

## 02\_range\_2000\_ensemble\_model

July 14, 2024

```
[ ]: # Import libraries
from sklearn.preprocessing import StandardScaler, OneHotEncoder
from sklearn.compose import ColumnTransformer
from sklearn.pipeline import Pipeline
from sklearn.metrics import mean_squared_error
from sklearn.linear_model import LinearRegression, Lasso
from sklearn.ensemble import RandomForestRegressor, GradientBoostingRegressor, \
    VotingRegressor
from xgboost import XGBRegressor
from sklearn.model_selection import train_test_split
from sklearn.model_selection import GridSearchCV, learning_curve

import numpy as np
import pandas as pd
import seaborn as sns
import matplotlib.pyplot as plt

import warnings
warnings.filterwarnings("ignore")

RSEED=42
```

```
[ ]: # Load the final DataFrame from EDA_upto_2000.ipynb
df = pd.read_pickle('../data/final_df_2000.pkl')
df.head()
```

```
[ ]:  serviceCharge    heatingType  newlyConst  balcony  pricetrend  \
0          245.0    Central Heating      False    False         4.62
2          255.0    Electric Heating       True     True         2.72
4          138.0    Central Heating      False     True         2.46
6           70.0    Central Heating      False    False         1.01
7           88.0    Central Heating      False     True         1.89

    totalRent  yearConstructed  firingTypes  hasKitchen  cellar  livingSpace  \
0      840.00          1965.0         Oil        False     True        86.00
2     1300.00          2019.0  Other_imputed        False     True        83.80
4      903.00          1950.0         Gas        False    False        84.97
```

6	380.00	1881.0	Other_imputed	False	True	62.00
7	584.25	1959.0	Gas	False	True	60.30

	condition	lift	typeOfFlat	geo_plz	noRooms	floor	garden
0	well_kept	False	ground_floor	44269	4.0	1.0	True
2	first_time_use	True	apartment	1097	3.0	3.0	False
4	refurbished	False	apartment	28213	3.0	1.0	False
6	fully_renovated	False	Other_imputed	9599	2.0	1.0	True
7	Other	False	ground_floor	28717	3.0	2.0	False

```
[ ]: # Initial Data Cleaning: Convert boolean to int
bool_columns = ['newlyConst', 'balcony', 'hasKitchen', 'cellar', 'lift', 'garden']
df[bool_columns] = df[bool_columns].astype(int)
```

```
[ ]: # Define features and target
X = df.drop('totalRent', axis=1)
y = df['totalRent']
```

```
[ ]: # Identify categorical and numerical columns
categorical_cols = X.select_dtypes(include=['object']).columns.tolist()
numerical_cols = X.select_dtypes(include=['float64', 'int64']).columns.tolist()
numerical_cols = [col for col in numerical_cols if col not in bool_columns]
```

```
[ ]: # Preprocessing Pipelines
numeric_transformer = Pipeline(steps=[
    ('scaler', StandardScaler())
])

categorical_transformer = Pipeline(steps=[
    ('onehot', OneHotEncoder(handle_unknown='ignore'))
])
```

```
[ ]: # Combine preprocessing steps
preprocessor = ColumnTransformer(
    transformers=[
        ('num', numeric_transformer, numerical_cols),
        ('cat', categorical_transformer, categorical_cols)
    ],
    remainder='passthrough' # Keep bool columns as they are already numeric
)
```

```
[ ]: # Define individual models
lr = Pipeline(steps=[
    ('preprocessor', preprocessor),
    ('model', LinearRegression())
])
```

```

lasso = Pipeline(steps=[
    ('preprocessor', preprocessor),
    ('model', Lasso(random_state=42))
])

rf = Pipeline(steps=[
    ('preprocessor', preprocessor),
    ('model', RandomForestRegressor(random_state=42))
])

gb = Pipeline(steps=[
    ('preprocessor', preprocessor),
    ('model', GradientBoostingRegressor(random_state=42))
])

xgb = Pipeline(steps=[
    ('preprocessor', preprocessor),
    ('model', XGBRegressor(random_state=42, n_jobs=-1))
])

```

[ ]: *# Hyperparameter tuning for some models (using GridSearchCV)*

```

param_grid_lasso = {
    'model__alpha': [0.1, 1, 10, 100]
}

param_grid_rf = {
    'model__n_estimators': [100, 200],
    'model__max_depth': [None, 10, 20]
}

param_grid_gb = {
    'model__n_estimators': [100, 200],
    'model__learning_rate': [0.05, 0.1, 0.2],
    'model__max_depth': [3, 5, 7]
}

param_grid_xgb = {
    'model__n_estimators': [100, 200],
    'model__learning_rate': [0.05, 0.1, 0.2],
    'model__max_depth': [3, 5, 7]
}

```

[ ]: *# Initialize GridSearchCV for models*

```

grid_search_lasso = GridSearchCV(lasso, param_grid_lasso, cv=5, n_jobs=-1,
    ↪scoring='neg_mean_squared_error')

```

```

grid_search_rf = GridSearchCV(rf, param_grid_rf, cv=5, n_jobs=-1,
    ↳scoring='neg_mean_squared_error')
grid_search_gb = GridSearchCV(gb, param_grid_gb, cv=5, n_jobs=-1,
    ↳scoring='neg_mean_squared_error')
grid_search_xgb = GridSearchCV(xgb, param_grid_xgb, cv=5, n_jobs=-1,
    ↳scoring='neg_mean_squared_error')

```

GridSearchCV exhaustively searches over a specified parameter grid to find the best hyperparameters for the model.

```

[ ]: # Fit models to training data
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3,
    ↳random_state=RSEED)

```

```

[ ]: grid_search_lasso.fit(X_train, y_train)

```

```

[ ]: GridSearchCV(cv=5,
            estimator=Pipeline(steps=[('preprocessor',
            ColumnTransformer(remainder='passthrough',
                                transformers=[('num',
            Pipeline(steps=[('scaler',
                            StandardScaler()))],
            ['serviceCharge',
            'pricetrend',
            'yearConstructed',
            'livingSpace',
            'geo_plz',
            'noRooms',
            'floor'])],
                                ('cat',
            Pipeline(steps=[('onehot',
                            OneHotEncoder(handle_unknown='ignore'))]),
            ['heatingType',
            'firingTypes',
            'condition',
            'typeOfFlat'])]])),
            ('model', Lasso(random_state=42))),
            n_jobs=-1, param_grid={'model__alpha': [0.1, 1, 10, 100]},
            scoring='neg_mean_squared_error')

```

```

[ ]: grid_search_rf.fit(X_train, y_train)

```

```

[ ]: GridSearchCV(cv=5,
            estimator=Pipeline(steps=[('preprocessor',
            ColumnTransformer(remainder='passthrough',
                                transformers=[('num',
            Pipeline(steps=[('scaler',
                            StandardScaler()))],

```

```

['serviceCharge',
'pricetrend',
'yearConstructed',
'livingSpace',
'geo_plz',
'noRooms',
'floor']],

('cat',

Pipeline(steps=[('onehot',
                  OneHotEncoder(handle_unknown='ignore'))]),
['heatingType',
'firingTypes',
'condition',
'typeOfFlat']]))),

('model',
RandomForestRegressor(random_state=42))),
n_jobs=-1,
param_grid={'model__max_depth': [None, 10, 20],
            'model__n_estimators': [100, 200]},
scoring='neg_mean_squared_error')

```

```
[ ]: grid_search_gb.fit(X_train, y_train)
```

```

[ ]: GridSearchCV(cv=5,
                  estimator=Pipeline(steps=[('preprocessor',
ColumnTransformer(remainder='passthrough',

transformers=[('num',

Pipeline(steps=[('scaler',
                  StandardScaler()))]),
['serviceCharge',
'pricetrend',
'yearConstructed',
'livingSpace',
'geo_plz',
'noRooms',
'floor']],

('cat',

Pipeline(steps=[('onehot',
                  OneHotEncoder(handle_unknown='ignore'))]),
['heatingType',
'firingTypes',
'condition',
'typeOfFlat']]))),

('model',
GradientBoostingRegressor(random_state=42))),
n_jobs=-1,
param_grid={'model__learning_rate': [0.05, 0.1, 0.2],

```

```

        'model__max_depth': [3, 5, 7],
        'model__n_estimators': [100, 200]},
    scoring='neg_mean_squared_error')

```

```
[ ]: grid_search_xgb.fit(X_train, y_train)
```

```
[ ]: GridSearchCV(cv=5,
                  estimator=Pipeline(steps=[('preprocessor',
ColumnTransformer(remainder='passthrough',
                                transformers=[('num',
Pipeline(steps=[('scaler',
                  StandardScaler()))],
['serviceCharge',
'pricetrend',
'yearConstructed',
'livingSpace',
'geo_plz',
'noRooms',
'floor']),
                                ('cat',
Pipeline(steps=[('onehot',
                  OneHotEncoder(handle_unknown='ignore'))]),
['heatingType'...
                                max_delta_step=None,
                                max_depth=None,
                                max_leaves=None,
                                min_child_weight=None,
                                missing=nan,
                                monotone_constraints=None,
                                multi_strategy=None,
                                n_estimators=None,
                                n_jobs=-1,
                                num_parallel_tree=None,
                                random_state=42, ...)])),
n_jobs=-1,
param_grid={'model__learning_rate': [0.05, 0.1, 0.2],
            'model__max_depth': [3, 5, 7],
            'model__n_estimators': [100, 200]},
scoring='neg_mean_squared_error')

```

```
[ ]: # Best estimators
best_lasso = grid_search_lasso.best_estimator_
best_rf = grid_search_rf.best_estimator_
best_gb = grid_search_gb.best_estimator_
best_xgb = grid_search_xgb.best_estimator_

```

```
[ ]: # Create VotingRegressor
voting_regressor = VotingRegressor(estimators=[
    ('lr', lr),
    ('lasso', best_lasso),
    ('rf', best_rf),
    ('gb', best_gb),
    ('xgb', best_xgb)
])
```

using an ensemble method by combining multiple models (Lasso, Random Forest, Gradient Boosting, XGBoost) into a single VotingRegressor.

```
[ ]: # Fit VotingRegressor to the training data
voting_regressor.fit(X_train, y_train)
```

```
[ ]: VotingRegressor(estimators=[('lr',
                                Pipeline(steps=[('preprocessor',
                                                    ColumnTransformer(remainder='passthrough',
                                                    transformers=[('num',
                                                                    Pipeline(steps=[('scaler',
                                                                                          StandardScaler()))]),
                                                                    ['serviceCharge',
                                                                    'pricetrend',
                                                                    'yearConstructed',
                                                                    'livingSpace',
                                                                    'geo_plz',
                                                                    'noRooms',
                                                                    'floor'])],
                                                                    ('cat',
                                                                    Pipeline(steps=[('onehot',
                                                                                          OneHotEncoder(handle_unknown='ignore'))])),
                                                                    ['heatin...
                                                                    gamma=None,
                                                                    grow_policy=None,
                                                                    importance_type=None,

                                                                    learning_rate=0.2,
                                                                    max_bin=None,

                                                                    max_delta_step=None,
                                                                    max_depth=7,
                                                                    max_leaves=None,

                                                                    missing=nan,

                                                                    multi_strategy=None,
                                                                    n_estimators=200,
```

```

num_parallel_tree=None,
n_jobs=-1,
random_state=42,
...)))])))]

```

```

[ ]: # Make predictions
y_pred = voting_regressor.predict(X_test)

```

```

[ ]: # Evaluate the model
rmse = mean_squared_error(y_test, y_pred, squared=False)

```

```

[ ]: # Print the RMSE
print(f"Root Mean Squared Error of Voting Regressor: {rmse}")

```

Root Mean Squared Error of Voting Regressor: 130.3362053801899

```

[ ]: # Individual model RMSEs for comparison
rmse_lr = mean_squared_error(y_test, lr.fit(X_train, y_train).predict(X_test),
    ↪squared=False)
rmse_lasso = mean_squared_error(y_test, best_lasso.predict(X_test),
    ↪squared=False)
rmse_rf = mean_squared_error(y_test, best_rf.predict(X_test), squared=False)
rmse_gb = mean_squared_error(y_test, best_gb.predict(X_test), squared=False)
rmse_xgb = mean_squared_error(y_test, best_xgb.predict(X_test), squared=False)

print(f"RMSE of Linear Regression: {rmse_lr}")
print(f"RMSE of Best Lasso: {rmse_lasso}")
print(f"RMSE of Best Random Forest: {rmse_rf}")
print(f"RMSE of Best Gradient Boosting: {rmse_gb}")
print(f"RMSE of Best XGBoost: {rmse_xgb}")

```

RMSE of Linear Regression: 182.11693263343457  
 RMSE of Best Lasso: 182.15263860937318  
 RMSE of Best Random Forest: 132.6869698890814  
 RMSE of Best Gradient Boosting: 109.9028656958718  
 RMSE of Best XGBoost: 118.16864722893187

```

[ ]: # Calculate RMSE ensemble model
rmse = 130.34 # Replace with the actual RMSE value
# Assuming you have a DataFrame called 'df' with a column 'totalRent'
    ↪containing rent values
rent_range = df['totalRent'].max() - df['totalRent'].min()
mean_rent = df['totalRent'].mean()

# Compare RMSE to rent value range
rmse_vs_range = rmse / rent_range

# Compare RMSE to mean rent value

```



```
rmse_vs_mean = rmse / mean_rent

print(f"RMSE vs. Rent Range: {rmse_vs_range:.2%}")
print(f"RMSE vs. Mean Rent: {rmse_vs_mean:.2%}")
```

RMSE vs. Rent Range: 7.24%

RMSE vs. Mean Rent: 17.45%

```
[ ]: # Calculate RMSE Gradient Boosting
rmse = 109.90 # Replace with the actual RMSE value
# Assuming you have a DataFrame called 'df' with a column 'totalRent'
↳ containing rent values
rent_range = df['totalRent'].max() - df['totalRent'].min()
mean_rent = df['totalRent'].mean()

# Compare RMSE to rent value range
rmse_vs_range = rmse / rent_range

# Compare RMSE to mean rent value
rmse_vs_mean = rmse / mean_rent

print(f"RMSE vs. Rent Range: {rmse_vs_range:.2%}")
print(f"RMSE vs. Mean Rent: {rmse_vs_mean:.2%}")
```

RMSE vs. Rent Range: 6.11%

RMSE vs. Mean Rent: 14.71%

## 1 Visualizing the results

### 1.1 Scatter plots actual vs. predicted of each model

to following Scatter plots compares the actual rent values ( $y_{\text{test}}$ ) to the predicted rent values ( $y_{\text{pred}}$ ) from the different models. First the best one from ensemble Method. (GBM) separated, than all next to each other to compare:

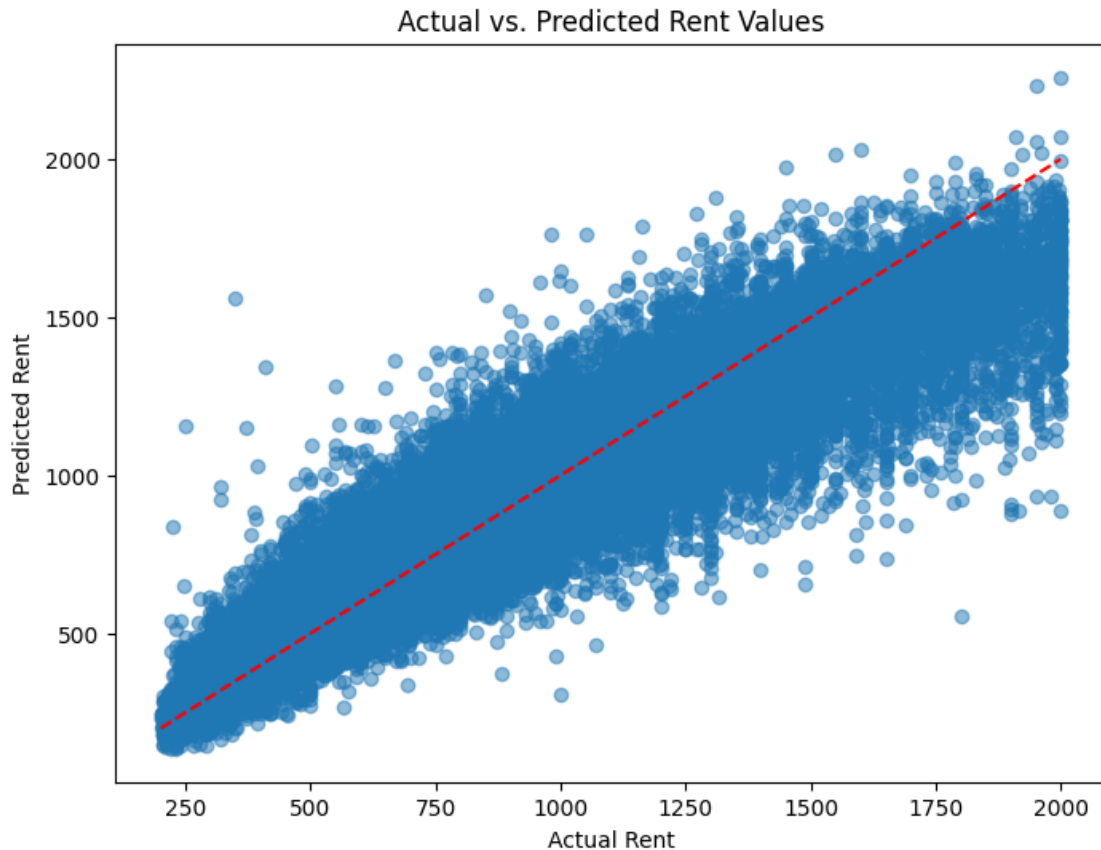
The scatter plot helps in visually assessing the performance of your regression model by comparing predicted values against actual values. It provides insight into the accuracy, consistency, and potential biases in the model's predictions. A good model would show points closely clustered around the diagonal line with minimal spread, indicating accurate and reliable predictions across the entire range of rent values.

#### 1.1.1 Plot Components:

- A scatter plot of actual rent values vs. predicted rent values.
- A red dashed line representing the ideal scenario where predicted values perfectly match actual values.

```
[ ]: plt.figure(figsize=(8, 6))
plt.scatter(y_test, y_pred, alpha=0.5)
```

```
plt.plot([min(y_test), max(y_test)], [min(y_test), max(y_test)], '--',
         color='red') # Diagonal line
plt.title('Actual vs. Predicted Rent Values')
plt.xlabel('Actual Rent')
plt.ylabel('Predicted Rent')
plt.show()
```



for all Models side by side

```
[ ]: # Predict using each model
y_pred_lr = lr.predict(X_test)
y_pred_lasso = best_lasso.predict(X_test)
y_pred_rf = best_rf.predict(X_test)
y_pred_gb = best_gb.predict(X_test)
y_pred_xgb = best_xgb.predict(X_test)
y_pred_voting = voting_regressor.predict(X_test)

# Create a 3x2 grid of subplots
fig, axes = plt.subplots(3, 2, figsize=(15, 18))
```

```

# Plot for Linear Regression
axes[0, 0].scatter(y_test, y_pred_lr, alpha=0.5)
axes[0, 0].plot([min(y_test), max(y_test)], [min(y_test), max(y_test)], '--',
               color='red')
axes[0, 0].set_title('Actual vs. Predicted Rent Values (Linear Regression)')
axes[0, 0].set_xlabel('Actual Rent')
axes[0, 0].set_ylabel('Predicted Rent')

# Plot for Best Lasso
axes[0, 1].scatter(y_test, y_pred_lasso, alpha=0.5)
axes[0, 1].plot([min(y_test), max(y_test)], [min(y_test), max(y_test)], '--',
               color='red')
axes[0, 1].set_title('Actual vs. Predicted Rent Values (Best Lasso)')
axes[0, 1].set_xlabel('Actual Rent')
axes[0, 1].set_ylabel('Predicted Rent')

# Plot for Best Random Forest
axes[1, 0].scatter(y_test, y_pred_rf, alpha=0.5)
axes[1, 0].plot([min(y_test), max(y_test)], [min(y_test), max(y_test)], '--',
               color='red')
axes[1, 0].set_title('Actual vs. Predicted Rent Values (Best Random Forest)')
axes[1, 0].set_xlabel('Actual Rent')
axes[1, 0].set_ylabel('Predicted Rent')

# Plot for Best Gradient Boosting
axes[1, 1].scatter(y_test, y_pred_gb, alpha=0.5)
axes[1, 1].plot([min(y_test), max(y_test)], [min(y_test), max(y_test)], '--',
               color='red')
axes[1, 1].set_title('Actual vs. Predicted Rent Values (Best Gradient_
               Boosting)')
axes[1, 1].set_xlabel('Actual Rent')
axes[1, 1].set_ylabel('Predicted Rent')

# Plot for Best XGBoost
axes[2, 0].scatter(y_test, y_pred_xgb, alpha=0.5)
axes[2, 0].plot([min(y_test), max(y_test)], [min(y_test), max(y_test)], '--',
               color='red')
axes[2, 0].set_title('Actual vs. Predicted Rent Values (Best XGBoost)')
axes[2, 0].set_xlabel('Actual Rent')
axes[2, 0].set_ylabel('Predicted Rent')

# Plot for Voting Regressor
axes[2, 1].scatter(y_test, y_pred_voting, alpha=0.5)
axes[2, 1].plot([min(y_test), max(y_test)], [min(y_test), max(y_test)], '--',
               color='red')
axes[2, 1].set_title('Actual vs. Predicted Rent Values (Voting Regressor)')

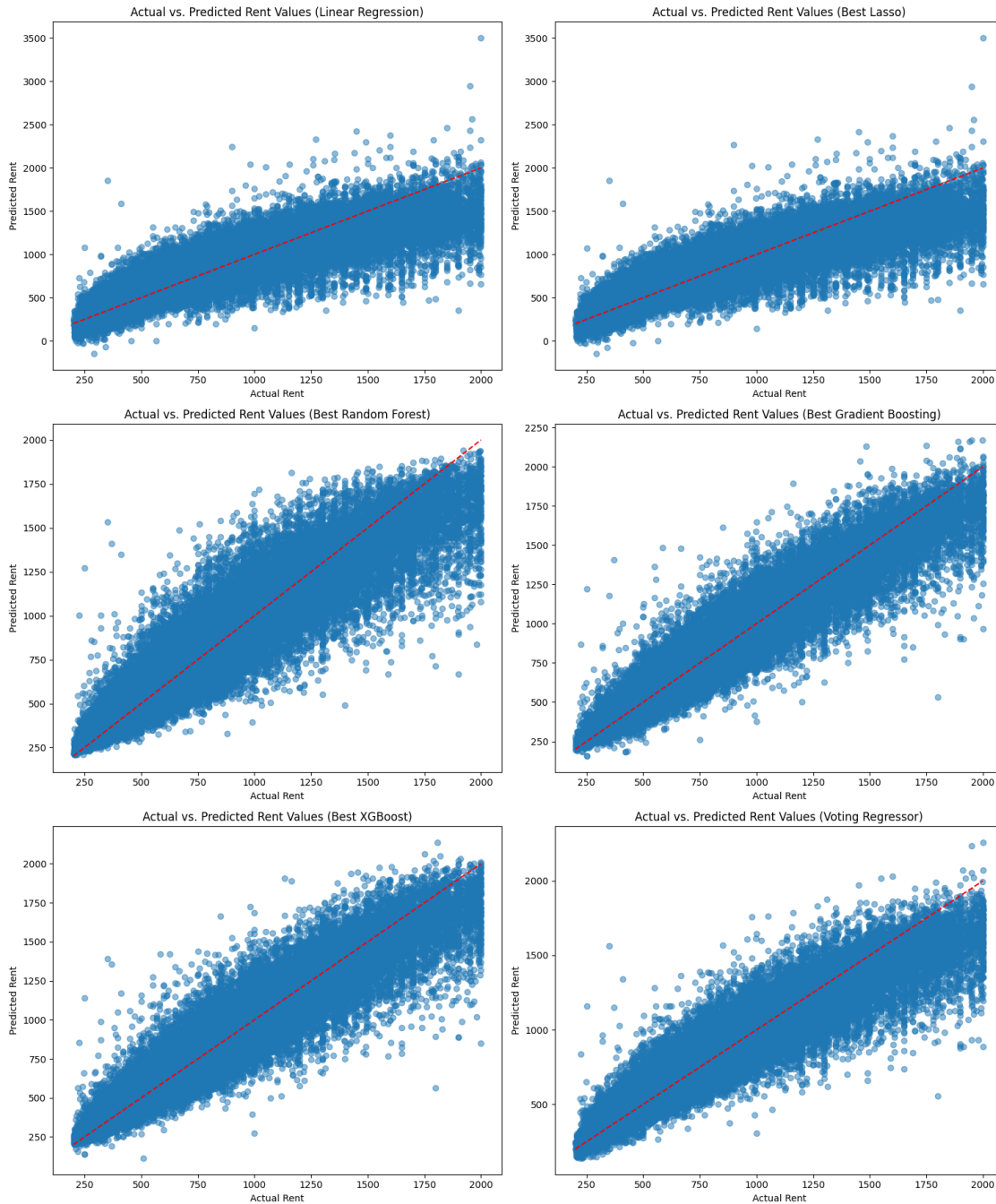
```

```

axes[2, 1].set_xlabel('Actual Rent')
axes[2, 1].set_ylabel('Predicted Rent')

plt.tight_layout()
plt.show()

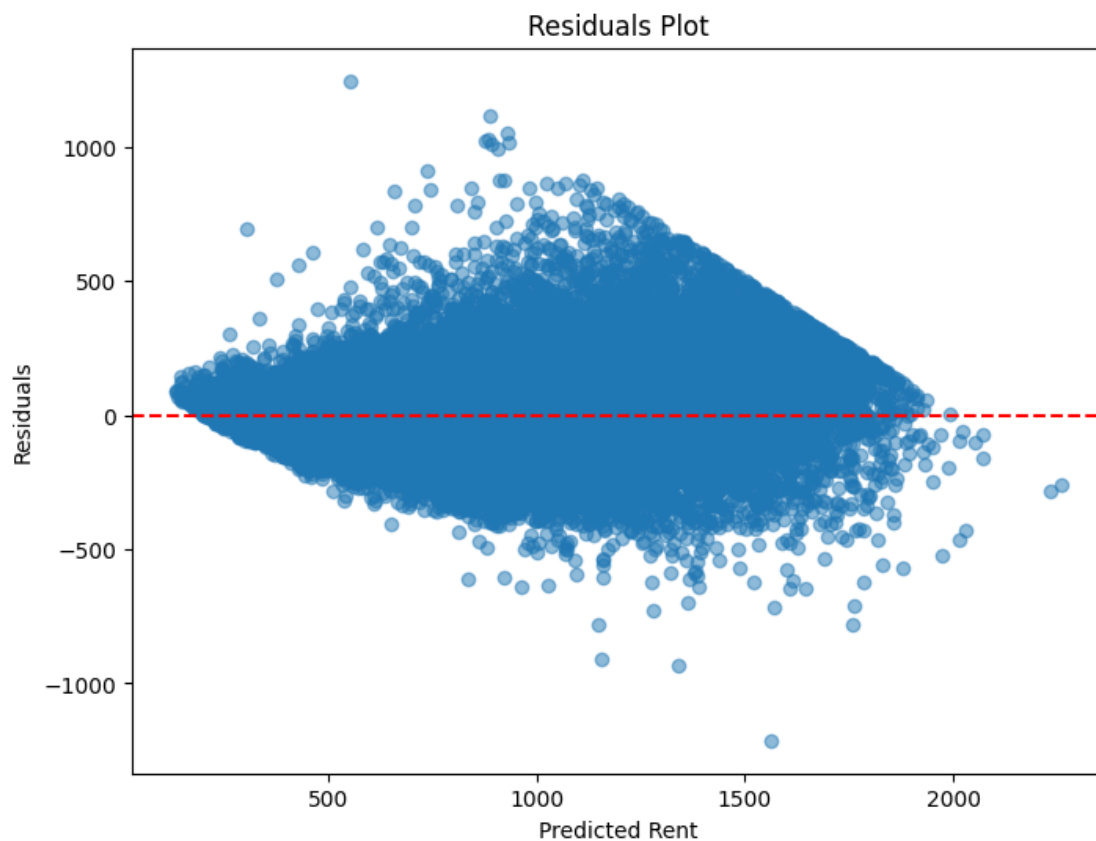
```



## 1.2 Residuals Plots

A residuals plot helps you evaluate the goodness of fit of a regression model. Ideally, the Voting Regressor should have the most evenly scattered residuals around zero, indicating it's capturing the patterns in the data well.

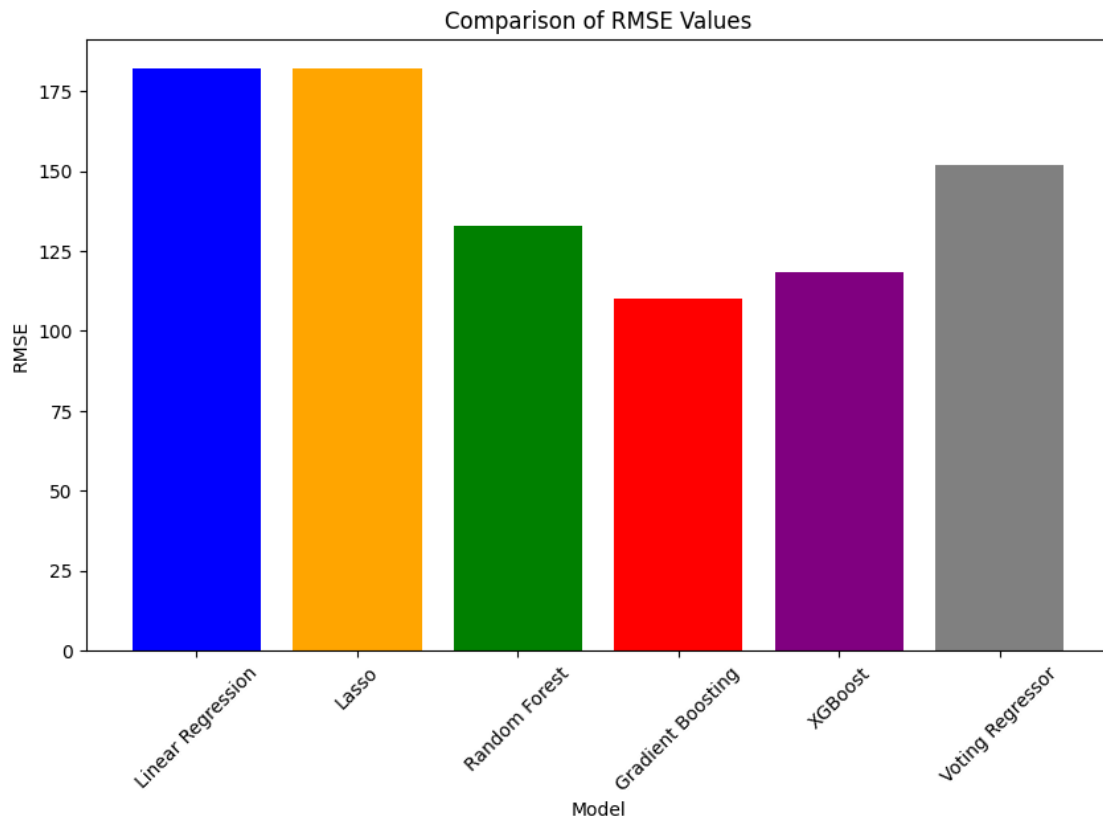
```
[ ]: residuals = y_test - y_pred
plt.figure(figsize=(8, 6))
plt.scatter(y_pred, residuals, alpha=0.5)
plt.axhline(y=0, color='red', linestyle='--') # Horizontal line at y=0
plt.title('Residuals Plot')
plt.xlabel('Predicted Rent')
plt.ylabel('Residuals')
plt.show()
```



```
[ ]: models = ['Linear Regression', 'Lasso', 'Random Forest', 'Gradient Boosting', 'XGBoost', 'Voting Regressor']
rmse_values = [rmse_lr, rmse_lasso, rmse_rf, rmse_gb, rmse_xgb, rmse]

plt.figure(figsize=(10, 6))
```

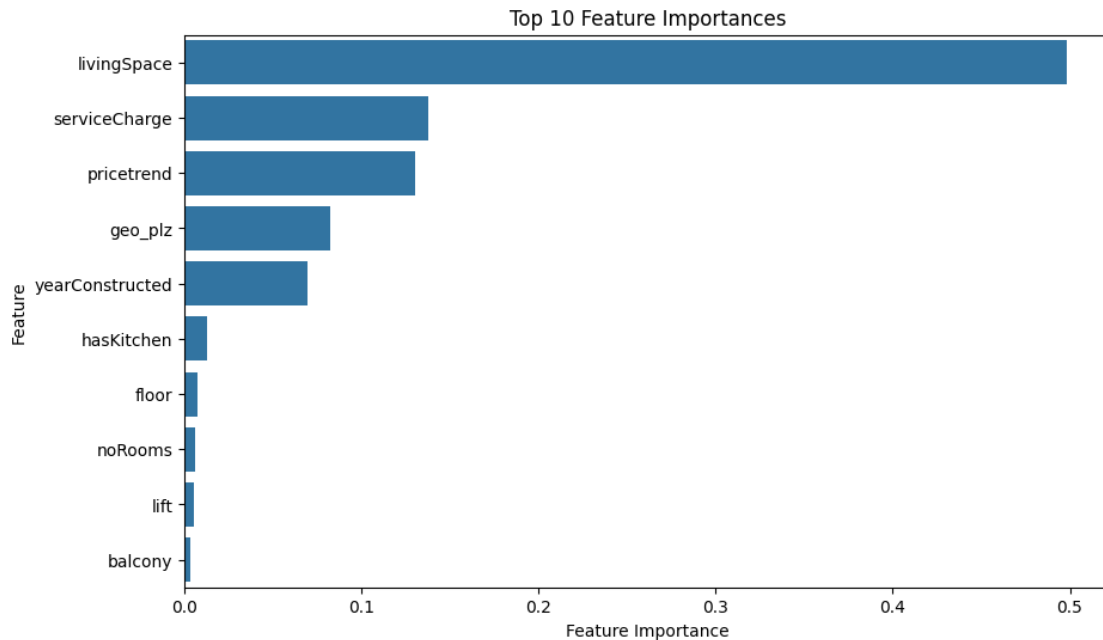
```
plt.bar(models, rmse_values, color=['blue', 'orange', 'green', 'red', 'purple', 'gray'])
plt.title('Comparison of RMSE Values')
plt.xlabel('Model')
plt.ylabel('RMSE')
plt.xticks(rotation=45)
plt.show()
```



```
[ ]: # Check if the model inside the pipeline has feature importances
if hasattr(best_rf.named_steps['model'], 'feature_importances_'):
    feature_importances = best_rf.named_steps['model'].feature_importances_
    sorted_indices = np.argsort(feature_importances)[::-1] # Sort indices in
    ↪descending order

    # Create a list of feature names
    preprocessor_features = numerical_cols + list(best_rf.
    ↪named_steps['preprocessor'].transformers_[1][1].named_steps['onehot'].
    ↪get_feature_names_out(categorical_cols)) + bool_columns
    top_features = [preprocessor_features[i] for i in sorted_indices][:10] #
    ↪Display top 10 features
```

```
plt.figure(figsize=(10, 6))
sns.barplot(x=feature_importances[sorted_indices][:10], y=top_features)
plt.title('Top 10 Feature Importances')
plt.xlabel('Feature Importance')
plt.ylabel('Feature')
plt.show()
else:
    print("The model does not have feature importances attribute.")
```



### 1.3 Hyperparameter Tuning Curves

Each subplot shows the relationship between a specific hyperparameter and the model's performance, typically measured using a metric such as the negative mean squared error (MSE).

The plot displayed illustrates the results of hyperparameter tuning for four different models: Lasso, Random Forest, Gradient Boosting, and XGBoost. Here's an analysis and explanation of each subplot:

Lasso Hyperparameter Tuning Curve:

The plot shows the relationship between the alpha parameter (regularization strength) of the Lasso regression model and the negative mean squared error (MSE). As the value of alpha increases, the negative MSE also increases, indicating higher prediction error. This suggests that higher regularization leads to less overfitting but may increase bias. The optimal alpha value appears to be around 0.1, where the negative MSE is minimized. Random Forest Hyperparameter Tuning Curve:

This plot illustrates the effect of the number of estimators (decision trees) in the Random Forest model on the negative MSE. As the number of estimators increases, the negative MSE generally decreases, suggesting improved model performance. The plot shows diminishing returns, indicating that adding more estimators beyond a certain point may not significantly improve performance. The optimal number of estimators appears to be around 100. Gradient Boosting Hyperparameter Tuning Curve:

The plot demonstrates the impact of the number of estimators on the negative MSE for the Gradient Boosting model. Similar to Random Forest, increasing the number of estimators generally leads to a decrease in negative MSE, indicating better model performance. The optimal number of estimators seems to be around 200, where the negative MSE is minimized. XGBoost Hyperparameter Tuning Curve:

This subplot shows how the negative MSE changes with the number of estimators in the XGBoost model. As the number of estimators increases, the negative MSE initially decreases, indicating improved model performance. Similar to the other models, there are diminishing returns, and beyond a certain point, adding more estimators may not significantly reduce the negative MSE. The optimal number of estimators appears to be around 200. Overall, these plots provide valuable insights into how different hyperparameters affect model performance. They help in selecting the optimal hyperparameter values that minimize prediction error and improve the generalization ability of the models.

```
[ ]: # Extract grid search results
lasso_results = pd.DataFrame(grid_search_lasso.cv_results_)
rf_results = pd.DataFrame(grid_search_rf.cv_results_)
gb_results = pd.DataFrame(grid_search_gb.cv_results_)
xgb_results = pd.DataFrame(grid_search_xgb.cv_results_)

# Plot grid search results
plt.figure(figsize=(12, 8))

plt.subplot(2, 2, 1)
plt.plot(lasso_results['param_model__alpha'],
         ↪-lasso_results['mean_test_score'], label='Lasso')
plt.title('Lasso Hyperparameter Tuning')
plt.xlabel('Alpha')
plt.ylabel('Negative MSE')
plt.legend()

plt.subplot(2, 2, 2)
plt.plot(rf_results['param_model__n_estimators'],
         ↪-rf_results['mean_test_score'], label='Random Forest')
plt.title('Random Forest Hyperparameter Tuning')
plt.xlabel('Number of Estimators')
plt.ylabel('Negative MSE')
plt.legend()

plt.subplot(2, 2, 3)
```



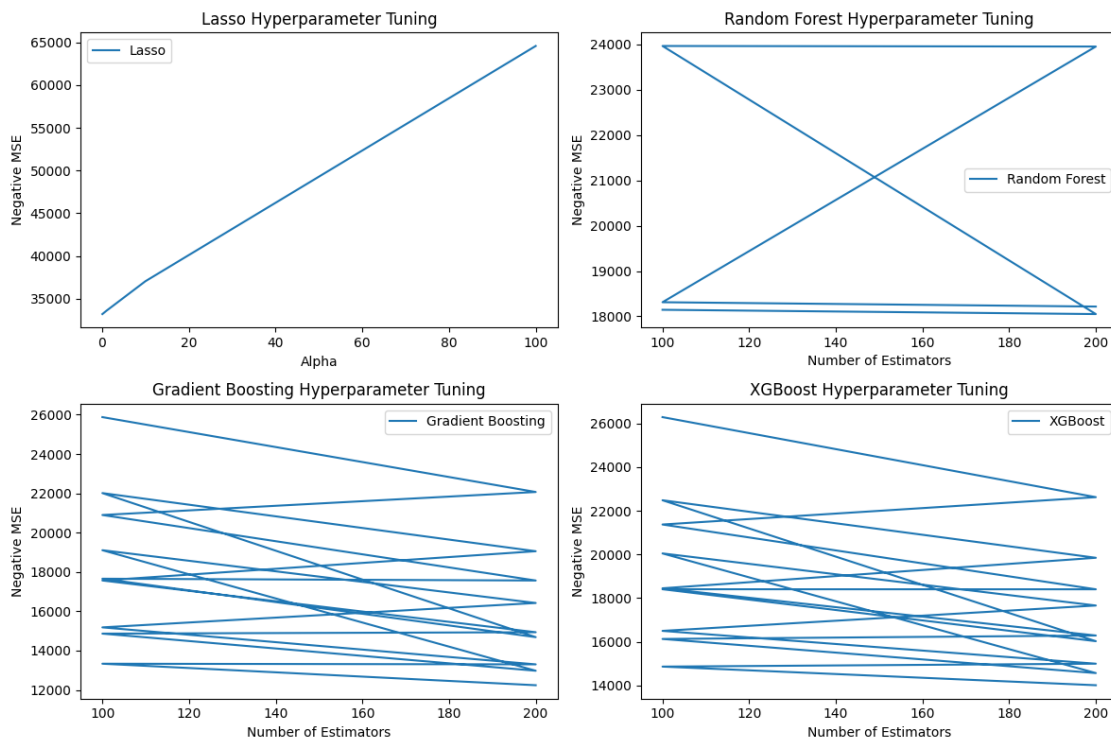
```

plt.plot(gb_results['param_model__n_estimators'],
         ↪gb_results['mean_test_score'], label='Gradient Boosting')
plt.title('Gradient Boosting Hyperparameter Tuning')
plt.xlabel('Number of Estimators')
plt.ylabel('Negative MSE')
plt.legend()

plt.subplot(2, 2, 4)
plt.plot(xgb_results['param_model__n_estimators'],
         ↪xgb_results['mean_test_score'], label='XGBoost')
plt.title('XGBoost Hyperparameter Tuning')
plt.xlabel('Number of Estimators')
plt.ylabel('Negative MSE')
plt.legend()

plt.tight_layout()
plt.show()

```



```

[ ]: # Reduce data size by taking a subset of the data
X_subset = X.sample(frac=0.5, random_state=RSEED)
y_subset = y[X_subset.index]

# Reduce the number of cross-validation folds and training sizes

```

```

train_sizes, train_scores, test_scores = learning_curve(
    voting_regressor, X_subset, y_subset, cv=3, n_jobs=-1,
    ↪scoring='neg_mean_squared_error', train_sizes=np.linspace(0.1, 1.0, 5)
)

train_scores_mean = np.mean(train_scores, axis=1)
train_scores_std = np.std(train_scores, axis=1)
test_scores_mean = np.mean(test_scores, axis=1)
test_scores_std = np.std(test_scores, axis=1)

plt.figure(figsize=(10, 6))
plt.fill_between(train_sizes, train_scores_mean - train_scores_std,
                 train_scores_mean + train_scores_std, alpha=0.1,
                 color="r")
plt.fill_between(train_sizes, test_scores_mean - test_scores_std,
                 test_scores_mean + test_scores_std, alpha=0.1, color="g")
plt.plot(train_sizes, train_scores_mean, 'o-', color="r", label="Training ↪
    ↪score")
plt.plot(train_sizes, test_scores_mean, 'o-', color="g",
    ↪label="Cross-validation score")
plt.title("Learning Curves")
plt.xlabel("Training examples")
plt.ylabel("Score")
plt.legend(loc="best")
plt.show()

```

