

It best Practise

\bar{X} , mean, mode is best

$N \rightarrow \bar{X}$ mean

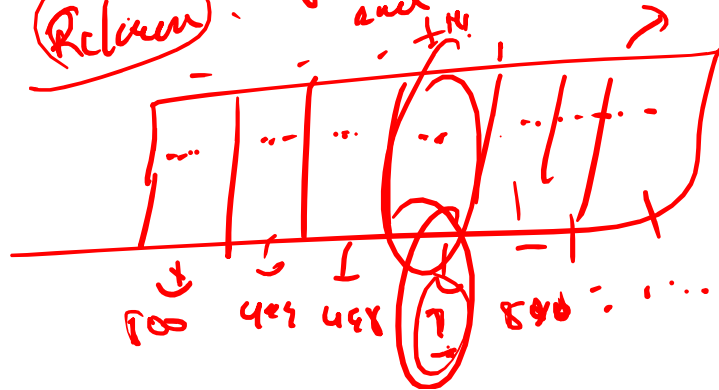
How is it better

$N \times 0.1 \rightarrow \bar{X}$ ✓

~~30/08~~ → Delhi Street
19/08

Return

May 1987 → 1988 → Predict



Testing process
↓
Structure
↓
Test set
↓
3 cur → X

$\bar{X} \rightarrow$ Predict
↓
+
14
data nos
↓
logit
↓
mean of value

→ Entropy → Splitting criterion → Information Gain (I.G.)
 ↓
 degree of randomness
 ↓
 In the node, there exist multiple Classes
 ↳ Impure ↑ Entropy ↑
 ↳ measure of Purity
 ↳ measure of Impurity

$$\Rightarrow I.G. = 1 - \text{Entropy}$$

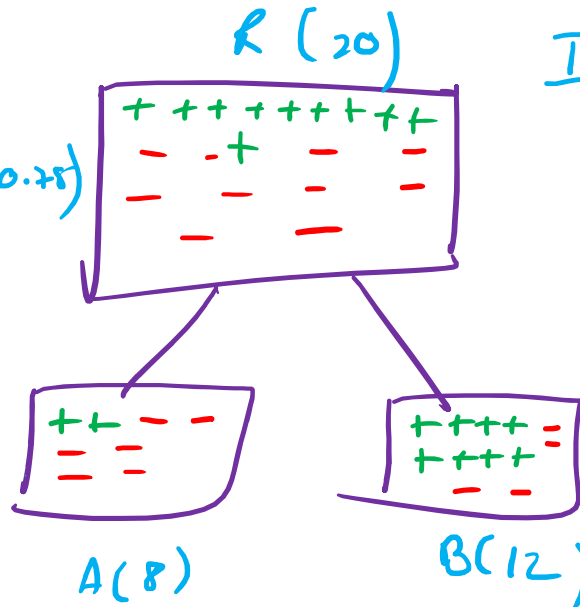
$$\Rightarrow \text{Entropy}_{\text{node}} = -P_1 \log_2 P_1 - P_2 \log_2 P_2 - P_3 \log_2 P_3 - \dots - P_n \log_2 P_n$$

$$I.G. \text{ of the split} \Rightarrow \text{Weighted I.G.} = \underline{\underline{W_1 I_{G1} + W_2 I_{G2}}}$$

→ split on height based on Entropy / IG

$$\begin{aligned}
 I.G._A &\Rightarrow 1 - (-P_+ \log_2 P_+ - P_- \log_2 P_-) \\
 &\Rightarrow 1 - (-0.25 \log_2 0.25 - 0.75 \log_2 0.75) \\
 &\Rightarrow 0.189
 \end{aligned}$$

$$\begin{aligned}
 P(+ve) &= 0.25 \\
 P(-ve) &= 0.75
 \end{aligned}$$



$$\begin{aligned}
 I.G._B &= 1 - (-P_+ \log_2 P_+ - P_- \log_2 P_-) \\
 &= 1 - (-0.67 \log_2 0.67 - 0.33 \log_2 0.33) \\
 &\Rightarrow 0.086
 \end{aligned}$$

$$\begin{aligned}
 P(+ve) &= 0.67 \\
 P(-ve) &= 0.33
 \end{aligned}$$

⇒ I.G. on the split

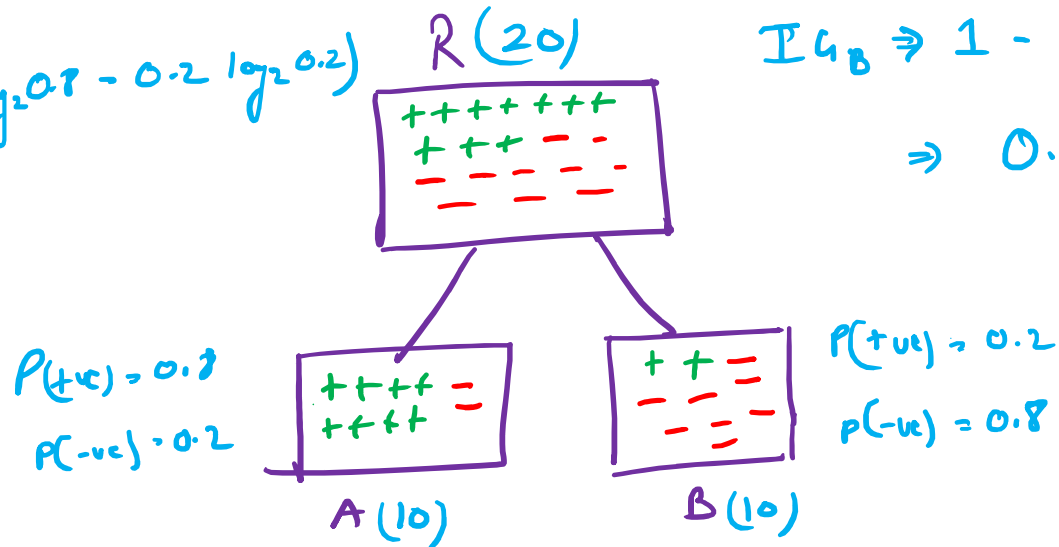
$$\Rightarrow I.G._{height} \Rightarrow W_A I.G._A + W_B I.G._B$$

$$\Rightarrow \frac{8}{20} * 0.189 + \frac{12}{20} * 0.086 \Rightarrow 0.127$$

→ Split on class based on Entropy / IG.

$$IG_A = 1 - (-0.8 \log_2 0.8 - 0.2 \log_2 0.2) \Rightarrow 0.28$$

$$IG_B \Rightarrow 1 - (-0.2 \log_2 0.2 - 0.8 \log_2 0.8) \Rightarrow 0.28$$



IG on split

$$IG_{class} = W_A IG_A + W_B IG_B$$

$$\Rightarrow \frac{10}{20} (0.28) + \frac{10}{20} (0.28) = 0.28$$

Best split \Rightarrow

Feature	IG
Height	0.127
Class	0.28

→ Chi-square (χ^2) → quality comparison

→ Mostly when more categorical variables are present

Purity Index =

homogeneity

↑ χ^2 ↑ Homogeneity

⇔
Pure Node

$$\chi^2 = \frac{(\text{Actual} - \text{Expected})^2}{\text{Expected}}$$

$$\chi = \sqrt{\frac{(\text{Actual} - \text{Expected})^2}{\text{Expected}}}$$

colors of 2 car

C₁ C₂
(Red) (Red)

Same = Green

↓
high value of
Chi-square

Cheng Red

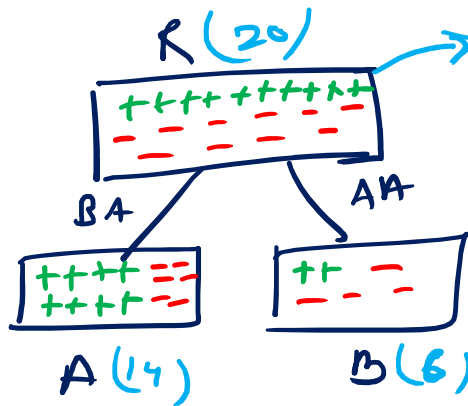
Brick Red

↓
down value of
Chi-sq.

→ Split on Performance based on Chi-Square

χ is calc for node
per class

$$\begin{aligned} E(+ve) &= 7 \\ E(-ve) &= 7 \\ A(+ve) &= 8 \\ A(-ve) &= 6 \end{aligned}$$



$$\frac{10}{10} = \frac{1:1}{1}$$

Expected for the child

$$\begin{aligned} \text{Exp}(+ve) &= 3 \\ \text{Exp}(-ve) &= 3 \\ A(+ve) &= 2 \\ A(-ve) &= 4 \end{aligned}$$

$$\chi = \sqrt{\frac{(Act - Exp)^2}{Exp}}$$

$$\chi_{A+ve} = \sqrt{\frac{(8-7)^2}{7}} \Rightarrow 0.38$$

$$\chi_{B+ve} = \sqrt{\frac{(2-3)^2}{3}} \Rightarrow 0.57$$

$$\chi_{A-ve} = \sqrt{\frac{(6-7)^2}{7}} \Rightarrow 0.38$$

$$\chi_{B-ve} = \sqrt{\frac{(4-3)^2}{3}} \Rightarrow 0.57$$

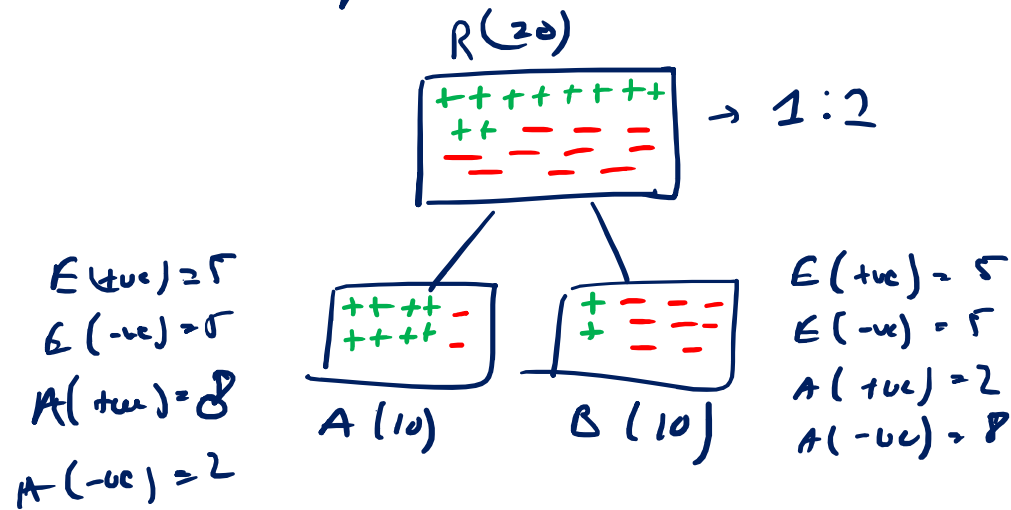
$\chi_{\text{split}} = \text{Sum of } \chi \text{ of all the nodes}$

$$\Rightarrow \chi_{A+ve} + \chi_{A-ve} + \chi_{B+ve} + \chi_{B-ve}$$

$$\Rightarrow 0.38 + 0.38 + 0.57 + 0.57$$

$$\Rightarrow \boxed{1.9 = \chi_{\text{perf}}}$$

→ split on class based on, chi-square



$$\chi = \sqrt{\frac{(A-E)^2}{E}}$$

$$\chi_{A(+ve)} = \sqrt{\frac{(8-5)^2}{5}} \Rightarrow 1.34$$

$$\chi_{B(+ve)} = \sqrt{\frac{(2-5)^2}{5}} \Rightarrow 1.34$$

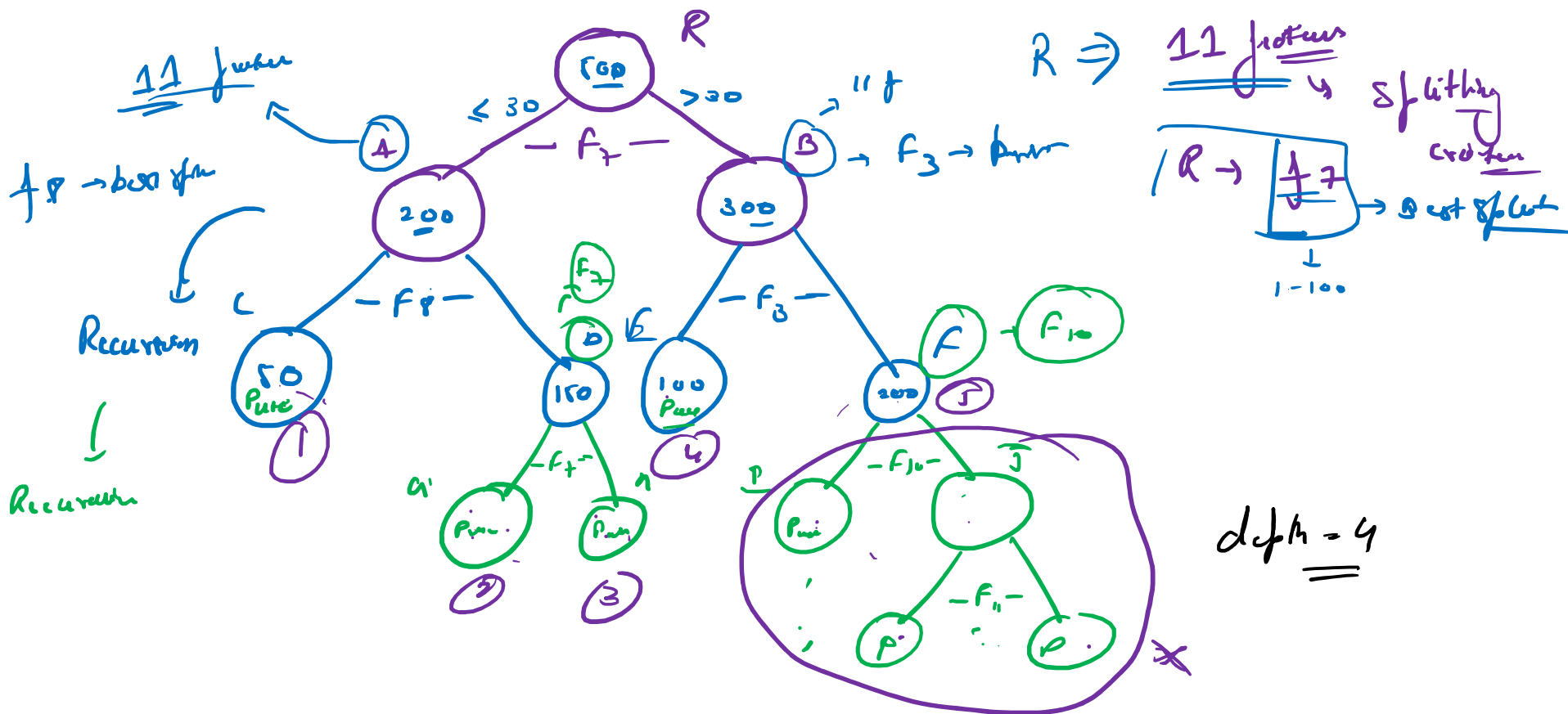
$$\chi_{\text{class}} = 1.34 + 1.34 + 1.34 + 1.34 \Rightarrow 5.36$$

$$\chi_{A(-ve)} = \sqrt{\frac{(2-5)^2}{5}} \Rightarrow 1.34$$

$$\chi_{B(-ve)} = \sqrt{\frac{(8-5)^2}{5}} \Rightarrow 1.34$$

Bought ⇒

John	JK
Pey	1.9
Ches	5.36



$$df_M = 4$$

→ (Hyperparameters) MLA can be customized on the behaviour of execution

→ depth = 2, 3, 7... Defaults

→ Perform/quality

Text, Train

→ min sample for a node to split = 12, 10, 8

→ min " for a terminal node = 8, 5, 11

→ Max no. of terminal nodes = 5

Pruning → OS.

controlling the growth of the tree

Default stopping rules

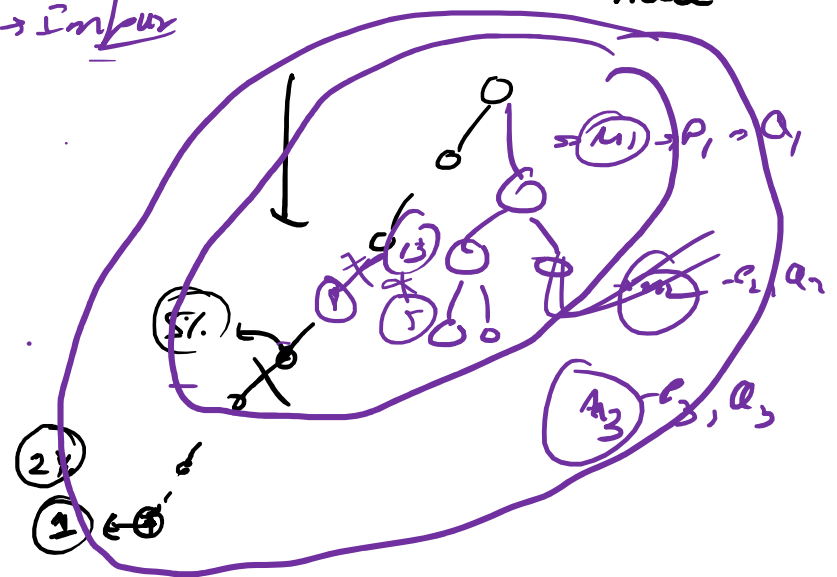
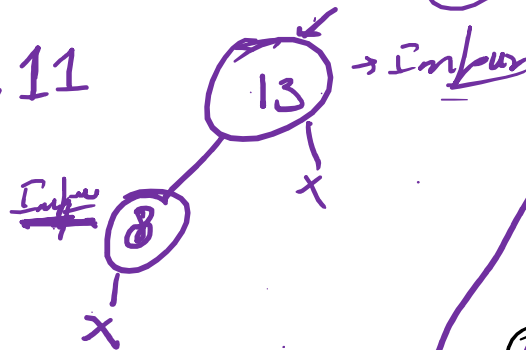
Whenever a node becomes pure the growth will stop

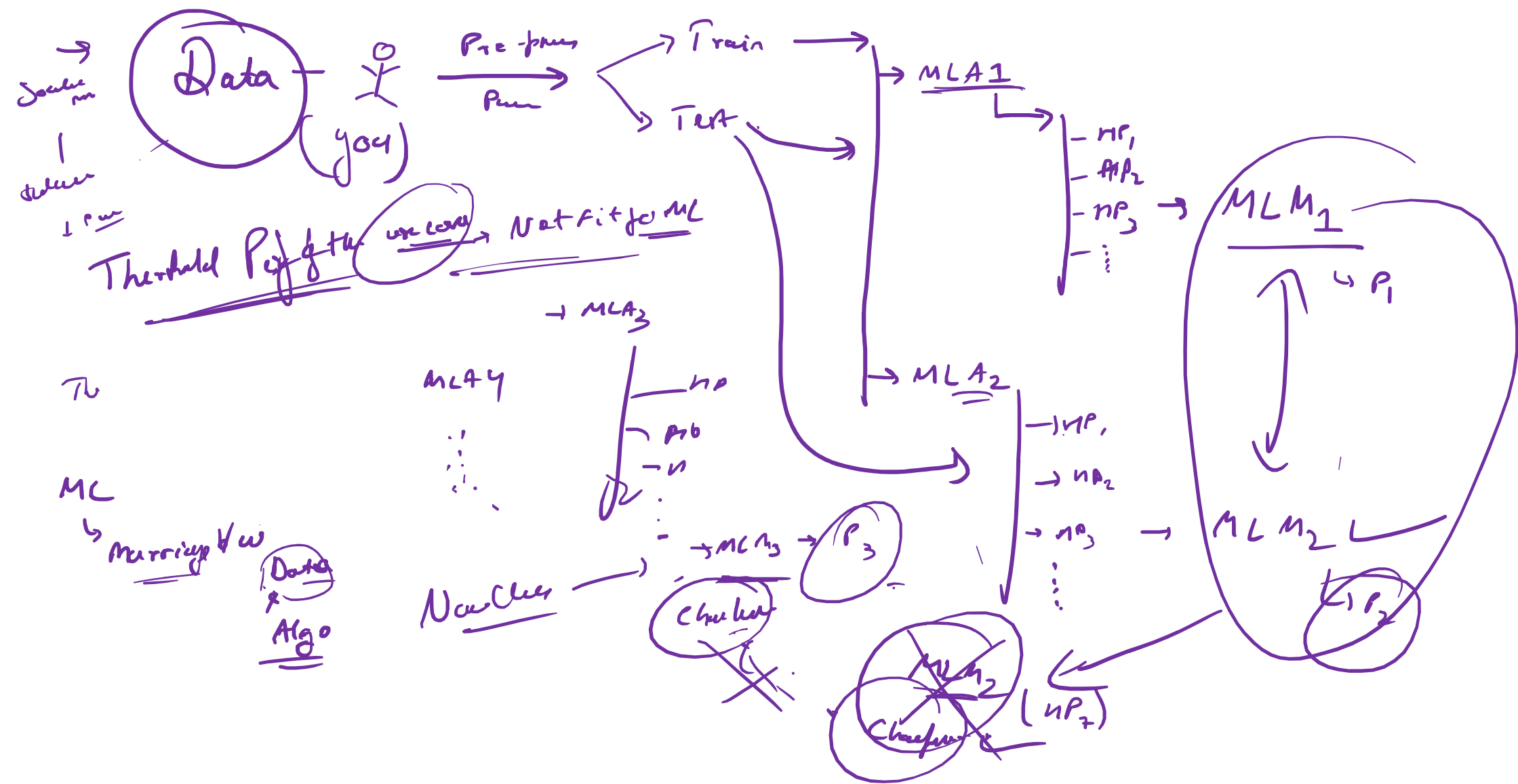
↓
If leafy can reach to a single row in one node

~~Only Training~~

2, 12	3, 12	7, 11
2, 10	3, 10	7, 10
2, 9	3, 9	7, 9

7, 12, 8





1- gr Data →

