P8106 Data ScienceII HW5

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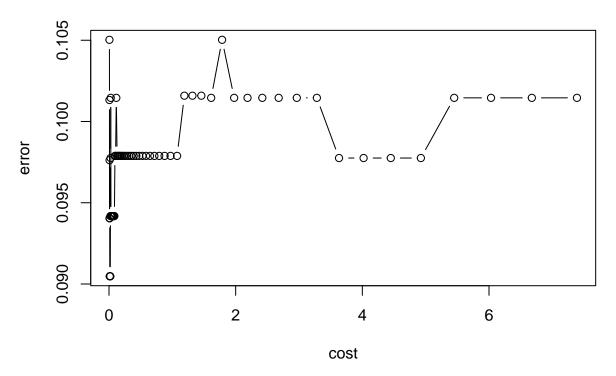
2023-04-29

```
library(tidyverse)
library(mlbench)
library(ISLR)
library(caret)
library(e1071)
library(kernlab)
library(factoextra)
library(gridExtra)
library(RColorBrewer)
library(jpeg)
library(knitr)
```

1. In this problem, we will apply support vector machines to predict whether a given car gets high or low gas mileage based on the dataset "auto.csv" (used in Homework 3; see Homework 3 for more details of the dataset). The response variable is mpg cat. The predictors are cylinders, displacement, horsepower, weight, acceleration, year, and origin. Split the dataset into two parts: training data (70%) and test data (30%).

Question A - Fit a support vector classifier (linear kernel) to the training data. What are the training and test error rates?

Performance of 'svm'



```
# summary(linear.tune)
linear.tune$best.parameters

## cost
## 7 0.01238456

best.linear <- linear.tune$best.model
summary(best.linear)

##
## Call:
## best.svm(x = mpg_cat ~ ., data = auto.data[RowTrain, ], cost = exp(seq(-5, ## 2, len = 70)), kernel = "linear", scale = TRUE)
##</pre>
```

```
##
## Parameters:
##
     SVM-Type: C-classification
  SVM-Kernel: linear
##
##
         cost: 0.01238456
##
## Number of Support Vectors: 125
##
##
  (6263)
##
##
## Number of Classes: 2
## Levels:
## low high
########################
# Training error rates
##########################
confusionMatrix(data = best.linear$fitted,
                reference = auto.data$mpg_cat[RowTrain])
## Confusion Matrix and Statistics
##
##
            Reference
## Prediction low high
         low 120
##
##
         high 18 131
##
##
                  Accuracy : 0.9094
                    95% CI : (0.8692, 0.9405)
##
##
       No Information Rate: 0.5
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.8188
##
   Mcnemar's Test P-Value: 0.0455
##
##
##
               Sensitivity: 0.8696
##
               Specificity: 0.9493
##
            Pos Pred Value: 0.9449
##
            Neg Pred Value: 0.8792
                Prevalence: 0.5000
##
##
            Detection Rate: 0.4348
##
      Detection Prevalence: 0.4601
##
         Balanced Accuracy: 0.9094
##
##
          'Positive' Class : low
##
#######################
# Test error rates
##########################
```

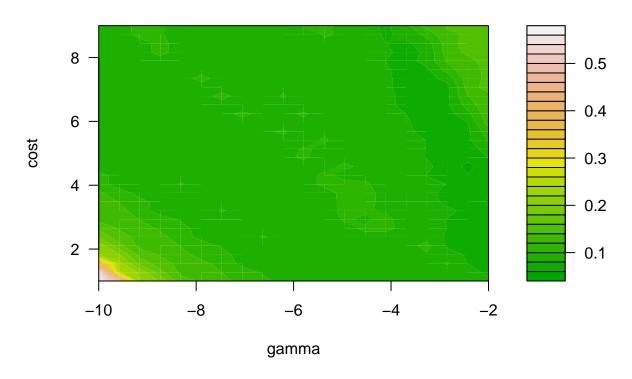
```
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction low high
##
         low
               50
                     3
##
         high
                    55
##
                  Accuracy: 0.9052
##
                    95% CI: (0.8367, 0.9517)
##
       No Information Rate: 0.5
##
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.8103
##
    Mcnemar's Test P-Value: 0.2278
##
##
##
               Sensitivity: 0.8621
               Specificity: 0.9483
##
##
            Pos Pred Value: 0.9434
##
            Neg Pred Value: 0.8730
##
                Prevalence: 0.5000
##
            Detection Rate: 0.4310
##
      Detection Prevalence: 0.4569
##
         Balanced Accuracy: 0.9052
##
##
          'Positive' Class : low
##
```

From above output when applying a support vector classifier to the training data,

- For the training data, the accuracy of the fitted support vector classifier reads as 0.9094(90.94%), for the given data and observations. If a model will perform at 92.03% accuracy then the error rate will be 1-0.9094 = 9.06%.
- For the testing data, the accuracy reads as 0.9052(90.52%), so the the error rate will be 1-0.9052 = 9.48%.

Question B - Fit a support vector machine with a radial kernel to the training data. What are the training and test error rates?

Performance of 'svm'



```
# summary(radial.tune)
best.radial <- radial.tune$best.model
summary(best.radial)</pre>
```

```
##
## best.svm(x = mpg_cat \sim ., data = auto.data[RowTrain, ], gamma = exp(seq(-10,
##
       -2, len = 20)), cost = exp(seq(1, 9, len = 30)), kernel = "radial")
##
##
## Parameters:
      SVM-Type: C-classification
##
##
    SVM-Kernel: radial
                 98.12154
##
          cost:
##
## Number of Support Vectors: 55
##
   (31 24)
##
##
##
```

```
## Number of Classes: 2
##
## Levels:
## low high
#######################
# Training error rates
#######################
confusionMatrix(data = best.radial$fitted,
                reference = auto.data$mpg_cat[RowTrain])
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction low high
         low 133 4
##
        high 5 134
##
##
                  Accuracy : 0.9674
##
                    95% CI: (0.939, 0.985)
##
       No Information Rate: 0.5
##
       P-Value [Acc > NIR] : <2e-16
##
##
                     Kappa: 0.9348
##
##
   Mcnemar's Test P-Value : 1
##
               Sensitivity: 0.9638
##
##
               Specificity: 0.9710
##
            Pos Pred Value : 0.9708
##
            Neg Pred Value: 0.9640
##
                Prevalence: 0.5000
            Detection Rate: 0.4819
##
##
     Detection Prevalence: 0.4964
##
         Balanced Accuracy: 0.9674
##
##
          'Positive' Class : low
##
############################
# Test error rates
########################
pred.radial <- predict(best.radial, newdata = auto.data[-RowTrain,])</pre>
confusionMatrix(data = pred.radial,
                reference = auto.data$mpg_cat[-RowTrain])
## Confusion Matrix and Statistics
##
##
             Reference
## Prediction low high
         low 54
         high 4
                    53
##
```

```
##
##
                  Accuracy : 0.9224
                    95% CI: (0.8578, 0.9639)
##
##
       No Information Rate: 0.5
       P-Value [Acc > NIR] : <2e-16
##
##
##
                     Kappa: 0.8448
##
##
    Mcnemar's Test P-Value : 1
##
##
               Sensitivity: 0.9310
               Specificity: 0.9138
##
            Pos Pred Value: 0.9153
##
##
            Neg Pred Value: 0.9298
                Prevalence : 0.5000
##
##
            Detection Rate: 0.4655
##
      Detection Prevalence: 0.5086
##
         Balanced Accuracy: 0.9224
##
          'Positive' Class : low
##
##
```

From above output when fitting a support vector machine with a radial kernel to the training data,

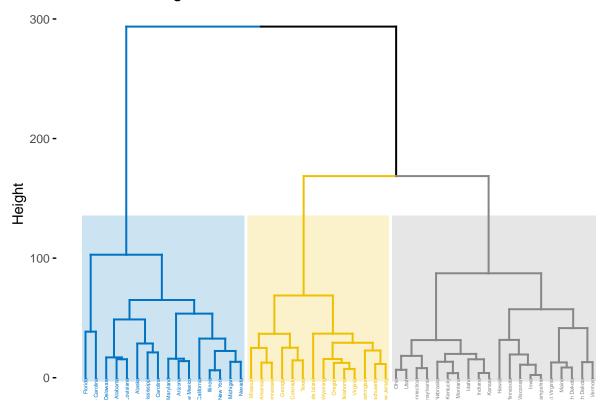
- For the training data, the accuracy of the fitted support vector classifier reads as 0.9674(96.74%), for the given data and observations. If a model will perform at 96.74% accuracy then the error rate will be 1-0.9674 = 3.26%.
- For the testing data, the accuracy reads as 0.9224(92.24%), so the the error rate will be 1-0.9224 = 7.76%.

2. In this problem, we perform hierarchical clustering on the states using the USArrests data in the ISLR package. For each of the 50 states in the United States, the dataset contains the number of arrests per 100,000 residents for each of three crimes: Assault, Murder, and Rape. The dataset also contains the percent of the population in each state living in urban areas, UrbanPop. The four variables will be used as features for clustering.

```
USArrests.dat <- USArrests %>%
   na.omit()
```

Question A - Using hierarchical clustering with complete linkage and Euclidean distance, cluster the states. Cut the dendrogram at a height that results in three distinct clusters. Which states belong to which clusters?

Cluster Dendrogram



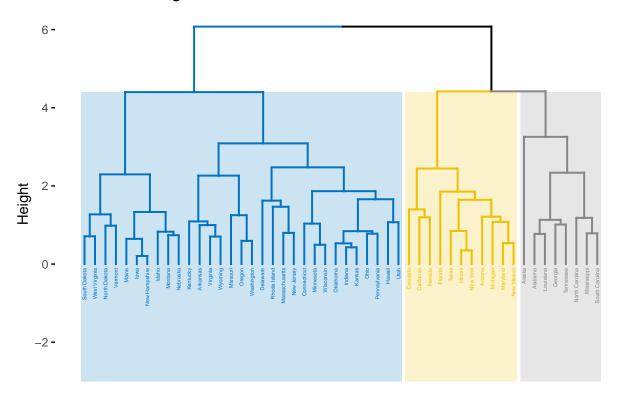
```
ind3.complete <- cutree(hc.complete, 3)</pre>
###################################
# The state in each cluster
##################################
col1 <- row.names(USArrests.dat[ind3.complete == 1,])</pre>
col2 <- row.names(USArrests.dat[ind3.complete == 2,])</pre>
col3 <- row.names(USArrests.dat[ind3.complete == 3,])</pre>
# Determine the length of the longest column
max_length <- max(length(col1), length(col2), length(col3))</pre>
Cluster1 <- c(col1, rep(" ", max_length - length(col1)))</pre>
Cluster2 <- c(col2, rep(" ", max_length - length(col2)))</pre>
Cluster3 <- c(col3, rep(" ", max_length - length(col3)))</pre>
# Combine the padded columns into a single table
cluster.table <- cbind(Cluster1, Cluster2,Cluster3)</pre>
# Print
knitr::kable(cluster.table, format = "simple",caption = "The state in each cluster")
```

Table 1: The state in each cluster

Cluster1	Cluster2	Cluster3
Alabama	Arkansas	Connecticut
Alaska	Colorado	Hawaii
Arizona	Georgia	Idaho
California	Massachusetts	Indiana
Delaware	Missouri	Iowa
Florida	New Jersey	Kansas
Illinois	Oklahoma	Kentucky
Louisiana	Oregon	Maine
Maryland	Rhode Island	Minnesota
Michigan	Tennessee	Montana
Mississippi	Texas	Nebraska
Nevada	Virginia	New Hampshire
New Mexico	Washington	North Dakota
New York	Wyoming	Ohio
North Carolina		Pennsylvania
South Carolina		South Dakota
		Utah
		Vermont
		West Virginia
		Wisconsin

Question B - Hierarchically cluster the states using complete linkage and Euclidean distance, after scaling the variables to have standard deviation one. Does scaling the variables change the clustering results? Why? In your opinion, should the variables be scaled before the inter-observation dissimilarities are computed?

Cluster Dendrogram



```
ind3.complete.sd <- cutree(hc.complete.sd, 3)</pre>
# The state in each cluster After Standardized
col1.sd <- row.names(USArrests.sd[ind3.complete.sd == 1,])</pre>
col2.sd <- row.names(USArrests.sd[ind3.complete.sd == 2,])</pre>
col3.sd <- row.names(USArrests.sd[ind3.complete.sd == 3,])</pre>
# Determine the length of the longest column
max_length <- max(length(col1.sd), length(col2.sd), length(col3.sd))</pre>
Cluster1 <- c(col1.sd, rep(" ", max_length - length(col1.sd)))</pre>
Cluster2 <- c(col2.sd, rep(" ", max_length - length(col2.sd)))</pre>
Cluster3 <- c(col3.sd, rep(" ", max_length - length(col3.sd)))</pre>
# Combine the padded columns into a single table
cluster.tibble <- cbind(Cluster1, Cluster2,Cluster3)</pre>
# Print
knitr::kable(cluster.tibble, format = "simple", caption = "The state in each cluster After Standardized
```

Table 2: The state in each cluster After Standardized

Alabama Arizona Alaska California Georgia Colorado Louisiana Florida Mississippi Illinois North Carolina Maryland South Carolina Michigan	Arkansas
Georgia Colorado Louisiana Florida Mississippi Illinois North Carolina Maryland	THAIDAD
Louisiana Florida Mississippi Illinois North Carolina Maryland	Connecticut
Mississippi Illinois North Carolina Maryland	Delaware
North Carolina Maryland	Hawaii
v	Idaho
South Carolina Michigan	Indiana
	Iowa
Tennessee Nevada	Kansas
New Mexic	o Kentucky
New York	Maine
Texas	Massachusetts
	Minnesota
	Missouri
	Montana
	Nebraska
	New Hampshire
	New Jersey
	North Dakota
	Ohio
	Oklahoma
	Oregon
	Pennsylvania
	Rhode Island
	South Dakota
	Utah
	Vermont
	Virginia
	Washington
	West Virginia
	Wisconsin
	Wyoming

- Compared these two tables, we know that scaling the variables can change the clustering results.
- It is important to scale the variables before computing inter-observation dissimilarities in hierarchical clustering, especially when the variables are measured on different scales, which ensures that each variable has an equal contribution to the clustering process and can help to avoid bias in the clustering results.