

1.

Classical model of for the Kundur 12 bus system utilizes the same reduced Y_{bus} matrix : Y_{gen} for the power flow equations.
(Refer to Hw A04 for its computation).

$$\dot{\theta}_i = (\omega_i - 1) \omega_s \quad i = 2 \text{ to } N_{pv} + 1$$

3×1

$$\dot{\omega}_i = \frac{1}{2H_i} \left[\begin{array}{c} P_{m_i} - \sum_{k=1}^{N_{pv}+1} Y_{genik} E'_{qk} E'_i \cos(\gamma_{ik} + \theta_k - \theta_i) \\ -K_{D_i} (\omega_i - 1) \end{array} \right]$$

3×2 $i = 2 \text{ to } N_{pv} + 1$

Assumptions:

- Angle dynamics are much faster than Voltage dynamics.
- Machine internal voltages $\sqrt{E'_{qi}{}^2 + E'_{di}{}^2} = E'_i$ are assumed constant. They are obtained either by initialization or simply given in the system

E'_{qi}, E'_{di} around slow variables.

\downarrow
 $E'_{qi} \rightarrow c$
 $E'_{di} \rightarrow c$
 $\Rightarrow E' \rightarrow c$

- $E'_{qi} \gg E'_{di} \Rightarrow \gamma \approx \frac{\pi}{2}$
and $\cancel{E'_{di} \cos(\theta - \frac{\pi}{2}) = E'_{di}}$

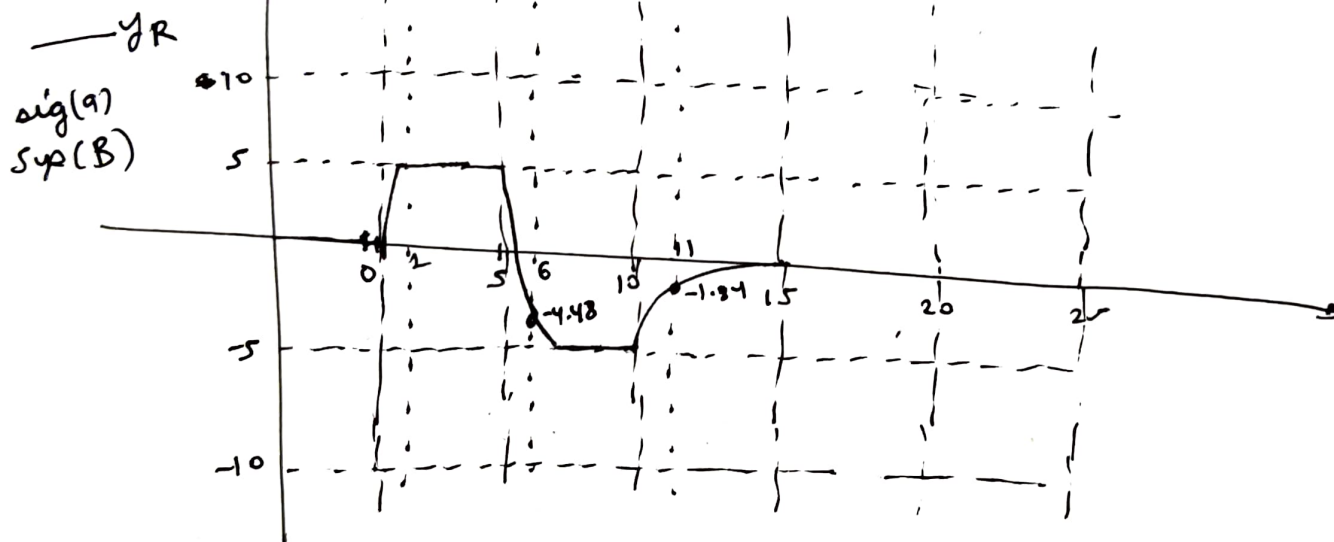
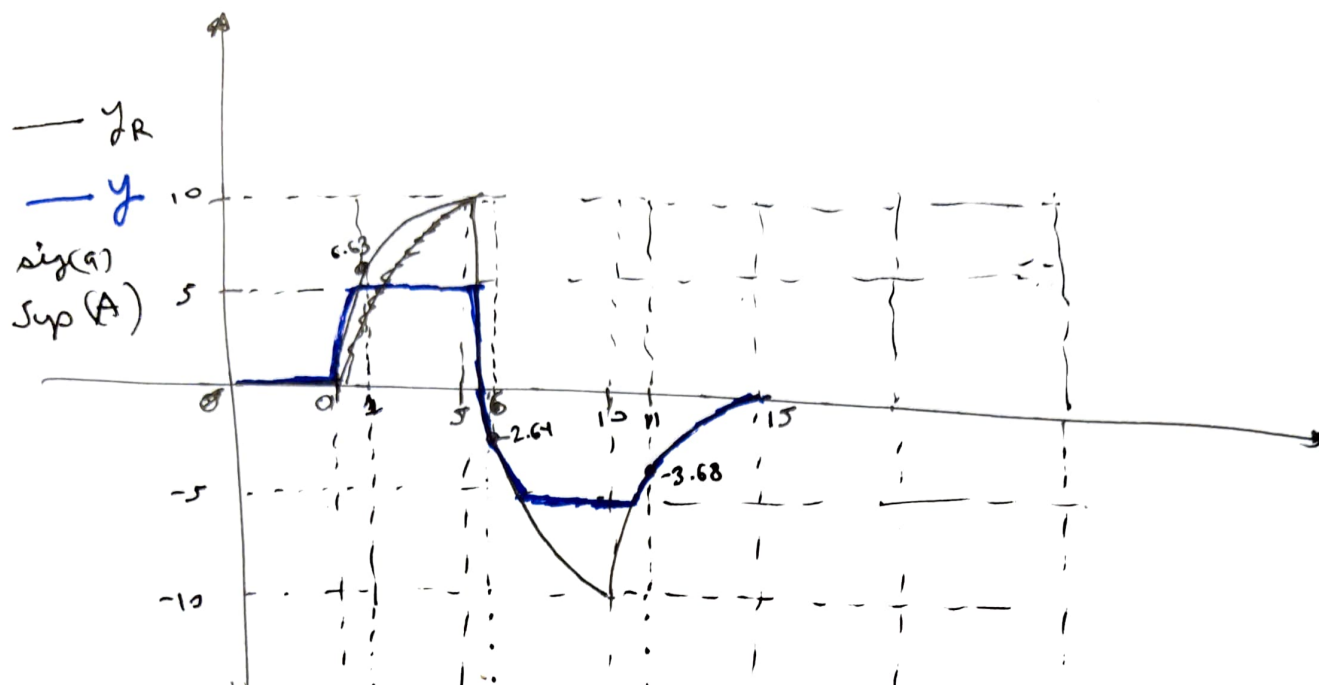
$$\therefore (E_{di} + jE_{qi}) \angle (\theta_i - \frac{\pi}{2}) = E'_i \angle \gamma_i$$

$$\& E'_i \angle \frac{\pi}{2} \angle \theta_i - \frac{\pi}{2} = E'_i \angle \gamma_i$$

$$\alpha \quad \theta_i \approx \gamma_i$$

So we can use θ_i instead of γ_i as we did was the case in Type 2.

2.1



R.W.

$u(t) = K + u(t)$
 $y(t) = K(t - 1 + e^{-t})$
 $u(t)$
 $K = K_1 K_2$
 $H(s) = \frac{K_2}{1+s}$

$K = K_1 K_2 = 0.2 \times 10$
 $\rightarrow K = 2$

$x(t) = -0.2t$

$-2(5 - 1 - e^{-5})$

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$2(t - 1 + e^{-t}) = 5$
 $t - 1 = \frac{5}{2}$
 $t = 3.5$

$-2(t)$

$-2(t - 1)$
 $-2(5) = -10$
 -10

$-2(t - 1) = -10$
 $t - 1 = 5$
 $t = 6$

$-2(t - 1) = -18$
 $t - 1 = 9$
 $t = 10$

$2(t - 1)$
 $2(4)$

