1 DataStructure

1.1 treap

```
1 struct Treap
       int pri, sz;
      int rev;
      11 data, sum; // tag: make-same
      Treap *lchild, *rchild;
      Treap(11 d):pri(rand()), sz(1), rev(0), data(d), sum(d),
           lchild(NULL), rchild(NULL)
      inline void up();
      inline void down();
12
  inline int size(Treap *t) { return t? t->sz:0; }
  inline 11 get data(Treap *t) { return t? t->data:0; }
  inline 11 get_sum(Treap *t) { return t? t->sum:0; }
17
   inline void Treap::up()
19
      if(lchild) lchild->down();
20
      if (rchild) rchild->down();
21
      sz = 1+size(lchild)+size(rchild);
23
      sum = get_sum(lchild) + data + get_sum(rchild);
24
25
  inline void Treap::down()
27
      if (rev)
28
29
           swap(mxpre, mxpost);
31
           swap(lchild, rchild);
          if(lchild) lchild->rev ^= 1;
32
           if(rchild) rchild->rev ^= 1;
33
           rev ^= 1;
34
35
36
   Treap *merge(Treap *a, Treap *b)
39
      if(!a || !b) return (a? a:b);
      if (a->pri < b->pri)
42
          a->down();
           a->rchild = merge(a->rchild, b);
          a->up();
           return a;
47
      else
          b->down();
          b->1child = merge(a, b->1child);
52
          b->up();
           return b;
54
   void split(Treap *o, Treap *&a, Treap *&b, int k)
```

```
if(!o) a = b = NULL;
60
       else
61
62
           o->down();
63
           if(k >= size(o->lchild)+1)
64
65
66
               split(o->rchild, a->rchild, b, k-size(o->lchild)
67
68
           else
69
70
               split(o->lchild, a, b->lchild, k);
72
73
           o->up();
74
75
```

1.2 disjoint set

```
1 // path compression
2 int f[N];
  int findrt(int x)
      if(f[x] == x) return x;
       else return f[x] = findrt(f[x]);
  int same(int x, int y)
10
11
12
      return findrt(x) == findrt(y);
13
14
15
   void uni(int x, int y)
16
17
      f[findrt(y)] = findrt(x);
18
20
  void init()
21
   for(int i = 0; i < N; i++) f[i] = i;</pre>
23
24
  //union by rank
  int f[N]; //disjoint set
27 int rk[N]; //union by rank
29
  int findrt(int x)
30
      if(f[x] == x) return x;
      else return f[x] = findrt(f[x]);
33
  bool same(int x, int y)
36
      return findrt(x) == findrt(y);
  void uni(int x, int y)
41
      x = findrt(x), y = findrt(y);
```

1.3 2d st tag

```
1 // 二維陣列單點查詢區間加值
2 class St1d
4 private:
     11 st[4*N];
7 public:
      void build():
      void modify(int 1, int r, int idx, int L, int R, 11 v);
      11 query(int 1, int r, int idx, int x);
      void down(int idx);
11
12 };
13
  void St1d::build()
15
      memset(st, 0, sizeof(st));
17
  void St1d::modify(int 1, int r, int idx, int L, int R, 11 v)
20
      if(r < L || R < 1) return;</pre>
21
      if(L <= 1 && r <= R)
22
23
^{24}
          st[idx] += v;
25
          return:
26
      assert(1 != r);
27
      down(idx);
28
29
      int mid = (1+r)/2;
      modify(1, mid, idx*2, L, R, v);
      modify(mid+1, r, idx*2+1, L, R, v);
  11 St1d::query(int 1, int r, int idx, int x)
35
36
      if(x < 1 || r < x) return 0;
      if(1 == x && r == x) return st[idx];
      down(idx);
      int mid = (1+r)/2;
      11 left = query(1, mid, idx*2, x);
      11 right = query(mid+1, r, idx*2+1, x);
      return left+right;
43
  void St1d::down(int idx)
      st[idx*2] += st[idx], st[idx*2+1] += st[idx];
      st[idx] = 0;
49 }
```

```
sort(tmp.begin(), tmp.end());
                                                                                                                                         st[idx].mul = 1, st[idx].add = 0;
                                                                        for(int i = 1; i <= n; i++) a[i] = lower bound(tmp.begin 35</pre>
                                                                                                                                         if(1 == r)
   class St2d
                                                                             (), tmp.end(), a[i]) - tmp.begin() + 1;
53
                                                                                                                                  36
54
                                                                 12
                                                                                                                                  37
                                                                                                                                             st[idx].data = arr[1];
55 private:
                                                                 13
                                                                                                                                             return;
                                                                                                                                  38
      St1d st[4*N];
                                                                   void buildbit() //每個bit[x]紀錄[x-lowbit(x)+1, x]的總和
                                                                                                                                  39
57
                                                                                                                                         int mid = 1+(r-1)/2;
                                                                 15
  public:
                                                                                                                                        buildst(1, mid, idx*2);
58
                                                                       for(int i = 0; i < n; i++) bit[i] = arr[i]-arr[i-lowbit(i 41</pre>
      void build(int il, int ir, int idx);
                                                                                                                                        buildst(mid+1, r, idx*2+1);
      void modify(int il, int ir, int jl, int jr, int idx, int
                                                                                                                                         up(1, r, idx);
                                                                                                                                  43
           iL, int iR, int jL, int jR, 11 v);
                                                                                                                                  44
      11 query(int il, int ir, int jl, int jr, int idx, int i,
                                                                                                                                  45
                                                                   int sum(int x) //查詢[1,x]的總和
                                                                19
           int j);
                                                                                                                                  46 void add(int 1, int r, int idx, int L, int R, int v) //操作L,
                                                                 20
62
                                                                 21
                                                                       int rtn = 0;
63
                                                                       for(;x;x-=lowbit(x)) rtn += bit[x];
                                                                                                                                  47
   void St2d::build(int il, int ir, int idx)
                                                                       return rtn;
                                                                                                                                        if(r < L | | R < 1) return;
65
                                                                                                                                         if(L <= 1 && r <= R)
                                                                                                                                  49
                                                                 24
66
      st[idx].build();
                                                                 25
      if(i1 == ir) return:
67
                                                                                                                                             st[idx].add = (st[idx].add+v)%MD;
                                                                                                                                  51
                                                                    void modify(int x, int d) //把位置x的東西加上d
      int mid = (i1+ir)/2;
                                                                                                                                  52
                                                                                                                                             return;
                                                                 27
69
      build(il, mid, idx*2);
                                                                                                                                  53
                                                                 28
                                                                       for(;x<=n;x+=lowbit(x)) bit[x] += d;</pre>
      build(mid+1, ir, idx*2+1);
70
                                                                                                                                         down(1, r, idx);
71
                                                                                                                                         int mid = 1+(r-1)/2;
72
                                                                                                                                         add(1, mid, idx*2, L, R, v);
   void St2d::modify(int il, int ir, int jl, int jr, int idx,
                                                                                                                                         add(mid+1, r, idx*2+1, L, R, v);
       int iL, int iR, int jL, int jR, 11 v)
                                                                                                                                         up(1, r, idx);
                                                                   1.5 1d segTree tag
74
      if(ir < iL || iR < i1) return;</pre>
75
      if(iL <= il && ir <= iR)</pre>
76
                                                                                                                                     void mul(int 1, int r, int idx, int L, int R, int v)
                                                                                                                                  61
                                                                  1 //線段樹懶人標記:一維陣列區間加值區間乘值區間查詢總和
78
          st[idx].modify(jl, jr, 1, jL, jR, v); return;
                                                                   struct Node //data = data*mul+add;
                                                                                                                                         if(r < L || R < 1) return;
79
                                                                                                                                         if(L <= 1 && r <= R)
      int mid = (i1+ir)/2;
80
                                                                       11 data, mul, add;
                                                                                                                                  65
      modify(il, mid, jl, jr, idx*2, iL, iR, jL, jR, v);
                                                                                                                                             st[idx].add = st[idx].add*v%MD;
                                                                                                                                  66
      modify(mid+1, ir, jl, jr, idx*2+1, iL, iR, jL, jR, v);
82
                                                                                                                                  67
                                                                                                                                             st[idx].mul = st[idx].mul*v%MD;
                                                                   11 getval(int 1, int r, int idx)
83
                                                                                                                                             return:
   11 St2d::query(int il, int ir, int jl, int jr, int idx, int i
                                                                       return (st[idx].data*st[idx].mul%MD+(r-1+1)*st[idx].add%
                                                                                                                                        down(1, r, idx);
       , int i)
                                                                            MD)%MD;
                                                                                                                                         int mid = 1+(r-1)/2;
86
                                                                                                                                         mul(1, mid, idx*2, L, R, v);
87
      11 \text{ tot} = 0;
                                                                                                                                         mul(mid+1, r, idx*2+1, L, R, v);
      if(i < i1 || ir < i) return 0;</pre>
                                                                    void up(int 1, int r, int idx)
                                                                                                                                         up(1, r, idx);
      if(il <= i && i <= ir) tot += st[idx].query(jl, jr, 1, j) 13</pre>
                                                                       int mid = 1+(r-1)/2;
      if(i1 == i && ir == i) return tot;
                                                                       st[idx].data = (getval(1, mid, idx*2)+getval(mid+1, r,
90
                                                                 15
                                                                                                                                    11 guery (int 1, int r, int idx, int L, int R)
      int mid = (i1+ir)/2;
                                                                            idx*2+1))%MD;
       tot += query(i1, mid, j1, jr, idx*2, i, j);
92
                                                                 16
                                                                                                                                        if(r < L || R < 1) return 0;
      tot += query(mid+1, ir, jl, jr, idx*2+1, i, j);
                                                                                                                                         if(L <= 1 && r <= R)
                                                                                                                                  80
                                                                    void down(int 1, int r, int idx)
      return tot;
                                                                                                                                  81
                                                                 19
                                                                                                                                             return getval(1, r, idx);
                                                                                                                                  82
                                                                       st[idx].data = getval(1, r, idx);
                                                                                                                                  83
                                                                       int lson = idx*2, rson = idx*2+1;
                                                                 21
                                                                                                                                  84
                                                                                                                                        down(1, r, idx);
                                                                 22
                                                                       if(1 != r)
                                                                                                                                         int mid = 1+(r-1)/2;
                                                                 23
                                                                                                                                         return (query(1, mid, idx*2, L, R)+query(mid+1, r, idx
  1.4 BIT
                                                                            st[lson].mul = st[lson].mul*st[idx].mul%MD;
                                                                                                                                             *2+1, L, R))%MD;
                                                                            st[lson].add = (st[lson].add*st[idx].mul+st[idx].add) 87 }
                                                                 25
1 | #define lowbit(x) x&-x
                                                                            st[rson].mul = st[rson].mul*st[idx].mul%MD;
                                                                            st[rson].add = (st[rson].add*st[idx].mul+st[idx].add)
                                                                 27
3 int arr[N]; //紀錄前綴和
                                                                                                                                    1.6 1d segTree
4 int bit[N];
                                                                 29
                                                                       st[idx].mul = 1, st[idx].add = 0;
  | void conv(int a[], int n) //離散化
                                                                 30
                                                                                                                                   1 void buildst(int 1, int r, int idx) //1, r是st的區間
                                                                   void buildst(int 1, int r, int idx)
      vector<int> tmp;
```

if(1 == r)

for(int i = 1; i <= n; i++) tmp.push_back(a[i]);</pre>

```
st[idx] = arr[1];
           return;
       int mid = (1+r)/2;
       buildst(1, mid, idx*2);
10
       buildst(mid+1, r, idx*2+1);
       st[idx] = max(st[idx*2], st[idx*2+1]);
11
12
13
   ll query(int l, int r, int idx, int L, int R) //L,R是操作的
15
       if(r < L || R < 1) return -INF;</pre>
16
       if(L <= 1 && r <= R) return st[idx];</pre>
       int mid = (1+r)/2;
       return max(query(1, mid, idx*2, L, R), query(mid+1, r,
           idx*2+1, L, R));
20
21
   void modify(int 1, int r, int idx, int x, int v)
22
23
       if(r < x || x < 1) return;
       if(1 == r)
25
26
27
           st[idx] += v; return;
28
       int mid = (1+r)/2;
29
       modify(1, mid, idx*2, x, v);
       modify(mid+1, r, idx*2+1, x, v);
       st[idx] = max(st[idx*2], st[idx*2+1]);
32
```

1.7 Matrix

```
1 11 SZ, MOD;
  const int MAXSZ=105;
  struct Mat
5
       11 m[MAXSZ][MAXSZ];
       Mat() {memset(m, 0, sizeof(m));}
   Mat matMul(const Mat &A, const Mat &B)
       for(int i = 0; i < SZ; i++)</pre>
           for(int k = 0; k < SZ; k++)
                if (A.m[i][k]) for (int j = 0; j < SZ; j++)</pre>
                    rtn.m[i][j]+=(A.m[i][k]*B.m[k][j]);
       return rtn;
   //B is of size SZ
   vector<11> matMul(const Mat &A, const vector<11> &B)
       vector<11> rtn(SZ,0);
25
       for(int i = 0; i < SZ; i++)</pre>
           for(int j = 0; j < SZ; j++)</pre>
26
                rtn[i] = (rtn[i] + A.m[i] [j] *B[j]);
```

```
29
       return rtn;
30
31
   Mat matPow(Mat& M, 11 p)
34
       if(p == 0)
35
36
            for(int i=0;i<SZ;i++)iden.m[i][i]=1;</pre>
37
            return iden;
       if (p == 1) return M;
40
41
       Mat rtn = matPow(M, p/2);
42
       if (p&1) return matMul (matMul (rtn, rtn), M);
43
       else return matMul(rtn, rtn);
```

1.8 undo_disjoint_set

```
struct DisjointSet {
     // save() is like recursive
     // undo() is like return
     int n, fa[MXN], sz[MXN];
     vector<pair<int*,int>> h;
     vector<int> sp;
     void init(int tn) {
       for (int i=0; i<n; i++) sz[fa[i]=i]=1;</pre>
      sp.clear(); h.clear();
11
12
     void assign(int *k, int v) {
13
      h.PB({k, *k});
14
       *k=v;
15
16
     void save() { sp.PB(SZ(h)); }
17
     void undo() {
18
      assert(!sp.empty());
19
       int last=sp.back(); sp.pop_back();
20
       while (SZ(h)!=last) {
        auto x=h.back(); h.pop_back();
22
         *x.F=x.S;
23
24
     int f(int x) {
      while (fa[x]!=x) x=fa[x];
27
       return x;
28
     void uni(int x, int y) {
      x=f(x); y=f(y);
       if (x==y) return ;
      if (sz[x] < sz[y]) swap(x, y);
      assign(&sz[x], sz[x]+sz[y]);
      assign(&fa[y], x);
35
36 } dis;
```

2 Flow

2.1 dinic

```
1 template<typename T>
  struct DINIC{
    static const int MAXN=105;
     static const T INF=INT MAX;
     int n, level[MAXN], cur[MAXN];
     struct edge {
      int v.pre;
      T cap,flow,r;
       edge(int v,int pre,T cap):v(v),pre(pre),cap(cap),flow(0),
10
    int q[MAXN];
11
     vector<edge> e;
     void init(int n) {
      memset(g,-1, sizeof(int)*((n=_n)+1));
15
      e.clear();
16
17
     void add_edge(int u,int v,T cap,bool directed=false) {
      e.push_back(edge(v,g[u],cap));
19
      g[u] = e.size() - 1;
20
      e.push_back(edge(u,g[v],directed?0:cap));
21
      q[v]=e.size()-1;
22
23
     int bfs(int s,int t){
24
      memset(level,0,sizeof(int)*(n+1));
25
       memcpy(cur,g,sizeof(int)*(n+1));
26
       queue<int> q;
27
      q.push(s);
28
       level[s]=1;
29
       while(g.size()){
         int u=q.front();q.pop();
31
         for (int i=g[u];~i;i=e[i].pre) {
32
           if(!level[e[i].v]&&e[i].r){
             level[e[i].v]=level[u]+1;
33
34
             q.push(e[i].v);
             if(e[i].v==t)return 1;
35
36
37
38
39
      return 0;
40
    T dfs(int u,int t,T cur_flow=INF) {
      if (u==t) return cur_flow;
43
44
       for (int &i=cur[u]; ~i; i=e[i].pre) {
         if (level[e[i].v] ==level[u] +1&&e[i].r) {
           if (df=dfs(e[i].v,t,min(cur_flow,e[i].r))) {
47
             e[i].flow+=df;
             e[i^1].flow-=df;
48
             e[i].r-=df;
             e[i^1].r+=df;
51
             return df;
52
53
54
      return level[u]=0;
    T dinic(int s, int t, bool clean=true) {
      if (clean) {
```

```
for(size_t i=0;i<e.size();++i){</pre>
                                                                                             f=dfs(v,e[i].flow>minflow-flow?minflow-flow:e111
                                                                                                                                                         dfs1(start);
            e[i].flow=0;
                                                                                                                                                         printf("%d \setminus n", sum);
                                                                                                   [i].flow);
            e[i].r=e[i].cap;
                                                                                              flow+=f:
                                                                                                                                                         for (i=1; i<=n; i++)</pre>
61
                                                                        49
                                                                                                                                                113
                                                                                             e[i].flow-=f;
62
                                                                        50
                                                                                                                                                           if(vis[i]==true)//残留网络中源点能到达的点
                                                                                                                                                114
63
                                                                        51
                                                                                             e[i^1].flow+=f;
                                                                                                                                                115
                                                                                                                                                             printf("%d \setminus n",i);
                                                                                             if (minflow-flow<=1e-8) return flow;</pre>
       T ans=0, mf=0;
                                                                                                                                                116
65
       while(bfs(s,t))while(mf=dfs(s,t))ans+=mf;
                                                                        53
                                                                                             if (dis[start]>=ans)return flow;
                                                                                                                                                117
                                                                                                                                                      return 0;
       return ans;
                                                                        54
66
                                                                                                                                                118 }
67
                                                                        55
                                                                        56
```

if (--gap[dis[u]]==0)

double maxflow=0.0:

while(dis[start] < ans)</pre>

return 1.0*m-maxflow;

double Left, Right, mid, flow;

mid=(Left+Right)/2;

for(i=0;i<m;i++)</pre>

Left=0;Right=m;

makemap(mid);

Right=mid;

else Left=mid;

dis[u]++;

double isap()

gap[dis[u]]++;

return flow:

gap[0]=ans;

void dfs1(int u)

vis[u]=true;

S11m++:

int main()

int i:

if (u>=1&&u<=n)

int v=e[i].ed;

dfs1(v);

dis[start]=ans;

57

58

59

60

61

62

63

64

65

66

67

71

72

74

75

77

78

79

80

84

86

89

90

91

92

93

94

95

96

97

98

99

2.2 MaxDensitySubgraph

```
1 | #include < stdio.h>
  #include<string.h>
  const int N=1500;
  const double inf=0x3ffffffff;
  const double eps=1e-8;
6 int gap[N].dis[N].start.end.ans.sum.head[N].num.dep[N].n.m;
7 bool vis[N]:
  struct edge
9
    int st,ed,next;
    double flow;
  }e[80*N];
   struct node
14
    int x,y;
   }P[1100];
   void addedge(int x,int y,double w)
18
    e[num].st=x;e[num].ed=y;e[num].flow=w;e[num].next=head[x];
          head[x]=num++;
20
    e[num].st=y;e[num].ed=x;e[num].flow=0;e[num].next=head[y];
          head[v]=num++;
21
   void makemap(double g)
23
    int i;
25
    memset(head, -1, sizeof(head));
26
    for (i=1; i<=n; i++)</pre>
28
       addedge(i,end,g);
29
     for (i=0; i < m; i++)</pre>
30
31
       addedge(n+i+1,P[i].y,inf);
       addedge(n+i+1,P[i].x,inf);
32
       addedge(start,n+i+1,1.0);
   double dfs(int u, double minflow)
                                                                    100
                                                                    101
       if (u==end) return minflow;
                                                                    102
       int i.v;
                                                                    103
       double f,flow=0.0;
                                                                    104
       for(i=head[u];i!=-1;i=e[i].next)
                                                                    105
                                                                    106
           v=e[i].ed;
                                                                    107
           if(e[i].flow>0)
                                                                    108
45
                                                                    109
               if (dis[v]+1==dis[u])
46
```

```
2.3 MinCostMaxFlow
```

```
1 template<typename TP>
                                                                struct MCMF {
                                                                  static const int MAXN=440;
                                                                  static const TP INF=999999999;
                                                                  struct edge {
 memset(gap,0,sizeof(gap));
                                                                    int v.pre;
 memset(dis,0,sizeof(dis));
                                                                     TP r, cost;
                                                                     edge(int v,int pre,TP r,TP cost):v(v),pre(pre),r(r),cost(
     maxflow+=dfs(start.inf):
                                                                  };
                                                                  int n.S.T:
                                                              10
                                                                   TP dis[MAXN], PIS, ans;
                                                              11
                                                                  bool vis[MAXN];
                                                              12
                                                              13
                                                                  vector<edge> e;
                                                              14
                                                                   int q[MAXN];
                                                                   void init(int _n) {
                                                              16
                                                                     memset(g, -1, sizeof(int) * ((n=_n) +1));
for(int i=head[u];i!=-1;i=e[i].next)
                                                              17
                                                                     e.clear();
                                                              18
                                                              19
                                                                   void add_edge(int u,int v,TP r,TP cost,bool directed=false)
 if (vis[v] ==false&&e[i].flow>0)
                                                              20
                                                                     e.push_back(edge(v,g[u],r,cost));
                                                              21
                                                                     g[u] = e.size() - 1;
                                                              22
                                                                     e.push back (
                                                              23
                                                                     edge(u,g[v],directed?0:r,-cost));
                                                              24
                                                                     g[v] = e.size() - 1;
                                                              25
                                                              26
                                                                   TP augment (int u, TP CF) {
while (scanf ("%d%d", &n, &m)!=-1)
                                                                     if (u==T||!CF) return ans+=PIS*CF, CF;
                                                              27
                                                              28
                                                                     vis[u]=1;
                                                              29
                                                                     TP r=CF.d:
 if (m==0) {printf("1\n1\n");continue;}
 start=0,end=n+m+1,ans=end+1;
                                                                     for (int i=q[u];~i;i=e[i].pre) {
                                                              31
                                                                       if(e[i].r&&!e[i].cost&&!vis[e[i].v]){
                                                              32
                                                                         d=augment(e[i].v,min(r,e[i].r));
   scanf("%d%d",&P[i].x,&P[i].y);
                                                                         e[i].r-=d;
                                                              34
                                                                         e[i^1].r+=d;
                                                                         if(!(r-=d))break;
  while (Right-Left>=1.0/n/n) //胡伯涛的论文给出了证明,不同解 36
       之间误差的精度不超过1/(n*n)
                                                                     return CF-r;
                                                              39
                                                                   bool modlabel() {
                                                                     for (int u=0; u<=n; ++u) dis[u] =INF;</pre>
    flow=isap();//求出最大权值闭合图
                                                                     static deque<int>q;
   if (flow<eps) //如果小于0、q值太大
                                                                     dis[T]=0,q.push_back(T);
                                                                     while(g.size()){
                                                                       int u=q.front();q.pop_front();
 makemap(Left);//最大密度建图
                                                              47
                                                                       for (int i=g[u];~i;i=e[i].pre) {
                                                                         if (e[i^1].r&&(dt=dis[u]-e[i].cost) < dis[e[i].v]) {</pre>
                                                              48
  memset(vis, false, sizeof(vis));
                                                                           if ((dis[e[i].v]=dt) <= dis[g.size()?g.front():S]) {</pre>
                                                                             q.push_front(e[i].v);
```

```
}else q.push_back(e[i].v);
52
53
54
55
       for(int u=0;u<=n;++u)</pre>
         for(int i=g[u];~i;i=e[i].pre)
57
           e[i].cost+=dis[e[i].v]-dis[u];
58
       return PIS+=dis[S], dis[S]<INF;</pre>
59
60
     TP mincost(int s,int t) {
61
       S=s, T=t;
62
       PIS=ans=0;
       while (modlabel()) {
         do memset(vis,0,sizeof(bool)*(n+1));
65
         while(augment(S,INF));
66
       } return ans;
67
```

3 Geometry

3.1 nearestDist

```
1 bool cmp_y(P a, P b)
       return a.y < b.y;</pre>
  bool cmp_x(P a, P b)
       return a.x < b.x;</pre>
   double dc(P *arr, int n)
       if (n == 1) return INF;
       int mid = n/2;
       double cx = arr[mid].x;
       double dist = min( dc(arr, mid), dc(arr+mid, n-mid) );
       inplace_merge(arr, arr+mid, arr+n, cmp_y);
       static vector<P> brr; brr.clear();
       for(int i = 0; i < n; i++)</pre>
19
20
           if (fabs(arr[i].x)-cx >= dist) continue;
22
           for(int j = brr.size()-1; j >= 0; j--)
23
24
               double dx = brr[j].x-arr[i].x;
25
               double dy = brr[j].y-arr[i].y;
               if (fabs(dy) >= dist) break;
               dist = min(dist, sqrt(dx*dx+dy*dy));
27
28
29
           brr.push back(arr[i]);
30
       return dist;
32
   double nearestDist(P *arr, int n)
       sort(arr, arr+n, cmp x);
       return dc(arr, n);
```

3.2 SegmentGeometry

```
1 double EPS = 1e-10;
                                                                      63
   double add(double a, double b)
      if (abs (a+b) < EPS* (abs (a) + abs (b) ) ) return 0;</pre>
       else return a+b;
                                                                      67
                                                                      69
   struct P//struct for 2d vector/point
                                                                     70
10
                                                                     71
11
       double x.v:
                                                                      72
12
       P() {}
                                                                      73
13
       P(double x, double y):x(x),y(y) {}
                                                                     74
       P operator+(P p) {return P(add(x,p.x), add(y,p.y));}
14
                                                                      75
15
       P operator - (P p) {return P(add(x, -p.x), add(y, -p.y));}
       P operator*(double d) {return P(x*d, v*d):}
16
       double dot(P p) {return add( x*p.x, y*p.y );}
17
                                                                     78
18
       double det(P p) {return add( x*p.y, -y*p.x );}
                                                                      79
19
20
21
   //is point q on p1p2
                                                                      82
  bool on_seg(P p1, P p2, P q) {return (p1-q).det(p2-q) == 0 && (p1-
       a).dot(p2-a) <= 0;
24 P intersection (P p1, P p2, P q1, P q2) //p and q Must not be
                                                                     86
   {return p1 + (p2-p1)*((q2-q1).det(q1-p1)/(q2-q1).det(p2-p1))
                                                                      90
27 bool par (P p1, P p2, P p3, P p4) {return (p2-p1).det(p4-p3)
                                                                     91
                                                                      92
                                                                      93
29 bool operator < (const P& lhs, const P& rhs)
                                                                     94
   {return (lhs.x==rhs.x)?lhs.y<rhs.y:lhs.x<rhs.x;}
                                                                      95
  bool operator == (const P& lhs, const P& rhs)
   {return lhs.x==rhs.x&&lhs.y==rhs.y;}
                                                                      97
                                                                     98
35
   double len(P vec)
                                                                     99
   {return sqrt(add(vec.x*vec.x, vec.y*vec.y));}
                                                                     100
                                                                     101
   double dis(P p1, P p2)
                                                                     102
39
   {return len(p2-p1);}
                                                                     103
40
41
   struct seq
42
      seg(){}
       seg(P _p1, P _p2)
                                                                     108
45
                                                                     109
           p[0] = p1;
47
           p[1] = p2;
48
           if (p[1] < p[0]) swap(p[0], p[1]);</pre>
49
                                                                     113
      P p[2];
53 bool par(seg& lhs, seg& rhs)
   {return par(lhs.p[0],lhs.p[1],rhs.p[0],rhs.p[1]);}
  P intersection(seg& lhs, seg& rhs)//p and q Must not be
                                                                     120
   {return intersection(lhs.p[0],lhs.p[1],rhs.p[0],rhs.p[1]);}
```

```
59 bool on_seg(seg& sg, P g)
   {return on seg(sg.p[0],sg.p[1],g);}
   bool overlap(seg s1, seg s2)
       return par(s1,s2)&&
       (on seg(s1, s2.p[0]) | lon <math>seg(s1, s2.p[1]) | l
       on seg(s2, s1.p[0]) | lon seg(s2, s1.p[1]);
   bool is intersect(seg s1, seg s2)
       if(par(s1,s2))return false;
       P p0 = intersection(s1,s2);
       return on_seg(s1,p0)&&on_seg(s2,p0);
    //make sure the vec is not vertical
   double interpolate (seq& vec. double X)
       double y0=vec.p[0].y,y1=vec.p[1].y,
       x0=vec.p[0].x,x1=vec.p[1].x;
       return v0+(v1-v0)*(X-x0)/(x1-x0);
   //pts in clockwise order, p[N]=p[0]
   bool in poly(P* pol, int N, P pt)
       double X = pt.x,Y=pt.y;
       int pas=0;
       for(int i=0;i<N;i++)</pre>
            if (pol[i].x==pol[i+1].x) continue;
            seg s0(pol[i],pol[i+1]);
            //up or down?
            double Y1 = interpolate(s0,X);
            if (Y1<Y-EPS) continue;</pre>
            double xl=min(pol[i].x,pol[i+1].x),xr=max(pol[i].x,
                pol[i+1].x);
            if (x1<X-EPS&&xr>=X-EPS) pas++;
       return pas&1;
   double dpseg(P p, P p1, P p2)//p to p1p2, p1!=p2
       P v=p2-p1, v1=p-p1, v2=p-p2;
       if( v.dot(v1) < EPS )return dis(p,p1);</pre>
       if( v.dot(v2) > EPS )return dis(p,p2);
       return fabs((p-p1).det(v))/len(v);
110 double dpseg(P p, seg s1)
       return dpseg(p,s1.p[0],s1.p[1]);
   double dsegseg(P p1, P p2, P p3, P p4)
       if( is_intersect( seg(p1,p2), seg(p3,p4) ) ) return 0;
       return min( min( dpseg(p1,p3,p4),dpseg(p2,p3,p4) ), min(
            dpseq(p3,p1,p2),dpseq(p4,p1,p2));
121 double dsegseg(seg s1, seg s2)
```

```
Graph
```

1 int d[N][N];

124

flovd warshall

```
void init()
       for(int i = 0; i < v; i++)</pre>
            for(int j = 0; j < v; j++)</pre>
                if(i == j) d[i][j] = 0;
                else d[i][j] = INF;
   void floyd warshall()
12
       for(int k = 0; k < v; k++)
13
14
            for(int i = 0; i < v; i++)</pre>
15
                for(int j = 0; j < v; j++)</pre>
                     if (d[i][k] != INF && d[k][j] != INF)
16
                         d[i][j] = min(d[i][j], d[i][k] + d[k][j]) 11
17
18
```

return dsegseg(s1.p[0],s1.p[1],s2.p[0],s2.p[1]);

4.2 mst prim

```
1 int cost[100][100];
2 bool used[100];
3 int mincost[100];
4 int v, e;
   #define INF 2147483647
   int prim()
       for(int i = 0; i < v; i++)</pre>
           mincost[i] = INF;
12
           used[i] = false;
       mincost[0] = 0;
       int res = 0;
17
       while(true)
19
           int x = -1;
           for(int u = 0; u < v; u++)
20
               if (!used[u] && (x == -1 || mincost[u] < mincost[x 37</pre>
                    ])) x = u;
           if(x == -1) break;
           used[x] = true;
           res += mincost[x];
26
           for(int u = 0; u < v; u++)
27
               mincost[u] = min(mincost[u], cost[x][u]);
```

```
30
       return res;
31
32
33
   void init()
34
35
       for(int i = 0; i < v; i++)</pre>
            for(int j = 0; j < v; j++)
36
37
                if(i == j) cost[i][j] = 0;
                else cost[i][j] = INF;
38
```

vector<int> link[MAX_N]; //edge

const int MAX N;

4.3 HeavyLightDecomposition

```
void dfs build(int now, int fa, int *weight, int *depth, int
        *pa, int *son)
     weight[now]=1;
     son[now] = -1:
     pa[now]=fa;
     for(auto i:link[now])
10
      if(i==fa) continue;
12
       depth[i] =depth[now]+1;
13
       dfs_build(i,now,weight,depth,pa,son);
14
       if (son[now] == -1 | | weight[son[now]] < weight[i]) son[now] = i;</pre>
15
       weight[now] +=weight[i];
16
17
   void build_top(int now, int top,int *pa, int *son, int *
       link_top)
19
20
     link_top[now] = top;
     if (son[now] == -1) return;
22
     build_top(son[now],top,pa,son,link_top);
23
     for(auto i:link[now])
24
25
       if (i==son[now] | |i==pa[now]) continue;
26
      build_top(i,i,pa,son,link_top);
27
28
   inline void HLD(int *weight, int *depth, int *pa, int *son,
        int *link_top)
30
     memset(son, -1, sizeof(int) *MAX_N);
     depth[1]=1; //set node(1) as root
     dfs_build(1,0,weight,depth,pa,son);
    build_top(1,1,pa,son,link_top);
35
   inline int find_lca(int x, int y, int *depth, int *pa, int *
     int tx=link_top[x], ty=link_top[y];
     while(tx!=tv)
40
41
       if (depth[tx] <depth[ty])</pre>
42
43
         swap(tx,ty);
44
         swap(x,y);
```

```
tx=link_top[x=pa[x]];
47
     return depth[x] < depth[y] ?x:y;</pre>
48
49
50
   //build HeavyLightDecomposition: HLD
51
52 //find LCA(x, y): find lca
```

匹配問題轉換

4.4.1 一般圖匹配問題轉換

1. | 最大匹配邊數 | + | 最小邊涵蓋 | = | V | (無孤立點) 2. | 最大獨立集 | + | 最小點涵蓋 | = | V | 3. 最大權匹配-> 最大權完美匹配: 用 0 邊補成完全圖

4. 最大權最大匹配-> 最大權匹配: 先把所有邊加上 | 最負邊權重 |+1,得到 新的圖 G'上沒有任何負邊,然後所有邊再加上 G'上所有邊權重和,這樣 最大權匹配就會 = 最大權最大匹配.

TarjanBridge

```
1 void tarjan(int u, int p) { // p -> u
       dfn[u] = low[u] = ++tim;
       for (auto v: G[u]) { //u -> v
           if(!dfn[v]){
               tarjan(v, u);
               low[u] = min(low[u], low[v]);
               if(low[v] > dfn[u]){
                    E.push back(edge(u ,v));
11
12
           else if(v != p)
13
14
               low[u] = min(low[u], dfn[v]);
15
16
17
  struct edge {
18
19
       int from, to;
       edge(int u, int v):
20
            from(u), to(v) {}
21
22 };
23 for (int i=0; i<n; i++)
24
    if(!dnf[i])
      tarjan(i, -1);
```

4.6 BridgeConnected

```
1 struct edge {
      edge(int u, int v):from(u), to(v){}
5 vector<edge> bridge;
6 vector<int> G[MAXN];
7 int dfn [MAXN], low [MAXN], tim;
8 int bccID[MAXN], bccCNT;
9 int st[MAXN], top;
```

```
void tarjan(int u, int p) { // p->u
       dfn[u] = low[u] = ++tim;
       st[top++] = u;
13
       for (auto v:G[u]) { // u->v
14
           if(!dfn[v]){
16
                tarian(v, u);
                low[u] = min(low[u], low[v]);
17
                if (low[v] > dfn[u])
                   bridge.push back(edge(u, v));
19
20
           else if(v != p)
21
                low[u] = min(low[u], dfn[v]);
22
23
24
25
       if(dfn[u] == low[u]) {
26
           int w;
27
28
                w= st[--top];
                bccID[w] = bccCNT;
29
30
           }while(w != u);
           bccCNT++;
31
32
33
```

4.7 mst_kruskal

```
1 struct edge { int u, v, cost; };
  bool comp(const edge& e1, const edge& e2)
       return e1.cost < e2.cost;</pre>
   int kruskal()
       sort(es, es + e, comp);
       dset s(v);
       int res = 0;
       for(int i = 0; i < e; i++)</pre>
14
           edge E = es[i];
           if(s.Find(E.u) != s.Find(E.v))
17
                s.Union(E.u, E.v);
18
19
                res += E.cost;
20
22
       return res;
```

4.8 bellman Ford

```
1 struct edge{ int from, to, cost; };
2 #define INF 2147483647
3 
4 edge es[100];
5 
int d[100]; //min distance
7 int V, E, s, f;
```

```
stk.pop_back();
   bool bellman ford() // return true if there is negative loop 35
                                                                            return false;
10
       for(int i = 0; i < V; i++) d[i] = INF;</pre>
11
                                                                     37
                                                                          int solve() {
12
       d[s] = 0;
                                                                            // find a match
                                                                            for (int i=0; i<n; i+=2) {</pre>
13
14
       for(int i = 0; i < V; i++)</pre>
                                                                     40
                                                                              match[i] = i+1, match[i+1] = i;
15
                                                                     41
16
           for(int j = 0; j < E; j++)</pre>
                                                                     42
                                                                            for(;;) {
17
                                                                              int found = 0;
18
               edge e = es[i];
                                                                     44
                                                                              for (int i=0; i<n; i++) dis[i] = onstk[i] = 0;</pre>
               if (d[e.from] != INF && d[e.to] > d[e.from] + e.
                                                                              for (int i=0; i<n; i++) {</pre>
19
                                                                                stk.clear();
20
                                                                     47
                                                                                if (!onstk[i] && SPFA(i)){
21
                   d[e.to] = d[e.from] + e.cost;
                                                                     48
                                                                                  found = 1;
22
                    if(i == V - 1) return true; //got neg loop
                                                                                  while (stk.size()>=2) {
23
                                                                                    int u = stk.back(); stk.pop_back();
24
                if (d[e.to] != INF && d[e.from] > d[e.to] + e.cost 51
                                                                                    int v = stk.back(); stk.pop_back();
                                                                                    match[u] = v;
                                                                     52
                                                                                    match[v] = u;
25
                                                                     53
26
                   d[e.from] = d[e.to] + e.cost;
                                                                     54
                   if(i == V - 1) return true; //got neg loop
27
                                                                     55
28
                                                                     56
29
                                                                     57
                                                                              if (!found) break;
30
                                                                     58
31
       return false:
                                                                     59
                                                                            int ret = 0;
                                                                            for (int i=0; i<n; i++)</pre>
                                                                     60
                                                                              ret += edge[i][match[i]];
                                                                            ret /= 2;
                                                                            return ret;
  4.9 MaxWeightPerfectMatch
                                                                     65 } graph;
```

```
// Minimum General Weighted Matching (Perfect Match) 0-base
     static const int MXN = 105;
    int n, edge[MXN][MXN];
    int match[MXN], dis[MXN], onstk[MXN];
    vector<int> stk:
    void init(int _n) {
      n = _n;
       for (int i=0; i<n; i++)</pre>
         for (int j=0; j<n; j++)</pre>
10
11
           edge[i][j] = 0;
12
    void add_edge(int u, int v, int w) {
14
      edge[u][v] = edge[v][u] = w;
15
16
    bool SPFA(int u) {
17
      if (onstk[u]) return true;
18
      stk.push_back(u);
       onstk[u] = 1;
19
       for (int v=0; v<n; v++) {</pre>
         if (u != v \&\& match[u] != v \&\& !onstk[v]) {
           int m = match[v];
           if (dis[m] > dis[u] - edge[v][m] + edge[u][v]){
             dis[m] = dis[u] - edge[v][m] + edge[u][v];
             onstk[v] = 1;
             stk.push_back(v);
             if (SPFA(m)) return true;
             stk.pop_back();
29
             onstk[v] = 0;
30
31
32
```

1 struct Graph {

onstk[u] = 0;

4.10 StronglyConnectedComponent

```
1 int V, E;
vector<int> G[MAXV];
3 vector<int> rG[MAXV];
 4 vector<int> vs;//postorder
5 bool used[MAXV];
6 int comp[MAXV];//scc id, topologically ordered
8 void add_edge(int from, int to)
      G[from].pb(to);
      rG[to].pb(from);
  void dfs(int u)//get postorder
15
      used[u] = true;
       for(int i=0;i<G[u].size();i++)</pre>
           if(!used[G[u][i]])dfs(G[u][i]);
       vs.pb(u);
20
  void rdfs(int u, int k)
23
      used[u]=true;
       comp[u]=k;
       for (int i=0;i<rG[u].size();i++)</pre>
27
           if(!used[rG[u][i]])rdfs(rG[u][i],k);
```

```
int scc()//return scc cnt
31
32
       memset (used, 0, sizeof (used));
33
       vs.clear();
       FOR (v, 1, V) if (!used[v]) dfs(v);
34
35
       memset (used, 0, sizeof (used));
       int k = 0; //sccID
36
37
       FORD (i, V-1, 0)
            if(!used[ vs[i] ])
38
39
                rdfs(vs[i],k);
40
41
42
43
       return k:
44
```

4.11 MaxBiMatching

```
1 / / 注意: 變數 V
  #define MAXV 505
3 int V; //# of vertex
  vector<int> G[MAXV];
5 int match[MAXV];
  int used[MAXV];
   void add edge(int u, int v)
       G[u].pb(v);
       G[v].pb(u);
12
   bool dfs(int u)
       used[u]=true;
       for(int i = 0; i < G[u].size(); i++)</pre>
           int v = G[u][i], w = match[v];
19
           if (w<0 || !used[w] &&dfs(w) )</pre>
20
21
                match[u]=v;
23
                match[v]=u;
24
                return true;
25
26
       return false;
28
   int bip match()
       int res=0;
       memset(match, -1, sizeof(match));
       for(int v=0; v<V; v++)</pre>
35
           if (match[v]<0)</pre>
37
                memset(used, 0, sizeof(used));
38
                if (dfs(v))res++;
40
41
42
       return res;
43
```

4.12 dijkstra

```
struct edge{int to, cost;};
   typedef pair<int, int> P; //first = min distance, second = v
   #define f first
   #define s second
   #define INF 2147483647
   int V, E, S, F;
   vector<edge> G[100];
   int d[100];
12
   void dijkstra()
13
14
       priority_queue<P, vector<P>, greater<P>> q;
15
       fill(d, d + V, INF);
       d[S] = 0;
16
17
       g.push(P(0, S));
18
19
       while(!q.empty())
20
21
           P p = q.top(); q.pop();
22
           int v = p.s;
23
           if(d[v] < p.f) continue;</pre>
           for(int i = 0; i < G[v].size(); i++)</pre>
24
25
26
                edge e = G[v][i];
27
               if(d[e.to] > d[v] + e.cost)
28
29
                   d[e.to] = d[v] + e.cost;
                    q.push(P(d[e.to], e.to));
30
31
32
33
34
```

4.13 TwoConnected

```
1 vector<int> G[MAXN];
  vector<int> bcc[MAXN]; // bcc內的點
  int dfn[MAXN], low[MAXN], tim, ans;
  int st[MAXN], top;
6 int bccID[MAXN], bcc_cnt;// 每個點的bcc編號
7 bool is_cut[MAXN]; // 是否為割點, 割點的ID會被覆蓋
  void tarjan(int u, int p) { // p->u
      int child= 0, w;
      dfn[u] = low[u] = ++tim;
      st[top++] = u;
      for(auto v:G[u]) { // u->v
14
          if(!dfn[v]){
15
              tarjan(v, u); child++;
16
              low[u] = min(low[u], low[v]);
17
              if(low[v] >= dfn[u]){
18
                  is_cut[u] = true;
19
20
                      w = st[--top];
                      bccID[w] = bcc_cnt;
```

```
bcc[bcc_cnt].push_back(w);
                    }while(dfn[w] > dfn[v]);
23
                    bccID[u] = bcc cnt;
24
25
                    bcc[bcc_cnt++].push_back(u);
26
28
           else if(v != p)
               low[u] = min(low[u], dfn[v]);
29
30
31
32
       if(p == -1 && child<2)
33
           is cut[u] = false;
```

4.14 ArticulationPoint

```
1 | vector<int> G[MAXN];
2 int dfn[MAXN], low[MAXN], tim, ans;
  void tarjan(int u, int p) { // p -> u
       int child=0, cut node=0;
       dfn[u] = low[u] = ++tim;
       for (auto v:G[u]) { // u -> v
           if(!dfn[v]){ // tree edge
               tarjan(v, u); child++;
               low[u] = min(low[u], low[v]);
               if (low[v] >= dfn[u]) cut_node=1;
10
11
           else if(v!=p) //back edge
12
13
               low[u] = min(low[u], dfn[v]);
14
15
       if (p!=-1 && cut_node) ans++;
16
       if (p==-1 && child>=2) ans++;
17
18
19 //how to call
20 for (int i=0; i<n; i++)
21
    if(!dnf[i])
      tarjan(i, -1);
```

4.15 MaxWeightPerfectBiMatch

```
1 const int maxn = 500 + 3, INF = 0x3f3f3f3f3f;
1 int n, W[maxn] [maxn];
3 int mat[maxn];
 4 int Lx[maxn], Ly[maxn], slack[maxn];
5 bool S[maxn], T[maxn];
  inline void tension(int &a, const int b) {
      if(b < a) a = b;
11 inline bool match(int u) {
      S[u] = true;
       for (int v = 0; v < n; ++v) {
           if(T[v]) continue;
15
           int t = Lx[u] + Ly[v] - W[u][v];
           if(!t) {
17
               T[v] = true;
               if (mat[v] == -1 || match(mat[v])) {
18
                   mat[v] = u;
```

if ((P&(1LL<<j))&&(v[i]&(1LL<<j)))</pre>

for(int j = 0; j < i; j++)</pre>

30

31

```
return true:
21
22
           }else tension(slack[v], t);
23
24
       return false;
25
26
   inline void update() {
27
       int d = INF;
       for(int i = 0; i < n; ++i)
           if(!T[i]) tension(d, slack[i]);
30
       for(int i = 0; i < n; ++i) {</pre>
31
           if(S[i]) Lx[i] -= d;
32
33
           if (T[i]) Lv[i] += d;
34
35
36
   inline void KM() {
       for(int i = 0; i < n; ++i) {</pre>
           Lx[i] = Ly[i] = 0; mat[i] = -1;
39
40
           for (int j = 0; j < n; ++j) Lx[i] = max(Lx[i], W[i][j
41
42
       for(int i = 0; i < n; ++i) {</pre>
           fill(slack, slack + n, INF);
43
           while(true) {
44
                for(int j = 0; j < n; ++j) S[j] = T[j] = false;</pre>
45
                if (match(i)) break;
46
47
                else update();
48
49
```

4.16 MaximalClique

```
1 #define MAXN 32
  int n, m, Max;
  11 v [MAXN], deg [MAXN]; //neighbors
   void update maximum(11 R)
       int Size = 0;
       while (R)
10
           if (R&1) Size++;
           R >> = 1;
12
       Max = max(Size, Max);
14
   int pickPivot(11 P)
       int pivot = -1, Max = -1;
       memset(deg, 0, sizeof(deg));
       for(int i = 0; i < n; i++)</pre>
           if (P&(1LL<<i)) //i is in P
22
23
24
                if (pivot == -1) //i = default pivot
25
26
                    pivot = i;
                    Max = deg[i];
27
```

```
32
33
                          deg[i]++;
                          if (deg[i] > Max)
34
35
36
                              Max = deg[i];
37
                              pivot = i;
38
39
                          deg[i]++;
                          if (deg[j] > Max)
40
41
42
                              Max = deg[i];
43
                              pivot = j;
44
45
46
47
49
        return pivot;
   void BronKerbosch(11 R, 11 P, 11 X)
53
       if(!P) //P is empty, no candidates left
            if(!X)
57
                 //clique
58
59
                  update_maximum(R);
60
61
            return:
62
63
        int u = pickPivot(P|X);
64
        for(int i = 0; i <= n-1; i++)</pre>
65
66
            if (P&(~v[u])&(1LL<<i)) //vi is in P</pre>
67
68
                 BronKerbosch( R|(1LL<<i), P&v[i], X&v[i] );</pre>
69
                 P&=(~(1LL<<i));
                X | = (1LL << i);
70
71
72
73
75
   int main()
76
       ios::sync_with_stdio(false);
        cin.tie(0);
        while(cin >> n)
80
            cin >> m;
83
            Max = 0:
            FOR(i, 0, n-1)v[i] = 0;
            int a, b;
            FOR (i, 1, m)
                 cin >> a >> b;
90
                v[a] = (1LL << b);
91
                v[b] = (1LL << a);
92
            BronKerbosch(0, (1LL << n) -1, 0);
```

cout << Max << '\n';

4.17 MaxMatching

return 0;

```
1 #define FZ(x) memset(x,0,sizeof(x))
  struct GenMatch // 1-base
       static const int MAXN = 250;
       int V:
       bool el[MAXN][MAXN];
       int pr[MAXN];
       bool ing[MAXN], inp[MAXN], inb[MAXN];
       queue<int> qe;
       int st.ed:
10
       int nb:
11
12
       int bk[MAXN],dis[MAXN];
13
14
       void init(int V)
15
           v = v;
16
17
           FZ(el);
           F7 (pr):
18
19
           FZ(ing);
20
           FZ(inp);
21
           FZ(inb);
22
           F7.(bk):
23
           FZ(dis);
24
           ans = 0;
25
26
       void add_edge(int u, int v)
27
28
           el[u][v] = el[v][u] = 1;
29
30
       int lca(int u.int v)
31
           memset(inp,0,sizeof(inp));
32
33
           while(1)
34
35
               u = djs[u];
36
               inp[u] = true;
37
               if(u == st) break;
38
               u = bk[pr[u]];
39
           while(1)
40
41
               v = dis[v];
42
               if(inp[v]) return v;
43
44
               v = bk[pr[v]];
45
46
           return v;
47
       void upd(int u)
49
51
           while (djs[u] != nb)
52
54
               inb[djs[u]] = inb[djs[v]] = true;
               u = bk[v];
               if(djs[u] != nb) bk[u] = v;
```

```
122
                                                                                       pr[v] = u;
       void blo(int u,int v)
59
                                                                     123
                                                                                      pr[u] = v;
                                                                                      u = w;
60
                                                                     124
61
            nb = 1ca(u,v);
                                                                     125
            memset(inb,0,sizeof(inb));
62
                                                                     126
63
                                                                     127
                                                                              int solve()
64
                    upd(v);
                                                                     128
            if(djs[u] != nb) bk[u] = v;
                                                                                  memset(pr,0,sizeof(pr));
65
                                                                     129
66
            if(djs[v] != nb) bk[v] = u;
                                                                     130
                                                                                  for(int u = 1; u <= V; u++)</pre>
            for(int tu = 1; tu <= V; tu++)</pre>
                                                                                       if(pr[u] == 0)
67
                                                                     131
68
                if (inb[djs[tu]])
                                                                     132
69
                                                                     133
                                                                                           st = u;
                    dis[tu] = nb;
                                                                                           flow();
70
                                                                     134
71
                    if (!inq[tu])
                                                                     135
                                                                                           if(ed > 0)
72
                                                                     136
73
                         ge.push(tu);
                                                                                               aug();
                                                                     137
                         inq[tu] = 1;
74
                                                                     138
                                                                                               ans ++;
75
                                                                     139
76
                                                                     140
77
                                                                     141
                                                                                  return ans:
78
       void flow()
                                                                     142
79
                                                                     143 } gm;
80
            memset(ing, false, sizeof(ing));
            memset(bk,0,sizeof(bk));
81
            for(int i = 1; i <= V; i++)</pre>
82
                                                                         4.18 spfa
83
                djs[i] = i;
84
85
            while(qe.size()) qe.pop();
                                                                       1 typedef pair<int, 11> P;
            qe.push(st);
86
                                                                         #define idx first
87
            inq[st] = 1;
                                                                         #define w second
88
            ed = 0;
                                                                         int vn, en;
89
            while(ge.size())
                                                                         vector<P> graph[N];
90
                                                                         11 dist[N];
91
                int u = qe.front();
92
                qe.pop();
                                                                         bool spfa() // return true if neg cycle
                for(int v = 1; v <= V; v++)</pre>
93
                    if (el[u][v] && (djs[u] != djs[v]) && (pr[u]
94
                                                                             for(int i = 0; i < vn; i++) dist[i] = INF; dist[0] = 0;</pre>
                                                                              int cnt[N] = {0};
95
                                                                             bool inq[N] = {false};
                         if((v == st) || ((pr[v] > 0) && bk[pr[v]]
96
                                                                              queue<int> q; q.push(0); inq[0] = true;
                               > 0))
                                                                              while(!q.empty())
                                                                      14
                             blo(u,v);
97
                                                                      15
                         else if(bk[v] == 0)
98
                                                                      16
                                                                                  int s = q.front(); q.pop();
99
                                                                                  inq[s] = false;
                                                                      17
                             bk[v] = u;
100
                                                                                  for(auto e:graph[s])
                                                                      18
101
                             if(pr[v] > 0)
                                                                      19
102
                                                                                      if (dist[e.idx] > dist[s]+e.w)
                                 if(!inq[pr[v]]) qe.push(pr[v]);
103
                                                                      21
104
                                                                                          dist[e.idx] = dist[s]+e.w;
                                                                      22
105
                             else
                                                                                           if (++cnt[e.idx] >= vn) return true;
                                                                      23
106
                                                                      24
                                                                                           if(!inq[e.idx])
107
                                 ed = v;
                                                                      25
108
                                 return:
                                                                                               inq[e.idx] = true;
                                                                      26
109
                                                                      27
                                                                                               q.push(e.idx);
110
                                                                      28
111
                                                                      29
112
                                                                      30
113
                                                                      31
114
        void aug()
                                                                              return false;
                                                                      32
115
                                                                      33
116
            int u, v, w;
117
            u = ed;
            while(u > 0)
119
                                                                         4.19 MinimumMeanCycle
```

v = bk[u];

w = pr[v];

120

121

```
1 #include <cfloat > //for DBL_MAX
  int dp[MAXN] [MAXN]; // 1-base, O(NM)
   vector<tuple<int,int,int>> edge;
   double mmc(int n) {//allow negative weight
     const int INF=0x3f3f3f3f;
     for (int t=0; t<n; ++t) {</pre>
       memset(dp[t+1],0x3f,sizeof(dp[t+1]));
       for(const auto &e:edge) {
         int u, v, w;
         tie(u,v,w) = e;
10
         dp[t+1][v] = min(dp[t+1][v], dp[t][u]+w);
11
12
13
14
     double res = DBL MAX;
15
     for (int u=1;u<=n;++u) {</pre>
16
       if (dp[n][u] == INF) continue;
       double val = -DBL_MAX;
17
       for (int t=0; t<n; ++t)</pre>
18
19
         val=max(val, (dp[n][u]-dp[t][u])*1.0/(n-t));
20
       res=min(res,val);
21
22
     return res:
23
```

Math

5.1 EulerPhi

```
1 //find in O(sqrt(N))
   int euler_phi(int N)
       int res=N;
       for (int i=2;i*i<=N;i++)</pre>
            if(N%i==0)
                 res=res/i*(i-1);
10
                 for(;N%i==0;N/=i);
11
12
13
       if (N!=1) res=res/N* (N-1); //self=prime
14
15
       return res;
16
17
   //tabulate in O(MAXN)
19
20
   int euler[MAXN];
21
22
   void euler_phi2()
23
       for (int i=0;i<MAXN;i++)euler[i]=i;</pre>
       for(int i=2;i<MAXN;i++)</pre>
25
26
27
            if (euler[i] == i)
28
29
                 for(int j=i;j<MAXN;j+=i)</pre>
30
31
                     euler[i]=euler[i]/i*(i-1);
32
```

```
5 }
```

5.2 exgcd

```
1 1 exgcd(11 a, 11 & ar, 11 b) // ## ## a*ar+b*as=gcd(a, b)
     11 as = 0, br = 0, bs = 1;
     while(a && b)
        ar -= br*(a/b);
        as -= bs*(a/b);
        a %= b;
        if(a == 0) break;
        br -= ar*(b/a);
        bs -= as*(b/a);
        b %= a;
12
13
     if (a == 0) a = b, ar = br; //維護a*ar+b*as=gcd(a, b)
14
     return a; //return gcd(a, b)
15
16
```

5.3 NTT

```
typedef long long 11;
  const 11 P = (479 << 21) +1;
  const 11 G = 3;
  inline 11 fpw(11 x, 11 y, 11 m)
6
     11 \text{ rt.n} = 1:
     for (x=(x>=m?x%m:x);y;y>>=1)
       if(y&1) rtn = rtn*x%m;
       x = x*x%m;
12
13
     return rtn;
14
   inline vector<11> ntt(vector<11> rtn, int Rev = 1)
16
     int ntt n = rtn.size();
     for(int i=0, j=0; i < ntt_n; i++)</pre>
19
20
       if(i>j) swap(rtn[i],rtn[j]);
21
       for (int k=(ntt_n>>1); (j^=k)<k;k>>=1);
22
23
     for(int i=2,m=1;i<=ntt_n;i<<=1,m++)</pre>
24
25
       11 w = 1, wn = fpw(G, (P-1) >> m, P), u, t;
       int mh = i>>1;
26
27
       for(int j=0;j<mh;j++)</pre>
28
29
         for(int k=j;k<ntt_n;k+=i)</pre>
30
31
           u = rtn[k], t = w*rtn[k+mh]%P;
32
           rtn[k] = (u+t)%P;
33
           rtn[k+mh] = (u-t+P)%P;
34
         w = w*wn%P;
```

5.4 BigInteger

```
class BigInt
    public:
       // constructors
      BigInt();
      BigInt(11);
       BigInt(const char*);
       BigInt(string);
       BigInt(bool, vector<int>);
       // functions
10
       inline void print();
11
12
       // operators
13
       bool operator== (const BigInt &a) const;
14
       bool operator!= (const BigInt &a) const;
15
      bool operator< (const BigInt &a) const;</pre>
16
       bool operator> (const BigInt &a) const;
      bool operator<= (const BigInt &a) const;</pre>
17
      bool operator>= (const BigInt &a) const;
18
       BigInt operator- () const;
19
       BigInt operator+ (const BigInt &a) const;
20
       BigInt operator- (const BigInt &a) const;
21
22
       BigInt operator* (const BigInt &a) const;
23
       BigInt operator/ (const BigInt &a) const;
      BigInt operator% (const BigInt &a) const;
24
       // variables
25
       const static int MAX = 1000000;
26
      bool Neg = false;
27
28
      vector<int> seq;
29
30
31
   // constructors
32 BigInt::BigInt() {}
   BigInt::BigInt(11 in)
34
    if (in<0) Neg=true, in=-in;</pre>
35
36
     while(in!=0)
37
38
      seq.emplace_back(in%MAX);
39
      in/=MAX;
40
41
     if (seg.empty()) seg.emplace back(0);
42
43
   BigInt::BigInt(const char *s)
44
     int i, j, tmp, end=0;
     if(s[0]=='-') Neg=true, end=1;
     for(i=strlen(s)-1, j=1, tmp=0; i>=end; i--, j*=10)
48
49
      if (j==MAX)
```

```
seq.emplace_back(tmp);
51
52
         j=1, tmp=0;
53
54
       tmp += (s[i] - '0')*j;
     } seg.emplace back(tmp);
55
56
57 BigInt::BigInt(string s):BigInt(s.c str()) {}
   BigInt::BigInt(bool b, vector<int> v):Neg(b),seg(v) {}
   // functions
   void BigInt::print()
61
    if(Neg) putchar('-');
62
     printf("%d", seq.back());
63
     for(int i=(int)(seg.size())-2; i>=0; i--)
     printf("%06d",seq[i]);
66
    puts("");
67 }
68
   // operators
69
   bool BigInt::operator == (const BigInt &a) const
70
71
    return Neg==a.Neg&&seg==a.seg;
72
73
   bool BigInt::operator!= (const BigInt &a) const
74
75
     return !((*this)==a);
76
77
   bool BigInt::operator< (const BigInt &a) const
78
79
     if (Neg^a.Neg) return Neg;
     if (seq.size()!=a.seq.size()) return Neg^(seq.size() <a.seq.</pre>
          size());
     for(int i=seq.size()-1; i>=0; i--)
81
      if (seq[i]!=a.seq[i]) return Neg^(seq[i] < a.seq[i]);</pre>
82
83
     return false:
84
85 bool BigInt::operator> (const BigInt &a) const
86
     if (Neg^a.Neg) return a.Neg;
     if(seq.size()!=a.seq.size()) return a.Neg^(seq.size()>a.seq
          .size());
     for(int i=seq.size()-1; i>=0; i--)
      if (seq[i]!=a.seq[i]) return a.Neg^(seq[i]>a.seq[i]);
91
     return false;
92
93 bool BigInt::operator <= (const BigInt &a) const
94
95
     return !((*this)>a);
96
   bool BigInt::operator>= (const BigInt &a) const
98
     return !((*this) <a);</pre>
100
101 BigInt BigInt::operator- () const
102
     return BigInt(Neg^1, seg);
104
   BigInt BigInt::operator+ (const BigInt &a) const
106
    if (Neg^a.Neg)
       return Neg?a-(-(*this)):(*this)-(-a);
     BigInt rtn(Neg, vector<int>(max(seq.size(),a.seq.size())));
     for(int i=0; i<(int)(seq.size()); i++) rtn.seq[i]+=seq[i];</pre>
     for(int i=0; i<(int) (a.seq.size()); i++) rtn.seq[i]+=a.seq[</pre>
     for(int i=0; i<(int)(rtn.seg.size())-1; i++)</pre>
      if (rtn.seq[i]>=MAX)
```

```
rtn.seq[i+1]+=rtn.seq[i]/MAX, rtn.seq[i]%=MAX;
                                                                           bool found = false:
     if (rtn.seg.back()>=MAX)
115
                                                                     178
116
                                                                     179
117
       rtn.seq.emplace_back(rtn.seq.back()/MAX);
                                                                     180
       rtn.seg[rtn.seg.size()-2]%=MAX;
                                                                     181
118
119
                                                                     182
120
     return rtn;
                                                                     183
121
                                                                     184
122
    BigInt BigInt::operator- (const BigInt &a) const
                                                                     185
123
                                                                     186
124
     if (Neg^a.Neg) return (*this)+(-a);
                                                                     187
     if (Neg^((*this) <a)) return (-a) - (-(*this));</pre>
125
                                                                     188
     BigInt rtn(Neg, vector<int>(max(seg.size(),a.seg.size())));189
126
127
     for(int i=0; i<(int)(seq.size()); i++) rtn.seq[i]+=seq[i]; 190</pre>
128
     for (int i=0; i < (int) (a.seq.size()); i++) rtn.seq[i] -=a.seq[191</pre>
                                                                                if (tmp)
     for(int i=0; i<(int)(rtn.seg.size())-1; i++)</pre>
129
                                                                     193
      if (rtn.seg[i]<0)
130
                                                                     194
          rtn.seg[i+1] --, rtn.seg[i] +=MAX;
131
                                                                     195
     while(!rtn.seq.empty()&&!rtn.seq.back()) rtn.seq.pop_back() 196
132
     if(rtn.seq.empty()) rtn = BigInt(011);
133
                                                                     198
134
     return rtn:
                                                                     199
                                                                     200
135
    BigInt BigInt::operator* (const BigInt &a) const
136
                                                                     201
                                                                     202
137
     BigInt rtn(Neg^a.Neg, vector<int>(0));
                                                                     203
138
     vector<Complex> x, y;
                                                                     204
139
     for(auto i:seq) x.emplace_back(i);
                                                                     205
140
141
     for(auto i:a.seq) y.emplace_back(i);
                                                                     206
142
     int N=1:
                                                                     207
1/13
     while(N<(int)(x.size()+y.size())) N <<= 1;</pre>
                                                                     208
     while(N!=(int)(x.size())) x.emplace_back(0);
                                                                     209
144
     while(N!=(int)(y.size())) y.emplace_back(0);
145
                                                                     210
     x = fft(x), y = fft(y);
                                                                     211
146
     for(int i=0; i<N; i++) x[i] = x[i]*y[i];</pre>
147
                                                                     212
1/18
     x = fft(x, -1);
                                                                     213
     11 tmp = 0;
149
                                                                     214
150
     for(int i=0; i<N; i++)</pre>
                                                                     215
                                                                     216
151
152
       tmp += (11)(x[i].x+0.1);
                                                                     217
       rtn.seq.emplace_back(tmp%MAX);
                                                                     218
153
       tmp /= MAX;
154
     } rtn.seq.emplace_back(tmp);
155
     while(!rtn.seq.empty()&&!rtn.seq.back()) rtn.seq.pop_back()221
156
     if(rtn.seq.empty()) rtn = BigInt(011);
157
     return rtn;
158
159
    BigInt BigInt::operator/ (const BigInt &a) const
162
     if (a==BigInt(011)) return a;
     BigInt rtn, check, BItmp, posiA, posiB;
                                                                           BItmp = check+posiB;
                                                                     227
     posiA = (*this), posiA.Neg = false;
                                                                           while(posiA>=BItmp)
                                                                            rtn = rtn+BigInt(1), check = BItmp, BItmp = check+posiB; 38 }
     posiB = a, posiB.Neg = false;
     int PRECISION = max(seq.size(),a.seq.size())+6, N = 1;
                                                                           BItmp = check-posiB;
     11 \text{ tmp} = 0;
                                                                           while(posiA<=BItmp)</pre>
     while(N<PRECISION+6) N <<= 1;</pre>
168
                                                                             rtn = rtn-BigInt(1), check = BItmp, BItmp = check-posiB;
169
                                                                           rtn.Neg = Neg^a.Neg;
170
     vector<Complex> B, c1(N,0), c2(N,0), c3(N,0);
                                                                           return rtn:
     vector < Complex > *x = (&c1), *xp = (&c2), *calc = (&c3);
     for(int i=a.seq.size()-1; i>=0; i--)
                                                                         BigInt BigInt::operator% (const BigInt &a) const
     B.emplace_back(a.seq[i]);
                                                                     237
     B.resize(N,0);
                                                                           return (*this) - ((*this)/a) *a;
                                                                     239
```

(*x)[a.seq.size()] = MAX/a.seq.back();

```
while(!found)
  (*x) = fft(*x);
  for(int i=0; i<N; i++) (*calc)[i] = (*x)[i]*B[i];</pre>
  (*calc) = fft(*calc,-1);
  for(int i=a.seg.size()-1; i<N; i++)</pre>
   (*calc)[i-a.seg.size()+1] = (*calc)[i];
  for(int i=N-a.seq.size()+1; i<N; i++)</pre>
   (*calc)[i] = 0;
  for(int i=N-1; i>=1; i--)
    tmp = (11)((*calc)[i].x+0.1);
    (*calc)[i-1] = (11)((*calc)[i-1].x+0.1)+tmp/MAX;
    (*calc)[i] = tmp %= MAX;
      (*calc)[i-1] = (11)((*calc)[i-1].x+0.1)+1;
      (*calc)[i] = MAX-tmp;
  (*calc)[0] = 2-(11)((*calc)[0].x+0.1);
  for(int i=PRECISION+6; i<N; i++) (*calc)[i] = 0;</pre>
  (*calc) = fft(*calc);
  for(int i=0; i<N; i++) (*xp)[i] = (*calc)[i]*(*x)[i];</pre>
  (*xp) = fft(*xp, -1);
  (*x) = fft(*x, -1);
  for(int i=N-1; i>=1; i--)
    tmp = (11)((*xp)[i].x+0.1);
    (*xp)[i] = tmp%MAX;
    (*xp)[i-1] = (11)((*xp)[i-1].x+0.1)+tmp/MAX;
  for(int i=PRECISION+6; i<N; i++) (*xp)[i] = 0;</pre>
  found = true:
  for(int i=0; i<=PRECISION&&found; i++)</pre>
    if ((11)((*xp)[i].x+0.1)!=(11)((*x)[i].x+0.1))
      found = false;
 calc = x, x = xp, xp = calc, calc = (&c3);
for(int i=N-1; i>=(int)(a.seq.size())-1; i--)
 rtn.seq.emplace_back((11)((*x)[i].x+0.1));
while(!rtn.seq.back()) rtn.seq.pop_back();
rtn = rtn*posiA;
for(int i=N-1; i<(int)(rtn.seq.size()); i++)</pre>
 rtn.seq[i-N+1] = rtn.seq[i];
for(int i=max((int)(rtn.seq.size()-N+1),0); i<(int)(rtn.seq 29</pre>
     .size()); i++)
  rtn.seq[i] = 0;
while(!rtn.seq.empty()&&!rtn.seq.back()) rtn.seq.pop_back() 32
if(rtn.seg.empty()) rtn = BigInt(011);
check = rtn*posiB;
```

5.5 prime detect

```
1 const int N = 10000000;
2 bool isprime[N] = {true};
3 void prime detect()
      for(int i = 2; i < sq; i++)</pre>
          if(isprime[i])
               for(int j = i*i; j < N; j+=i) isprime[j] = false;</pre>
```

5.6 Gaussian Jordan

```
1 const double EPS = 1e-8;
  typedef vector<double> vec;
   typedef vector<vec> mat:
   //if no sol/inf sol, return vec of size 0
   vec gauss jordan(const mat& A, const vec& b)
       int n = A.size();
       mat B(n, \text{vec}(n+1)):
       for(int i=0;i<n;i++)for(int j=0;j<n;j++)B[i][j]=A[i][j];</pre>
       for (int i=0;i<n;i++)B[i][n]=b[i];</pre>
14
       for(int i=0;i<n;i++)</pre>
15
16
            int pivot=i;
17
            for (int j=i; j<n; j++)</pre>
                 if (abs(B[j][i])>abs(B[pivot][i]))pivot=j;
21
            swap(B[i],B[pivot]);
23
            if (abs(B[i][i]) < EPS) return vec(); //no/inf sol</pre>
24
            for (int j=i+1; j<=n; j++) B[i][j]/=B[i][i];</pre>
25
            for (int j=0; j < n; j++)</pre>
                 if(i!=i)
                      for(int k=i+1; k<=n; k++)</pre>
                          B[j][k] -=B[j][i]*B[i][k];
35
       for (int i=0; i < n; i++) x[i] = B[i][n];</pre>
36
       return x;
```

$5.7 \mod eq$

```
1 // 解線性模方程組(最小非負整數解)
2 const int N; //N個方程
3 11 A[N], B[N], M[N]; // A * X = B (%M)
4 11 solve() //解X, return INF if no solution
```

```
11 k = 0, h = 1;
      for(11 i = 0; i < N; i++)</pre>
         11 a = A[i]*h, b = B[i]-A[i]*k, m = M[i], ar;
         11 d = exgcd(a, ar=1, m);
10
         if (b%d != 0) return INF;
12
         11 n = abs(m/d);
         11 t = ar*b/d; t%=n; t+=n; t%=n;
13
14
         k += h*t, h *= n; k%=h; //維護解是正的
15
16
17
     int ret = (k%h+h)%h;
     return ret;
```

5.8 FFT

```
1 const double PI = acos(-1.0);
  struct Complex
     double x.v:
     Complex() {}
     Complex(double a):x(a),y(0){}
     Complex(double a, double b):x(a),y(b) {}
     Complex operator+ (const Complex &a) { return Complex(x+a.x,
     Complex operator- (const Complex &a) { return Complex(x-a.x,
          y-a.y); }
     Complex operator* (const Complex &a) { return Complex(x*a.x-
          y*a.y,x*a.y+y*a.x); }
11
   inline vector<Complex> fft(vector<Complex> rtn, int Rev = 1)
     int fft n = rtn.size();
     for(int i=0,j=0;i<fft_n;i++)</pre>
16
                                                                      14
       if(i>j) swap(rtn[i],rtn[j]);
                                                                      15
       for(int k=(fft_n>>1);(j^=k)<k;k>>=1);
                                                                      16
19
                                                                      17
     for (int i=2, m; i <= fft_n; i <<= 1)</pre>
20
                                                                      18
21
                                                                      19
22
                                                                      20
       for(int j=0;j<fft_n;j+=i)</pre>
23
                                                                      21
24
                                                                      22
25
         for (int k=0; k<m; k++)</pre>
26
           Complex y = rtn[j+k+m] *Complex(cos(2*PI/i*k), Rev*sin^{24})
                                                                      25
                (2*PI/i*k));
           rtn[j+k+m] = rtn[j+k]-y;
           rtn[j+k] = rtn[j+k]+y;
     for(int i=0;!~Rev&&i<fft_n;i++)</pre>
       rtn[i].x = rtn[i].x/fft n;
35
     return rtn;
```

6 String

6.1 hash

```
1 | #define MAXN 1000000
  #define mod 1073676287
  /*mod 必須要是質數*/
  typedef long long T;
  char s[MAXN+5];
6 T h [MAXN+5]; /*hash 陣列*/
  T h base [MAXN+5]; /*h base [n] = (prime^n) %mod*/
  void hash init(int len.T prime) {
    h base[0]=1;
    for(int i=1;i<=len;++i){</pre>
      h[i] = (h[i-1] * prime + s[i-1]) % mod;
12
      h base[i]=(h base[i-1]*prime)%mod;
13
14
15 T get_hash(int 1, int r) {/*閉區間寫法,設編號為0~1en-1*/
    return (h[r+1] - (h[1] *h_base[r-1+1])%mod+mod)%mod;
```

6.2 SuffixArray-STL

```
1 struct CMP
     int len,k,*Rank,a,b;
     inline bool operator()(int i, int j)
      if (Rank[i]!=Rank[j])return Rank[i] < Rank[j];</pre>
       a=(i+=k)<len?Rank[i]:-1;
      b=(i+=k)<len?Rank[i]:-1;
       return a < b;</pre>
11
   void SA_build(int *SA, int *Rank, char *S) {
     int tmp[MAX_N], len=strlen(S);
     for(int i=0;i<len;i++) SA[i]=i, Rank[i]=S[i];</pre>
     CMP cmp={len,1};
     while(cmp.k*=2)
       cmp.Rank=Rank;
       sort(SA,SA+len,cmp);
       tmp[SA[0]]=0;
       for(int i=1;i<len;i++)</pre>
        tmp[SA[i]]=tmp[SA[i-1]]+cmp(SA[i-1],SA[i]);
       if (tmp[SA[len-1]] == len-1) break;
       for(int i=0;i<len;i++) Rank[i]=tmp[i];</pre>
```

6.3 Z-value

```
5     for (int i=1;S[i];i++)
6     {
7         if(Z[b]+b<i) Z[i]=0;
8         else Z[i]=min(Z[b]+b-i,Z[i-b]);
9         while(S[i+Z[i]]&&S[Z[i]]==S[i+Z[i]]) Z[i]++;
10         if(Z[i]+i>Z[b]+b) b=i;
11     }
12 }
```

6.4 BWT

```
1 // use with suffix array
2 int pivot;
3 // BWT array size must be double of the data size
  inline void BWT(char *tmp, char *in, char *out, int *SA, int
     int len=strlen(in);
     for (int i=0; i<len; i++) tmp[i] = tmp[i+len] = in[i];</pre>
     tmp[len*2]='\0';
     SA build(SA, Rank, tmp);
     for(int i=0, j=0;i<2*len;i++)</pre>
11
12
       if(SA[i]==len) pivot=j;
13
       if (SA[i] < len)
14
         out[j++]=in[(SA[i]+len-1)%len];
15
16
     out[len] = '\0';
17
18
   inline void IBWT(char *in, char *out, int *tmp)
20
21
     int len=strlen(in);
22
     vector<int> idx[256];
     for(int i=0;i<len;i++)</pre>
24
       idx[in[i]].emplace_back(i);
     for(int i=0,k=0;i<256;i++)</pre>
26
       for (int j=0; j < (int) (idx[i].size()); j++)</pre>
27
         tmp[k++]=idx[i][j];
     int p=pivot;
     for (int i=0; i<len; i++)</pre>
       out[i]=in[p=tmp[p]];
     out [len] = ' \setminus 0';
```

6.5 LCP

void SA radix sort(int *s, int *e, int *Rank, int rankcnt)

6.6 SuffixArray

```
2
    int box[MAX_N], tmp[MAX_N], len=e-s;
    memset(box,0,sizeof(int)*rankcnt);
    for(int i=0;i<len;i++) box[Rank[i]]++;</pre>
    for(int i=1;i<rankcnt;i++) box[i]=box[i]+box[i-1];</pre>
    for(int i=len-1;i>=0;i--) tmp[--box[Rank[s[i]]]]=s[i];
    for(int i=0;i<len;i++) s[i]=tmp[i];</pre>
9
   #define equal(a,b,c) c[a]!=c[b]||a+k>=len||c[a+k]!=c[b+k]
   void SA build(int *SA, int *Rank, char *S)
12
    int ranktmp[MAX N], len=strlen(S), rankcnt='z'+1;
     for(int i=0;i<len;i++) Rank[i]=S[i];</pre>
15
     for(int k=1;rankcnt!=len;k*=2)
16
17
       for(int i=0;i<len;i++) SA[i]=(i+len-k)%len;</pre>
       SA_radix_sort(SA+k, SA+len, Rank+k, rankcnt);
18
       SA_radix_sort(SA, SA+len, Rank, rankcnt);
19
       ranktmp[SA[0]]=0, rankcnt=0;
20
       for(int i=1;i<len;i++)</pre>
21
22
         ranktmp[SA[i]]=rankcnt+=equal(SA[i-1], SA[i], Rank);
23
       for(int i=0;i<1en;i++) Rank[i]=ranktmp[i];</pre>
24
25
26
27 #undef equal
```

6.7 AC-Automation

```
#define SZ 25000
int nx[SZ][26], spt;
int f1[SZ], ef1[SZ], ed[SZ];
int newnode()

for(int i=0;i<26;i++) nx[spt][i]=0;
ed[spt]=0;
return spt++;

int add(char *s, int sptnow)

for(int i=0;s[i];i++)

{
   int tmp=s[i]-'a';
   if(nx[sptnow][tmp]==0) nx[sptnow][tmp]=newnode();
   sptnow=nx[sptnow][tmp];
}</pre>
```

```
return sptnow;
20
   int bfsq[SZ], qs, qe;
   void make fl(int root)
23
     fl[root]=efl[root]=qs=qe=0;
     bfsq[qe++]=root;
     while(qs!=qe)
27
28
       int p=bfsq[qs++];
       for(int i=0;i<26;i++)</pre>
29
30
31
         int t=nx[p][i];
32
         if(t==0) continue;
33
         int tmp=f1[p];
         for(; tmp&&nx[tmp][i] == 0; tmp=f1[tmp]);
34
         fl[t]=tmp?nx[tmp][i]:root;
35
         efl[t]=ed[fl[t]]?fl[t]:efl[fl[t]];
36
         bfsq[qe++]=t;
37
38
39
```

6.8 KMP

ed[sptnow]=1;

```
1 void failure_build(const char *p, int *fail)
    for(int i=1, j=fail[0]=-1; p[i]; i++)
      while(j>=0&&p[j+1]!=p[i]) j=fail[j];
      if (p[j+1] == p[i]) j++;
      fail[i]=j;
  int KMP(const char *T, const char *P, int *fail)
11
    failure_build(P, fail);
    for(int i=0, j=-1; T[i]; i++)
13
14
      while(i>=0&&P[i+1]!=T[i]) i=fail[i];
15
      if (P[j+1]==T[i]) j++;
16
17
      if(!P[j+1]) return i-j;
18
19
    return -1;
20
21
  //使用方法: KMP(主字串, 待匹配字串, failure array)
23 //回傳:第一個完全匹配的位置
```

7 other

7.1 2sat

```
1 const int N = 10; // 變數數量
2 bool adj[20][20]; // adjacency matrix
3 int visit[20]; // DFS visit record
```

```
// 解
4 int sat[20];
   int not(int a) {return a<N ? a+N : a-N;}</pre>
8 // 另外一種方式
10 int not(int a) {return a&1 ? a : a+1;}
int not(int a) {return a^1;}
12 */
13
14 bool dfs_try(int i)
15
16
      if (visit[i] == 1 || sat[i] == 1) return true;
       if (visit[i] == 2 || sat[i] == 2) return false;
17
      visit[i] = 1;
18
       visit[not(i)] = 2;
19
       for (int j=0; j<N+N; ++j)</pre>
20
           if (adj[i][j] && !dfs try(j))
22
               return false:
23
       return true;
24
25
   void dfs mark(int i)
27
       if (sat[i] == 1) return;
       sat[i] = 1;
       sat[not(i)] = 2;
       for (int j=0; j<N+N; ++j)</pre>
32
           if (adj[i][j])
33
               dfs_mark(j);
34
35
36
   void two satisfiability()
37
      // 一次輸入一個括號
38
       memset(adj, false, sizeof(adj));
39
       int a, b;
40
       while (cin >> a >> b)
41
42
43
           map[not(a)][b] = true;
44
           map[not(b)][a] = true;
45
46
47
       // 找出一組解
48
       for (int i=0; i<N; ++i)</pre>
49
50
           memset(visit, 0, sizeof(visit));
51
           if (dfs_try(i)) {dfs_mark(i); continue;}
52
53
           memset(visit, 0, sizeof(visit));
54
           if (dfs try(not(i))) {dfs mark(not(i)); continue;}
55
56
           // 無解則立即結束。
57
           return:
58
59
       // 印出一組解。
60
61
       for (int i=1; i<N; ++i)</pre>
           if (sat[i] == 1)
62
63
               cout << i;
64
           else /*if (sat[i] == 2)*/
               cout << "not" << i;
65
```

7.2 PojTree

```
1 | #include <bits/stdc++.h>
   using namespace std;
  typedef long long int 11;
  typedef pair<int, 11> P;
  #define idx first
   #define w second
   const int N = 10004;
   const 11 INF = (111 << 60);</pre>
11
12 int vn;
13 11 k;
14 vector<P> graph[N];
15 vector<int> dist;
16 11 subtreeSz[N]:
17 bool isCentroid[N];
18
   void init()
19
20
       for(int i = 1; i <= vn; i++)</pre>
21
           graph[i].clear(), isCentroid[i] = false;
22
23
24
25
   void buildTree()
26
27
       for(int i = 1; i < vn; i++)</pre>
28
29
           int u, v, 1; scanf("%d %d %d", &u, &v, &1);
           graph[u].push_back(P(v, 1));
30
           graph[v].push_back(P(u, 1));
31
32
33
34
35
   11 calSubsz(int v, int p)
36
       subtreeSz[v] = 1;
37
       for(auto c:graph[v])
38
39
           if(isCentroid[c.idx] || c.idx == p) continue;
40
           subtreeSz[v] += calSubsz(c.idx, v);
41
42
43
       return subtreeSz[v];
44
45
   P getCentroid(int v, int p, 11 subsz)
48
49
       P cen(-1, INF);
       11 \text{ mxsonSz} = -1;
       for(auto c:graph[v])
52
           if(c.idx == p || isCentroid[c.idx]) continue;
53
           P res = getCentroid(c.idx, v, subsz);
54
55
           if (res.w < cen.w) cen = res;</pre>
           mxsonSz = max(mxsonSz, subtreeSz[c.idx]);
56
57
       mxsonSz = max(mxsonSz, subsz-subtreeSz[v]);
       if (mxsonSz < cen.w) cen = P(v, mxsonSz);</pre>
       return cen;
61
63 void getDist(int v, int p, 11 w)
```

```
64
        if(w > k) return;
 65
 66
        dist.push back(w);
 67
        for(auto c:graph[v])
 68
             if (c.idx == p || isCentroid[c.idx]) continue;
 69
 70
             getDist(c.idx, v, w+c.w);
 71
 72
 73
 74
    11 calValidPair(int idx, 11 w)
 75
 76
        dist.clear();
 77
        getDist(idx, -1, w);
 78
        sort(dist.begin(), dist.end());
 79
        11 \text{ sum} = 0;
        for(int 1 = 0, r = dist.size()-1; 1 < r; )</pre>
 80
 81
 82
             if (dist[r]+dist[1] <= k) sum += r-1, 1++;</pre>
 83
             else r--:
 84
 85
        return sum;
 86
    11 treedc(int v)
 88
 89
 90
        11 \text{ sum} = 0;
        // find centroid
 91
 92
        calSubsz(v, v);
 93
        int cen = getCentroid(v, v, subtreeSz[v]).idx;
 94
        isCentroid[cen] = true;
 95
 96
        sum += calValidPair(cen, 0);
 97
        for(auto c:graph[cen])
 98
 99
             if(isCentroid[c.idx]) continue;
100
             sum -= calValidPair(c.idx, c.w);
             sum += treedc(c.idx);
101
102
103
        return sum;
104
105
106
    int main()
107
        while(scanf("%d %11d", &vn, &k) && vn && k)
108
109
             init();
110
111
            buildTree();
             printf("%11d \setminus n", treedc(1));
112
113
114
        return 0;
115
```

7.3 definesss

```
#include <bits/stdc++.h>
using namespace std;
#define pb push_back
#define pii pair<int,int>
#define pil pair<II, ll>
#define pil pair<int,il>
#define pli pair<int,int>
#define pli pair<int,int>
#define pli pair
#define ppi pair
```

```
9 #define pip pair<int,pii>
10 #define pdd pair<double, double>
  #define f first
11
12 #define s second
  #define MOD 1000000007
  #define mkp make_pair
  #define M PI 3.14159265358979323846
  #define FOR(i,1,r) for (int i=1;i<=r;i++)
  #define LOR(i,1,r) for (11 i=1;i<=r;i++)
  #define FORD(i,r,1) for (int i=r;i>=1;i--)
  #define LORD(i,r,1) for (11 i=r;i>=1;i--)
  #define INF 1000000000
  #define CL(x) memset(x,0,sizeof(x))
  typedef long long 11:
23
24
  int main()
25
26
      ios::sync with stdio(false);
27
      cin.tie(0);
28
29
      return 0;
```

A	CM ICPC TEAM		2.2 2.3	$\begin{aligned} & MaxDensitySubgraph & . & . & . & . & . & . & . & . & . & $	4		4.18 spfa	
Reference -			3 Geometry 3.1 nearestDist	5 5	5	Math 5.1 EulerPhi 5.2 exgcd		
$I_{N,1}$	THU_FURRYFORCE		3.2 G ra	Ç ,	о 6		5.3 NTT	11 11
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Contents			4.4	匹配問題轉換	6	6	String 6.1 hash	13
1 Dat 1.1 1.2 1.3 1.4 1.5 1.6 1.7 1.8	aStructure treap disjoint_set 2d_st_tag BIT 1d_segTree_tag 1d_segTree Matrix undo_disjoint_set	1 1 1 1 2 2 2 2 3 3	4.11 4.12 4.13	BridgeConnected mst_kruskal bellman_Ford MaxWeightPerfectMatch StronglyConnectedComponent MaxBiMatching dijkstra TwoConnected ArticulationPoint	6 7 7 7 8 8 8	7	6.2 SuffixArray-STL 6.3 Z-value 6.4 BWT 6.5 LCP 6.6 SuffixArray 6.7 AC-Automation 6.8 KMP other	13 13 13 13 14 14
2 Flo		3 3	4.15 4.16	MaxWeightPerfectBiMatch	8 9 9	-	7.1 2sat	14 15