

# Metrics and Model Analysis

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Confusion Matrix, MSE, MAE, Bias-variance tradeoff

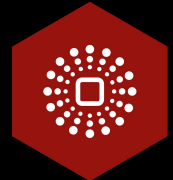


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# Classification problems

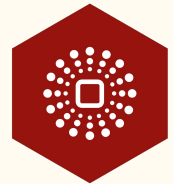
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Confusion Matrix



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- A confusion matrix is a table that is often used to describe the performance of a classification model (or "classifier") on a set of test data for which the true values are known.



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**Predicted Value**  
(predicted by the test)

	positives	negatives
positives	<b>TP</b> True Positive	<b>FP</b> False Positive
negatives	<b>FN</b> False Negative	<b>TN</b> True Negative



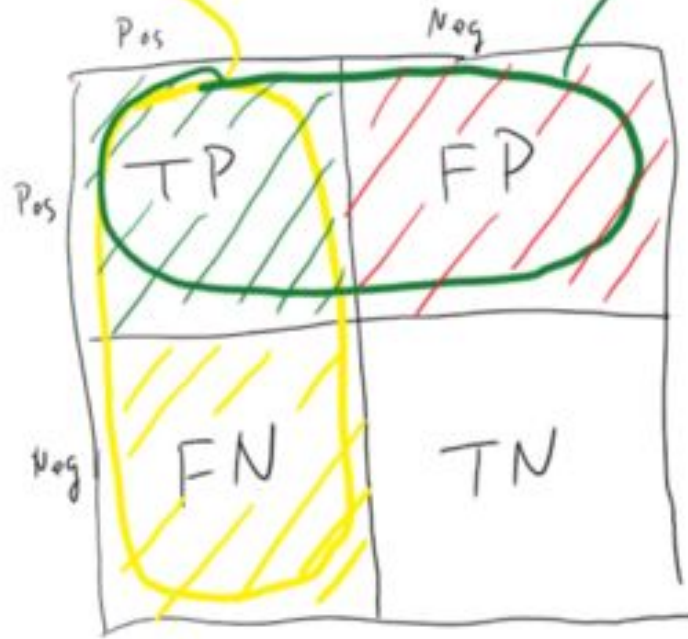
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$$\text{Recall} = \frac{TP}{TP + FN} \quad \text{Actual}$$

$$\text{Precision} = \frac{TP}{TP + FP}$$

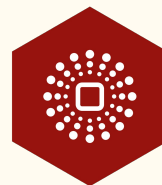
Predicted



$$\text{Accuracy} = \frac{TP + TN}{\text{Total}}$$

# Problems with Accuracy

- Assumes equal cost for both kinds of error
- Accuracy alone doesn't tell the full story when you're working with a class-imbalanced data set



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# Example

## True Positive (TP):

- Reality: Malignant
- ML model predicted: Malignant
- Number of TP results: 1

## False Positive (FP):

- Reality: Benign
- ML model predicted: Malignant
- Number of FP results: 1

## False Negative (FN):

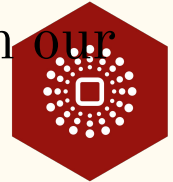
- Reality: Malignant
- ML model predicted: Benign
- Number of FN results: 8

## True Negative (TN):

- Reality: Benign
- ML model predicted: Benign
- Number of TN results: 90

$$\text{Accuracy} = \frac{TP + TN}{TP + TN + FP + FN} = \frac{1 + 90}{1 + 90 + 1 + 8} = 0.91$$

- Of the 91 benign tumors, the model correctly identifies 90 as benign. However, of the 9 malignant tumors, the model only correctly identifies 1 as malignant—a terrible outcome, as 8 out of 9 malignancies go undiagnosed!
- While 91% accuracy may seem good at first glance, another tumor-classifier model that always predicts benign would achieve the exact same accuracy (91/100 correct predictions) on our examples.





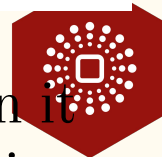
# Better Alternatives:

- Precision: What proportion of positive identifications was actually correct?

True Positives (TPs): 1	False Positives (FPs): 1
False Negatives (FNs): 8	True Negatives (TNs): 90

$$\text{Precision} = \frac{TP}{TP + FP} = \frac{1}{1 + 1} = 0.5$$

- Our model has a precision of 0.5—in other words, when it predicts a tumor is malignant, it is correct 50% of the time.

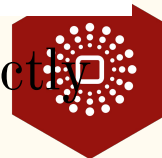


- Recall: What proportion of actual positives was identified correctly?

True Positives (TPs): 1	False Positives (FPs): 1
False Negatives (FNs): 8	True Negatives (TNs): 90

$$\text{Recall} = \frac{TP}{TP + FN} = \frac{1}{1 + 8} = 0.11$$

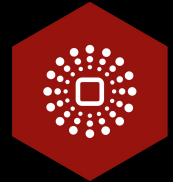
- Our model has a recall of 0.11—in other words, it correctly identifies 11% of all malignant tumors.



# Regression problems

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MAE, RMSE, MSE

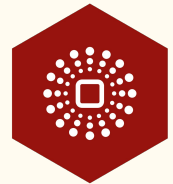


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# Mean Absolute Error

- Less sensitive to outliers

$$\text{MAE} = \frac{\sum_{i=1}^n |y_i - x_i|}{n} = \frac{\sum_{i=1}^n |e_i|}{n}.$$

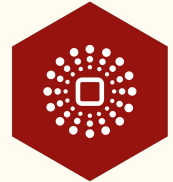


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# Mean Squared Error

- Very sensitive to outliers

$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2.$$



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# Root Mean Squared Error

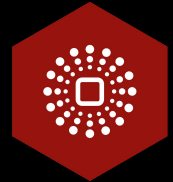
- RMSD is the square root of the average of squared errors. The effect of each error on RMSD is proportional to the size of the squared error; thus larger errors have a disproportionately large effect on RMSD. Consequently, RMSD is sensitive to outliers.

$$RMSE_{errors} = \sqrt{\frac{\sum_{i=1}^n (\hat{y}_i - y_i)^2}{n}}$$



# Bias-Variance tradeoff

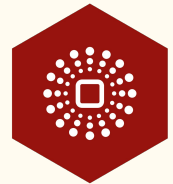
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# Error due to bias

- The error due to bias is taken as the difference between the expected (or average) prediction of our model and the correct value which we are trying to predict.
- Bias measures how far off in general these models' predictions are from the correct value.

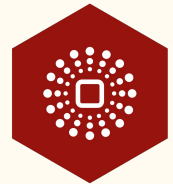


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# Error due to variance

- The error due to variance is taken as the variability of a model prediction for a given data point.
- The variance is how much the predictions for a given point vary between different realizations of the model.

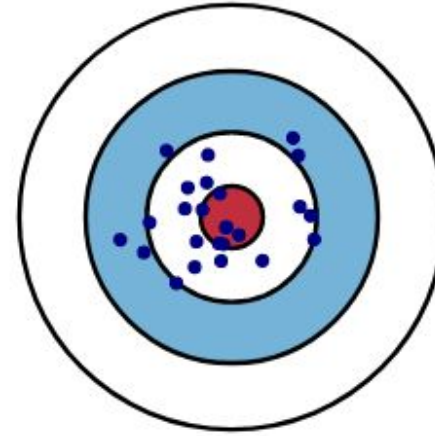
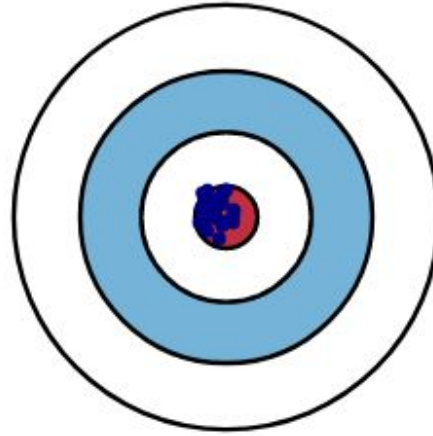


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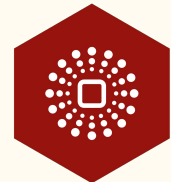
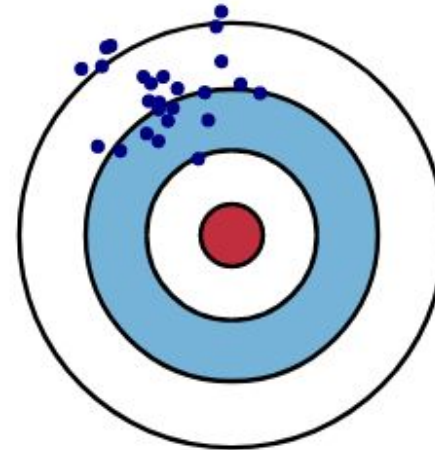
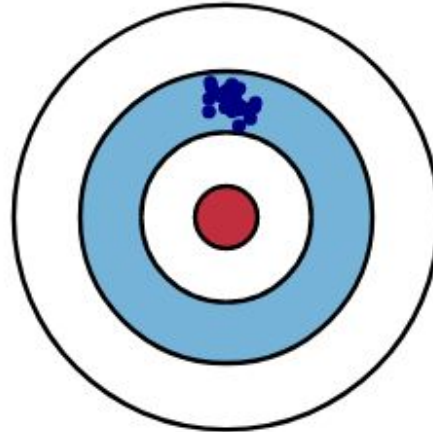
Low Variance

High Variance

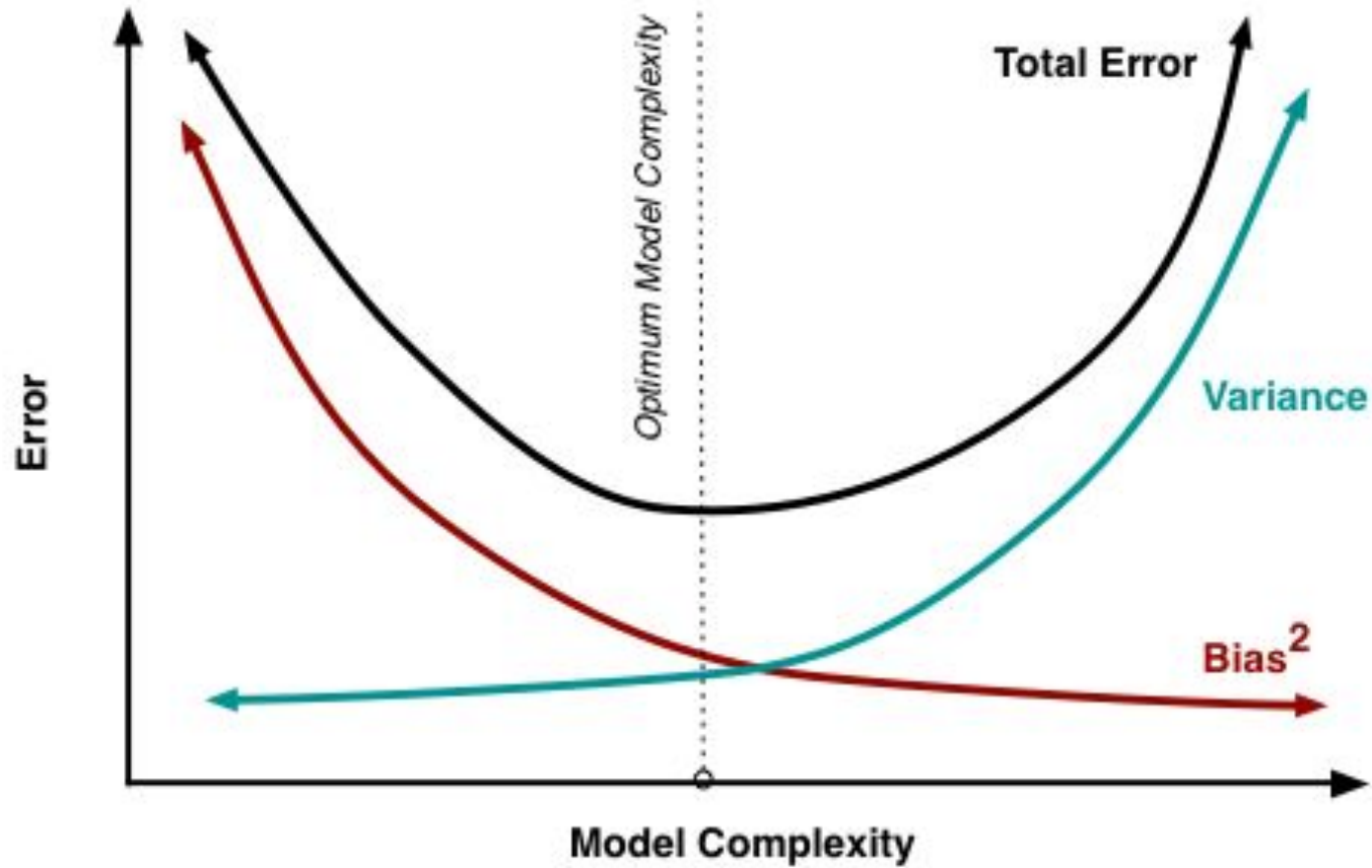
Low Bias



High Bias



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