Control Systems

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***Abstract*—This manual is an introduction to control systems based on GATE problems.Links to sample Python codes are available in the text.**

Download python codes using

```
svn co https://github.com/gadepall/school/trunk/
    control/codes
```

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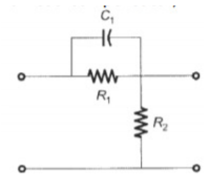
A lead Compensator network includes a parallel combination of R and C in feed-forward path. If the transfer function of compensator is

$$G_c(s) = \frac{s+2}{s+4}$$

, the value of RC is ?
Solution:



t

This is the circuit of lead compensator with parallel RC combination.

The transfer function for the following circuit is

$$T(s) = \frac{V_o}{V_i}$$

Let

$$\alpha = \frac{R_2}{R_1 + R_2}$$

and

$$\tau = R_1 C$$

Now our T(s) is

$$T(s) = \frac{R_2}{\frac{\frac{1}{sC}R1}{\frac{1}{sC}+R1} + R2}$$

Simplifying T(s)

$$T(s) = \frac{s + \frac{1}{\tau}}{s + \frac{1}{\tau\alpha}}$$

Comparing with the given

$$G_c(s) = \frac{s+2}{s+4}$$

$$\tau = R_1 C = 0.5$$

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