

Last Name:

ARORA

First Name

LAKSHAY

1. Write the state equation for the given circuit

$$a. \dot{X} = \frac{1}{RC} V_i - \frac{1}{RC} X$$

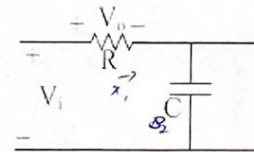
$$b. \dot{X} = \frac{1}{R} V_i - \frac{1}{R} X$$

$$c. V_0 = V_i - X_1$$

$$d. \dot{X} = V_i - X$$

$$i = \frac{V_0}{R}$$

$$V_i = R \times \frac{V_0}{R} - \frac{1}{C} \dot{X}$$



$$V_i - X = V_0$$

$$V_i - \frac{1}{C} \dot{X} = V_0$$

$$\dot{X} = \frac{1}{RC} V_i - \frac{1}{RC} X$$

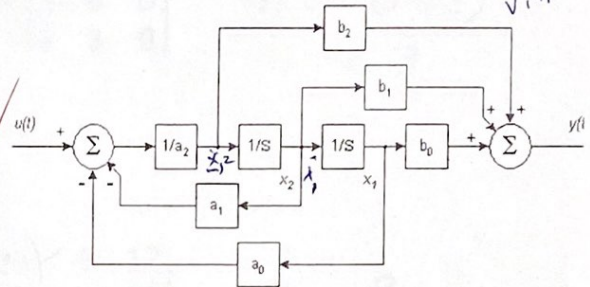
2. Write down the output equation for the given simulation diagram

$$a. \left[b_0 - \frac{b_2 a_0}{a_2} \right] X_1 + \left[b_1 - \frac{a_1 b_2}{a_2} \right] X_2 + \frac{b_2}{a_2} U$$

$$b. \left[b_0 + \frac{b_2 a_0}{a_2} \right] X_1 + \left[b_1 + \frac{a_1 b_2}{a_2} \right] X_2 + \frac{b_2}{a_2} U$$

$$c. \left[b_0 - \frac{b_2 a_0}{a_2} \right] X_1 - \left[b_1 - \frac{a_1 b_2}{a_2} \right] X_2 - \frac{b_2}{a_2} U$$

$$d. \left[b_0 + \frac{b_2 a_0}{a_2} \right] X_1 - \left[b_1 + \frac{a_1 b_2}{a_2} \right] X_2 - \frac{b_2}{a_2} U$$



3. Write the state equation (only
- \dot{X}_2
-) for given simulation diagram

$$a. \dot{X}_2 = [U + a_1 X_2 + a_0 X_1]$$

$$b. \dot{X}_2 = [U - a_1 X_2 - a_0 X_1]$$

$$c. \dot{X}_2 = [U + a_1 X_2 + a_0 X_1] \frac{1}{a_2}$$

$$d. \dot{X}_2 = [U - a_1 X_2 - a_0 X_1] \frac{1}{a_2}$$

$$y = b_2 \times \frac{1}{a_2} u + b_1 x_2 + b_0 x_1$$

$$\dot{x}_2 = -a_1 x_2 \times \frac{1}{a_2} - a_0 x_1 \times \frac{1}{a_2} + \frac{u}{a_2}$$

$$= \frac{1}{a_2} (-a_1 x_2 - a_0 x_1 + u)$$

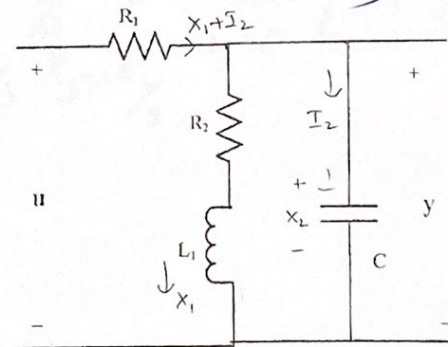
4. write the first loop equation for given circuit

$$a. U = R_1(X_1 + I_2) + R_2 X_1 + L_1 \dot{X}_1$$

$$b. U = R_1(X_1) + R_2 X_1 + L_1 \dot{X}_1$$

$$c. U = R_1(X_1) + R_2 X_1 + \dot{X}_1$$

$$d. U = R_1(X_1 + I_2) + X_1$$



5. Write the output equation for the given circuit

$$a. y = X_2$$

$$b. y = R_2 X_1 + L_1 \dot{X}_1$$

$$c. y = R_2 X_1 + L_1 X_1$$

$$d. y = R_2 X_1 + L_1 \dot{X}_1 + X_2$$

$$U = R_1(X_1 + I_2) + R_2 X_1 + L_1 \dot{X}_1$$

$$y = b_2 \times \frac{1}{a_2} u$$

$$y = x_2$$

Please show your work for partial credit.

Each question worth 2 points; this quiz worth 1 % of your final grade.

Last Name: ARORAFirst Name: LAKSHAY

1. What is the determinant of the following matrix
- $A = \begin{bmatrix} 4 & 2 & 1 \\ 5 & 6 & 0 \\ 4 & 3 & 1 \end{bmatrix}$

- a. -9
b. 9
c. 5
d. -15

$$\begin{bmatrix} 4 & 2 & 1 \\ 5 & 6 & 0 \\ 4 & 3 & 1 \end{bmatrix}$$

$$4(6-0) - 2(5-0) + 1(15-24) \\ 24 - 10 - 9 = 24 - 19$$

2. What is the cofactor of '5' the following matrix
- $A = \begin{bmatrix} 3 & 2 & 1 \\ 5 & 6 & 0 \\ 4 & 3 & 0 \end{bmatrix}$

- a. -3
b. 3
c. -15
d. 15

$$\begin{bmatrix} 3 & 2 & 1 \\ 5 & 6 & 0 \\ 4 & 3 & 0 \end{bmatrix}$$

$$a_{21} = 0 - (-3) \\ = 3$$

3. What is the rank of the following matrix
- $A = \begin{bmatrix} 3 & 6 & 9 & 12 \\ 8 & 16 & 24 & 32 \\ 4 & 8 & 12 & 16 \end{bmatrix}$

- a. 0
b. 2
c. 1
d. 3

$$\begin{bmatrix} 3 & 6 & 9 & 12 \\ 8 & 16 & 24 & 32 \\ 4 & 8 & 12 & 16 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 2 & 3 & 4 \\ 3 & 6 & 9 & 12 \\ 0 & 0 & 0 & 0 \\ 4 & 8 & 12 & 16 \end{bmatrix} \xrightarrow{R_2 \rightarrow R_2 - 3R_1, R_4 \rightarrow R_4 - 4R_1} \begin{bmatrix} 1 & 2 & 3 & 4 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

4. Find the inverse of A if
- $A = \begin{bmatrix} 2 & 0 \\ 4 & 1 \end{bmatrix}$

- a. $A^{-1} = \begin{bmatrix} 2 & 0 \\ 4 & 1 \end{bmatrix}$
b. $A^{-1} = \begin{bmatrix} 0 & 2 \\ 1 & 4 \end{bmatrix}$
c. $A^{-1} = \begin{bmatrix} 0.5 & 0 \\ -2 & 1 \end{bmatrix}$
d. $A^{-1} = \begin{bmatrix} 1 & 0 \\ -4 & 2 \end{bmatrix}$

$$A^{-1} = \frac{1}{\Delta} \text{adj} = \frac{1}{2-0} \begin{bmatrix} 1 & 0 \\ -4 & 2 \end{bmatrix}$$

5. Find matrix C if
- $C=AB$
- $A = \begin{bmatrix} 2 & 3 \end{bmatrix}$
- $B = \begin{bmatrix} 6 & 1 \\ 4 & 5 \end{bmatrix}$

- a. $C = \begin{bmatrix} 24 \\ 17 \end{bmatrix}$ b. $C = \begin{bmatrix} 24 & 17 \end{bmatrix}$ c. $C = \begin{bmatrix} 18 & 3 \\ 8 & 15 \end{bmatrix}$ d. Operation not possible

$$\begin{bmatrix} 2 & 3 \end{bmatrix}_{1 \times 2} \begin{bmatrix} 6 & 1 \\ 4 & 5 \end{bmatrix}_{2 \times 2} = \begin{bmatrix} 24 & 17 \end{bmatrix}_{1 \times 2}$$

Please show your work for partial credit.

Each question worth 4 points; this quiz worth 1 % of your final grade.

$$\begin{bmatrix} 12+12 & 2+15 \end{bmatrix}_{1 \times 2}$$

Last Name: ARORA 9/10First Name: LAKSHAY1. In controllable canonical form which of the following statement is **TRUE**

- a. All state variables depends upon the input
 b. All state variables depends upon the output
 ✓ c. Only one state variable depends upon the input
 d. Only one state variable depends upon the output

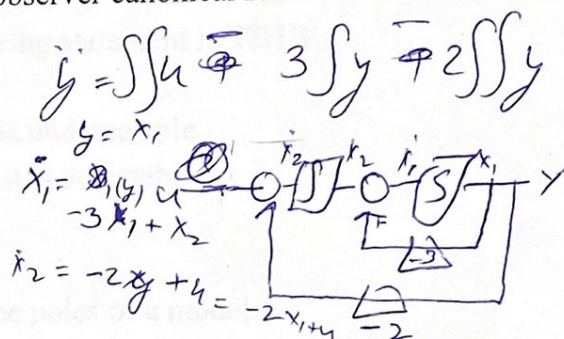
2. $\ddot{y} + 3\dot{y} + 2y = u$; write the state equation by using observer canonical form

a. $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$

b. $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -3 & -2 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$

c. $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -3 & 1 \\ -2 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u$

✓ d. $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -3 & 1 \\ -2 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$

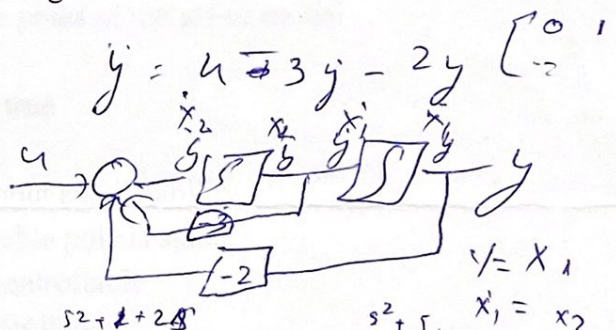
3. $\ddot{y} + 3\dot{y} + 2y = u$; write the state equation by using controllable canonical form

✓ a. $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} 0 & 1 \\ -2 & -3 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$

b. $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -3 & -2 \\ 1 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$

✓ c. $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -3 & 1 \\ -2 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 1 \\ 0 \end{bmatrix} u$

d. $\begin{bmatrix} \dot{x}_1 \\ \dot{x}_2 \end{bmatrix} = \begin{bmatrix} -3 & 1 \\ -2 & 0 \end{bmatrix} \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} + \begin{bmatrix} 0 \\ 1 \end{bmatrix} u$

4. Find 'C' in the following function $F(s) = \frac{1}{(s+2)(s+1)^2} = \frac{A}{s+2} + \frac{B}{s+1} + \frac{C}{(s+1)^2}$

✓ a. 1

b. -1

c. -2

d. 2

Handwritten solution for Question 4:

$$As^2 + A + 2As + B(s+2)(s+1) + C(s+1) = 1$$

$$As^2 + A + 2As + Bs^2 + 3Bs + 2B + Cs + C = 1$$

$$(A+B)s^2 + (2A+3B+C)s + (A+2B+C) = 1$$

$$A+B=0 \quad 2A+3B+C=0 \quad A+2B+C=1$$

$$A=-B \quad 2(-B)+3B+C=0 \quad -2B+3B+C=0 \quad B+C=0 \quad C=-B$$

$$A+2B+C=1 \quad A+2B-B=1 \quad A+B=1 \quad -B+B=1 \quad 0=1$$

$$A+B=0 \quad A=-B \quad -B+B=1 \quad 0=1$$

$$A+B=0 \quad A=-B \quad -B+B=1 \quad 0=1$$

$$A+B=0 \quad A=-B \quad -B+B=1 \quad 0=1$$

5. In observable canonical form which of the following statement is **TRUE**

- a. All state variables depends upon the input
 ✓ b. All state variables depends upon the output
 c. Only one state variable depends upon the input
 d. Only one state variable depends upon the output

Handwritten solution for Question 5:

$$2A + 3B + C = 0$$

$$-2B + 3B + C = 0 \quad B + C = 0 \quad C = -B$$

$$A + 2B + 2C = 1 \quad A + 2B - 2B = 1 \quad A = 1$$

$$B + 2B - 2B = 1 \quad B = 1$$

$$C = -1$$

Please show your work for partial credit.

Each question worth 2 points; this quiz worth 1 % of your final grade.

Last Name: ARORAFirst Name: LAKSHAY

1. If the model is controllable then which of the following statement is **TRUE**
- ☒ a. All poles can be changed anywhere a unique solution exists
 - b. All poles can be changed anywhere not unique solution exists
 - ☒ c. All poles can be changed anywhere a no solution exists
 - d. Poles are not interchangeable a unique solution exists
2. If the model is Observable then which of the following statement is **TRUE**
- a. The model is undetectable
 - b. If unobservable poles are stable then it is undetectable
 - ☒ c. If unobservable poles are unstable then it is detectable
 - ☒ d. The model is detectable
3. Which of the following statement is **TRUE** about the poles of a model
- a. The poles are the roots of the characteristic equation
 - b. Eigenvalues of 'A' matrix are the poles of the given model
 - ☒ c. Both statements are true
 - d. None of the above statements are true
4. Which of the following statement is **TRUE** about stabilizability
- a. A model is stabilizable if controllable pole is stable
 - b. A model is stabilizable if it is uncontrollable
 - ☒ c. A model is stabilizable if it is controllable
 - d. A model is stabilizable if uncontrollable pole is stable
5. The denominator of the transfer function is called
- a. Characteristic equation
 - ☒ b. Characteristic polynomial
 - c. Eigenvalues of the vectors
 - d. Poles of the given system

Please show your work for partial credit.

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