## MORE DETAILS ON GETTING YOUR AUGMENTED LAGRANGIAN CODE WORKING.

Remember that the goal is to formulate "stand-alone" code that can solve any appropriately formulated optimization problem. This means that for: min f(x) sit.  $C_E(x) = 0$ ,  $C_I(x) \ge 0$  where  $C_E(x)^T = [ ... C_i(x) ... ]$  if E and  $C_I(x)^T = [ ... C_i(x) ... ]$  if E. a problem is defined by a structure variable / dictionary / class:

Pr. obj -> function handle to f and Pf complitation

pr. earn -> function handle to CE and hE=VCE computation

pr. icon -> function handle to CI and hI=VCI computation

pr. Xo -> initial point in Rn.

pr. par -> parameters necessary for computing fg, CE etc.

(and hyperparameters)

The problem description can be complicated because there are two distinct (but related) problems to keep track of.

pr -> The user-defined problem

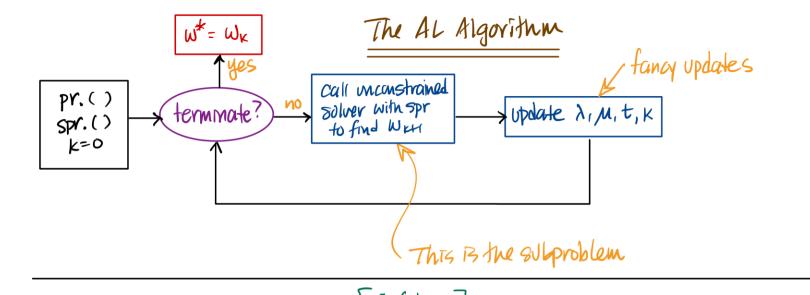
spr -> the Internally-defined inconstrained subproblem

Subproblem spr will call the Augmented Lagrangian objective function to compute  $F := La(\omega,\lambda,\mu)$  and  $G := \nabla_{\!\!\!k} L_a(\omega,\lambda,\mu)$  where  $\omega^{T} = [X^T y^T]$ Sand the y's are slack variables used to convert the inequality constraints (  $C_{I}(x) \ge 0 \rightarrow C_{I}(x) - y^2 = 0$  ).

Spr. obj = @ ALOBJ = internally use this function to compute objective and gradient of La Spr. par = pr. parspr. par. obj = pr.obj with parameters it needs. Spr. par. icon = pr. icon

Spr. par. econ = pr. econ

Spr. par. mu = mu Spr. par. lambda = lambda



Define 
$$C(\omega) = C(x,y) = \begin{bmatrix} C_E(x) \\ C_I(x) - y^2 \end{bmatrix}$$

$$F := L_A(\omega;\lambda;\mu) = f(x) - \lambda^T C(\omega) + \frac{1}{Z} \mu C(\omega)^T C(\omega)$$

$$G := \nabla L_A(\omega;\lambda;\mu) = \begin{bmatrix} \nabla_x f(x) \\ \nabla_y f(x) \end{bmatrix} - \lambda^T \begin{bmatrix} C_E(x) \\ C_I(x) - y^2 \end{bmatrix} + \frac{1}{Z} \mu \begin{bmatrix} C_E(x) \\ C_I(x) - y^2 \end{bmatrix} \begin{bmatrix} C_E(x) \\ C_I(x) - y^2 \end{bmatrix}$$

$$= \begin{bmatrix} \nabla_x f(x) \\ 0 \end{bmatrix} - \begin{bmatrix} \nabla_x C_I(x) \\ 0 \end{bmatrix} \begin{pmatrix} \lambda - \mu \begin{bmatrix} C_E(x) \\ C_I(x) - y^2 \end{bmatrix} \end{pmatrix}$$

Skeleton of ALOBJ: this is spr.par function [F,6] = ALOBJ (W, P) P.I and P.E are the number of meg./eg. constraints  $N = length(\omega) - P.I \ll$  $X = \omega(1:n)$ ;  $Y = \omega(n+1:end)$ [f,g] = p.obj(x,p))calling user-defined [CE, he] = p.econ(xIP) This illustrates The case with functions both eq. and mag. constraints [CI, hi] = P.icon (xIP) and computing both Fand 6. Y = diag (y)  $C = [C_E; C_I - Y*Y]$  $F = f - \lambda * C + (M/2) * C^{T} * C$ G = [g; Zeros (P.I,1)] - [CE (I; Zeros (P.I, N) -2\*Y]\*[λ-μ\*C] refurn Notice that this is a fixed problem-independent function. The specific user-defined problem is only in the computations

the specific user-defined problem is only in the computator of figice etc and defined by the user elsewhere.