

Prime Articulation Theory (PAT)

Formal Experimental Specification and Replication Protocol

Status and Scope

This document is a **formal experimental specification**. It is not a theory paper, an interpretive essay, or a philosophical argument. Its sole purpose is to define, with sufficient precision, an experiment demonstrating that the prime set may emerge as a **self-sustaining coherence object** under structural constraints alone.

No symbolic prime tests, divisibility checks, or number-theoretic axioms are permitted. Any implementation that relies on such mechanisms is invalid relative to this specification.

1. Structural Posture

1.1 Ontological Separation

The experiment enforces a strict separation between:

- **Structure** — silent, invariant constraints that do not act
- **Instantiation** — an active process that must articulate under constraint

The experiment does *not* assume primes as objects. It tests whether articulation under constraint *forces* prime-like emergence.

1.2 Claim Type

This experiment provides an **existence proof by construction**:

There exists a non-symbolic process in which a prime-like set emerges as a stable, persistent object solely from coherence constraints.

No uniqueness, optimality, or completeness claims are made.

2. State Space

The runtime system maintains the following minimal state variables.

2.1 Core State Variables

- **t** : discrete time step (integer)

- **A(t)** : current articulated value (real or quantized scalar)
- **H(t)** : articulation history (ordered list of past A values)

2.2 Structural Scalars

These are real-valued parameters constrained but not semantically interpreted.

- **P(t)** — pressure
- **K(t)** — panic
- **R(t)** — resonance
- **C(t)** — coverage

These variables must be continuous (floating-point or fixed-point). Boolean or symbolic representations are disallowed.

3. Constraints

3.1 Pressure Constraint

Pressure increases monotonically when articulation fails to increase coverage.

Informal condition:

```
if  $\Delta C(t) \approx 0$ :
     $P(t+1) > P(t)$ 
```

3.2 Panic Constraint

Panic increases when pressure exceeds local structural tolerance.

```
if  $P(t) > \theta_P$ :
     $K(t+1) = K(t) + f(P(t))$ 
```

Panic must never directly generate articulation.

3.3 Resonance Constraint

Resonance measures alignment between current articulation and historical patterning.

```
 $R(t) = g(A(t), H(t))$ 
```

The function g must be history-sensitive (non-Markovian).

3.4 Coverage Constraint

Coverage measures how much of the articulation space has been spanned *without repetition*.

Coverage must increase only when articulation introduces genuinely new structure.

4. Articulation Rule

4.1 Necessity Condition

A new articulation **must** occur when:

$$K(t) > \theta_K$$

4.2 Articulation Selection

The next articulation $A(t+1)$ is selected to:

- reduce panic
- preserve or increase resonance
- minimally increase coverage

No optimization toward numeric novelty or magnitude is allowed.

4.3 Invalid Articulations

Any articulation that:

- trivially composes past articulations
- collapses resonance to zero
- artificially resets pressure or panic

is invalid and must be rejected.

5. Emergence Criteria

An articulated value **qualifies as prime-like** if and only if:

1. It cannot be expressed as a composition of prior articulations *under the experiment's allowed operations*
2. Its introduction produces a measurable drop in panic
3. It increases global coverage
4. It remains structurally relevant (continues to influence resonance)

No divisibility or factorization tests are permitted.

6. Prime Set Objecthood Criteria

The emergent collection of prime-like articulations qualifies as an **object** if it satisfies:

- **Persistence:** remains stable across extended runtime
- **Non-derivability:** cannot be eliminated without collapse of coherence
- **Generativity:** enables further articulation
- **Closure:** admits extension without redefinition

These criteria are structural, not semantic.

7. Termination and Freezing

7.1 Freezing Condition

A run may freeze when:

- panic is fully relieved
- resonance saturates
- coverage growth stalls

Freezing is *not failure*. It indicates over-resolution.

7.2 Continuation Condition

Continuation requires residual panic or unresolved pressure.

8. Replication Requirements

Any valid replication must report:

- parameter ranges for P, K, R, C
- articulation history
- panic and resonance trajectories
- emergence points

Symbolic shortcuts invalidate results.

9. Interpretation Discipline

This specification **does not** claim:

- that primes are linguistic
- that numbers are semantic
- that mathematics reduces to grammar

It claims only that **irreducible articulation under coherence pressure produces prime-like structure**.

All higher-level interpretations are downstream and optional.

10. End of Specification

This document is complete when it is precise enough to be implemented and interrogated without reference to metaphor, authority, or interpretation.