## EE 507, Homework $2\pi + 1$

dre November 9

## Problem 8

A random variable Y has the PDF shown below:

tr(ax)

- a. Please find the meximum probability estimate for Y.
- b. Please find the MMSE estimate for Y.
- c. Please find the \_\_\_ mean absolute estimate for Y.

## Problem 💡

A random variable X is uniform on [0,1]. Given X=x, the random variable Y is exponential with mean  $x^2$ .

- a. Please find the MMSE estimate for Y given X = x. What is the expected error of the estimate, given X = x? What is the (overall) average estimation error?
- b. Please find the MMSE estimate for  $Y^2$  given X = x. Conceptually, why isn't this estimate just the square of the MMSE estimate of Y given X = x?
- c. Please find the MMSE estimate of X given Y = y. What is the (overall) average estimation error?
- d. What is the LMMSE estimate for Y given X = x?

# EE 507, Homework 9 due December 4, 2015

#### Problem 10

- a. What is a random process?
- b. Why are random processes of interest to scientists and engineers?
- c. Find a signal in the world around you that can be viewed as a random process. Actually measure a sample trajectory of this process.
- d. When we defined random processes, we associated entire signals with outcomes of an experiment rather than using a different experiments to define the process values at particular times. What is the advantage of this approach?

#### Problem 12

An uncertain experiment has two equally likely outcomes, A and B. A random process  $X(\omega,t)$ ,  $t \in R$ , is defined for this experiment as follows: X(A,t) = cos(t) and X(B,t) = sin(t).

- a. Please find the first-order PDF for X(t).
- b. Please find the second-order PDF for X(t).
- c. Please find the *n*th-order PDF for X(t). (Assume WLOG that the times in the joint PDF are increasing, i.e.  $t_1 < t_2 < \ldots < t_n$ ).
- d. Please find E[X(t)] and  $R_{XX}(t_1, t_2)$ .

## Problem 32

Consider a discrete-time random process X[k], k = 0, 1, 2, ..., where each X[k] is an independent random variable that equals 0 with probability 0.6 amd equals 1 with probability 0.4.

a. Please find the nth-order PMF for X[k]. (Assume without loss of generality that that the times in the joint PMF are increasing.)

b. Please find E[X(t)],  $R_{XX}(t,\tau)$ , and  $C_{XX}(t,\tau)$ .

Now consider the process  $Y[k] = \sum_{i=0}^{k-1} X[k], k = 1, 2, 3, \dots$ 

- c. Please find the first-order PMF for Y[k].
- d. Please find the *n*th-order PMF for Y[k]. (Assume without loss of generality that the times in the joint PMF are increasing.)
- e. Please find E[Y(t)],  $R_{YY}(t,\tau)$ , and  $C_{YY}(t,\tau)$ .
- f. Please find  $R_{XY}(t,\tau)$ .

## Problem 43

Let T be an exponential random variable with mean 1. We define a random process X(t),  $t \in \mathbb{R}^+$ , as follows: X(t) = 1 for  $t \leq T$  and X(t) = 0 for  $t \geq T$ . Please find the second-order joint PDF of X(t).