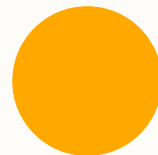




# Callstacks and Recursion

---



0



# Callstack

---

- We've briefly talked about the callstack
  - Stack ADT
  - Method call  $\Rightarrow$  `Stack.push()`
  - Return  $\Rightarrow$  `Stack.pop()`
- Track the execution of our programs with this idea





# Callstack

---

```
public static void main(String[] args){  
    int a = 6;  
    int b = 8  
  
    int result = doMath(a, b)  
  
    System.out.print(result)  
  
}
```

Programs Call Stack






# Callstack

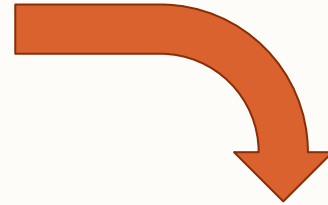
---

Main gets  
called



```
public static void main(String[] args){  
    int a = 6;  
    int b = 8  
  
    int result = doMath(a, b)  
  
    System.out.print(result)  
  
}
```

Put main on  
the stack



\$ main()

Programs Call Stack





# Callstack

---

```
public static void main(String[] args){
```



```
    int a = 6;
```

```
    int b = 8
```

```
    int result = doMath(a, b)
```

```
    System.out.print(result)
```

```
}
```

\$ main()

Programs Call Stack





# Callstack

---

```
public static void main(String[] args){
```

```
    int a = 6;
```



```
    int b = 8
```

```
    int result = doMath(a, b)
```

```
    System.out.print(result)
```

```
}
```

\$ main()

Programs Call Stack





# Callstack

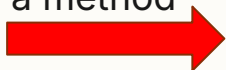
---

```
public static void main(String[] args){
```

```
    int a = 6;
```

```
    int b = 8
```

Need to call  
a method



```
    int result = doMath(a, b)
```

```
    System.out.print(result)
```

```
}
```

\$ main()


Programs Call Stack





# Callstack

---



```
public static int doMath(int a, int b){  
    int mathResult;
```

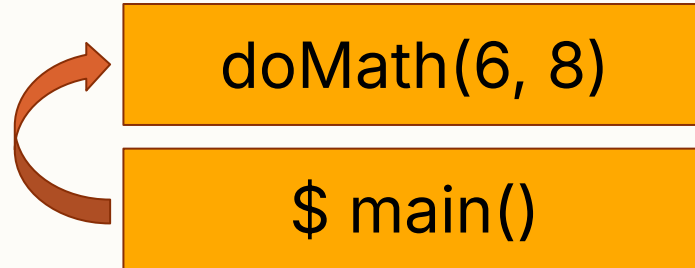
```
    int halfOfA = divide(a, 2)
```

```
    mathResult = mult(halfOfA, b)
```

```
    return mathResult
```

```
}
```

Put doMath()  
on the stack



Programs Call Stack







# Callstack

---

```
public static int doMath(int a, int b){
```



```
    int mathResult;
```

```
    int halfOfA = divide(a, 2)
```

```
    mathResult = mult(halfOfA, b)
```

```
    return mathResult
```

```
}
```

doMath(6, 8)

\$ main()

Programs Call Stack





# Callstack

---

```
public static int doMath(int a, int b){  
    int mathResult;
```

Need to call  
a method



```
    int halfOfA = divide(a, 2)
```

```
    mathResult = mult(halfOfA, b)
```

```
    return mathResult
```

```
}
```

doMath(6, 8)

\$ main()


Programs Call Stack





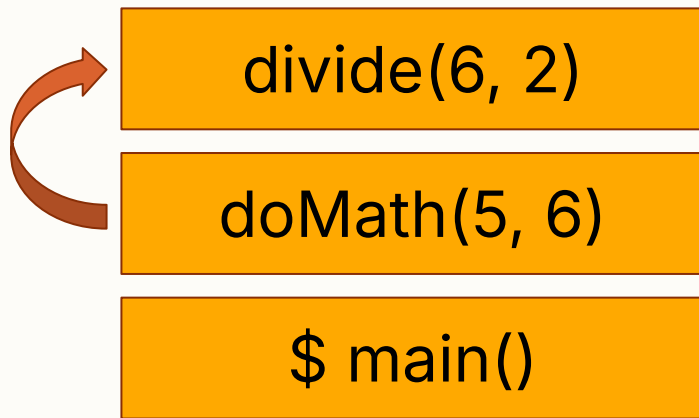
# Callstack

---



```
public static int divide(int n, int d){  
    int result = n / d;  
  
    return result;  
}
```

Put divide() on  
the stack



Programs Call Stack





# Callstack

---

```
public static int divide(int n, int d){  
    int result = n / d;  
  
    return result;  
}
```



divide(6, 2)

doMath(5, 6)

\$ main()

Programs Call Stack





# Callstack

---

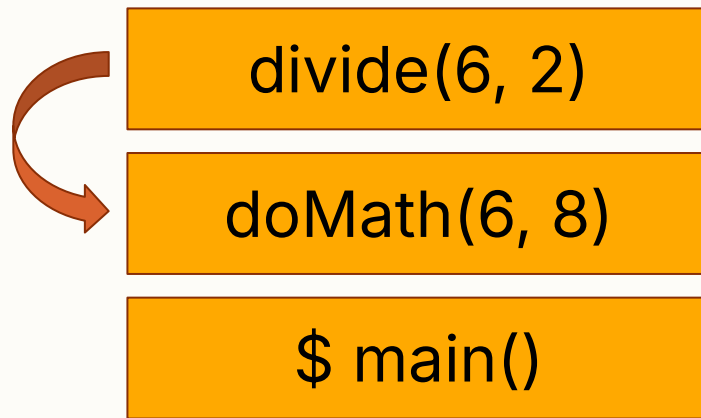
```
public static int divide(int n, int d){  
    int result = n / d;
```

Return ⇒  
stack pop



```
    return result;  
}
```

Return right back to where we  
left off in doMath



Programs Call Stack





# Callstack

---

```
public static int doMath(int a, int b){
```

```
    int mathResult;
```

```
    int halfOfA = divide(a, 2) // 3
```

```
    mathResult = mult(halfOfA, b)
```

```
    return mathResult
```

```
}
```

We have  
returned  
from divide



doMath(6, 8)

\$ main()

Programs Call Stack





# Callstack

---

```
public static int doMath(int a, int b){  
    int mathResult;
```

```
    int halfOfA = divide(a, 2); // 3
```

Call another  
method



```
    mathResult = mult(halfOfA, b); //mult(3, 8)
```

```
    return mathResult
```

```
}
```

doMath(6, 8)

\$ main()

Programs Call Stack





# Callstack

---



```
public static int mult(int num, int times){  
    int multResult = num * times  
  
    return multResult  
  
}
```

Put mult() on  
the stack



mult(3, 8)

doMath(5, 6)

\$ main()

Programs Call Stack







# Callstack

---

```
public static int mult(int num, int times){  
    int multResult = num * times  
  
    return multResult  
  
}
```



mult(3, 8)

doMath(5, 6)

\$ main()

Programs Call Stack

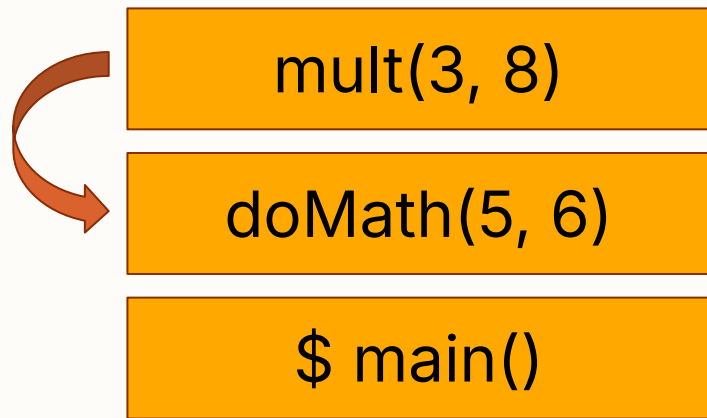




# Callstack

---

```
public static int mult(int num, int times){  
    int multResult = num * times  
  
    → return multResult  
}
```



Programs Call Stack





# Callstack

---

```
public static int doMath(int a, int b){  
    int mathResult;
```

```
    int halfOfA = divide(a, 2); // 3
```

Returned  
from mult()



```
    mathResult = mult(halfOfA, b); // 24
```

```
    return mathResult;
```

```
}
```

doMath(6, 8)

\$ main()

Programs Call Stack





# Callstack

---

```
public static int doMath(int a, int b){  
    int mathResult;  
  
    int halfOfA = divide(a, 2); // 3  
  
    mathResult = mult(halfOfA, b); // 24  
  
    return mathResult;  
}
```



doMath(6, 8)

\$ main()

Programs Call Stack





# Callstack


---

```
public static void main(String[] args){
```

```
    int a = 6;
```

```
    int b = 8;
```

Returned from  
doMath()

 `int result = doMath(a, b); // 24`

```
    System.out.print(result);
```

```
}
```

\$ main()

Programs Call Stack





# Callstack

---

```
public static void main(String[] args){  
    int a = 6;  
    int b = 8;  
  
    int result = doMath(a, b); // 24  
  
    System.out.print(result); // 24  
  
}
```



\$ main()

Programs Call Stack





# Callstack

---

```
public static void main(String[] args){
```

```
    int a = 6;
```

```
    int b = 8;
```

```
    int result = doMath(a, b); // 24
```

```
    System.out.print(result); // 24
```

```
    return; // omitted
```

```
}
```



\$ main()

Programs Call Stack





# Callstack

---

```
public static void main(String[] args){
```

```
    int a = 6;
```

```
    int b = 8;
```

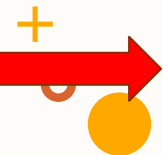
```
    int result = doMath(a, b); // 24
```

```
    System.out.print(result); // 24
```

```
    return; // omitted
```

```
}
```

Program finished  
when callstack is  
empty



Programs Call Stack





# Callstack

---

- You can see how this would scale for larger programs
  - Large call stacks
  - Even for methods you don't write





# Callstack

---

- When we called a method:
  - All of its parameters got “filled in” as variables we can use locally

- Let's keep this idea in mind going forward

mult(3, 8)

doMath(5, 6)

\$ main()





# Callstack

---

- Consider the following method
- What would our callstack look like?

```
public static void doThing(){  
    // do anything  
  
    doThing()  
}
```

\$ main()

Programs Call Stack






# Callstack

---

- Consider the following method
- What would our callstack look like?



```
public static void doThing(){  
    // do anything  
  
    doThing()  
}
```

doThing()

\$ main()

Programs Call Stack





# Callstack

---

- Consider the following method
- What would our callstack look like?

```
public static void doThing(){  
    // do anything
```



doThing()

}

doThing()

\$ main()

Programs Call Stack





# Callstack

---

- Consider the following method
- What would our callstack look like?



```
public static void doThing(){  
    // do anything
```

```
    doThing()  
}
```

doThing()

doThing()

\$ main()

Programs Call Stack





# Callstack

---

- Consider the following method
- What would our callstack look like?

```
public static void doThing(){  
    // do anything
```



```
doThing()  
}
```

doThing()

doThing()

\$ main()

Programs Call Stack





# Callstack

---

- Consider the following method
- What would our call



```
public static void doThing(){  
    // do anything  
  
    doThing()  
}
```

doThing()

doThing()

doThing()

\$ main()

Programs Call Stack







# Callstack

- Consider the following
- What would our call



```
public static void doThing(){  
    // do anything  
  
    doThing()  
}
```

doThing()

doThing()

doThing()

doThing()

\$ main()

Programs Call Stack





# Callstack

- Consider the following
- What would our call



```
public static void doThing(){  
    // do anything  
  
    doThing()  
}
```

doThing()

doThing()

doThing()

doThing()

doThing()

\$ main()


Programs Call Stack





## Callstack

- Consider the following
- What would our call



```
public static void doThing(){  
    // do anything  
  
    doThing()  
}
```

doThing()

doThing()

doThing()

doThing()

doThing()

doThing()

\$ main()

Programs Call Stack





# Callstack

---

- StackOverflowError
  - Let's see this
- Callstack has a "height" limit
- Cannot exceed it
- We need a way to stop it from running after a point





# Callstack

---

- Let's look at this method instead

➔ `public static void doThing(int timesRan){  
 if (timesRan >= 3) {  
 return  
 }`

`doThing(timesRan + 1)`

`}`

doThing(0)

\$ main()

Programs Call Stack





# Callstack

---

- Let's look at this method instead

```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
}
```

 doThing(timesRan + 1)

 return  
 }

doThing(0)

\$ main()

Programs Call Stack



# Callstack

---

- Let's look at this method instead

➔ public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }

doThing(timesRan + 1)

+  
○ }  
●  
return

doThing(1)

doThing(0)

\$ main()

Programs Call Stack



# Callstack

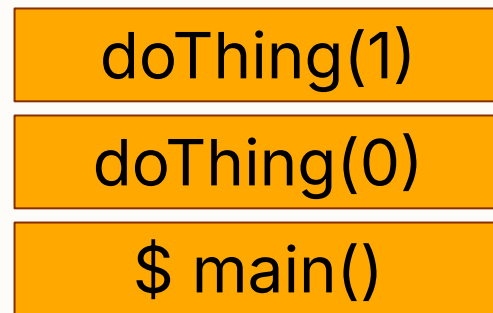
---

- Let's look at this method instead

```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
    doThing(timesRan + 1)  
    return  
}
```

 doThing(timesRan + 1)

   }  
return



Programs Call Stack



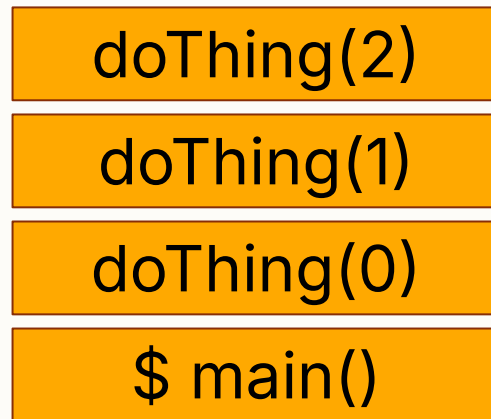


# Callstack

---

- Let's look at this method instead

→ public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
  
    doThing(timesRan + 1)  
  
    return  
}



Programs Call Stack



# Callstack

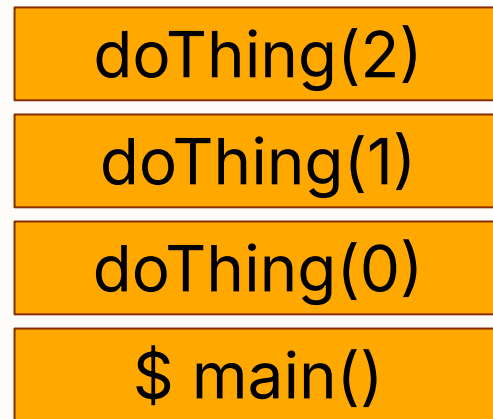
---

- Let's look at this method instead

```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
    doThing(timesRan + 1)  
    return  
}
```

 doThing(timesRan + 1)

+  
○ }  

Programs Call Stack



# Callstack

---

- Let's look at this method instead

→ public static void doThing(int timesRan) {  
    if (timesRan >= 3) {  
        return  
    }  
  
    doThing(timesRan + 1)  
  
    return  
}

doThing(3)

doThing(2)

doThing(1)

doThing(0)

\$ main()

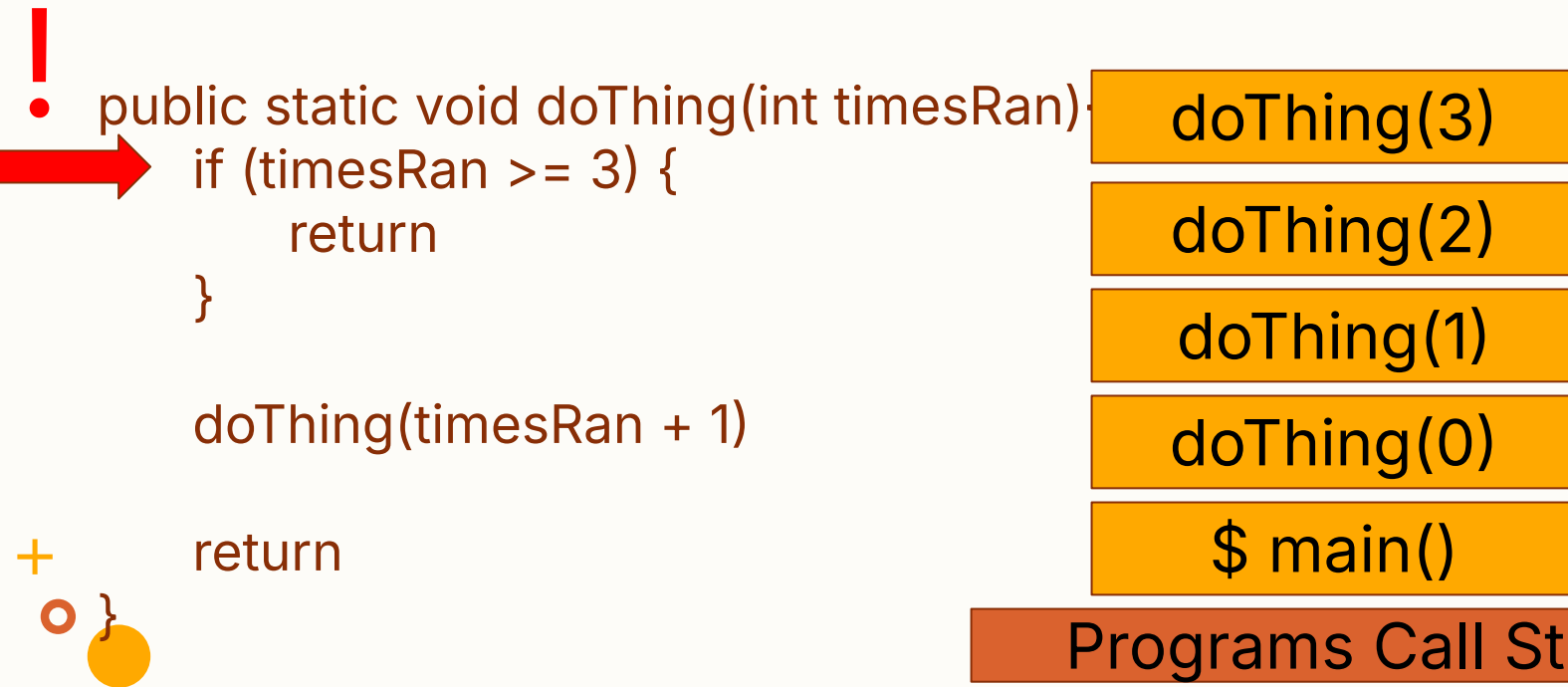
Programs Call Stack



# Callstack

---

- Let's look at this method instead





# Callstack

---

- Let's look at this method instead

```
public static void doThing(int timesRan) {  
    if (timesRan >= 3) {  
        return  
    }  
    doThing(timesRan + 1)  
}
```



doThing(3)

doThing(2)

doThing(1)

doThing(0)

\$ main()

Programs Call Stack





# Callstack

---

- Let's look at this method instead

```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
    doThing(timesRan + 1)  
    return  
}
```



doThing(timesRan + 1)



return

doThing(2)

doThing(1)

doThing(0)

\$ main()

Programs Call Stack



# Callstack

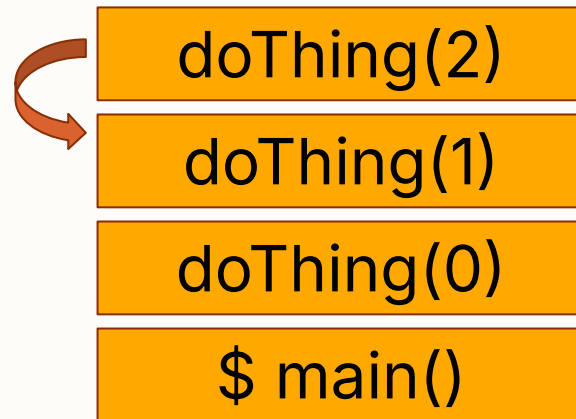
---

- Let's look at this method instead

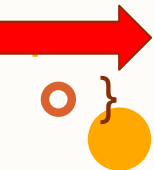
```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
    doThing(timesRan + 1)  
}
```

doThing(timesRan + 1)

return



Programs Call Stack





# Callstack

---

- Let's look at this method instead

```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
    doThing(timesRan + 1)  
    return  
}
```



doThing(timesRan + 1)



return

doThing(1)

doThing(0)

\$ main()

Programs Call Stack



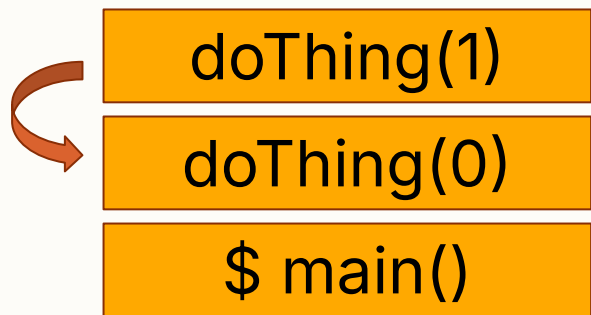
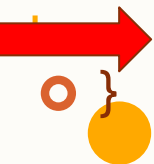


# Callstack

---

- Let's look at this method instead

```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
  
    doThing(timesRan + 1)  
  
    return  
}
```



Programs Call Stack



# Callstack

---

- Let's look at this method instead

```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
}
```

 doThing(timesRan + 1)

 return  
 }

doThing(0)

\$ main()

Programs Call Stack



# Callstack

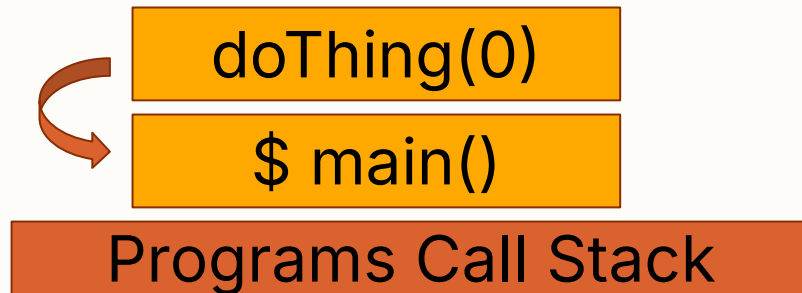
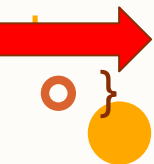
---

- Let's look at this method instead

```
public static void doThing(int timesRan){  
    if (timesRan >= 3) {  
        return  
    }  
}
```

doThing(timesRan + 1)

return





# Callstack

---

- We were able to write a method that
  - Calls itself within its body
  - Any number of times
  - But eventually terminated
- Made its way back down the callstack





# Recursion

---

- This idea is called recursion
  - Anytime a function is calling itself
- Recursion functions according to the exact same rules any other method does
- Not "special" in that regard





# Recursion

---

- Recursive functions *usually* can be broken down into two primary components
- Base Case
- Simplifying the problem





# Recursion

---

- Base Case:
  - Solve the simplest version of the problem that you can
  - Usually takes form of *if param == small case*
  - If this isn't the case, simplify





# Recursion

---

- Simplifying the problem
  - If your input is not in its smallest ideal form
  - Try to simplify your problem, then call the method again
  - Recombine elements to build solution







# Callstack

---

- We can use this idea to solve real problems
- Those two components can be unintuitive until you see them
- Let's try to solve that `countOccurrences()` problem again





# Callstack

---

- Base case
  - Simplest form of problem
  - Empty String has 0 occurrences
- Look at first character
  - If first character is target, add one
  - Else continue





# Callstack

---

- Look at first character
  - If first character is target, add one
  - Else continue

H	E	L	L	O
---	---	---	---	---





H	E	L	L	O
---	---	---	---	---



$0 + \text{countOccurrences}(\text{target}, \text{"ello"})$

Target = L



H	E	L	L	O
---	---	---	---	---



0 +

E	L	L	O
---	---	---	---



0 +

1 + countOccurrences(target, "llo")

Target = L



H	E	L	L	O
---	---	---	---	---



0 +

E	L	L	O
---	---	---	---



0 +

0 +

L	L	O
---	---	---

Target = L



0 +

0 +

1 + countOccurrences(target, "lo")



0 +

0 +

1 +

L	O
---	---



1 + countOccurrences(target, "o")

Target = L



0 +

0 +

1 +



1 + countOccurrences(target, "o")

0 +

0 +

1 +

1 +



0 + countOccurrences(target, "")

Target = L





0 +

0 +

1 +



$1 + \text{countOccurrences}(\text{target}, "o")$

0 +

0 +

1 +

1 +



$0 + \text{countOccurrences}(\text{target}, "")$

Target = L

0 +

0 +

1 +

1 +

0 +

0



= 2





# Callstack

---

- Let's do another simple recursion problem
- Discrete Math
  - Fibonacci Sequence
  - Compute the Nth fibonacci number





# Callstack

---

- Let's try countOccurrences again
  - Without loops
  - Common patterns





# Callstack

---

- Let's try countOccurrences again
  - Without loops
  - Common patterns
- Was difficult to accomplish without having another piece of state
  - Something that persists across methods call





# Callstack

---

- Common Recursion pattern:
- Helper methods:
- User friendly `countOccurrences()`
  - Less friendly, hidden `countOccurrencesHelper()`





## More recursion

---

- All problems that could be solved with loops:
  - Can be solved via recursion
- Some problems fit themselves nicely to recursion
  - Fib(n)
  - Factorial(n), etc.





## More recursion

---

- We're gonna do 7ish recursion problems
  - ~50% from CodingBat
- Common interview questions
- Start easier ones
- Get harder





## More recursion

---

- EndX
  - Input  $\Rightarrow$  string
  - Return  $\Rightarrow$  string with all 'x's moved to the end
- "Hexllxo"  $\Rightarrow$  "Helloxx"
- "xx\_java\_dev\_\_xx"  $\Rightarrow$  "\_java\_dev\_xxxx"







## More recursion

---

- Print Triangle
- Input  $\Rightarrow$  Height
- Return  $\Rightarrow$  None
  - Should print a triangle of size *height* to the screen





## More recursion

---

- Is Palindrome
- Input  $\Rightarrow$  String to check
- Return  $\Rightarrow$  T/F if string is a palindrome
  
- "hello"  $\Rightarrow$  false
- "racecar"  $\Rightarrow$  true





## More recursion

---

- Count 11's in an array
- Input  $\Rightarrow$  input array
- Return  $\Rightarrow$  how many 11's were present in that array
  
- $[4, 5, 6, 11, 5] \Rightarrow 1$
- $[11, 45, 12, 10, 11] \Rightarrow 2$





## More recursion

---

- Insert \* into between duplicate letters
  - Input  $\Rightarrow$  String to insert
  - Return  $\Rightarrow$  String with \* between any duplicate letter
- 
- "hello"  $\Rightarrow$  "hel\*lo"
  - "aabb"  $\Rightarrow$  "a\*ab\*b"
  - "aaa"  $\Rightarrow$  "a\*a\*a"





## More recursion

---

- Insert a value into a linked list
  - Input  $\Rightarrow$  value and index
  - Return  $\Rightarrow$  None, modify list
- 
- We'll use this weeks LP code to start with





## More recursion

---

- Find index of value
- Input  $\Rightarrow$  sorted array, target value
- Return  $\Rightarrow$  index of target value
  
- Special algorithm
- Binary search
- Very fast  $\Rightarrow O(n \log n)$  time

