\$	0	0	62.0107	0
4 \$Q_5\$	0	0	0	104.2507
5 \$Q_6\$	-7.0153	0	0	-6.9067
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0
8 \$Q_9\$	0	0	0	0
9 \$Q_{10}\$	0	0	-7.0155	0
10 \$Q_{11}\$	0	-7.2056	0	0

Iteration Number 9 Jacobian J11:

J11Table = 10×10 table

...

	\$delta_2\$	\$delta_3\$	\$delta_4\$	\$delta_5\$	\$delta_6\$	\$delta_7\$
1 \$P_2\$	60.7986	0	0	0	-61.1998	0
2 \$P_3\$	0	61.7913	0	0	0	0
3 \$P_4\$	0	0	59.8468	0	0	0
4 \$P_5\$	0	0	0	104.0488	-41.2702	0
5 \$P_6\$	-61.1998	0	0	-41.2702	204.5091	-103.1980
6 \$P_7\$	0	0	0	0	-103.1980	137.9928
7 \$P_8\$	0	0	0	0	0	-28.0466
8 \$P_9\$	0	0	0	0	0	0
9 \$P_{10}\$	0	0	-60.2542	0	0	0
10 \$P_{11}\$	0	-62.2089	0	0	0	0

Iteration Number 9 Jacobians:
J22Table = 10×10 table

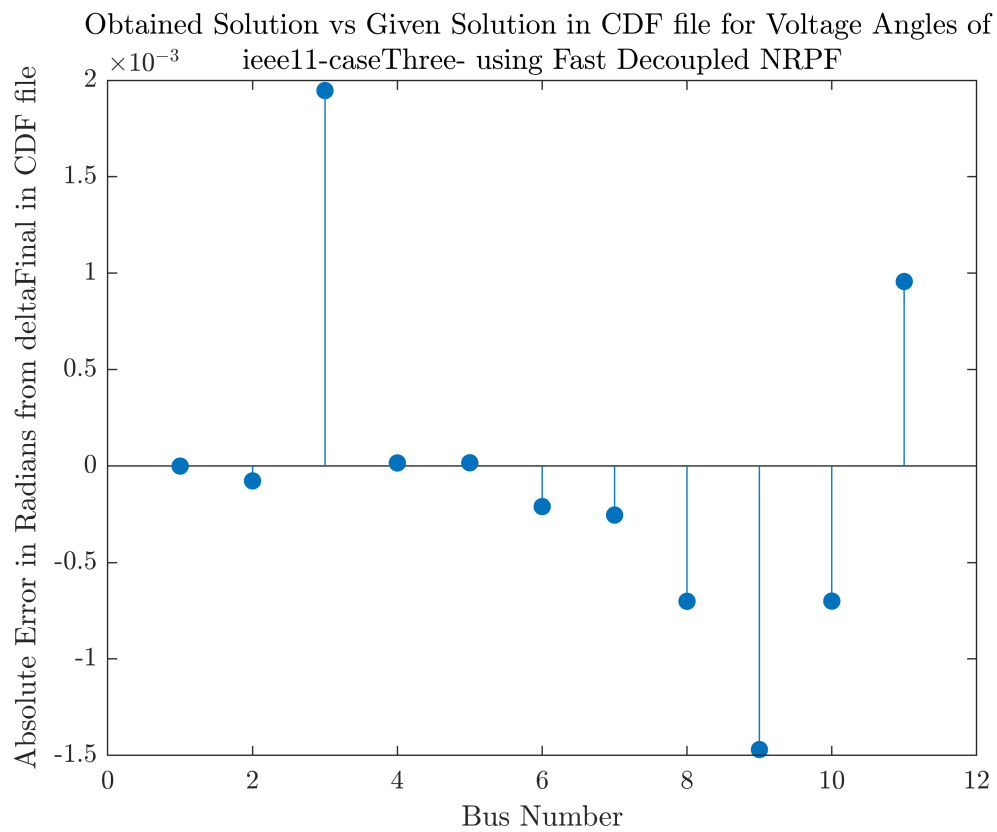
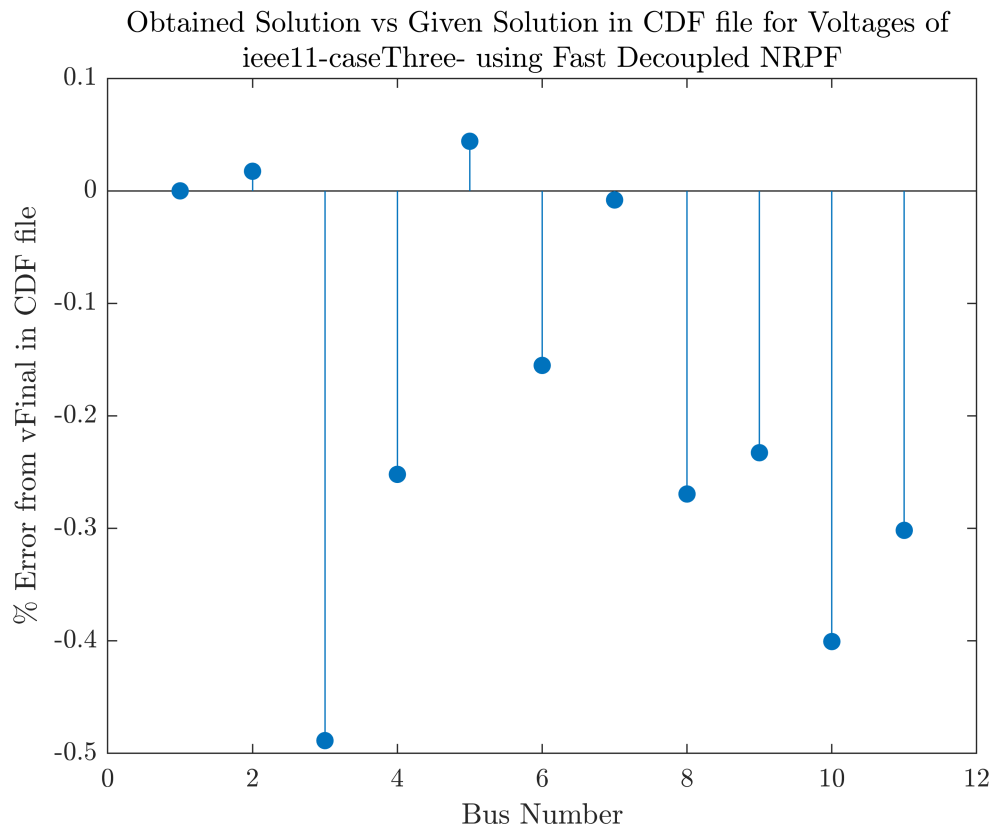
...

	\$DeltaVByV_2\$	\$DeltaVByV_3\$	\$DeltaVByV_4\$	\$DeltaVByV_5\$
1 \$Q_2\$	61.1525	0	0	0
2 \$Q_3\$	0	64.5755	0	0
3 \$Q_4\$	0	0	61.6367	0
4 \$Q_5\$	0	0	0	103.8961
5 \$Q_6\$	-7.0151	0	0	-6.9243
6 \$Q_7\$	0	0	0	0
7 \$Q_8\$	0	0	0	0
8 \$Q_9\$	0	0	0	0
9 \$Q_10\$	0	0	-7.0155	0
10 \$Q_11\$	0	-7.2058	0	0

Convergence using Fast Decoupled NRPF achieved in 9 iterations.
resultTable = 11×4 table

	P	Q	V	delta
1 \$Bus_1\$	6.9121	1.0222	1.0300	0
2 \$Bus_2\$	6.9998	0.1771	1.0102	-0.1631
3 \$Bus_3\$	7.1897	1.3917	1.0250	-0.3300
4 \$Bus_4\$	6.9996	0.8953	1.0075	-0.5075
5 \$Bus_5\$	-0.0001	-0.0752	1.0204	-0.1099
6 \$Bus_6\$	0.0001	0.3042	1.0104	-0.2777
7 \$Bus_7\$	-9.6692	-1.1596	1.0209	-0.4130
8 \$Bus_8\$	0.0006	0.0571	1.0073	-0.5533
9 \$Bus_9\$	-17.6669	-1.0855	0.9997	-0.7659
10 \$Bus_10\$	-0.0006	0.2508	0.9970	-0.6240
11 \$Bus_11\$	-0.0003	-0.1501	1.0119	-0.4458

Compare obtained snapshot values of V_i and δ_i against the ones given in the CDF file.



Economic Dispatch and Optimal Power Flow Calculations:

Elapsed time is 2.536898 seconds.

Have a nice day!

In case you encounter a Java Heap Memory error, delete the above gif, or go to Preferences -> General -> Java Heap Memory and increase the allocated size.