

N = node, E = Edge

Depth-First Search as implemented in

```
X.MyDFS.dfs(DirectedGraph<E> graph)
```

dfs non recursive method:

First I loop through every headnode in the graph: $O(N)$

In the non-recursive method I check if the collection with soon-to-visit-nodes is not empty. I then remove the node that will be checked, looping through all its edges. With each edge I add it to the soon-to-visit-nodes-collection and it's starts over.

The two sets that a contains-method is runned on, is both a hashset for a $O(1)$ in time complexity.

In worst case i have to loop through all the heads and every node's edges once, that makes the time complexity: $O(N) + O(N+E) \Rightarrow O(2N+E) \Rightarrow \mathbf{O(N+E)}$

dfs recursive:

First I loop through every node in the graph.

In the recursive method I loop through every edge to one specific node.

The set that a contains-method is runned at is a hashset for a $O(1)$ in time complexity.

In worst case we have to loop through every node's edges once, that makes the time complexity: $O(N+N+E) \Rightarrow O(2N+E) \Rightarrow \mathbf{O(N+E)}$

Breadth-First Search as implemented in

```
X.MyBFS.bfs(DirectedGraph<E> graph)
```

bfs non recursive:

BFS is almost the same as DFS non-recursive. Except the BFS visit the nodes in another order.

The set that a contains-method is runned at is a hashset for a $O(1)$ in time complexity.

Therefore the worst case and the time complexity is the same as in DFS: $\mathbf{O(N+E)}$

Transitive Closure as implemented in

```
X.MyTransitiveClosure.computeClosure(DirectedGraph<E> graph)
```

First I loop through every node in graph.

On every node I do a DFS to get it's "Reachables".

In worst case we need to go through all the nodes and do a DFS on it, therefore the time complexity is: $O(N) * O(N+E) \Rightarrow \mathbf{O(N^2+N*E)}$

Connected Components as implemented in

```
X.MyConnectedComponents.computeComponents(DirectedGraph<E> graph)
```

First I loop through the graph, for each node that isn't visited I do a DFS to get it's connections: $O(N) * O(N+E) \Rightarrow O(N^2+N*E)$

Then I loop through the returnCollections and for each collection I check if it has a element in common with the connections to the specific node. Add $O(N)$

Method "addAll" has time complexity $O(1)$.

This way i only go through the nodes once. Because of the nested loop the time complexity is: $O(N) * O(N+E) + O(N) \Rightarrow O(N^2 * N + E)$