

## 1. Overview

To enhance the predictive performance of our model and capture meaningful market dynamics, we designed a comprehensive feature-engineering pipeline. This step transforms the raw Hull Tactical dataset—mainly consisting of  $M^*$ ,  $V^*$ , and macroeconomic columns—into a more informative representation that reflects trend, volatility, momentum, and market regimes. All engineered features were created without introducing look-ahead bias.

## 2. Lag-Based Momentum Features

We generated lag features for key return-related variables, including `forward_returns`, `market_forward_excess_returns`, and `risk_free_rate`.

- Lags used: **1, 2, 3, 5, 10 days**
- Purpose: capture short-term momentum, autocorrelation, and mean-reversion signals

These lagged features help the model understand how recent price movements influence future returns.

## 3. Rolling Statistics (MA, Volatility, Momentum)

To capture medium-term market structure, we computed several rolling-window statistics over **5, 10, 20, and 60 days**:

- **Rolling mean** (`ret_mean_*d`) → measures local trend strength
- **Rolling volatility** (`ret_std_*d`) → captures risk and uncertainty
- **Rolling cumulative momentum** (`ret_mom_*d`) → aggregates directional persistence

These are widely used in quantitative trading strategies because they encode trend-following and risk-based signals.

## 4. Volatility Aggregation from V\* Columns

The dataset provides dozens of volatility-related predictors (V\*).

To summarize their combined information, we computed:

- `vol_mean` – average volatility signal
- `vol_std` – cross-volatility dispersion
- `vol_max` – maximum volatility across V\* columns

This provides a stable volatility proxy rather than relying on a single noisy V\* feature.

## 5. Drawdown Features

Using a synthetic cumulative price index:

$$\text{price\_index} = \prod(1+rt) \quad \text{price\_index} = \prod(1 + r_t)$$

we computed:

- **Cumulative max price (cum\_max\_price)**
- **Drawdown (drawdown = price\_index / cum\_max\_price - 1)**

This measures market stress and investors' risk aversion.

Large drawdowns often lead to strong rebounds or trend continuation—both predictive signals.

## 6. Market Regime Indicator

We constructed a simple **bull/bear regime flag**:

$$\text{regime} = 1 \text{ if } 60\text{-day mean return} > 0 \\ \text{regime} = 0 \text{ if } 60\text{-day mean return} < 0$$

This binary feature helps the model behave differently in uptrending vs. downtrending environments.

## 7. Interaction Features

To capture potential non-linear effects, we created:

- `M_interaction = M0 * M1` (first two major M\* macro features)

Such cross-features often help tree-based models detect higher-order structure.

## 8. Final Feature Set

After removing ID columns, target variables, and intermediate calculation fields, the final dataset contained:

- **127 engineered features**, including  
lagged returns, moving averages, volatility, drawdown, regime, and interaction signals.

This enriched feature set significantly improved model performance, especially in LightGBM and XGBoost, as shown in our feature-importance and backtesting results.