

2-7 Part 2 Lesson Notes

Derivatives and Rates of Change

Name: _____

1 Definition The **tangent line** to the curve $y = f(x)$ at the point $P(a, f(a))$ is the line through P with slope

$$m = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$$

provided that this limit exists.

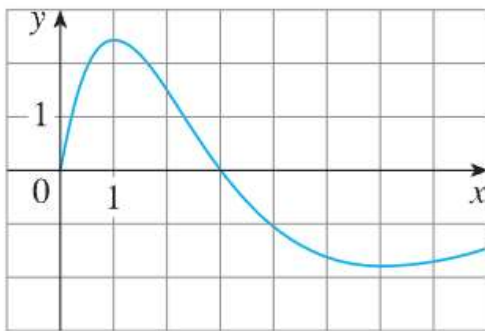
$$m = \lim_{h \rightarrow 0} \frac{f(a + h) - f(a)}{h}$$

The tangent slope at any point $(a, f(a))$ is referred to by the notation $f'(a)$.

$f'(a)$ means: The derivative of $f(x)$ at some point $x=a$ / The tangent slope at any point $x=a$ / The instantaneous rate of change at $x=a$.

1. Write the equation of a line tangent to $f(x)$ at $x=1$ if $f(1)=2$ and $f'(1)=-3$.

2. a. Order the values from least to greatest: $f'(1)$, $f'(3)$, $f(1)$, $f(1/2)$, $f'(6)$, $f'(1/2)$



b. T/F

i. $f(0)=f'(1)$

ii. $f'(2)>f'(6)$

iii. $f'(1)>f'(4)$

3. On a planet with a different gravitational pull, a rock is thrown with initial velocity 10 m/s and the height of the rock is given as $h(t) = 10t - 2t^2$.

a.) Find the instantaneous velocity at any time $t=a$.

b.) Find the instantaneous velocity at any time $t=1$ second.

c.) Find the average velocity from $t=1$ second to $t=3$ seconds.

d.) How fast is the rock moving when it hits the ground?