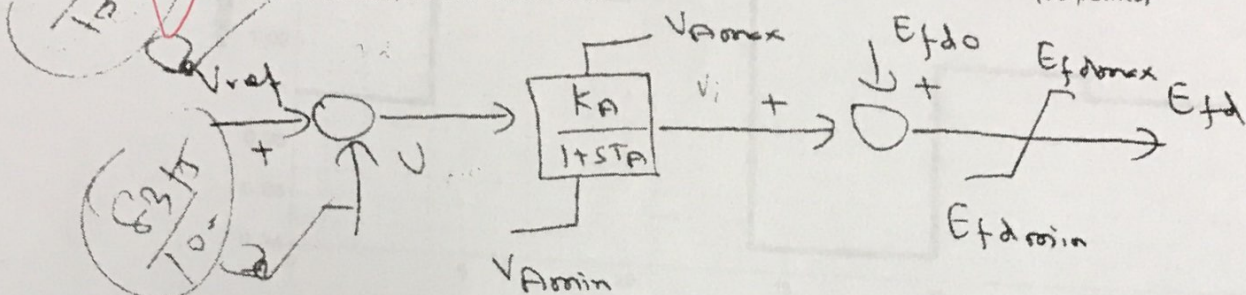


Hamid H. Alkhalifa

EE581 Power System Stability and Control

Midterm Examination

- 1) Consider the exciter model below. Exciter response from a step response test is shown in the plot below. Assume  $V_{ref}=1.03$ . Estimate the exciter parameters  $K_A$ ,  $T_A$ ,  $E_{fd0}$ , and  $V_{Amin}$ ,  $V_{Amax}$ ,  $E_{fdmin}$  and  $E_{fdmax}$ . (30 points)



$$20 < t < 25 \quad 4 + E_{fd0} - K_A \times 0.03 = 0$$

$$E_{fdss} = E_{fd0} + K_A (V_{ref} - V)$$

$$\Rightarrow E_{fd0} + K_A \times 0 = 0 \Rightarrow E_{fd0} = 0$$

$$25 < t < 30 \Rightarrow E_{fd0} + K_A \times 0.01 = 1 \Rightarrow K_A = \frac{1}{0.01} = 100$$

Zero

$$4 < t < 10 \Rightarrow T_A = 1$$

the time that needs to reach 63% of final value

$$V_{Amax} = 4$$

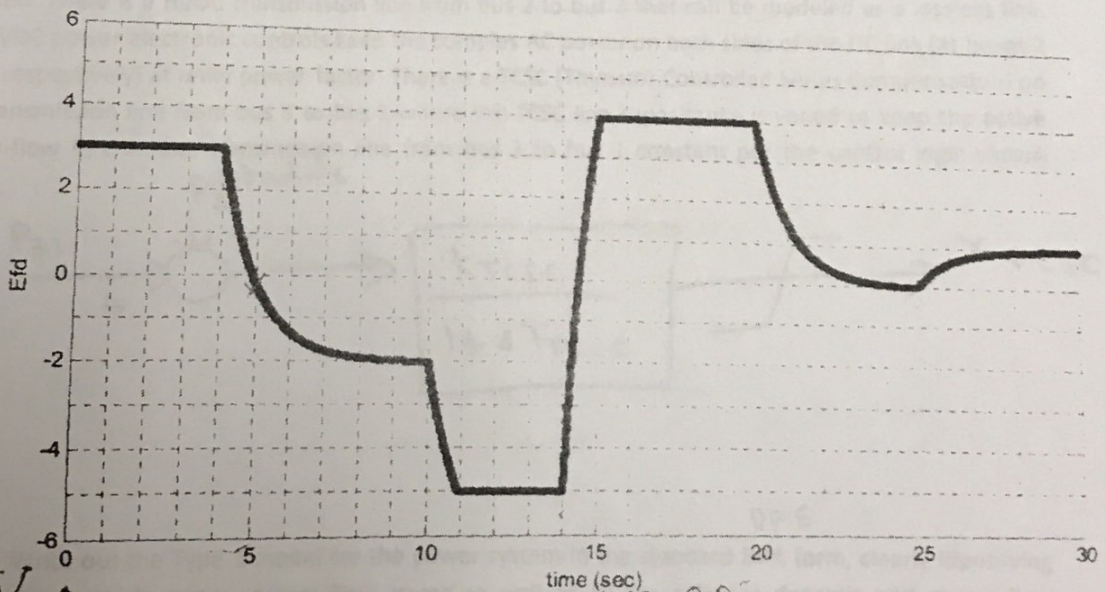
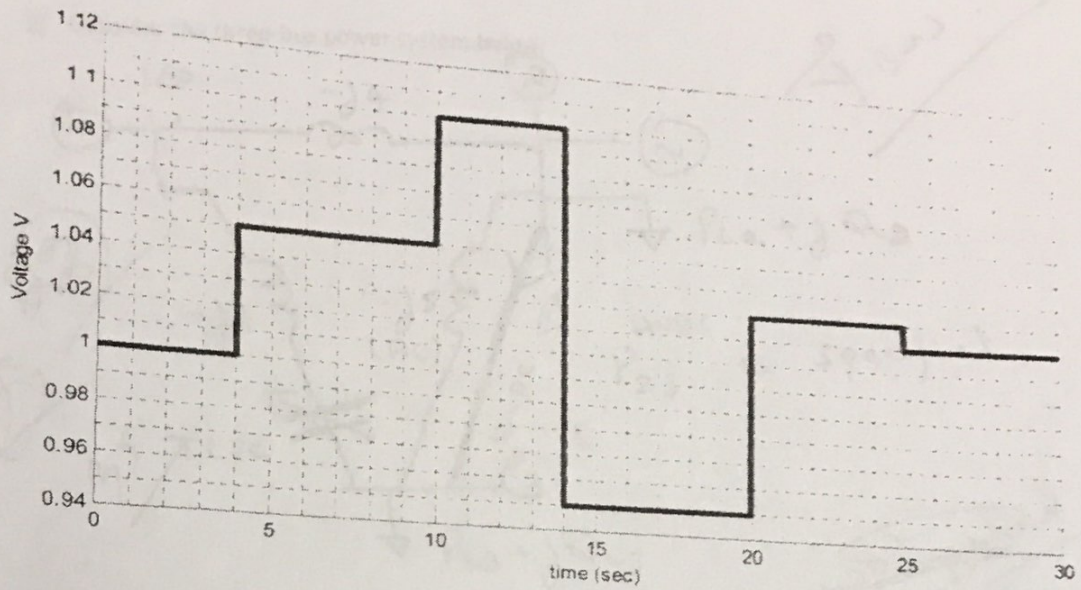
$$V_{Amin} = -5$$

$$E_{fdmax} = 4$$

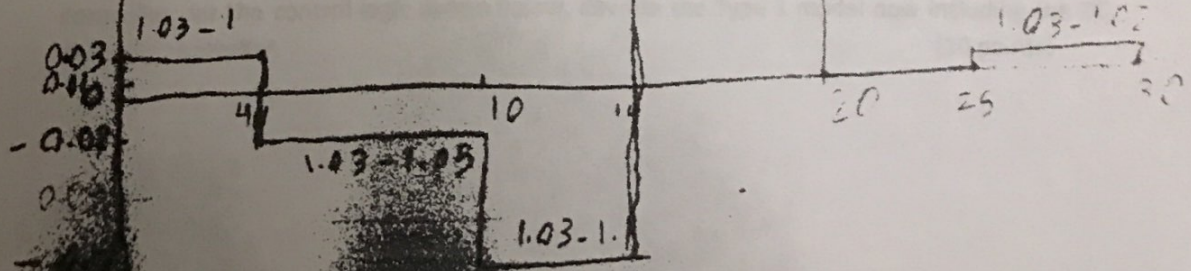
$$E_{fdmin} = -5$$



Qualitativa in (5.0) (4)

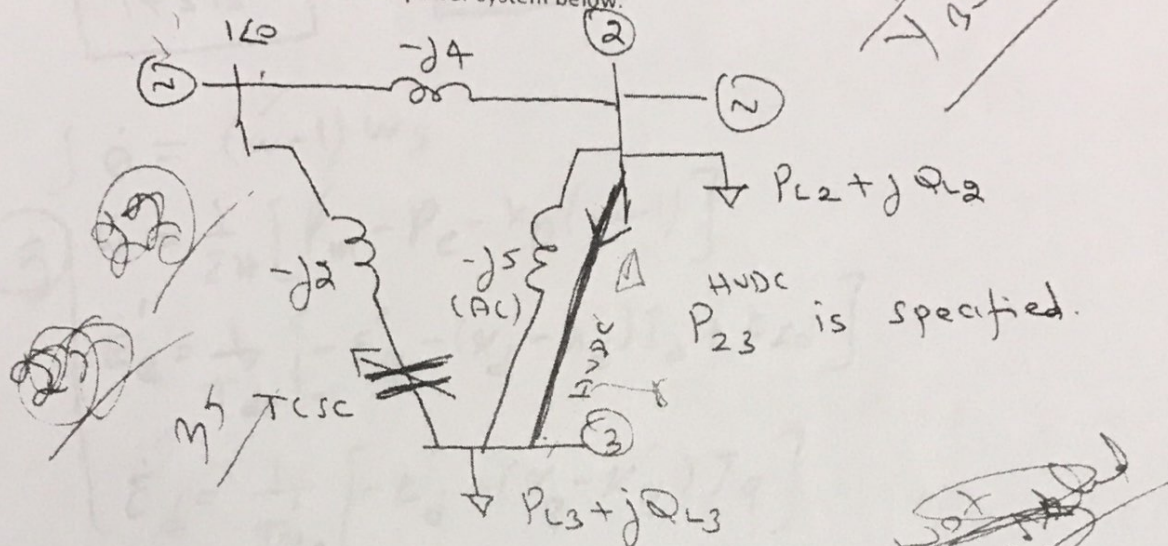


$V_{ref} - V$   
0.02

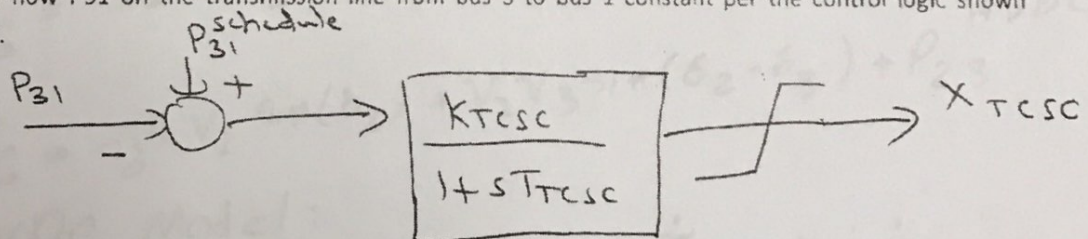




2) Consider the three-bus power system below.



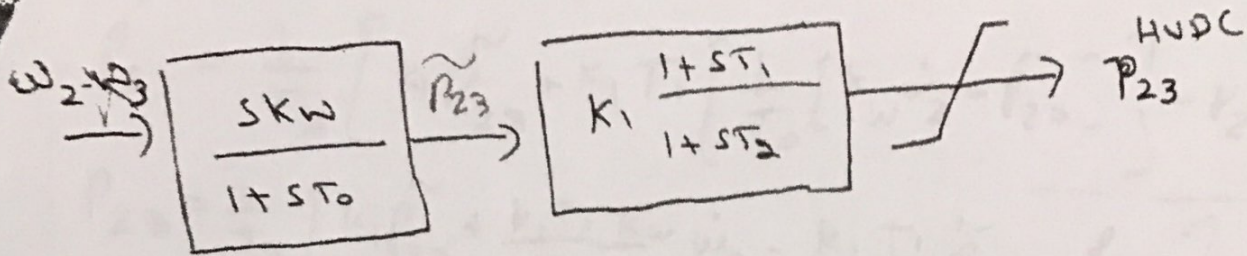
Assume the generator is modeled by a standard first order exciter control with no governor control modeled. There is a HVDC transmission line from bus-2 to bus-3 that can be modeled as a lossless link. The HVDC power electronic controls keep the complex AC power on both sides of the DC link (at buses 2 and 3 respectively) at unity power-factor. There is a TCSC (Thyristor Controlled Series Compensation) on the transmission line from bus 3 to bus 1 where the TCSC line capacitance is varied to keep the active power-flow  $P_{31}$  on the transmission line from bus 3 to bus 1 constant per the control logic shown below.



DPE

- Write out the Type 1 model for the power system in the standard DAE form, clearly identifying the dynamic states, power-flow states as well as all the relevant dynamic and power-flow equations. (40 points)
- Suppose the utility decides to vary 10% of the DC power transfer from bus 2 to 3 as a damping controller per the control logic shown below. Rewrite the Type 1 model now including the DC damping controller. (10 points)





$$\begin{cases} \dot{\theta} = (\tilde{\omega} - 1) \omega_s \\ \textcircled{5} \quad \tilde{\omega} = \frac{1}{2H} [\tilde{P}_m - P_e - k_D(\tilde{\omega} - 1)] \\ \dot{E}'_q = \frac{1}{T_{do}} [-E'_q - (x_d - x'_d)I_d + E_{zd}] \\ \dot{E}'_d = \frac{1}{T_{dq}} [-E'_d + (x_q - x'_q)I_q] \end{cases}$$

$$\underline{P_e = P_G + R_s I_C^2} \quad \rightarrow P_{G \text{ and } I_C}$$

$$P_G = V_2 V_1 Y_{21} \sin(\delta_2 - \delta_1) + V_2 V_3 \sin(\delta_2 - \delta_3) + P_{23}^{HVDC}$$

$$P_G = -j4 V_2 \sin(\delta_2) + V_2 V_3 \sin(\delta_2 - \delta_3) + P_{23}^{HVDC}$$

HVDC Model:

$$\tilde{P}_{23} = \frac{SK_w}{1+sT_0} \omega_2 \Rightarrow \tilde{P}_{23} + T_0 \dot{\tilde{P}}_{23} = K_w \dot{\omega}_2$$

$$T_0 \dot{\tilde{P}}_{23} = K_w \dot{\omega}_2 - \tilde{P}_{23}$$

$$\textcircled{3} \quad \dot{\tilde{P}}_{23} = \frac{1}{T_0} [K_w \dot{\omega}_2 - \tilde{P}_{23}]$$

$$P_{23} = K_1 \frac{1+sT_1}{1+sT_2} \tilde{P}_{23} \Rightarrow P_{23} + T_2 \dot{P}_{23} = K_1 \tilde{P}_{23} + K_1 T_1 \dot{\tilde{P}}_{23}$$

$$\Rightarrow T_2 \dot{P}_{23} = K_1 \tilde{P}_{23} + K_1 T_1 \dot{\tilde{P}}_{23} - P_{23} \Rightarrow \dot{P}_{23} = \frac{1}{T_2} [K_1 \tilde{P}_{23} + K_1 T_1 \dot{\tilde{P}}_{23} - P_{23}]$$



$$\dot{P}_{23} = \frac{1}{T_2} \left[ k_1 \tilde{P}_{23} + k_1 T_1 \left[ \frac{1}{T_0} [k_w \dot{w}_2 - \tilde{P}_{23}] \right] - P_{23} \right]$$

$$\dot{P}_{23} = \frac{1}{T_2} \left[ k_1 \tilde{P}_{23} + \frac{k_1 T_1 k_w}{T_0} \dot{w}_2 - \frac{k_1 T_1}{T_0} \tilde{P}_{23} - P_{23} \right] \quad (4)$$

$$E'_d = V_d + R_a I_d - x'_d I_q$$

$$E'_q = V_q + R_a I_q + x'_d I_d$$

$$E'_d - V_d = R_a I_d - x'_d I_q$$

$$E'_q - V_q = R_a I_q + x'_d I_d$$

$$\Rightarrow \begin{bmatrix} E'_d - V_d \\ E'_q - V_q \end{bmatrix} = \begin{bmatrix} R_a & -x'_d \\ x'_d & R_a \end{bmatrix} \begin{bmatrix} I_d \\ I_q \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} I_d \\ I_q \end{bmatrix} = \frac{1}{R_a^2 + x_d'^2} \begin{bmatrix} R_a & x'_q \\ -x'_d & R_a \end{bmatrix} \begin{bmatrix} E'_d - V_d \\ E'_q - V_q \end{bmatrix}$$

$$\begin{bmatrix} I_d \\ I_q \end{bmatrix} = \begin{bmatrix} \frac{R_a}{R_a^2 + x_d'^2} & \frac{x'_q}{R_a^2 + x_d'^2} \\ \frac{-x'_d}{R_a^2 + x_d'^2} & \frac{R_a}{R_a^2 + x_d'^2} \end{bmatrix} \begin{bmatrix} E'_d - V_d \\ E'_q - V_q \end{bmatrix}$$

$Y_{21}$ 
 $Y_{11}$ 
 $Y_{12}$ 
 $Y_{22}$

$$\Rightarrow \begin{cases} I_d = Y_{11} (E'_d - V_d) + Y_{12} (E'_q - V_q) \\ I_q = Y_{21} (E'_d - V_d) + Y_{22} (E'_q - V_q) \end{cases}$$



# TCSC: Model

$$(P_{31}^{\text{schedule}} - P_{31}) \frac{K_{TCSC}}{1 + sT_{TCSC}} = X_{TCSC}$$

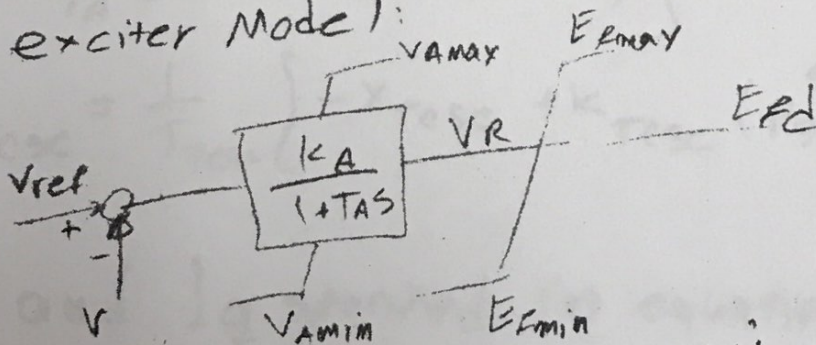
$$\Rightarrow (P_{31}^{\text{schedule}} - P_{31}) K_{TCSC} = X_{TCSC} (1 + sT_{TCSC})$$

$$\frac{X_{TCSC}}{T_{TCSC}} = -X_{TCSC} + K_{TCSC} (P_{31}^{\text{schedule}} - P_{31})$$

$$P_{31} = V_3 V_1 (1 - j2) \sin(\delta_3 - \delta_1) = -j2 V_3 \sin(\delta_3)$$

$$\Rightarrow X_{TCSC} = \frac{1}{T_{TCSC}} \left[ -X_{TCSC} + K_{TCSC} (P_{31}^{\text{schedule}} + j2 V_3 \sin(\delta_3)) \right]$$

exciter Model:



$$K_A (V_{ref} - V) = (1 + sT_{AS}) V_R \Rightarrow T_A \dot{V}_R = -V_R + K_A (V_{ref} - V)$$

$$\dot{V}_R = \frac{1}{T_A} [-V_R + K_A (V_{ref} - V)]$$

$$\dot{V}_R = \begin{cases} 0 & V_R = V_{max} \\ 0 & V_R = V_{min} \\ \dot{V}_{Rdot} & V_{min} < V_R < V_{max} \end{cases} \quad E_{fd} = \begin{cases} E_{max} & V_R = V_{max} \\ E_{min} & V_R = V_{min} \\ V_R & V_{min} < V_R < V_{max} \end{cases}$$



a) In the first case without HVDC damping controllers state of the system are:  $\theta, \omega, E_q', E_d', V_R, X_{TSC}$  and

y variables are  $V_2, \delta_2, V_3, \delta_3$

The state equations will be:

$$\begin{cases} \dot{\theta} = (\omega - 1)/\omega_s \\ \dot{\omega} = \frac{1}{2H} \left[ P_m - \left[ (-j4V_2 \sin(\delta_2) + V_2 V_3 \sin(\delta_2 - \delta_3) + P_{23}) + P_s(I_q^2 + I_d^2) \right] - K_D(\omega - 1) \right] \\ \dot{E}_q' = \frac{1}{T_{d0}} \left[ -E_q' - (x_d - x_d')I_d + E_{fd} \right] \\ \dot{E}_d' = \frac{1}{T_{q0}} \left[ -E_d' + (x_q - x_q')I_q \right] \\ \dot{V}_R = \frac{1}{T_A} \left[ -V_R + K_A(V_{ref} - V) \right] \\ \dot{X}_{TSC} = \frac{1}{T_{TSC}} \left[ -X_{TSC} + K_{TSC} (P_{31}^{exhale} + j2V_3 \sin(\delta_3)) \right] \end{cases}$$

$I_d$  and  $I_q$  specified in equation 1 based on

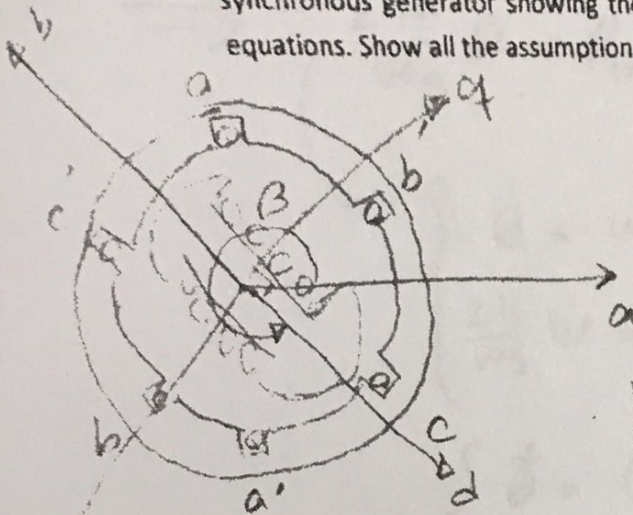
$x$  and  $y$  in this equations  $V_d = V \cos(\theta - \delta)$   
 $V_q = V \sin(\theta - \delta)$







- 3) Derive the standard swing equations that describe the electromechanical angle dynamics of the generator starting from Newton's equations. Draw a cross-section of a typical synchronous generator showing the windings and define the angles involved in the swing equations. Show all the assumptions and definitions needed in deriving the swing equations. (20 points)



Define

$\beta = \omega_s t + \theta - \frac{\pi}{2}$

$\omega_s = \omega - \omega_s$

$$J \ddot{\beta} = T_m - T_e - T_D$$

$$\beta = \omega_s t + \theta - \frac{\pi}{2}$$

$$\dot{\beta} = \omega_s + \dot{\theta} \Rightarrow \ddot{\theta} = \omega - \omega_s$$

$$\ddot{\beta} = \ddot{\theta}$$

$$J \ddot{\theta} = T_m - T_e - T_D$$

$$J \ddot{\theta} \omega_s = T_m \omega_s - T_e \omega_s - T_D \omega_s$$

$$J \ddot{\theta} \omega_s = P_m - P_e - P_D$$

$$\frac{J \ddot{\theta} \omega_s}{s_{rating}} = \frac{P_m}{s_{rating}} - \frac{P_e}{s_{rating}} - \frac{P_D}{s_{rating}}$$

We define  $H = \frac{\text{Energy in rotor}}{s_{rating}} = \frac{\frac{1}{2} J \omega_s^2}{s_{rating}}$

$$\Rightarrow \frac{J \ddot{\theta} \omega_s}{s_{rating}} = \frac{2H}{\omega_s} \ddot{\theta}$$

$$\Rightarrow \frac{2H}{\omega_s} \ddot{\theta} = P_m(pu) - P_e(pu) - P_D(pu)$$

$$P_D = K_D (\omega - \omega_s)$$



$$\Rightarrow \frac{2H}{\omega_s} \ddot{\theta} = P_m(pu) - P_e(pu) - k_D(\omega - \omega_s)$$

$$\begin{cases} \dot{\theta} = \omega - \omega_s \\ \frac{2H}{\omega_s} \dot{\omega} = P_m(pu) - P_e(pu) - k_D(\omega - \omega_s) \end{cases}$$

$$\begin{cases} \dot{\tilde{\theta}} = (\tilde{\omega} - 1)\omega_s \\ 2H\tilde{\omega} = P_m(pu) - P_e(pu) - \underbrace{k_D \omega_s}_{\tilde{k}_D}(\tilde{\omega} - 1) \end{cases}$$

$$\begin{cases} \dot{\tilde{\theta}} = (\tilde{\omega} - 1)\omega_s \\ 2H\tilde{\omega} = P_m(pu) - P_e(pu) - \tilde{k}_D(\tilde{\omega} - 1) \end{cases}$$