

Assignment 1

Q5

Q5

$$\Delta E = E_{\text{init}} - E_{\text{final}} = -\frac{A}{n_{\text{init}}^2} + \frac{A}{n_{\text{final}}^2}, \quad n_{\text{init}} = 5$$

for  $n_{\text{final}} = 1$ ;  $\Delta E = -\frac{A}{5^2} + \frac{A}{1^2} = 13.6 \text{ eV} \left(1 - \frac{1}{25}\right) = 13.056 \text{ eV} \approx 13.06 \text{ eV}$

$n_{\text{final}} = 2$ ;  $\Delta E = 13.6 \text{ eV} \left(\frac{1}{4} - \frac{1}{25}\right) = 2.816 \text{ eV}$

$n_{\text{final}} = 3$ ;  $\Delta E = 13.6 \text{ eV} \left(\frac{1}{9} - \frac{1}{25}\right) = 0.97 \text{ eV}$

$$E = h\nu \Rightarrow \frac{E}{h} = \nu, \quad \lambda = \frac{c}{\nu}$$

for  $n_{\text{final}} = 1$ ,  $\nu_1 = \frac{13.06 \cdot 1.6 \cdot 10^{-19}}{6.626 \cdot 10^{-34}} \approx 3.16 \cdot 10^{15} \text{ Hz}$ ,  $\lambda = \frac{3 \cdot 10^8}{3.16 \cdot 10^{15}} \approx 95 \text{ nm}$

"  $n_{\text{final}} = 2$ ,  $\nu_2 = 0.69 \cdot 10^{15} \text{ Hz}$ ,  $\lambda = 434 \text{ nm}$

"  $n_{\text{final}} = 3$ ,  $\nu_3 = 0.23 \cdot 10^{15} \text{ Hz}$ ,  $\lambda = 1.2 \mu\text{m}$

Q2

$$Q2 \quad \Phi_c = E_e + E_r = \left( -\frac{N_A e^2 \alpha Z^2}{4\pi\epsilon_0 r} + \frac{N_A B}{r^n} \right)$$

$$E_e = N_A \left( \frac{-e^2}{4\pi\epsilon_0 r} \right) \alpha Z^2$$

$$E_r = \frac{N_A B}{r^n}$$

$\Rightarrow$  To find constants at equilibrium, we find minimum energy. The energy being a function of the distance  $r$  we get:

$$\frac{d\Phi_c}{dr} = 0 = \frac{N_A e^2 \alpha Z^2}{4\pi\epsilon_0 r^2} - \frac{N_A B n}{r^{n+1}} = 0$$

$$\Rightarrow B = \frac{N_A e^2 \alpha Z^2}{n \cdot 4\pi\epsilon_0 r^2 \cdot N_A} = \frac{e^2 \alpha Z^2}{n \cdot 4\pi\epsilon_0} r^{n-1}$$

$$U_{\text{min}} = \Phi_{c \text{ min}} = - \left( \frac{N_A \alpha Z^2 e^2}{4\pi\epsilon_0 r} \right) \left( 1 - \frac{1}{n} \right)$$