We have considered various derivative free methods: Nelder Mead Simplex Method benetic Algorithms Simulated Annealing Coordinate Search For each of these methods we can employ a simple strategy for enforcing constraints: Extreme Barrier Method. MM f(x)S.t.  $\chi \in \Omega$ min  $\overline{f}(x)$ I(x) is an extended value s.t. XERM function with range RU 3003.

Important Observation If f(x) is convex and bounded below and I is convex then f(x) is convex and bounded below. And, thus a global minimizer of & exists. Suppose fite">R convex and I convex  $f(x) := \begin{cases} f(x) & \text{if } x \in \Omega \subseteq \mathbb{R}^n \\ \infty & \text{otherwise} \end{cases}$ 

Let  $X, y \in \mathbb{R}^n$ ,  $Z = \lambda x + (1-\lambda)y$ ,  $0 \le \lambda \le 1$ .

Consider  $\overline{f}(z) = \overline{f}(xx + (1-x)y)$ . If  $x,y \in Q$  then

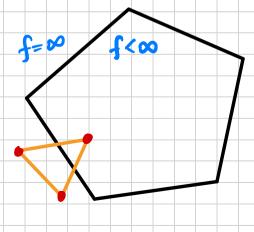
 $\overline{f}(z) = f(z) \leq \lambda f(x) + (1-\lambda)f(y) = \lambda \overline{f}(x) + (1-\lambda)\overline{f}(y)$ 

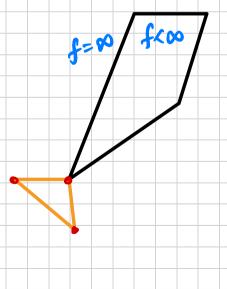
If either X & 2 or y & 2 or both, then

 $f(z) = \infty \leq \lambda f(x) + (1-\lambda)f(y)$ .
Thus  $f: \mathbb{R}^n \to \mathbb{R} \cup \{\infty\}$ 

is convex.

As long as SA, GA, NM start with at least one feasible point then you can expect convergence to a local minimizer. The exact behavior for NM is complicated, depending on the nature of the constraints and the choice of initial simplex.





Filter Methods (We will not employ filter methods this semester mess we have lots of time) Then, for various methods we Consider the problem can track and Utilize pareto min f(x) optimal points relative to f and h. S.t.  $C_1(x) = 0$ n(x)  $C_2(x) \geq 0$ hmax T XERM And define the constraint violation function current best f(x) $h(x) = |C_1(x)| - \min \{0, C_2(x)\}$ feasible point. region of improved points

