

HW1

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2019-01-26

Problem 1

1. Find the probability that a random number from 1 to 1000 is divisible by 2 or 3.

$$f(x) = x^2$$

Problem 2

2. For events A and B such that

$$P(A) = 0.5, P(B) = 0.4, P(A \cap B) = 0.2$$

find the probability that either A or B happened but not both.

Problem 3

3. (SOA) Upon arrival at a hospital emergency room, patients are categorized according to their condition as critical, serious, or stable. In the past year, 10% of the ER patients were critical, 30% serious, and the rest stable. Moreover, 40% of critical patients died, 10% of serious patients died, and 1% of stable patients died. Given that the patient survived, what is the probability that this patient was categorized as serious?

Problem 4

4. (SOA) For two events A and B, determine the probability of A if

$$P(A \cup B) = 0.7, P(A \cup B^c) = 0.9.$$

Problem 5

5. Assume that 0.1% of people from a certain population have a germ. A test gives false positive (that is, shows a person has this germ if this person does not actually have a germ) in 10% of cases when the person does not have this germ. This test gives false negative (shows a person does not have this germ if this person actually has it) in 20% of cases when this person has this germ. Suppose you pick a random person from the population and apply this test twice. Both times it gives you positive result (that is, the test says that this person has this germ). What is the probability that this person actually has this germ?

Problem 6

6. A dashboard warning light is supposed to flash red if the car's pressure is too low. The probability of light flashing when it should is 98%, and 3% of the time it flashes for no reason. If there is a 10% chance that the oil pressure is low, what is the chance that the driver should be concerned when light is flashing?

Problem 7

7. A real estate agent has 20 clients from Reno, 14 clients from Sparks, and 6 clients from Carson City. The agent will choose today's client at random, uniformly. Each communication with a client results in a closed deal with probability 20% if this client is from Reno, 25% from Sparks, and 15% from Carson City. Find the probability that today the deal will be closed.

Problem 8

8. The probability of A is 0.7, the probability of B is 0.8. What are the possible values for the probability of both A and B happening?

Problem 9

9. Two events A and B are such that the probability of at least one of them occurring is 0.8, the probability of exactly one of them occurring is 0.6, and $P(A | B) = 0.6$ Find the probability of A and the probability of B.

Problem 10

10. (SOA) A survey of a group's viewing habits over the last year revealed the following information:

- (i) 28% watched gymnastics
- (ii) 29% watched baseball
- (iii) 19% watched soccer
- (iv) 14% watched gymnastics and baseball
- (v) 12% watched baseball and soccer
- (vi) 10% watched gymnastics and soccer
- (vii) 8% watched all three sports.

Calculate the percentage of the group that watched none of the three sports during the last year.