RITWATEET 13 Oct 2.22 +99.5/100 6PM to 9PM Great work! 1.  $(a) P(a|P) = \frac{P(P|a) \cdot P(a)}{P(P)}$ +5  $P(G|P) = \frac{(0.8)(0.1)}{P(P|G).P(G)} + P(P|G).P(G)$ DE COLORS & CERTIFICATION ~ P(a | 1) = (0.8)(0.1) + (0.2)(0.9) p(p1 = 0.26 1(a) = (a) = 0.3077 mm (b) P(P1.P2 P3) = P(P1) P(P2) . P(P3) (Independent P(P3) = (P(P19)) P(P2) . P(P3) (Independent Perfection propries ~ P(P1P2P3) = {P(P)}3 P(P3)(G).P(G). P(a | P1P2P3) = P(P3 | G). P(G)
P(G | P3)

P(G | P3) ~ P(G|P1P2P3) = {P(R1G)}3. P(G) {P(B)}3. P(G) +P(P3|C).P(C)

1.2

$$P(G | P_1 P_2 P_3) = \frac{(0.8)^3 (0.1)}{\{0.8 \times 0.1 + 0.2 \times 0.9\}^3}$$

(b) v + c + P3 denate a mark passing all theree tests

$$eyon P(P3|G) = [P(P|G)]^3$$
5 and  $P(P3|C) = [P(P|G)]^3$ 

$$P(a|P3) = P(P3|A).P(A).$$

$$P(P3|A).P(A) + P(P3|C).P(C)$$

$$\rho(G|P3) = \frac{(0.8)^3(0.1)}{(0.8)^3(0.1) + (0.2)^3(0.9)}$$

$$en | P(a | P3) = 0.8767$$
 Am

egin 
$$P(p) = 0.6$$
  
 $P(E) = 0.7$   
 $P(0+E) = 0.8$ 

$$0.8 = 0.6 + 0.7 - P(DF)$$

- Part Emporiturely independent

261

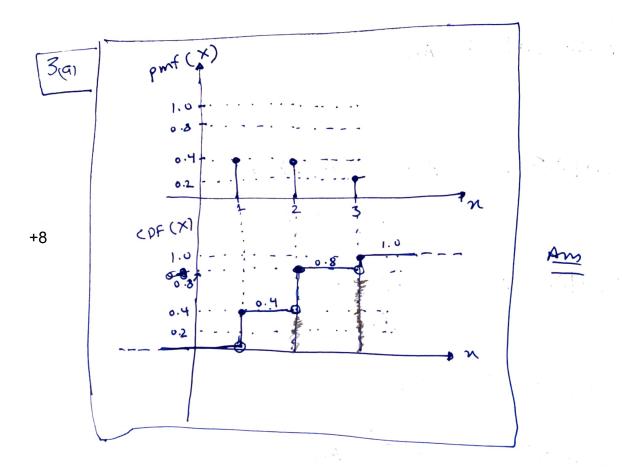
D and E are positively dependent.

\_\_\_\_\_ ×

· ...

.

3. constituent PMF(XI) ×7 CDE (XI) 002 PERT) = 0.2 0,8 1 0.4 P({a,e1) = 0.4 P( { b, d }) = 0.4 b, d 2 . 11.0 P((()) =0.2 3



 $P(A|X \leq 2) \quad \text{But} \quad X \leq 2 \equiv \{a,b,d,e\}$   $Se \quad P(\{a,b,d\},\{a,b,d,h\}) = 1$   $3(b) \quad P(A|X \leq 2) = 1 \quad \text{An}$ 

Note: Solving for 3(c) grøst, then 3(b):

$$P(A|X\leq 2) = P(X\leq 2|A).P(A)$$

$$P(X\leq 2)$$

$$P(A|X \le 2) = \frac{(1)(0.6)}{EDF(X=2)}$$

Am

$$f_{\times}(n) = \{c e^{-n} \text{ for } n \in [c, T]\}$$

(a) 
$$\int_{N=0}^{\infty} (e^{-N} dN = 1)$$
 (Aug uden  $Pdf = 1$ )

$$Ce^{-n}\Big|_{n=1}^{n=2}$$

$$C(e - e^{-T}) = 1$$

$$C = \frac{1}{1 - e^{-T}}$$
Ans

(b) 
$$F_{X}(n=d) = \int_{n=0}^{n=d} Ce^{-n} dn$$
,  $n \in [0,T]$ 

$$\alpha F_{\times}(n=d) = C(1-e^{-d}) \quad n \in (0,T)$$

$$F_{\times}(x=d) = \begin{cases} 0 & \text{id} < 0 \\ \frac{1-e^{-d}}{1-e^{-T}} & \text{id} \in (0,T) \end{cases}$$

$$\frac{1}{1} & \text{id} > T$$

$$E(X) = \int_{R=0}^{R=T} f_{x}(n) \cdot n \, dn$$

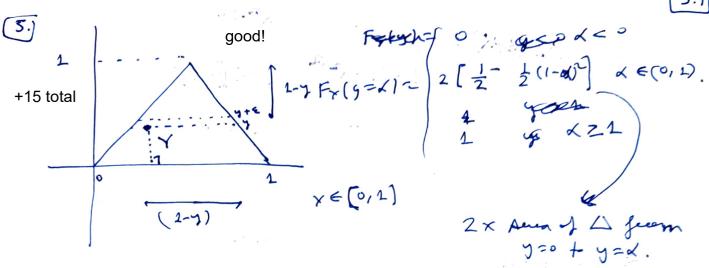
$$\sim E(X) = C \left[ -ne^{-n} \right]_{n=0}^{n=T} - \int_{n=0}^{n=T} -n dn = \frac{ne^{-n}}{ne^{-n}} dn$$

$$\sim E(X) = C \left[ -te^{-T} + (1-e^{-T}) \right]$$

$$o = E(X) = 1 - (1+T)e^{-T}$$
 $1 - e^{-T}$ 

E REA

nen- en



$$F_{\gamma}(y=d) = \begin{cases} 0 & < 0 \\ 1-(1-d)^{2} & < [0,1] \end{cases}$$

$$1 & < 21$$

$$f_{\gamma}(y=\lambda) = \begin{cases} 0 & \alpha < 0 \\ 2(1-\alpha) & \alpha \in (0,1) \end{cases}$$

$$0 & \alpha < 0 \end{cases}$$

(b) 
$$z = 57$$
  $z \in (0,1)$   
 $F_{z}(z) = p(z \leq d)$   
 $F_{z}(z) = p(57 \leq d)$   
 $F_{z}(z) = p(7 \leq d) = F_{x}(7 = d^{2})$ 

$$F_{2}(274) = \begin{cases} 1 - (1 - \lambda^{2})^{2} & \lambda^{2} \in [0,1] \\ 1 & \lambda^{2} > 1 \end{cases}$$

$$\frac{2}{4} = \frac{1 - (1 - \lambda^{2})^{2}}{4} = \frac{1 - (1 - \lambda^{2})^$$

(6.)

$$- f_{X|T}(n|T) = unid (0,2). \qquad n \in (0,2)$$

on 
$$f_{\times}(n) = \begin{cases} \frac{1}{\sqrt{2n}} e^{-\left(\frac{n-\mu}{\sigma}\right)^2} & (\frac{1}{2})(\frac{1}{2}) \\ \frac{1}{\sqrt{2n}} e^{-\left(\frac{n-\mu}{\sigma}\right)^2} & (\frac{1}{2}) \end{cases}$$

$$n \in (0,2)$$

$$\frac{1}{\sqrt{2n}} e^{-\left(\frac{n-\mu}{\sigma}\right)^2} (\frac{1}{2})$$

$$n \in (0,2)$$

$$f_{\times}(m) = \begin{cases} \frac{1}{4\sqrt{2\pi}} & e^{-\left(\frac{\pi}{2}\right)^2} \\ \frac{1}{4\sqrt{2\pi}} & e^{-\left(\frac{\pi}{2}\right)^2} \end{cases}$$

$$= \begin{cases} \frac{1}{4\sqrt{2\pi}} & e^{-\left(\frac{\pi}{2}\right)^2} \\ \frac{1}{4\sqrt{2\pi}} & e^{-\left(\frac{\pi}{2}\right)^2} \end{cases}$$

$$P(1 \le x \le 3) = \left[\frac{1}{2} \left\{ G(\frac{2-0}{2}) - G(\frac{1-0}{2}) \right\} + \frac{1}{2} \left\{ \frac{1}{2} (-1) - 0 \right\} \right]$$

$$+ \left[\frac{1}{2}\left\{\alpha\left(\frac{3-0}{2}\right) - \alpha\left(\frac{2-0}{2}\right)\right\}\right]$$

of 15x53)

$$P(H|X=1) = f(X=1|H) - P(H)$$

$$P(H|X=1) = \frac{\int_{X} (n=1|H) \cdot P(H)}{\int_{X} (n=1)}$$

+4.5

$$\frac{P(N|X=1) = f_{X}(n=1|N).P(N)}{f_{X}(n=1|N).P(N) + f_{X}(n=1|T).P(T)}$$

$$P(H|X=1) = \frac{2!\sqrt{2}}{2!\sqrt{2}}e^{-\left(\frac{1}{2}\right)^2}$$
 Small math error in exponent

$$(\frac{1}{21\sqrt{2n}}e^{-(\frac{1}{2})^2}+e^{-(\frac{1}{2})^2}+(\frac{1}{2})(\frac{1}{2})^2$$

 $y = P_{\times}(n) = \frac{2}{2}$ , x = 1/2, 3, 4/5, 6.

)= P(x=2) + P(x=3) + P(X=4)

and the secretary of the second secon

the same of the sa

p(2 < x < 5) = 2 + 3 + 4

p(25x<5)= 9 21 Am

(b) E(x) = Enpx (m)

 $a \in (x)^{-}$   $F(x)^{-}$   $F(x)^{-}$   $F(x)^{-}$   $F(x)^{-}$   $F(x)^{-}$   $F(x)^{-}$   $F(x)^{-}$   $F(x)^{-}$   $F(x)^{-}$ 

 given an enferench 5 with set of outcomes this

entromes of S,

we define an event E uniquely via what whether outcome n; happened as part of the event on not, for every possible ordinare in so.

Frent E is basically a set of ordinare of so.

For eventle, If the enforcement 5 has a finite remarker of possible ordinare n, m and ng.

we can define 23 events defending on whether a pointicular outcome is purt of the event or net.

The conflete set of events for this hypothebreal enperiment would be:

Eo  $\overline{M_{1}}, \overline{M_{2}}, \overline{N_{3}} = \emptyset$  Ey  $\overline{M_{1}}, \overline{M_{2}}, \overline{N_{3}}$ E1  $\overline{M_{1}}, \overline{M_{2}}, \overline{M_{3}}$  E5  $\overline{M_{1}}, \overline{M_{2}}, \overline{M_{3}}$ E2  $\overline{M_{1}}, \overline{M_{2}}, \overline{M_{3}}$  E4  $\overline{M_{1}}, \overline{M_{2}}, \overline{M_{3}}$ E3  $\overline{M_{1}}, \overline{M_{2}}, \overline{M_{3}}$  E4  $\overline{M_{1}}, \overline{M_{2}}, \overline{M_{3}}$  where a dash on n; outcome indicates that n; is not included in the event.

For the events are labelled For Er, .... Ex.

In other words, an event E is & an element of the power set of & A: P.

where  $P = \{\{\phi\}, \{n\}, \{n_2\}, \{n_3\}, \{n_1, n_2\}, \{n_2, n_3\}, \{n_1, n_3\}, \{n_1, n_2, n_3\}\}$  as pur the perenions enoughle of  $\mathcal{N} = \{\{n_1, n_1, n_3\}\}$ .

+10

Random Vacuales are numerical mappings of the outcomes of an enperiment.

Assingle

Every outcome will be assigned only one Random Vaeriable value, but a pourticulaes Random Varrable value can book be neverse-mapped to multiple outcomes.

eg. 21 in enforment 5 there coirs are indehendentle Lindependently tossed, me can define a andom variable X as the # Meads obtained.

and the second		
	entione	X.
2	TTT	6 0
_	TTV	)
	THT	1
	TNH	2
	# 77	1
	nTh	2
	rith	2
	HHT	3
	иии	