# HOMEWOEK 2

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Question 1

As we known, shellsort would become insertion sort when h reduce to one. Meanwhile, the insertion sort will be more efficient when the sequence is almost sorted. The shellsort is more efficient because it take a little time to sort some shorter sequences divided from the original sequence, so that the sequence becomes an almost sorted sequence. By doing so, the insertion sort phase can save much more time.
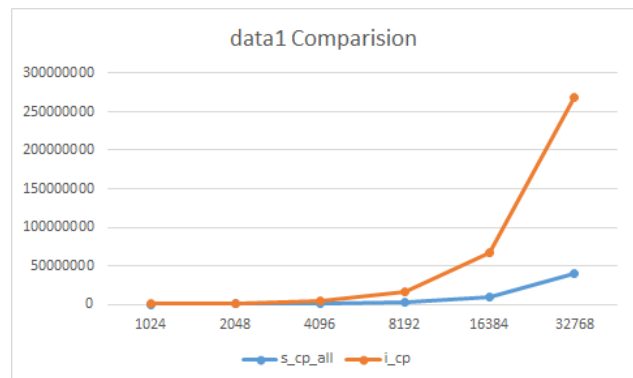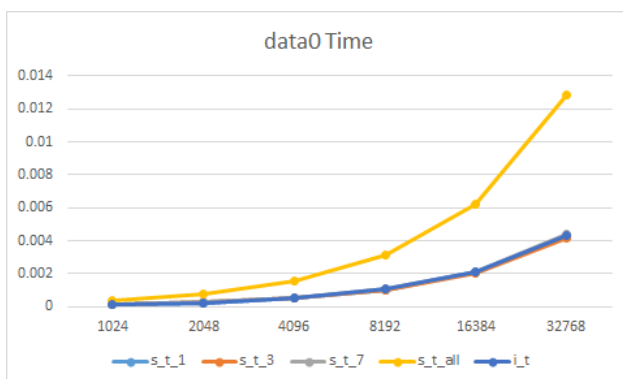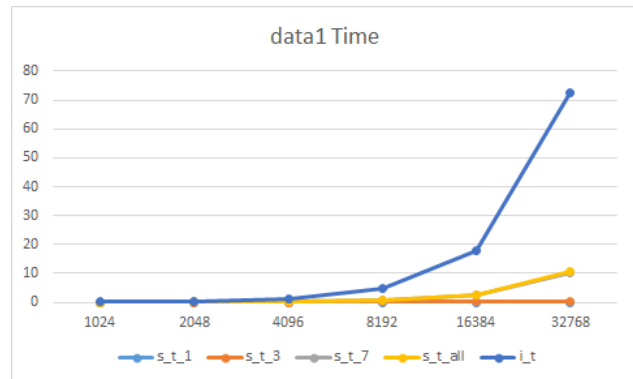
As we can see in the graph, we deal with a sorted sequence. Time consumption and comparision amount of shellsort are both three times of the insertion sort, since insertion sort just do a traversal but shell do three times.

But as we can see, when we are dealing with a chaotic sequence, insertion sort takes much more time and comparision. Because every data is far from where it should be, it would takes more comparision to find its position.

Question 2

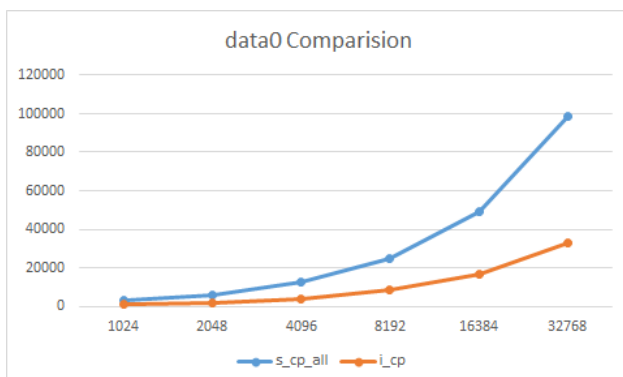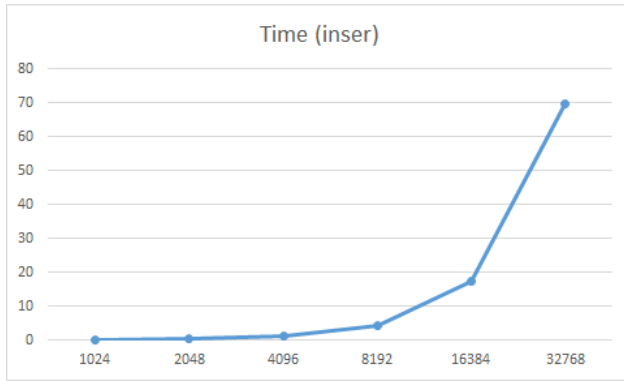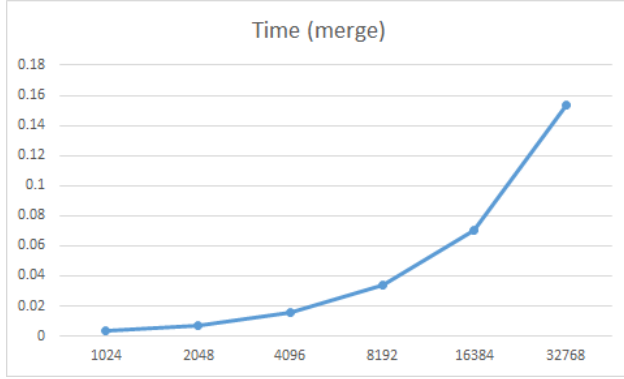The result and time consumption are as follow:

TABLE I
KENDALL TAU DISTANCE

1024	264541
2048	1027236
4096	4183804
8192	16928767
16384	66641183
32768	267933908

Time (merge)

Time (inser)

My basic logic of deciding KTD is to set one sequence as reference sequence, which means we will take whatever the fisrt value in the reference sequence is the smallest and whatever the last value in the reference sequence is the largest value. Then we will resort the other sequence based on the index of the reference sequence. Then we find the inverse pairs in the 2nd sequence, we find the KTD.

The way to decide the amount of inserve pairs would is to find the exchange time of a stable sort algorithm. Cause every exchange means the latter value is smaller than the former value, which is a pair of inverse values.

In my implementatoin, I use both merge sort and insertion sort to find KTD. As expected, the time consumption refers to $(O(NlogN))$ and $O(N^2)$.

Question 3

Comparision and array access are the two operations should be consider in merge sort. For the comparisions, every time we finish a merge to the whole array takes N comparisions.

And we will take $logN$ whole merge, since every time will take half of the array to merge together.

And for array access operation, we can decide from the amount of merge happens. Every merge is going to take a comparision, which means two read of arrays. And after deciding the smaller value, we will write it to the auxiliary array, which means one read from the original array and one write to the auxiliary array. Then we will write the value from auxiliary array back to original array, which mean one read from auxiliary array and one write to the original array. So we total have 6 array access in each merge, 2 writes and 4 reads. For whole process we will have $6NlogN$ array access.

data0 Time

data1 Time
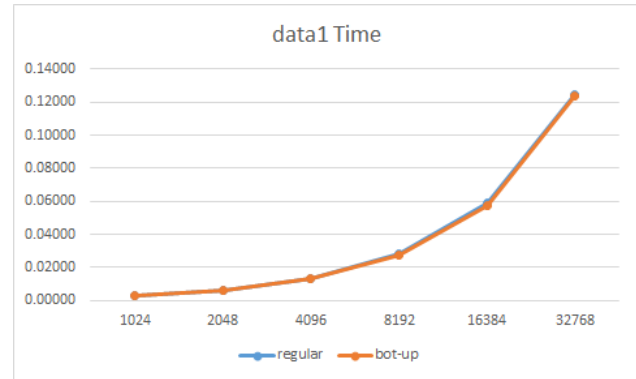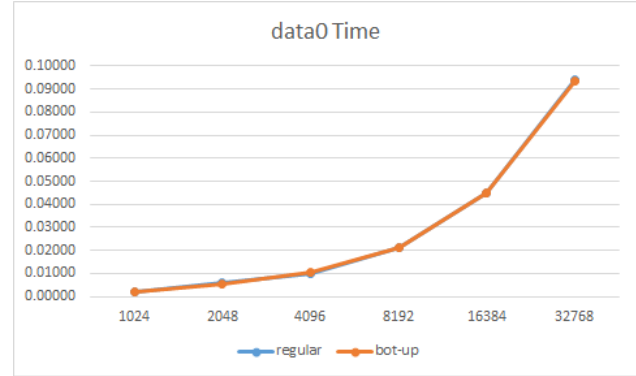
From the time consumption we can see that the two algorithm as expected have a pretty similar time consumption.

Question 4

For this problem, I assume we know that the sequence we are going to deal with has 1024 repeats of 1, 2048 repeats of 11, 4096 repeats of 111 and 1024 repeats of 1111. So I set four pointers in a auxiliary array points to the positions where the 4 entities are supposed to start. So whin one traversal, I can set the entity into where it should be by moving the pointers. Then we write back this auxiliary array to sort it. The process rakes N comparisions and $2N$ writes. Which I think should be the smallest time consumption.

Question 5