1   **A Parametric Framework to Generate Visual Illusions using Python**

2   Dominique Makowski[1,*], Zen J. Lau[1], Tam Pham[1], Paul Boyce[2], & S.H. Annabel

3   Chen[1, 3, 4]

4   [1] School of Social Sciences, Nanyang Technological University, Singapore

5   [2] School of Psychology, University of New South Wales, Australia

6   [3] Centre for Research and Development in Learning, Nanyang Technological University,

7   Singapore

8   [4] Lee Kong Chian School of Medicine, Nanyang Technological University, Singapore

9   Author Note

10   Correspondence concerning this article should be addressed to Dominique Makowski,

11   HSS 04-18, 48 Nanyang Avenue, Singapore. E-mail: dmakowski@ntu.edu.sg

12   Abstract

13   Visual illusions are fascinating phenomena that have been used and studied by artists and

14 scientists for centuries, leading to important discoveries about the neurocognitive

15 underpinnings of perception, consciousness, and neuropsychiatric disorders such as

16 schizophrenia or autism. Surprisingly, despite their historical and theoretical importance

17 as psychological stimuli, there is no dedicated software, nor consistent approach, to

18 generate illusions in a systemic fashion. Instead, scientists have to craft them by hand in

19 an idiosyncratic fashion, or use pre-made images not tailored for the specific needs of their

20 studies. This, in turn, hinders the reproducibility of illusion-based research, narrowing

21 possibilities for scientific breakthroughs and their applications. With the aim of addressing

22 this gap, *Pyllusion* is a Python-based open-source software (freely available at

23 https://github.com/RealityBending/Pyllusion), that offers a framework to manipulate and

24 generate illusions in a systematic way, compatible with different output formats such as

25 image files (.png, .jpg, .tiff, etc.) or experimental software (such as *PsychoPy*).

26   *Keywords:* Pyllusion, Visual Illusions, Optical Illusions, Schizophrenia, Python,

27 PsychoPy

28   Word count: 3527

A Parametric Framework to Generate Visual Illusions using Python

Visual illusions have been observed for hundreds of years (Luckiesh, 1965), many of which were described in print by Helmholtz (1856) in 1856 (Helmholtz, 1856). In general terms, a visual illusion can be thought of as the inaccurate perception of a visual stimulus or a given attribute, be it geometrical (size, shape, or angle), or another property such as colour (Adelson, 2000; Delboeuf, 1893; Ebbinghaus, 1902; Howe & Purves, 2005; Muller-Lyer, 1896; Roberts, Harris, & Yates, 2005). Often, an illusory perception resists 'correction' in perception even after an observer has been made aware of the misperception. Novel examples of illusions are still observed and have even cropped up on social media platforms, a famous example being 'The Dress Illusion' (as discussed by Schlaffke et al. (2015)), which some people perceive as white and yellow, whereas others as black and blue - this is thought to illustrate how perceptual priors (i.e., expectations regarding lighting conditions) can bias our conscious representation of an object. See Ninio (2014), Luckiesh (1965), and Robinson (1972) for extensive collections of visual illusions. Overall, these illusions show how our phenomenological experience is critically shaped by contextual information and prior expectations.

Entertainment value aside, illusions can serve a more practical utility. Visual illusions have helped scientists understand the architecture of the eye and its relationship with processes and structures involved further up stream in the brain, the dynamic interaction of these processes, and visual coding in the brain in general (Carbon, 2014; Clifford, 2002; Forte & Clifford, 2005). Illusions such as the blind-spot or those associated with colour perception, orientation perception, and motion perception, have all been informative of neuronal activity/processes both at the level of the eye and the brain via the measurement of associated illusions (Curran, Clifford, & Benton, 2009; Durgin, Tripathy, & Levi, 1995; Holland, 1965; MacKay, 1957; Webster, 1996; Witkin & Asch, 1948). Visual illusions, and perceptual illusions more generally, are a powerful tool in human perception and brain research,

55 which in turn can inform artificial cognitive systems design considerations (Boyce, Lindsay,

56 Zgonnikov, Rano, & Wong-Lin, 2020; Carbon, 2014).

57 The use of visual illusions to demonstrate contextual influences on visual perception (Chen,

58 Chen, Gao, Yang, & Yan, 2015; Corbett & Enns, 2006; Roberts, Harris, & Yates, 2005) has

59 underlined their potential relevance in clinical contexts, for instance as markers or tools to

60 investigate typical integration processes in schizophrenia (Clifford, 2014; Palmer, Caruana,

61 Clifford, & Seymour, 2018; Thakkar et al., 2020). Indeed, several studies have demon-

62 strated a diminished susceptibility to visual illusions amongst patients with schizophrenia

63 relative to healthy controls (King, Hodgekins, Chouinard, Chouinard, & Sperandio, 2017;

64 Notredame, Pins, Deneve, & Jardri, 2014). People with schizotypal personality traits per-

65 form significantly better at making accurate judgements of contrasts under contextual sup-

66 pression (Dakin, Carlin, & Hemsley, 2005), are less prone to the perception of illusory motion

67 (Crawford et al., 2010), and are less susceptible to visual size illusions (Uhlhaas, Silverstein,

68 Phillips, & Lovell, 2004). While individuals along the schizophreniform spectrum display

69 apparent resistance to perceptual distortions, they concurrently experience a wide range of

70 cognitive deficits (e.g., working memory, object naming, concentration; Liddle, 1987). This

71 supports the idea that schizophrenia might be better characterized by a subset of specific

72 processing abnormalities, rather than by a generalized neurocognitive impairment (Dakin,

73 Carlin, & Hemsley, 2005; Tibber et al., 2013). Specific perceptual anomalies in schizophre-

74 nia have also been highlighted using different classes of visual illusions that tap on distinct

75 neurocognitive processes. For example, while patients with schizophrenia show a heightened

76 resistance to contrast illusions, they are indistinguishable from healthy controls in judging

77 brightness illusions (Tibber et al., 2013), arguing against a broad deficit in low-level percep-

78 tual integration since not all illusions are affected. In fact, other studies have emphasized the

79 role of high-level perceptual deficits in schizophrenia (e.g., problems in contextual processing

80 that manifest as greater resistance to the Ebbinghaus illusion; Massaro & Anderson, 1971;

81 Uhlhaas, Phillips, Schenkel, & Silverstein, 2006). However, the lack of consistency in the

tasks' methodologies has posed a significant challenge to advancing our theoretical under-
standing of the role of visual perception and reality construction in the psychopathology of
schizophrenia (King, Hodgekins, Chouinard, Chouinard, & Sperandio, 2017). Specifically,
the finding of an increased perceptual accuracy towards high-level illusions has failed to
replicate in several other studies (e.g., Parnas et al., 2001; Spencer & Ghorashi, 2014; Yang
et al., 2013), and other kinds of illusions (e.g., the Poggendorff illusion) have simply not been
sufficiently tested (Kantrowitz, Butler, Schecter, Silipo, & Javitt, 2009).

Individuals with autistic spectrum disorder (ASD) comprise another clinical group that
demonstrates a similar immunity to perceptual biases, supporting the existence of difficulties
in global processing and, conversely, an enhanced preference for idiosyncratic and detailed
information (F. G. Happe, 1996). Hence, individuals with ASD appear as protected as the
clinical schizophrenia population against the contextual influences of illusions in biasing per-
ception, allowing them to perceive elements accurately in a local fashion (Gori, Molteni, &
Facoetti, 2016; referred to as a 'weak central coherence'; Mitchell, Mottron, Soulieres, &
Ropar, 2010; Walter, Dassonville, & Bochsler, 2009). Some work has also been successful in
delineating the underlying cognitive mechanisms employed by different illusions, revealing
that autistic traits in a typical population were related to greater resistance to the Müller-
Lyer illusion, but not the Ebbinghaus or Ponzo illusions (Chouinard, Noulty, Sperandio, &
Landry, 2013). One possible explanation for this dissociation relates to the extent of global
processing engaged by the illusions, with the Müller-Lyer illusion (a within-object illusion
where contextual elements and the target stimulus are physically joined) requiring more
cognitive resources for the local binding of features than the Ebbinghaus and Ponzo illusions
(a between-object illusion where contextual elements and the target stimulus are physically
separate) (Ben-Shalom & Ganel, 2012). Regardless, findings of illusion resistance amongst
ASD face similar low replicability rates as with the literature on schizophrenia, even when
the same illusion tasks are used (Hoy, Hatton, & Hare, 2004; Ropar & Mitchell, 1999). These
mixed findings are attributed not only to the heterogenous nature of ASD as a clinical pop-

ulation, but also to the large variability in experimental instructions (e.g., asking whether lines: "looked the same length"; vs. "were the same length," see F. Happe and Frith (2006)) and the subsequent understanding of the task requirements (Chouinard, Noulty, Sperandio, & Landry, 2013).

In summary, these studies suggest that illusions, rather than being mere perceptual artifacts, engage specific neurocognitive processes involved in important higher order functions and neuropsychiatric disorders. A common approach to explain illusory phenomena is using the Predictive Coding framework (Friston & Kiebel, 2009), which posits that illusory perception typically arises because of a strong systematic bias for prior beliefs (top-down influence) that are mismatched with actual sensory evidence, causing the generation of an objectively wrong but more plausible percept (i.e., two objectively equivalent-sized circles being inter-preted as different sizes because of their surrounding context) (Notredame, Pins, Deneve, & Jardri, 2014). In the case of schizophrenia and also in other states of psychosis, a greater resistance to visual illusions is then interpreted as a product of reduced adaptive top-down influence (Koethe et al., 2009; Schneider et al., 2002) and an over-reliance on sensory evidence (bottom-up processes) in making perceptual judgements (Dima, Dietrich, Dillo, & Emrich, 2010). While evidence from visual illusions research has garnered substantial support for the predictive coding account, helping to underscore the neurocomputational mechanisms that are fundamental to psychiatric and psychological disorders (Sterzer et al., 2018), there are contradictory findings that fail to be integrated within this approach. The lack of consis-tency and replicability in experimental designs using illusion-based stimuli appear to be one of the main hurdles precluding theoretical consensus in the field.

Despite the relevance of visual illusions in psychology and neuroscience, the field of illusion research lacks a dedicated software to generate and report the stimuli, in order for them to be reproduced and re-used by other researchers and studies. As several reviews have highlighted (e.g., Gori, Molteni, & Facoetti, 2016), the lack of a validated paradigm and the improper measurement of visual illusion sensitivity (especially amongst individuals with communica-

136 tion problems) may be preventing progress in understanding the distinct mechanisms that

137 underlie psychopathology and other fields alike. This is particularly problematic in the con-

138 text of the replicability and reproducibility issues recently outlined in psychological science

139 (Maizey & Tzavella, 2019; Milkowski, Hensel, & Hohol, 2018; Nosek, Cohoon, Kidwell, &

140 Spies, 2015; Topalidou, Leblois, Boraud, & Rougier, 2015). Our software, *Pyllusion*, aims

141 at addressing this gap by proposing and implementing a parametric framework for illusions

142 generation.

A Parametric Framework for Illusion Research

144 The core idea of the "parametric" approach proposed here and implemented in *Pyllusion* is

145 to dissociate the parameters of an illusion from its rendered output. For instance, the Ponzo

146 illusion (see **Fig. 1**) can be described in terms of properties of the "distractor" lines (which

147 induce the illusion), such as the angle (related to the illusion strength), the color, width,

148 etc. and properties of the "target" lines (which are affected in perception by the illusion),

149 such as the size of the smallest line, the objective difference of the ratio of their lengths, or

150 their color, width, etc. This set of parameters can then be rendered in different formats with

151 further format-specific characteristics (in the case of images, the image size, ratio, resolution,

152 compression, etc.).

153 This essentially allows researchers to describe, manipulate, process and share their stimuli in

154 a concise yet consistent way. For instance, researchers could report a *"linear modulation of*

155 *the illusion strength between -15 and 15, resulting in a reduced reaction time of..."*, providing

156 details about the remaining parameters, as well as the Python code used to fully reproduce

157 their stimuli.

158 Moreover, this parametric approach is scalable and works well with different kinds of illusions,

159 as demonstrated in the software. Indeed, many visual illusions (especially the classical ones)

160 appear to have relatively similar parameters (such as a feature - like the angle or the size of

Parameters   **Render**

- Illusion strength = -15
- Objective difference = 0.3
- Size of the smallest rod = 0.5
- Color of the target = red
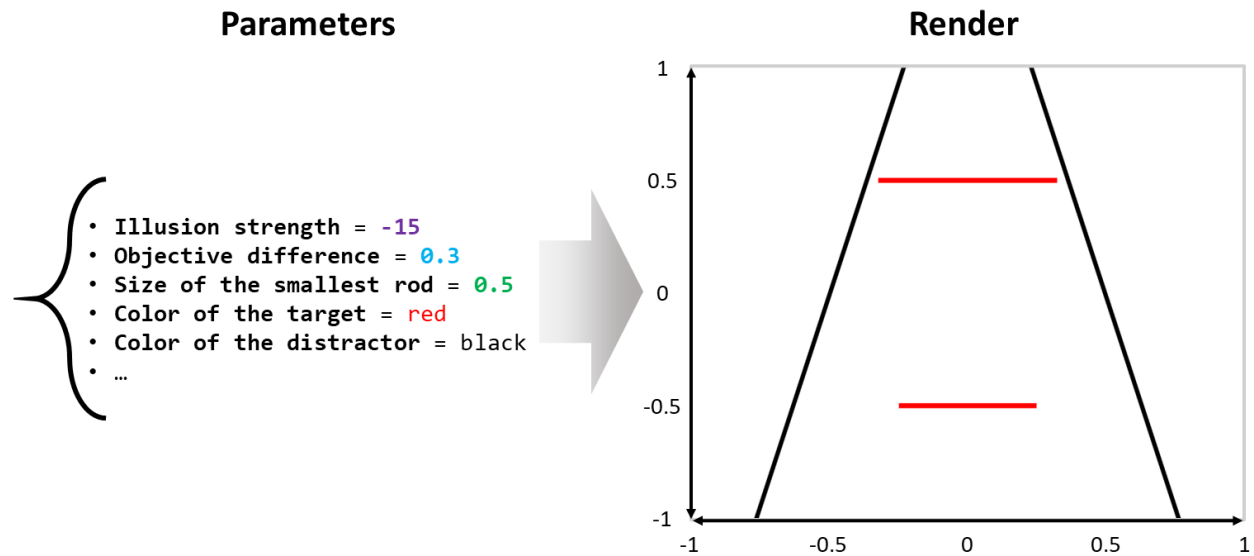- Color of the distractor = black
- …

Figure 1. The parametric framework for illusions originally implemented in *Pyllusion* aims at dissociating the *parametric* representation of an illusion (on the left) from its *rendered* representation, in this case as an image of the Ponzo illusion (on the right). In technical terms, an *illusion strength* of -15 represents a 15 degree tilt of the vertical lines (black distractor lines); an objective *difference* of 0.3 represents a 30% length difference of the upper and lower horizontal lines (red target lines) where the *size* of the shorter horizontal line is 0.5.

some shapes - related to the strength of the illusion, or the color of the "target" objects), which in turn allows for a consistent programming interface (API).

Interestingly, in most of the visual illusions, the strength of the illusion can be dissociated from the actual "difference" (which is impacted by the illusion). For instance, in the Müller-Lyer illusion (see **Fig. 1**), the difference between the two horizontal segments can be modulated orthogonally from the angle of the "distractors" arrows. Allowing researchers to easily manipulate these parameters opens the door for potentially interesting paradigms and experiments. In the following section, we will describe with concrete examples how we operationalized such a parametric approach in the *Pyllusion* software.

Pyllusion

171 This is not the first time that Python, illusions and cognitive science are brought together.

172 In his book, *"Programming visual illusions for everyone"*, Bertamini (2017) describes how

173 to use *PsychoPy* to generate famous illusions. That said, although being a fantastic tool

174 and resource for researchers and anybody interested in illusions, it is presented as a fun

175 introduction to programming and to Python, rather than a dedicated software for illusions

176 *per se*.

177 *Pyllusion* is an open-source package to programmatically generate illusions written in Python

178 3 (Van Rossum & Drake, 2009), which means that its users benefit from a large number of

179 learning resources and a vibrant community. However, although being a programming-

180 based tool, users not familiar with Python or other languages can easily use it as well, as it

181 requires minimal programming skills (one can essentially copy the few necessary lines from

182 the documentation and tweak the explicitly-named parameters). This makes it a very flexible

183 tool; advanced users can incorporate *Pyllusion* in their scripts or experiments (for instance,

184 to generate illusions "on the fly" based on the input of the user), whereas novice users can

185 simply copy the minimal code to pre-generate and save the illusions as images.

186 The source code is available under the MIT license on GitHub (*https://github.com/RealityBending/*

187 *Pyllusion/*). Its documentation (*https://realitybending.github.io/Pyllusion/*) is automati-

188 cally built and rendered from the code and includes guides for installation, a description of

189 the package's functions, as well as examples of use. Finally, the issue tracker on GitHub of-

190 fers a convenient and public forum that allows users to report bugs, get help and gain insight

191 into the development of the package. Additionally, the repository leverages a comprehensive

192 test suite (using *pytest*) and continuous integration (using GitHub actions) to ensure soft-

193 ware stability and quality. The test coverage and build status can transparently be tracked

194 via the GitHub repository. Thanks to its collaborative and open development, *Pyllusion*

195 can continuously evolve, adapt, and integrate new functionalities to meet the needs of the

196 community.

197 *Pyllusion* is available on PyPI, the main repository of software for Python and can thus be
198 installed by running the command `pip install Pyllusion`. Once the software is installed,
199 it must be loaded in Python scripts with `import pyllusion`. Once the package is loaded,
200 two further steps are required to generate the illusions, 1) specifying the parameters and 2)
201 rendering the output accordingly.

202 We will use the Delboeuf illusion in the hands-on example shown below. However, the same
203 workflow applies to the other illusions supported by *Pyllusion*, including the Ebbinghaus
204 illusion, the Müller-Lyer illusion, the Ponzo illusion, the Zöllner illusion, the Rod and Frame
205 illusion, the Poggendorff illusion and more (see **Fig. 2**, as well as the full list with examples
206 on the **readme**.

Step 1: Parameters

208 The parameters for each illusion can be generated using the `IllusionName_parameters()`
209 function. Many optional arguments are available for modifying, of which the description
210 and default values can be found in the API documentation (*https://realitybending.github.*
211 *io/Pyllusion/functions.html*). In the example below, we specify the `illusion_strength`
212 argument, and the function will compute all of the remaining parameters accordingly.

```python
# Load package
import pyllusion as ill


# Create parameters
parameters = ill.(illusion_strength=2)


# Visualize parameters
print(parameters)
```
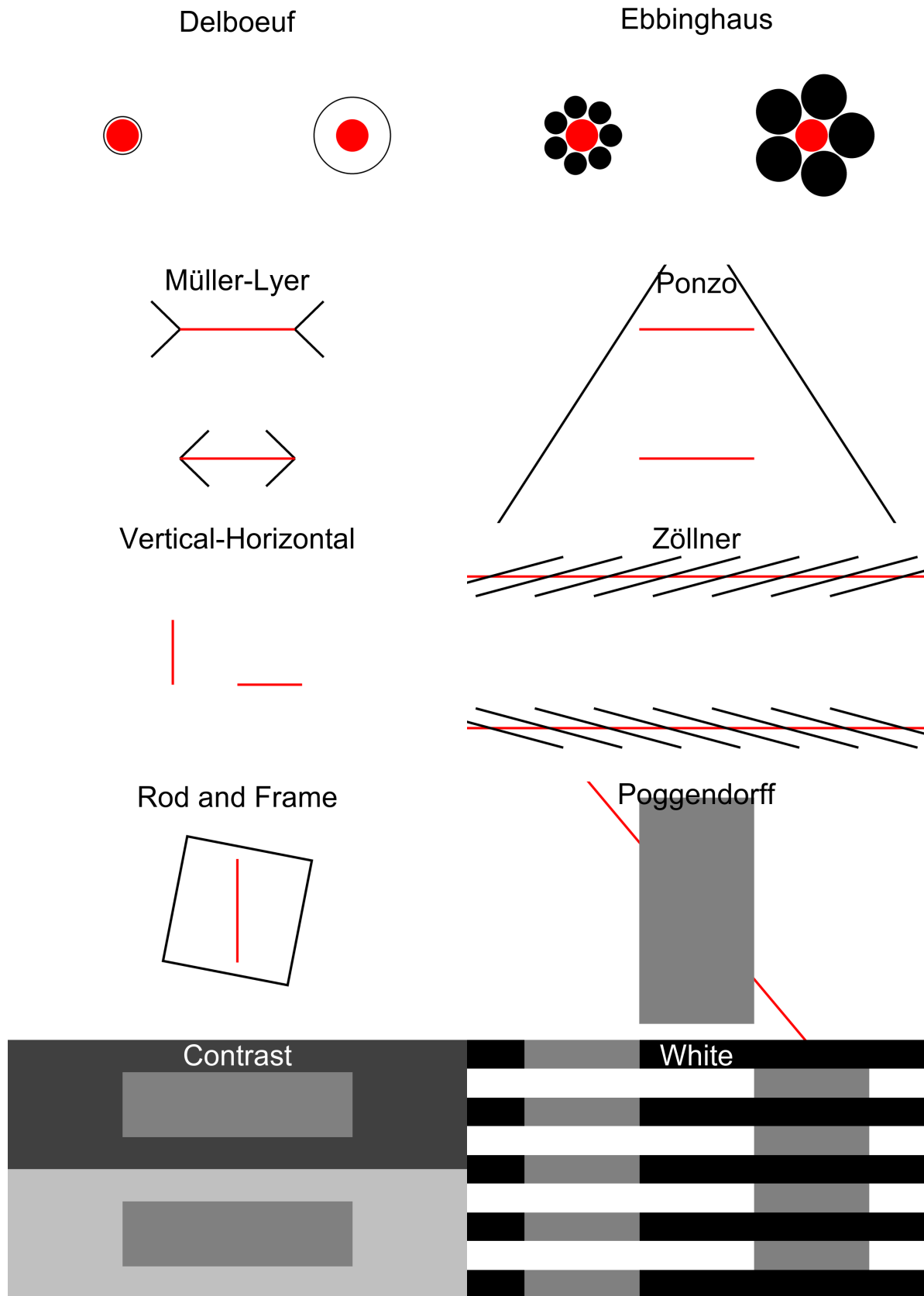
Figure 2. Different classical visual illusions currently supported by *Pyllusion*. These can all be generated using the parametric approach described in this paper, allowing for fully reproducible studies.

```
{'Difference': 0,
 'Size_Inner_Left': 0.25,
 'Size_Inner_Right': 0.25,
 'Size_Inner_Difference': 0.0,
 'Illusion_Strength': 2,
 'Size_Outer_Left': 0.3,
 'Size_Outer_Right': 0.52,
 'Distance_Centers': 1,
 'Distance_Edges_Outer': 0.59,
 'Position_Left': -0.5,
 'Position_Right': 0.5,
 ...}
```

As one can see, the output of this function is a basic Python dictionary (as denoted by the curly brackets), which makes it easy to further process, modify, share, store or investigate. This "container" object stores the values for a large number of parameters, such as the size of each (inner and outer) circle, the distance between the centers and edges of the circles, and their position, which is then passed to a "rendering" function which converts this set of parameters into the final output.

Note the two main parameters, `illusion_strength`, and `difference`, have fairly generic names. For instance, in the Ponzo illusion, less abstract names for these arguments could have been `difference_size_outer_circles` and `difference_size_inner_circles`). Indeed, the meaning of these parameters depends on the nature of the illusion. For instance, while `illusion_strength` currently refers to the the area of the outer circles in the Delboeuf illusion, it refers to the angle of the non-horizontal lines in the Ponzo illusion.

Conceptually, this term represents the extent to which the surrounding context biases the perceptual experience (see **Fig. 2**). The decision to unify the inducing parameters under

the "illusion strength" label was further motivated by the aim of having a consistent naming scheme for the API. This means that users can experiment with new illusions by modulating the illusion strength, without the need of learning what is the actual physical parameter (e.g., "angle of the distractor lines") driving the illusion.

Step 2: Rendering

The dictionary containing the parameters of the illusion, can then be passed to a "rendering" function, which actually draws (or displays) the illusion according to the specifications. Render-specific arguments are available at this stage, such as the dimensions of the image. Two output-engines are currently supported, images (in any format thanks to the PIL Python library for image processing; Clark, 2015), or as *PsychoPy* stimuli (Peirce, 2007), one of the most popular psychological experiments software.

Images.   Each function is illusion-specific and hence, uniform function names (in the form `IllusionName_FunctionGoal()`) are used in the process of creating the illusion. Parameters are computed using `*_parameters()` (the asterisk representing the illusion name), and images can be generated via `*_image()` (or similarly, `*_psychopy()`, as we will see later).

The following Python code shows the full and reproducible code to generate a PNG image with a Delboeuf illusion. However, note that the parameters generation and the rendering have been dissociated for illustrative purposes. In practice, the arguments related to the parameters of the illusion can be passed directly to the rendering function, which will automatically compute the parameters if no dictionary is passed. Similarly, the saving step can be done directly by adding `.save()` at the end of the the `*_image()` function, which reduces the amount of Python lines to one.

```python
# Load package
import pyllusion as ill
```

```python
# Create parameters
parameters = ill.delboeuf_parameters(illusion_strength=1, difference=2)


# Generate image from parameters
image = ill.delboeuf_image(parameters, height=600, width=800)


# Save it
image.save("my_illusion.png")
```

²⁴⁹ Images can be easily post-processed using the PIL library. For instance, with just a few lines,

²⁵⁰ one can loop through different combinations of parameters, generate illusions, add text on

²⁵¹ them, and collate together in a mosaic, as can be seen in **Fig. 3**.

²⁵² **PsychoPy.**   As illusions are frequently used in experimental psychology, we designed *Pyl-*

²⁵³ *lusion* so that it is directly usable within *PsychoPy* (Peirce, 2007) experiments. *PsychoPy* is

²⁵⁴ an open-source, free and Python-based package for experiment creation, recognized for its

²⁵⁵ timing accuracy (Bridges, Pitiot, MacAskill, & Peirce, 2020) and its GUI (the "builder"),

²⁵⁶ thereby allowing users who are not familiar with code to easily build experiments.

²⁵⁷ The *PsychoPy* "builder" interface allows for code components to be flexibly added, which

²⁵⁸ makes it convenient to insert the few lines necessary for displaying illusions. However, using

²⁵⁹ the programming interface of *PsychoPy* (which underlies the graphical interface) reveals how

²⁶⁰ seamless the integration with *Pyllusion* can be. The following code is a minimal example

²⁶¹ demonstrating how to use a Delboeuf illusion within a *PsychoPy* workflow. Running it opens

²⁶² a new window, displays the illusion in it, and then closes it once an input (a key press) is
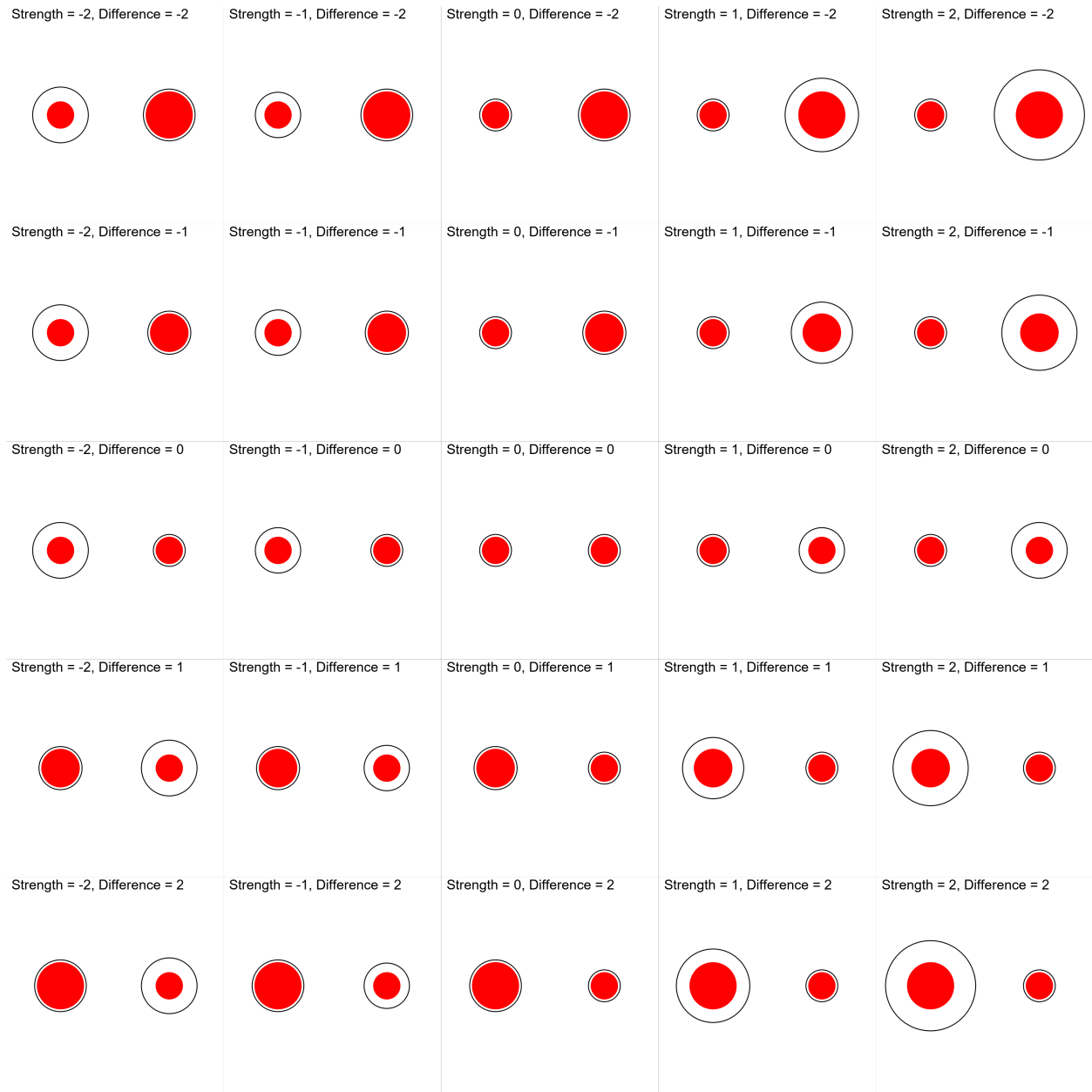
²⁶³ detected.

Figure 3. Different combinations of illusion strength and objective difference between the two target stimuli (the area of the red circles) for the Delboeuf illusion. The vertical central column shows varying magnitudes of size difference in both directions with no illusion, whereas the horizontal central row shows different magnitudes of illusion strength when the targets are of identical sizes. By using negative or positive values for the illusion strength, one can generate congruent or incongruent illusions (that reinforce or attenuate the actual difference respectively).

```python
# Load packages
import pyllusion as ill
from psychopy import visual, event


# Create parameters
parameters = ill.delboeuf_parameters(illusion_strength=1, difference=2)


# Initiate Window
window = visual.Window(size=[800, 600], winType='pygame', color='white')


# Display illusion
ill.delboeuf_psychopy(window=window, parameters=parameters)


# Refresh and close window
window.flip()
event.waitKeys()  # Press any key to close
window.close()
```

This native integration with *PsychoPy* could appear as somewhat redundant and unnecessary, as one could pre-generate all the illusions as images, and simply load them in *PsychoPy* as images, instead of generating them from scratches using *PsychoPy*'s drawing functionalities. However, this direct integration in experiment building software has multiple benefits, such as avoiding the storage of large image file sizes (resulting in more efficient use of space for experiments that can be uploaded and stored online), avoiding issues of image scaling and resolution on different screens, and allowing "on-the-fly" generation of stimuli, which opens the door for novel adaptive paradigms where the modulation of illusions crucially depends on the participant's input.

Future Plans and Developments

Being an open-source software, *Pyllusion* will continue to grow and evolve based on the community's input and needs. While the direction and state of the package in the long term can be hard to predict, several short term goals are highlighted below.

The initial release of *Pyllusion* focuses on a set of classical, well-described, visual illusions, as they are the most commonly used (for historical reasons mainly, as well as for their relative simplicity). That said, the number of existing illusions, or variations therein, is virtually infinite (and great advances are made to generate new ones using machine learning; Watanabe, Kitaoka, Sakamoto, Yasugi, & Tanaka, 2018). Thus, new illusions, as well as new illusion types (e.g., movement-based using GIF or video formats, or auditory illusions using sounds and music) could be added in the future. Due to the open and collaborative nature of the software, these evolutions will be driven by the needs of the community, ensuring that *Pyllusion* remains cutting-edge, adaptable and useful to address future issues.

Adding new illusions refers mostly to implementing an algorithm to conceptualise and essentialize them as sets of parameters, which is by design independent from their rendering. However, more rendering engines could be added down the road. For instance, one of the first milestones could take the form of an integration with other Python-based experiment building software, such as *OpenSesame* (Mathot, Schreij, & Theeuwes, 2012) or *Neuropsydia* (Makowski & Dutriaux, 2017). Additionally, a conversion to other languages could also be an interesting feature, especially *JavaScript*, as this would allow a closer integration with web browser apps (and online experiments software, such as *jsPsych*; Leeuw & Motz, 2016; or *lab.js* ; Henninger, Shevchenko, Mertens, Kieslich, & Hilbig, 2020).

Finally, we look forward to the creation of studies that would investigate how, for each illusion, the modulation of the parameters affect behavioural responses, conscious perception, and the associated neural underpinnings. This would in turn allow for a better understanding of the commonalities and differences between these fascinating stimuli. As such, we hope

299 that our tool contributes to the development of a strong axis that will unite the community

300 working with illusions to push the field forward.

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