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# WEEK FOURTEEN

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# ALGORITHMS

- Approach to solving a computational problem
- Algorithms must be:
  - Finite: must terminate eventually
  - Correct: must solve the problem every time
  - Deterministic: made of concrete, computer-executable steps, and produce the same output every time
- Good algorithms are:
  - Bug-free
  - Secure
  - Fast
  - Don't hog memory

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# SEARCH ALGORITHMS

- Linear search
  - Step through items one-by-one until the desired item is located
- Binary search
  - Requires a sorted list
  - Split the list in half, check if the value is greater than or less than the central pivot
    - If greater, move to the right side of the list and repeat
    - If less than, move to the left side of the list and repeat

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# SORTING ALGORITHMS

- Selection sort
  - Remove the min/max item from an unsorted list and add (swap) it to the beginning/end of a new sorted list
- Insertion sort
  - Take each element, in position order, and move it into the appropriate sorted location in a 'new' sorted list
- Bubble sort
  - Sort in multiple passes
  - In each pass, successively swap neighboring elements if they are in the wrong natural order
  - Continue passes until all elements are fully ordered

# Selection

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7 3 2 6 9 5 2  
[2] 3 2 6 9 5 7  
[2 2] 3 6 9 5 7  
[2 2 3] 6 9 5 7  
[2 2 3 5] 9 6 7  
[2 2 3 5 6] 9 7  
[2 2 3 5 6 7] 9

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7 3 2 6 9 5 2  
7 3 2 6 2 5 9  
5 3 2 6 2 7 9  
5 3 2 2 6 7 9  
2 3 2 5 6 7 9  
2 2 3 5 6 7 9  
2 2 3 5 6 7 9

# Insertion

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7 3 2 6 9 5 2

7 3 2 6 9 5 2

3 7 2 6 9 5 2

2 3 7 6 9 5 2

2 3 6 7 9 5 2

2 3 6 7 9 5 2

2 3 5 6 7 9 2

---

2 2 3 5 6 7 9

7 3 2 6 9 5 2

7 3 2 6 9 5 2

7 3 2 6 9 2 5

7 3 2 6 2 5 9

7 3 2 2 5 6 9

7 3 2 2 5 6 9

7 2 2 3 5 6 9

2 2 3 5 6 7 9

# Bubble Sort

★ 7 3 2 6 9 5 2    2 3 6 5 7 2 9    2 3 2 5 6 7 9    2 2 3 5 6 7 9  
3 7 2 6 9 5 2    2 3 6 5 2 7 9    2 3 2 5 6 7 9    2 2 3 5 6 7 9  
3 2 7 6 9 5 2    ★ 2 3 6 5 2 7 9    2 3 2 5 6 7 9    2 2 3 5 6 7 9  
3 2 6 7 9 5 2    2 3 6 5 2 7 9    ★ 2 3 2 5 6 7 9    2 2 3 5 6 7 9  
3 2 6 7 9 5 2    2 3 6 5 2 7 9    2 3 2 5 6 7 9    2 2 3 5 6 7 9  
3 2 6 7 5 9 2    2 3 5 6 2 7 9    2 2 3 5 6 7 9    2 2 3 5 6 7 9  
★ 3 2 6 7 5 2 9    2 3 5 2 6 7 9    2 2 3 5 6 7 9    2 2 3 5 6 7 9  
2 3 6 7 5 2 9    2 3 5 2 6 7 9    2 2 3 5 6 7 9    2 2 3 5 6 7 9  
2 3 6 7 5 2 9    ★ 2 3 5 2 6 7 9    2 2 3 5 6 7 9    2 2 3 5 6 7 9  
2 3 6 7 5 2 9    2 3 5 2 6 7 9    ★ 2 2 3 5 6 7 9    2 2 3 5 6 7 9  
2 3 6 7 5 2 9    2 3 5 2 6 7 9    2 2 3 5 6 7 9    2 2 3 5 6 7 9

# Selection

2 8 3 5 9 6 4  
2 8 3 5 9 6 4  
2 3 8 5 9 6 4  
2 3 4 5 9 6 8  
2 3 4 5 9 6 8  
2 3 4 5 6 9 8  
2 3 4 5 6 8 9

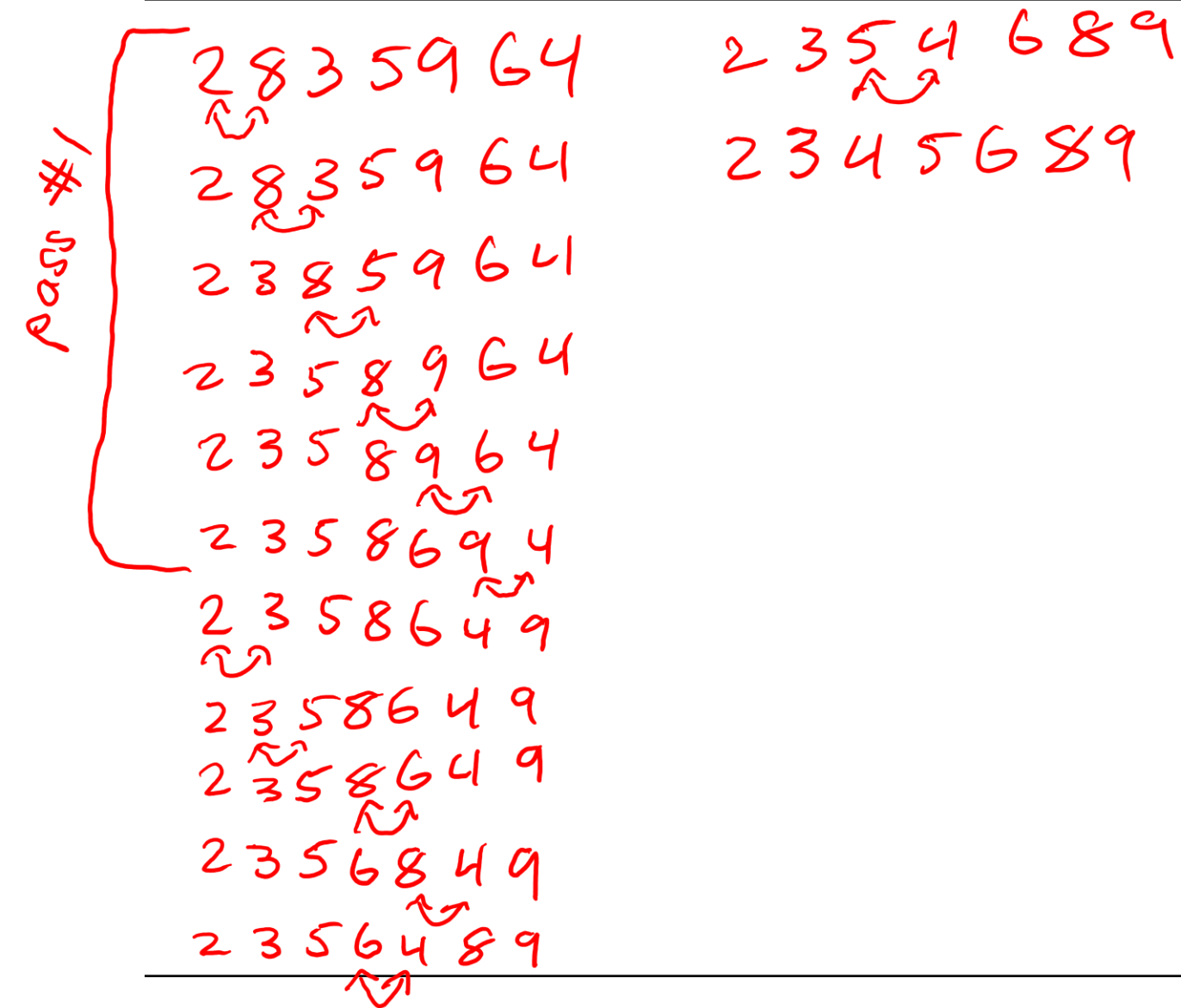
# Insertion

2 8 3 5 9 6 4  
2 8 3 5 9 6 4  
2 8 3 5 9 6 4  
2 3 8 5 9 6 4  
2 3 8 5 9 6 4  
2 3 5 8 9 6 4  
2 3 5 8 9 6 4  
2 3 5 6 8 9 4  
2 3 4 5 6 8 9



# Bubble

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# Merge

2835964

283

59 64

2      83  
↻

59 64  
↗ ↘

2 38

59 46

2 3 8

4 5 6 9

2 3 4

6 8 9

Quick

2 8 3 5 9 6 4

2 3 4

8 9 6

2 / 4

86

6  
↓  
68

234

689

234 5 689

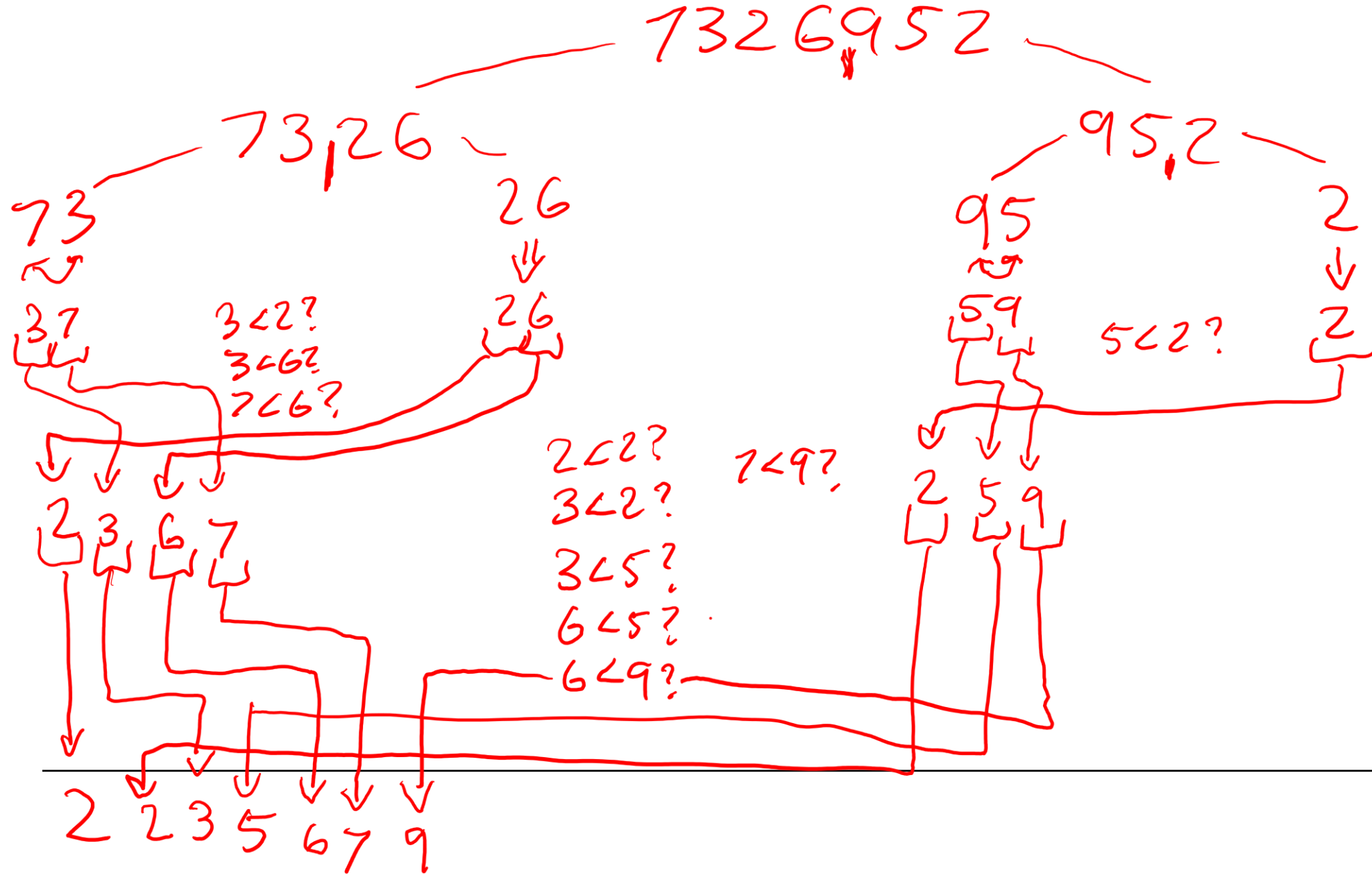
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# SORTING ALGORITHMS CONTINUED

- Merge sort
  - Usually done recursively
  - Divide array into two halves
  - As base case, sort the two remaining values
  - Upon exiting the recursive call, poll items from each half in order
- Quick sort
  - Pick a pivot
  - Reposition items so all items less than pivot will appear to its left and all greater items will appear on the right
  - Continue on smaller and smaller portions until the list is sorted

# Merge sort

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# Quick Sort (central pivot)

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7 3 2 6 9 5 2

first value > pivot      first value < pivot

7 3 2 9 5 2 6

↑      ↑

swap

2 3 2 9 5 7 6

next value > pivot      next value < pivot

↑      ↑

swap

2 3 2 5 9 7 6

↑      ↑

insert pivot

2 3 2 5 6 9 7

---

# Quick Sort Continued

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23 25 6 97

2 3 25

2 25 3

↑

insert pivot

2 2 3 5

22

↓

22

5

↓

5

2235

2235

6 79

9 7

7 9

↑

insert pivot

79

# Quicksort (first pivot)

3 2 6 9 5 2

7

3 2 6 9 5 2

> pivot    swap    < pivot

3 2 6 2 5 9

insert pivot

3 2 6 2 5 7 9 → 9

2 2 3 5 6

2 2 3 5 6 7 9

3 2 6 2 5

swap

3 2 2 6 5

2 2 3 6 5

2 2

5 6

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# BIG-O

- How long an algorithm takes to run in relation to the input
- Function can be simplified by:
  - Removing any constant coefficients
  - Removing all but the highest order term
- Example:
  - $5^n + 7n^2 + 3$  becomes...
  - $5^n$

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# COMMON RATES OF GROWTH (BY MAGNITUDE)

- $O(1)$  – constant
- $O(\log n)$  – logarithmic
- $O(n)$  – linear
- $O(n * \log n)$  – log-linear
- $O(n^c)$  – polynomial
  - $O(n^2)$  – quadratic
  - $O(n^3)$  – cubic
  - Etc.
- $O(c^n)$  – exponential
  - $O(2^n)$
  - $O(3^n)$
  - Etc.
- $O(n!)$  – factorial

<https://www.desmos.com/calculator/jpskgp3y7a>

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# SORTING ALGORITHMS AND THEIR COMPLEXITY

- Selection
  - Insertion
  - Bubble
  - Merge
  - Quick
- $O(n^2)$
  - $O(n^2)$
  - $O(n^2)$
  - $O(n \log(n))$
  - $O(n^2)$