

EE 521/ECE 582 – Analysis of Power systems

Class #13 – October 6, 2022

*Dr. Noel N. Schulz
Edmund O. Schweitzer III Chair in
Power Apparatus and Systems
Chief Scientist Joint Appointment, PNNL
Co-Director, PNNL/WSU Advanced Grid Institute (AGI)
Washington State University Pullman
Noel.Schulz@wsu.edu EME 35
509-335-0980 (o) and 509-336-5522 (c)*

Reminders

- Student Hours This Week & Next
 - **Friday 1:30-2:30 pm** Zoom or EME 35 Pullman
 - **Tuesday 4:30-5:30 pm (after class)** – Zoom or EME 35 Pullman
 - **Wednesday 4-5 pm** Zoom or EME 35 Pullman
 - **Friday 1:30-2:30 pm** Zoom or EME 35 PullmanAdditional Office Hours next week will be posted
- Remember the Discussion Set Assignment
 - **10/11 Discussions**
- Final Paper – Think about Topic - Oct 14
- NAPS or WPRC Next week?

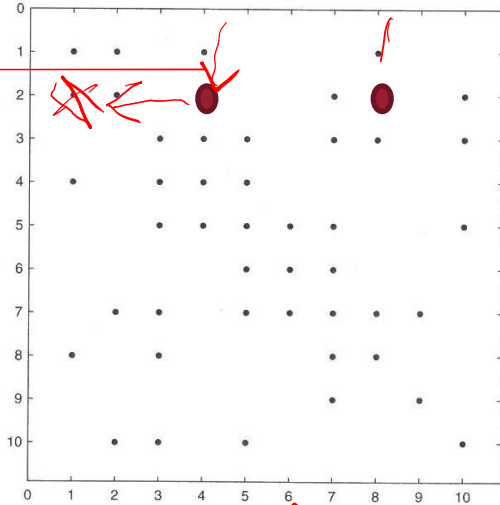
Program #2 – Sparse Matrices Program

- **Full Newton Raphson** -- Take the Jacobian Matrix from Program #1 (with taps) and solve the problem using Sparse Matrix Techniques
- **Fast Decoupled Power Flow** – Use Sparse Matrix Techniques for B' and B'' and solve. ~~Use Scheme 0 to solve Fast Decoupled Power Flow~~
- **Extra Credit** -- Fast Decoupled Power Flow – Use Sparse Matrix Techniques for B' and B'' and solve. Use Scheme 0 to solve Fast Decoupled Power Flow

**** Do not use the SEARCH function as that is not an acceptable method ****

NIR NIC

Example of Adding a New Term/Fill



Row
 2, 4
 2, 8

15 → 36
 2,1 2,2

34 → 23
 2,7 2,10

2,4
 4,5

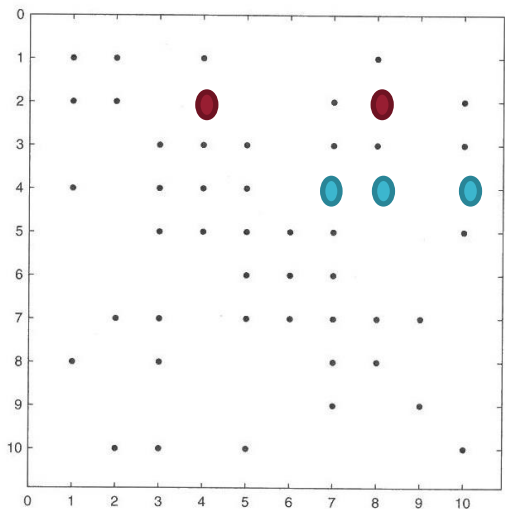
i	NROW	NCOL	NIR	NIC	Value
1	8	8	0	0	-28
2	7	2	35	17	5
3	10	5	41	0	7
4	5	10	0	41	7
5	5	7	4	25	3
6	6	6	25	42	-33
7	6	5	6	30	10
8	1	8	0	46	8
9	5	5	28	7	-44
10	1	<u>4</u>	8	45	19
11	4	3	27	40	6
12	8	3	44	14	1
13	3	4	29	27	6
14	10	3	3	0	9
15	2	1	36	20	2
16	9	7	43	0	13
17	10	2	14	0	10
18	3	8	19	<u>26</u>	1

i	FIR	FIC
1	37	37
2	15	32
3	24	24
4	20	10
5	40	29
6	7	28
7	2	34
8	22	8
9	16	38
10	17	23

19	3	10	0	4	9
20	4	1	11	22	19
21	7	7	26	44	-68
22	8	1	12	0	8
23	2	10	<u>0</u>	19	10
24	3	3	13	11	-40
25	6	7	0	21	19
26	7	8	38	1	15
27	4	4	39	31	-38
28	5	6	5	6	10
29	3	5	33	39	11
30	7	5	42	3	3
31	5	4	9	0	9
32	1	2	10	36	2
33	3	7	18	5	9
34	2	7	46	33	5
35	7	3	30	12	9
36	2	2	<u>45</u>	2	-21
37	1	1	32	15	-33
38	7	9	0	43	13
39	4	5	0	9	9
40	5	3	31	35	11
41	10	10	0	0	-30
42	7	6	21	0	19
43	9	9	0	0	-17
44	8	7	1	16	15

→ 45 2 4 34 13 X
 → 46 2 8 23 18 X

Example of Adding a New Term/Fill



i	NROW	NCOL	NIR	NIC	Value
1	8	8	0	0	-28
2	7	2	35	17	5
3	10	5	41	0	7
4	5	10	0	41	7
5	5	7	4	25	3
6	6	6	25	42	-33
7	6	5	6	30	10
8	1	8	0	18	46 8
9	5	5	28	7	-44
10	1	4	8	13	45 19
11	4	3	27	40	6
12	8	3	44	14	1
13	3	4	29	27	6
14	10	3	3	0	9
15	2	1	36	20	2
16	9	7	43	0	13
17	10	2	14	0	10
18	3	8	19	26	48 1
19	3	10	0	49	9
20	4	1	11	22	19
21	7	7	26	44	-68
22	8	1	12	0	8
23	2	10	0	19	10
24	3	3	13	11	-40
25	6	7	0	21	19
26	7	8	38	1	15
27	4	4	39	31	-38
28	5	6	5	6	10
29	3	5	33	39	11
30	7	5	42	3	3
31	5	4	9	0	9
32	1	2	10	36	2
33	3	7	24	5	9
34	2	7	23	46	33 5
35	7	3	30	12	9
36	2	2	45	2	-21
37	1	1	32	15	-33
38	7	9	0	43	13
39	4	5	20	7	9
40	5	3	31	35	11
41	10	10	0	0	-30
42	7	6	21	0	19
43	9	9	0	0	-17
44	8	7	1	16	15

i	FIR	FIC
1	37	37
2	15	32
3	24	24
4	20	10
5	40	29
6	7	28
7	2	34
8	22	8
9	16	38
10	17	23

45	2	4	34	13	X
46	2	8	23	18	X
47	4	7	48	20	X 5
48	4	8	49	26	X
49	4	10	04		X

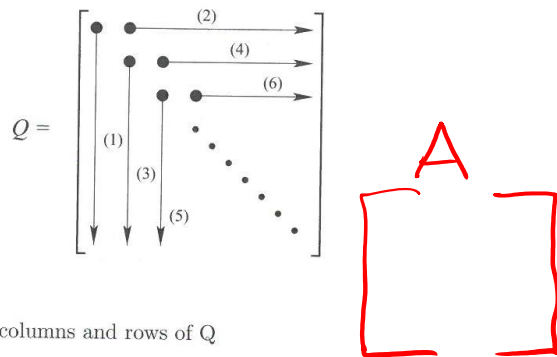


FIGURE 2.1

Order of calculating columns and rows of Q

known as *Crout's algorithm* for finding the LU factors [8]. Let the matrix Q be defined as

$$Q \triangleq L + U - I = \begin{bmatrix} l_{11} & u_{12} & u_{13} & \cdots & u_{1n} \\ l_{21} & l_{22} & u_{23} & \cdots & u_{2n} \\ l_{31} & l_{32} & l_{33} & \cdots & u_{3n} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ l_{n1} & l_{n2} & l_{n3} & \cdots & l_{nn} \end{bmatrix} \quad (2.24)$$

Crout's algorithm computes the elements of Q first by column and then row, as shown in Figure 2.1. Each element q_{ij} of Q depends only on the a_{ij} entry of A and previously computed values of Q .

Crout's Algorithm for Computing LU from A

1. Initialize Q to the zero matrix. Let $j = 1$.
2. Complete the j th column of Q (j th column of L) as

$$q_{kj} = a_{kj} - \sum_{i=1}^{j-1} q_{ki}q_{ij} \quad \text{for } k = j, \dots, n \quad (2.25)$$

3. If $j = n$, then stop.
4. Assuming that $q_{jj} \neq 0$, complete the j th row of Q (j th row of U) as

$$q_{jk} = \frac{1}{q_{jj}} \left(a_{jk} - \sum_{i=1}^{j-1} q_{ji}q_{ik} \right) \quad \text{for } k = j+1, \dots, n \quad (2.26)$$

5. Set $j = j+1$. Go to step 2.

Handwritten calculation of LU factors from matrix A:

Matrix A (from Figure 2.1):

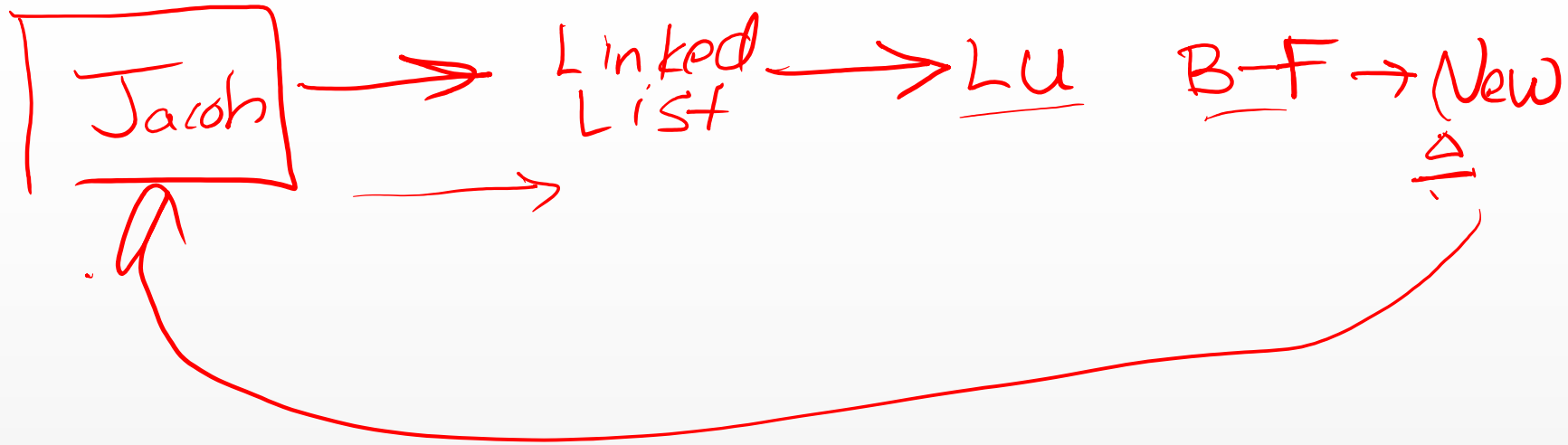
$$A = \begin{bmatrix} 1 & 3 & 4 \\ 2 & 1 & 2 \\ 4 & 3 & 5 \end{bmatrix}$$

Row and Column indices:

Row: 1, 2, 3, 4, 5, 6, 7, 8, 9
Col: 1, 2, 3

LU factors (NIR, NIC, #):

	Row	Col	NIR	NIC	#
1	1	1	2	4	1
2	1	2	3	5	3
3	1	3	0	6	4
4	2	1	5	7	2
5	2	2	6	8	1
6	2	3	0	9	2
7	3	1	0	0	4
8	3	2	0	0	2
9	3	3	0	0	5



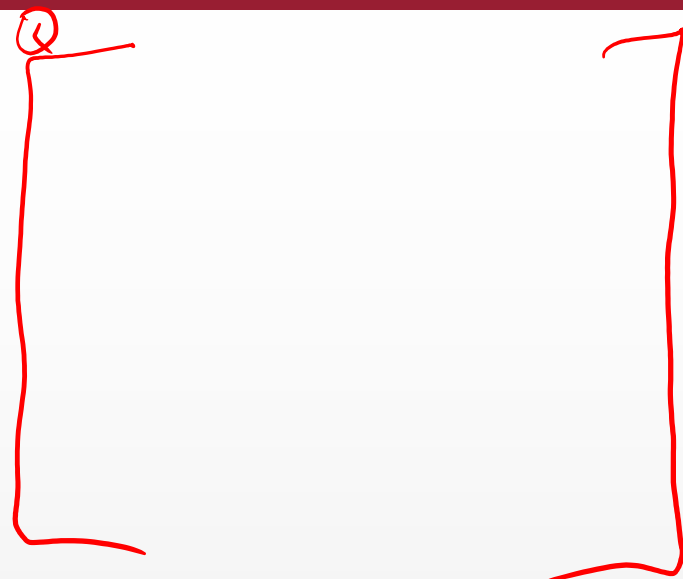
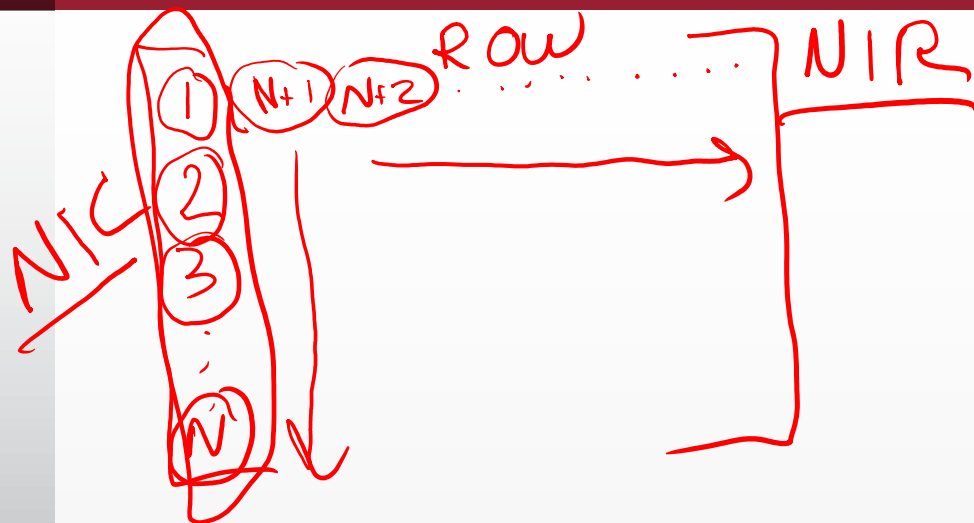
$$\begin{aligned}
 j &= 1 \\
 g_{11} &= a_{11} \\
 g_{21} &= a_{21} \\
 g_{31} &= a_{31} \\
 &\downarrow \text{NIC} \\
 &\downarrow
 \end{aligned}$$

~~$$g_{ki} = a_{ki} - \sum_{i=1}^j g_{ki} g_{il}$$~~

$$g(\text{row}, 1) = a(\text{row}, 1)$$

Row (a) NIR NIC ~~≠~~

1
2
3
4
5
6
7
8
9



$$c) \quad \underline{g_{kj}} = \underline{a_{kj}} \sum_{i=1}^{j-1} g_{ki} g_{ij} \quad k=j+1 \text{ to } N$$

row $g_{jk} = \frac{1}{g_{jj}} \left(a_{jk} - \sum_{i=1}^{j-1} g_{ji} g_{ik} \right)$ $k=j+1 \text{ to } N$

~~FIR~~ \rightarrow $\begin{matrix} g_{jj} \\ \text{FIC} \end{matrix}$
 \downarrow

$$j=1$$

$$g_{11} = \frac{a_{11}}{g_{11}} \text{ NIC}$$

$$g_{21} = \frac{a_{21}}{g_{11}} \text{ NIC}$$

$$g_{31} = \frac{a_{31}}{g_{11}} \text{ NIC}$$

$$g_{12} = \frac{a_{12}}{g_{11}} \text{ NIR}$$

$$g_{13} = \frac{a_{13}}{g_{11}} \text{ NIR}$$

$$\cancel{g(1,1)} = a(1,1)$$

$$g_{22} = \frac{a_{22}}{g_{11}} - g_{21}g_{12}$$

$$g_{32} = \frac{a_{32}}{g_{11}} - g_{31}g_{12}$$

$$g_{23} = \frac{1}{g_{22}} (a_{23} - g_{21}g_{13})$$

$$j=3$$

$$\frac{g_{33} = a_{33}}{g_{31}g_{13} + g_{32}g_{23}}$$



Q 11

FIR
[1]



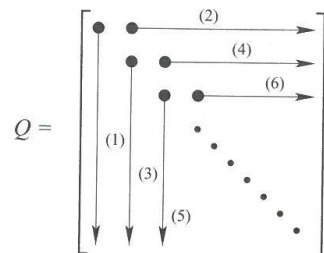
~~#A11~~

FIC
[1]



$$\begin{bmatrix} 1 & 2 & 3 \\ 4 & 5 & 6 \\ 7 & 8 & 9 \end{bmatrix} \times \begin{bmatrix} 0 & 3 & 5 \\ 1 & 6 & 7 \\ 3 & 8 & 2 \end{bmatrix} =$$



**FIGURE 2.1**

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5. Set $j = j+1$. Go to step 2.

<

0.001

Sparse

$a_{kj} = 0$

A 

Q

~~col row~~
row col nk nic #
↓
g₁₁ 1
g_{1n} N
g₁₂
D

Announcements

- Finish Chapter 4
- Review Sections 3.5.5 & 3.5.6
- Papers for Discussion Set #1 –Questions – Today and Responses by 10/11
- Work on Program #1
- Set up Time for Program #1 Discussions