

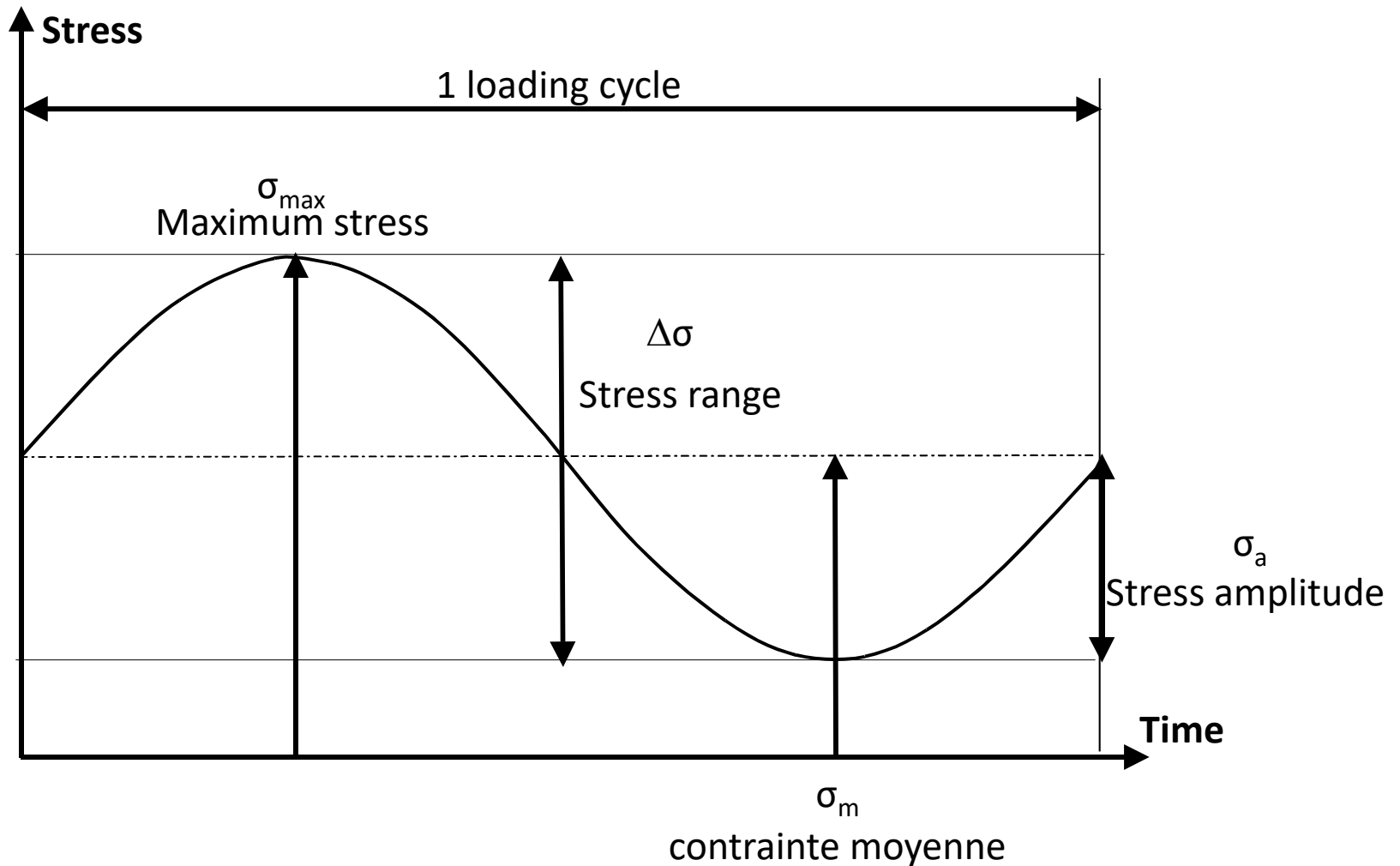


# FATIGUE OF MATERIALS & STRUCTURES

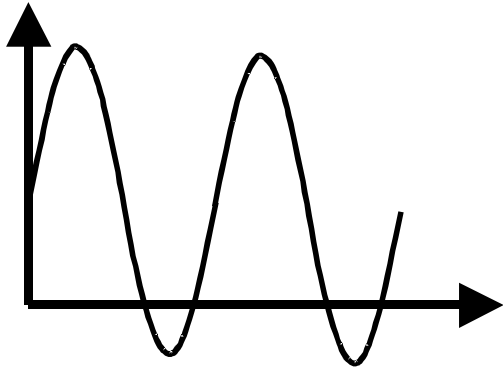


# HIGH CYCLE FATIGUE

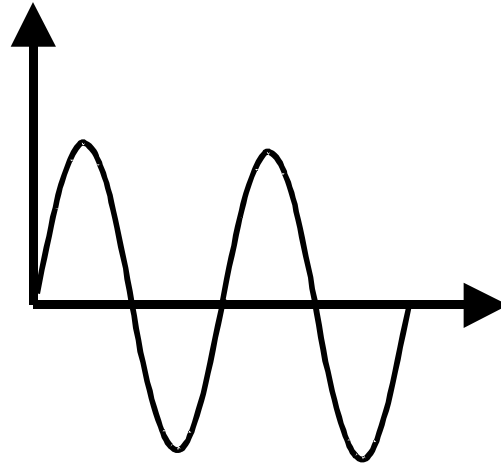
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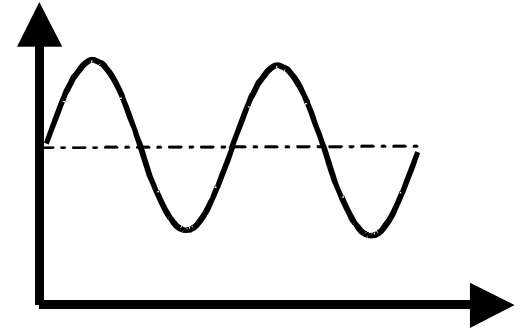
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Alternate Stress



Symetric  
alternate  
stress ( $R=-1$ )



Tensile  
alternate  
stress ( $R>0$ )

# Testing Machines



Electro-mechanical : low  
cycle fatigue ( $f < 1$  Hz)



Servo-hydraulic : high  
cycle fatigue,  
propagation  
( $f < 50$  Hz)

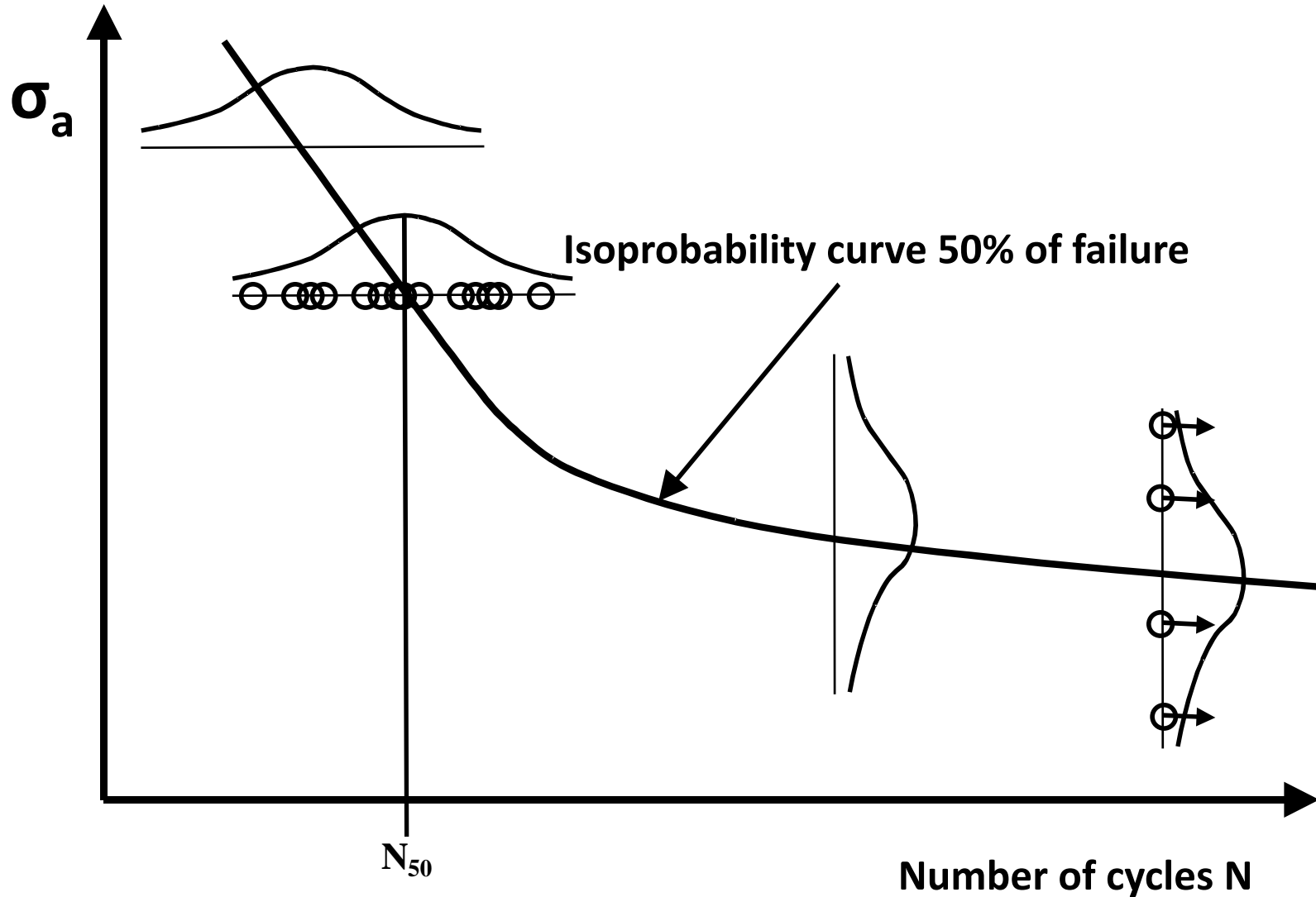


Resonant :  
high cycle fatigue,  
propagation  
( $100 \text{ Hz} < f < 200 \text{ Hz}$ )

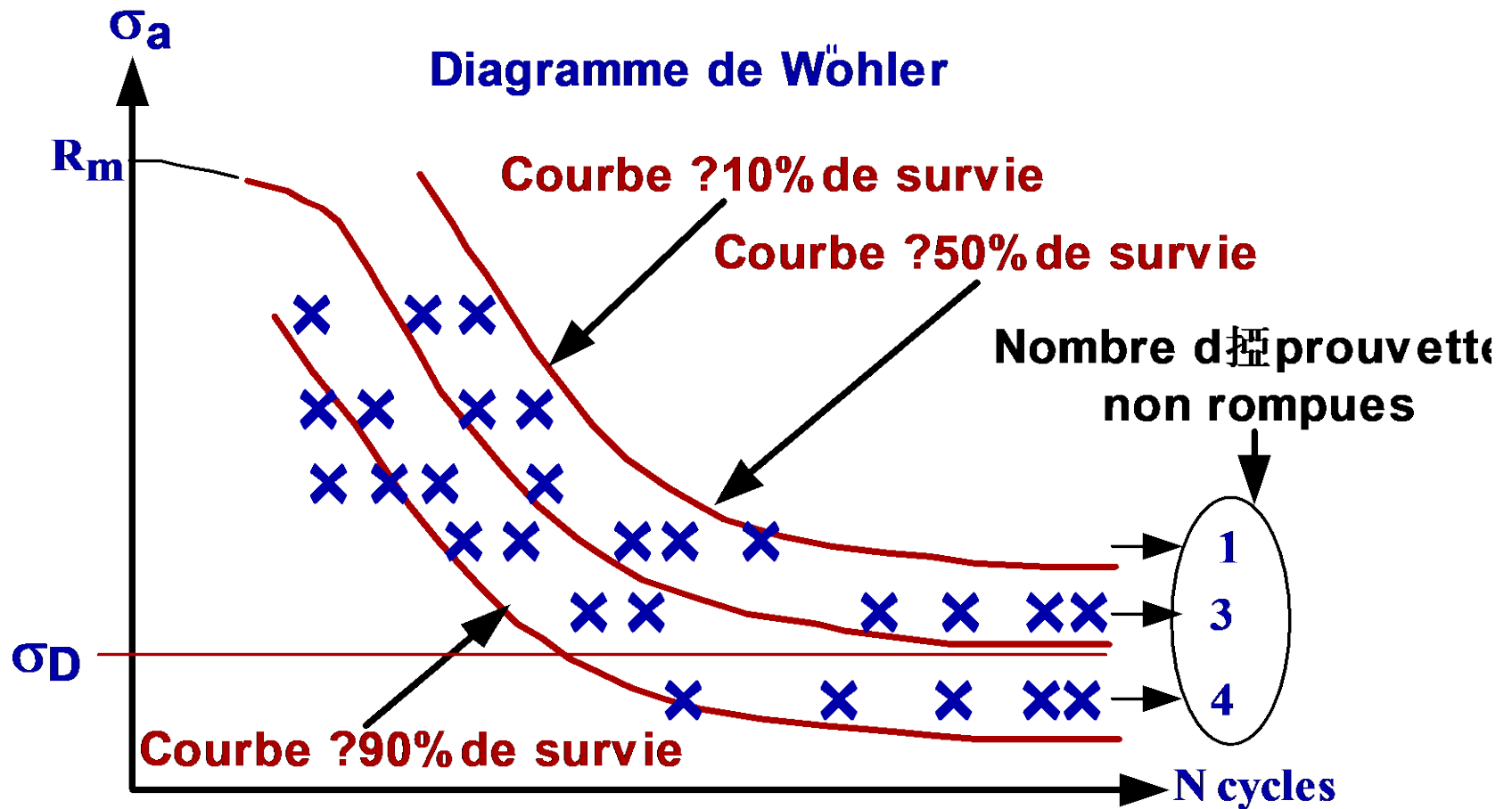
# Methodology

- Fixed number of samples (geometry, surface);
- Stress amplitude levels fixed prior to testing  
⇒ number of test pieces tested per stress level;
- For a given stress level, the distribution of lifetimes (number of cycles to failure) is determined.

# Isoprobability curves

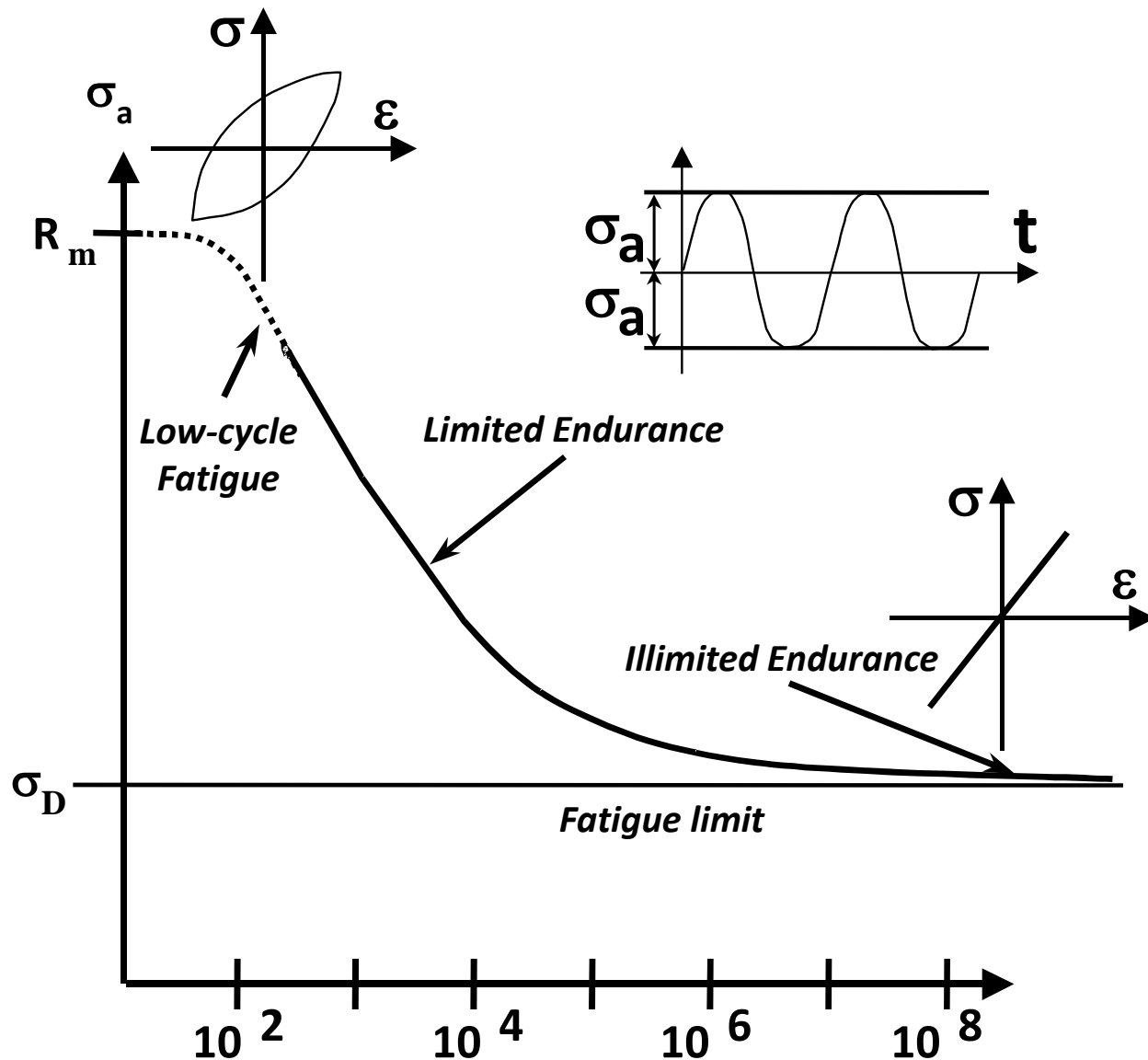


# Wöhler Diagram

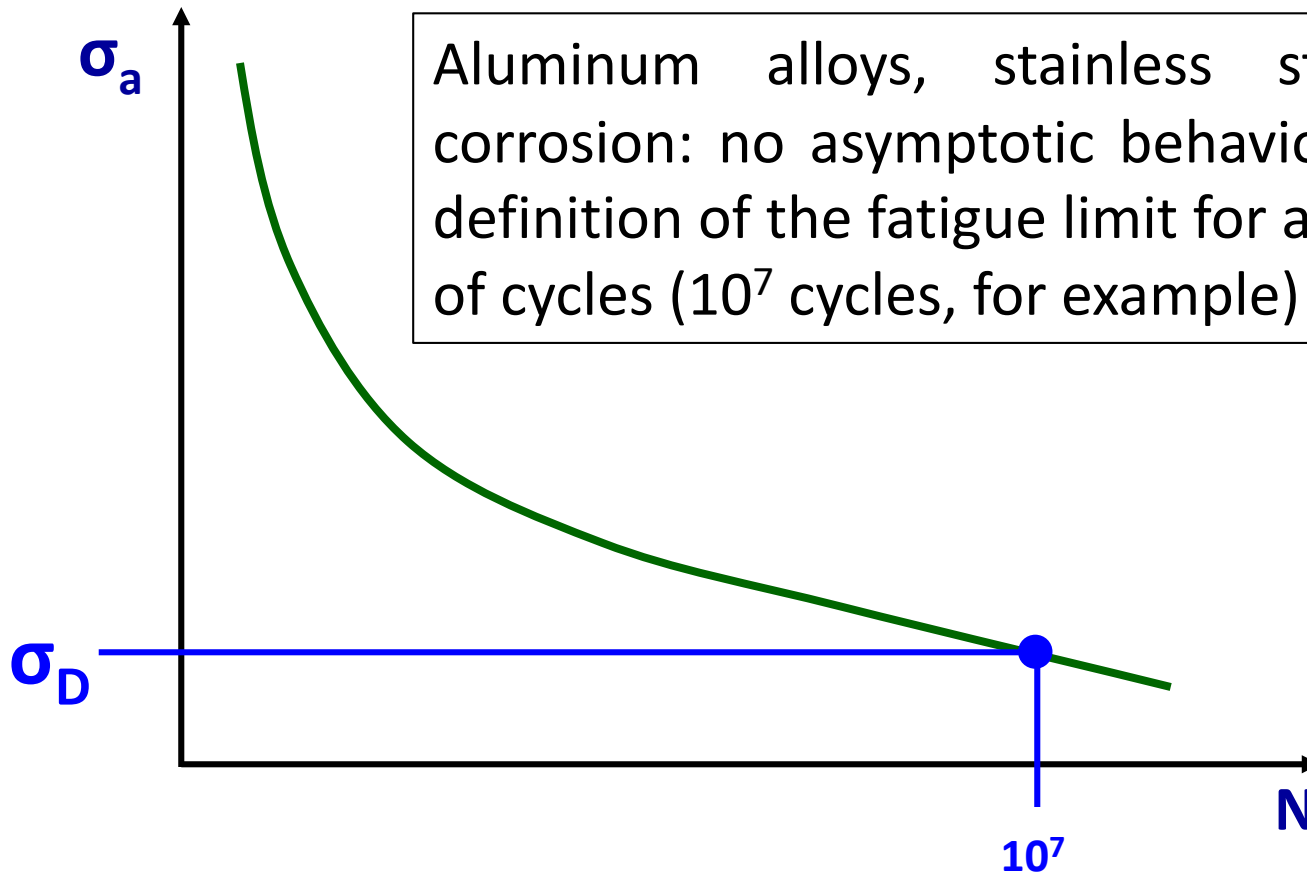




# Endurance diagram



# Arbitrary fatigue limit



# Limited Endurance

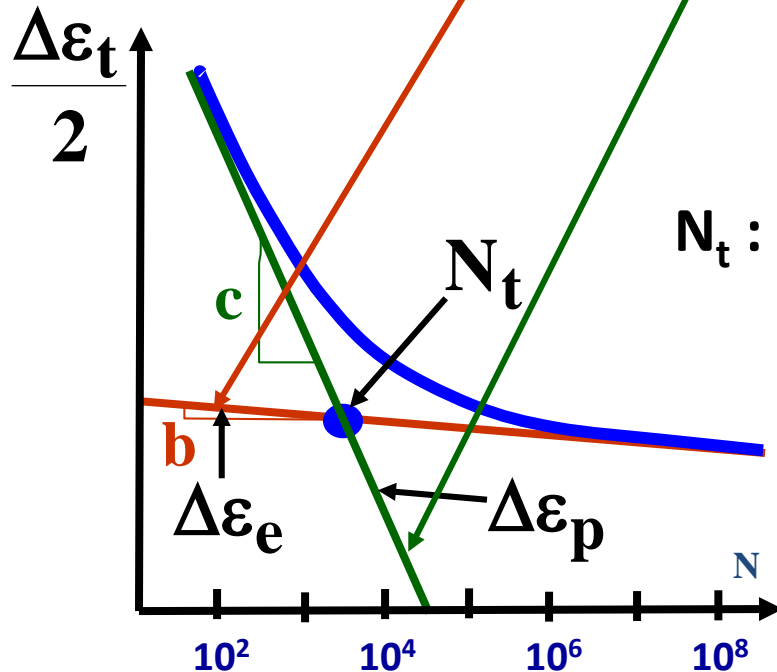
- About  $10^5$  to  $10^7$  cycles
- Empirical relations:
  - Weibull :  $N \times (\sigma - \sigma_D) = \text{Cste}$
  - Basquin :  $N_f \times \sigma^a = \text{Cste}$
  - Bastenaire :  $N_f + B = \frac{A \times e^{-C(\sigma - \sigma_D)}}{\sigma - \sigma_D}$

# $\varepsilon$ -N curve

$$\frac{\Delta \varepsilon_t}{2} = \frac{\Delta \varepsilon_e}{2} + \frac{\Delta \varepsilon_p}{2} = \frac{\sigma'_f}{E} \times N_f^b + \varepsilon'_f \times N_f^c$$

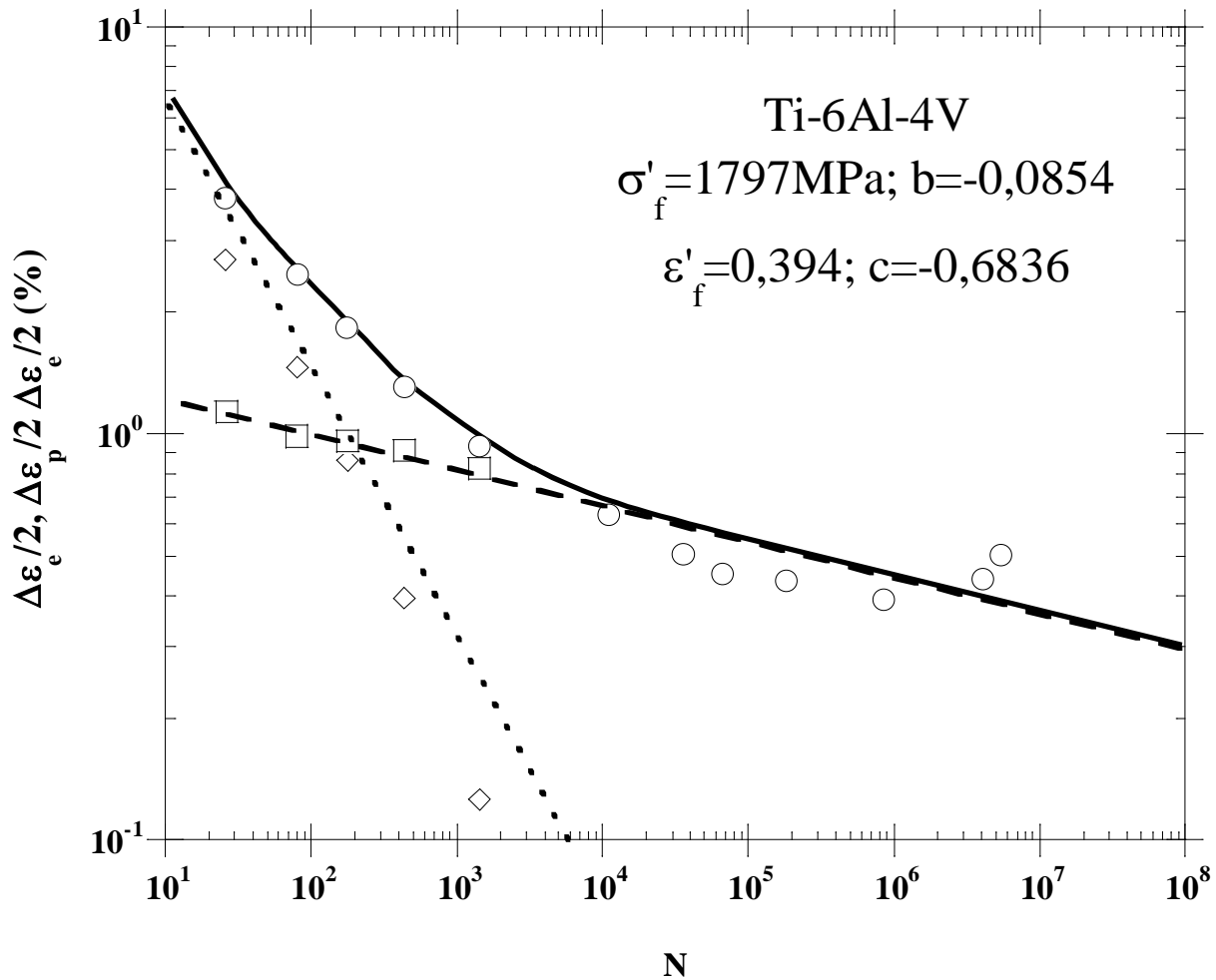
Basquin

Manson-Coffin

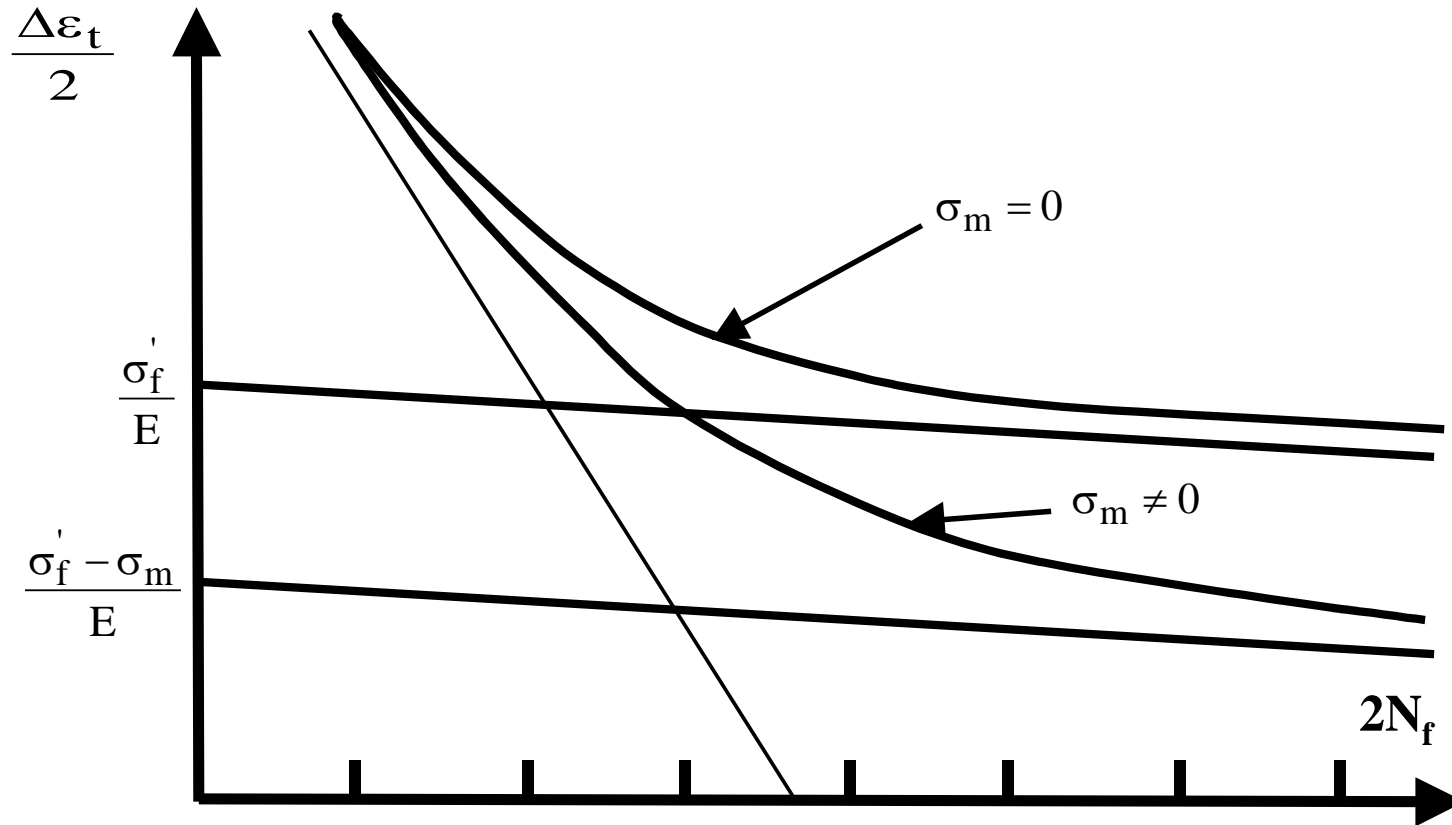


$N_t$  : « Elastic-Plastic » transition

# $\varepsilon$ -N curve

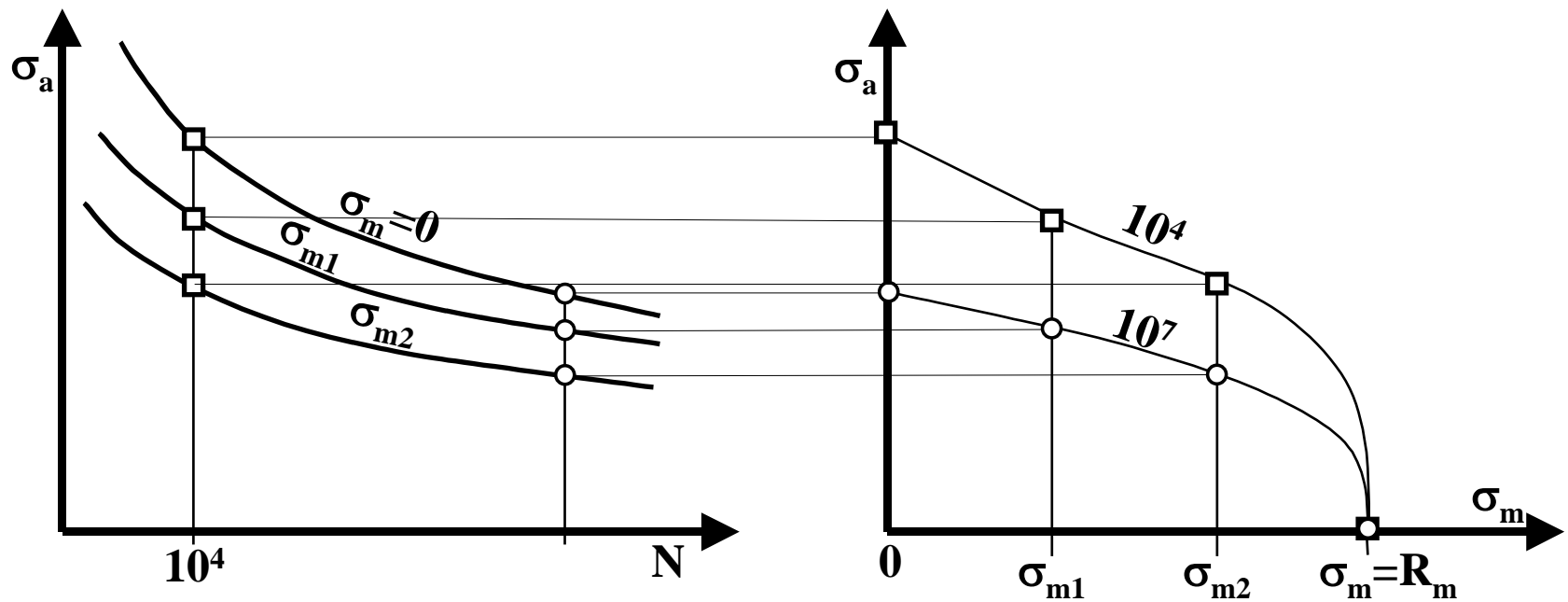


# Influence of Mean Stress



**Smith-Watson-Topper:** 
$$P_{SWT} = \sqrt{\left( \sigma_{\max} \times \frac{\Delta \varepsilon_t}{2} \times E \right)} = \sqrt{\left( (\sigma_a + \sigma_m) \times \frac{\Delta \varepsilon_t}{2} \times E \right)}$$

# Influence of Mean Stress

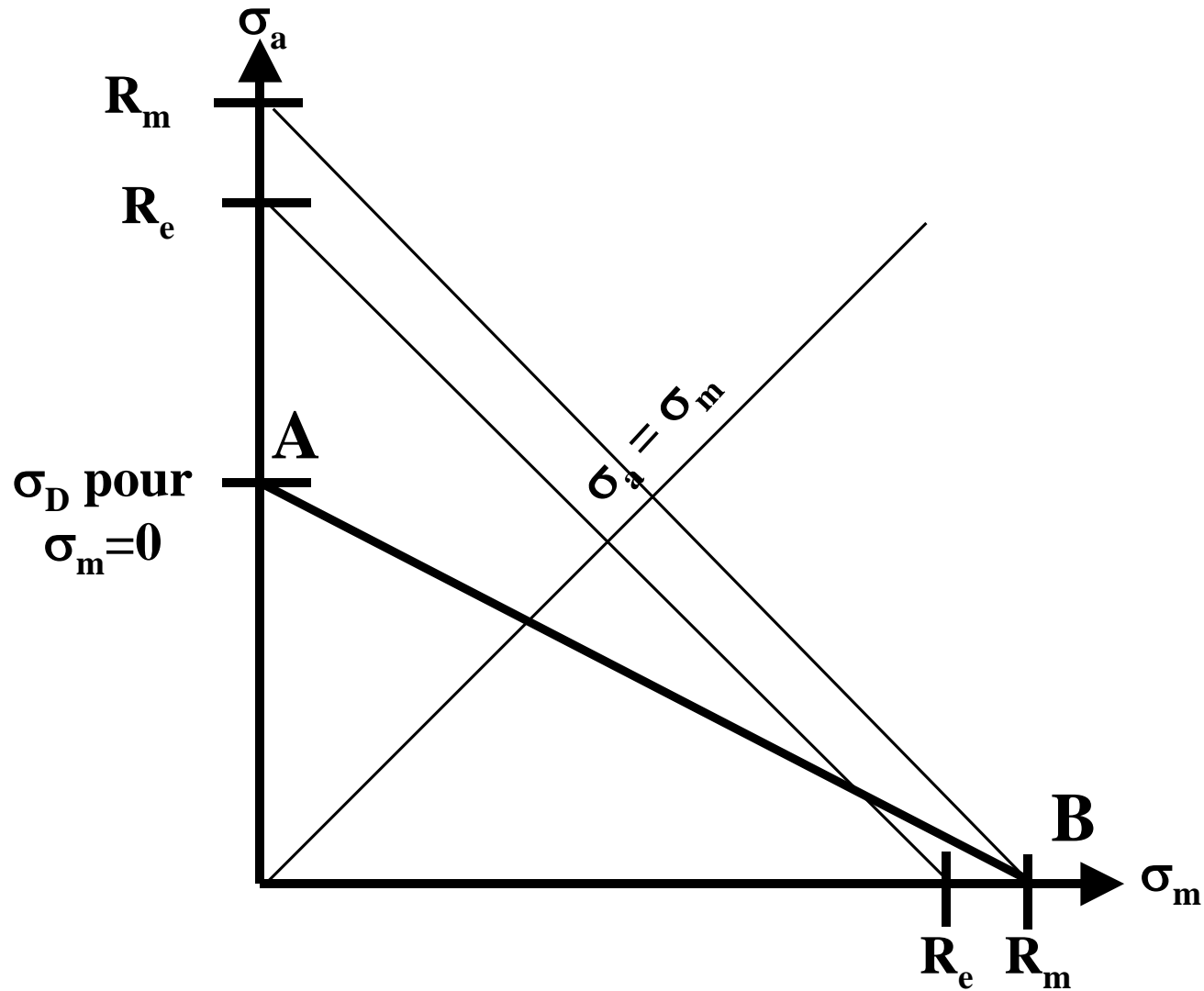


# Influence of Mean Stress

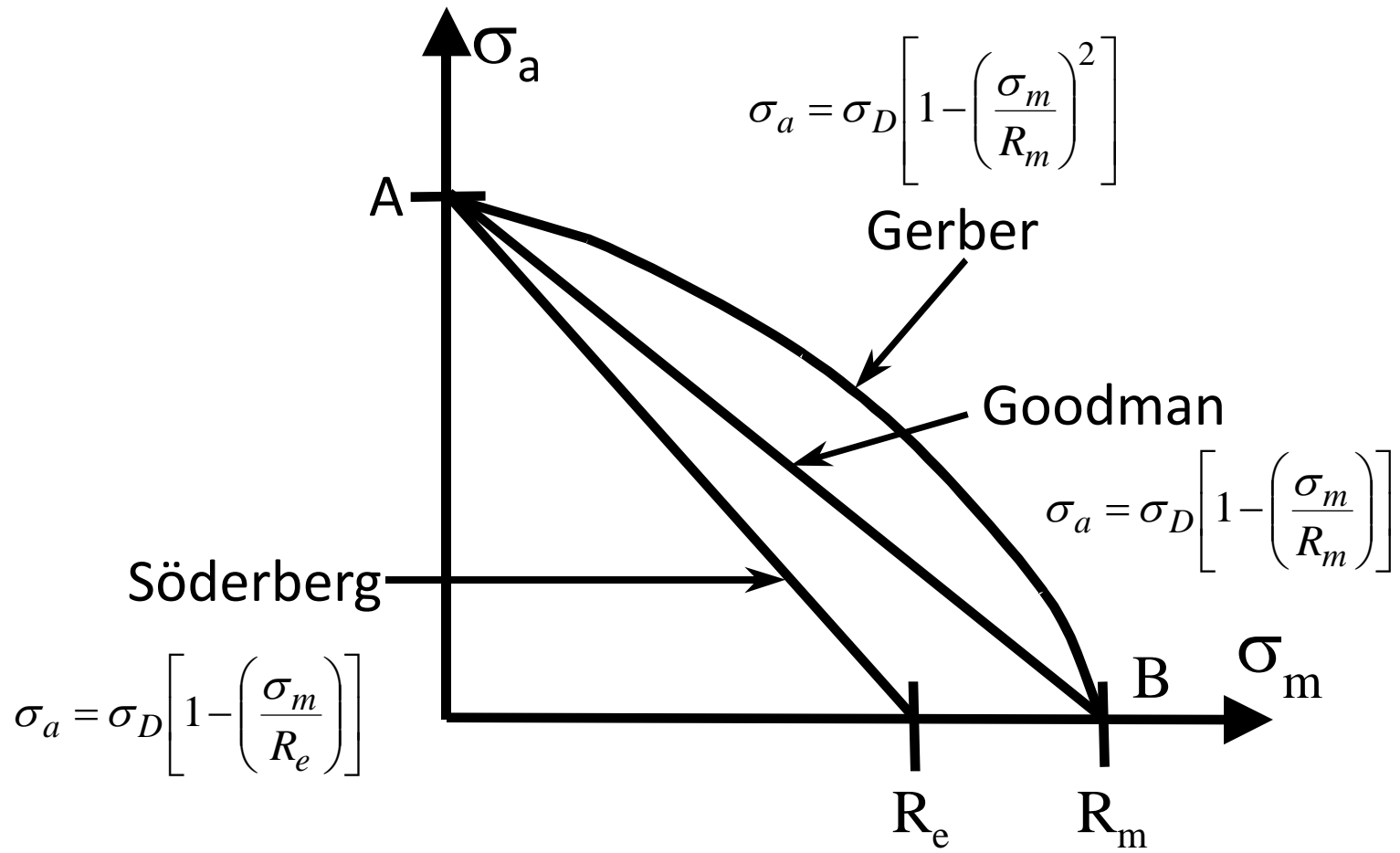
- Experimental observation: The permissible stress amplitude decreases when the mean stress increases
- Taken into account by the use of abacuses (*admissible stress as a function of the mean stress*)→ Different representations.



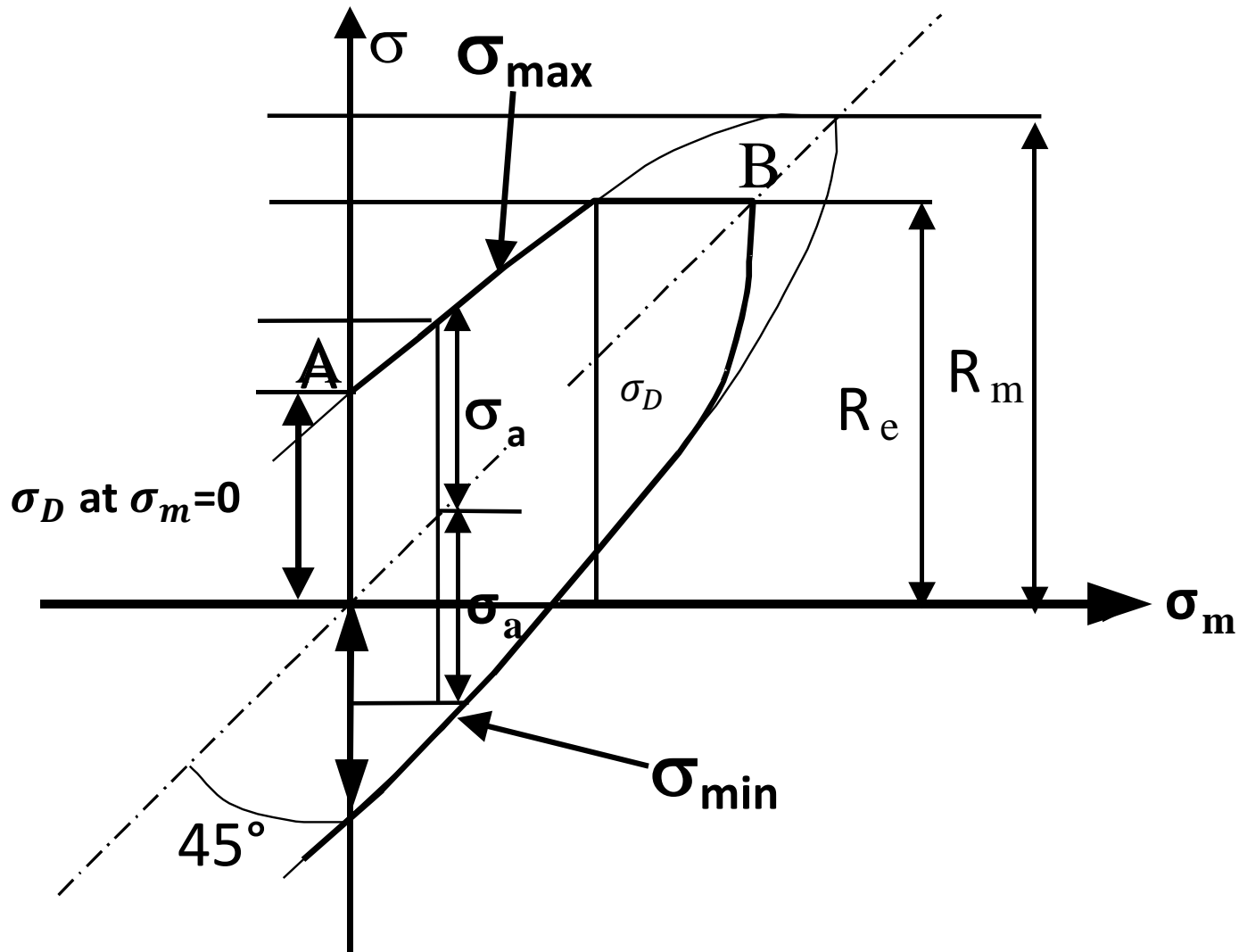
# Haigh Diagram



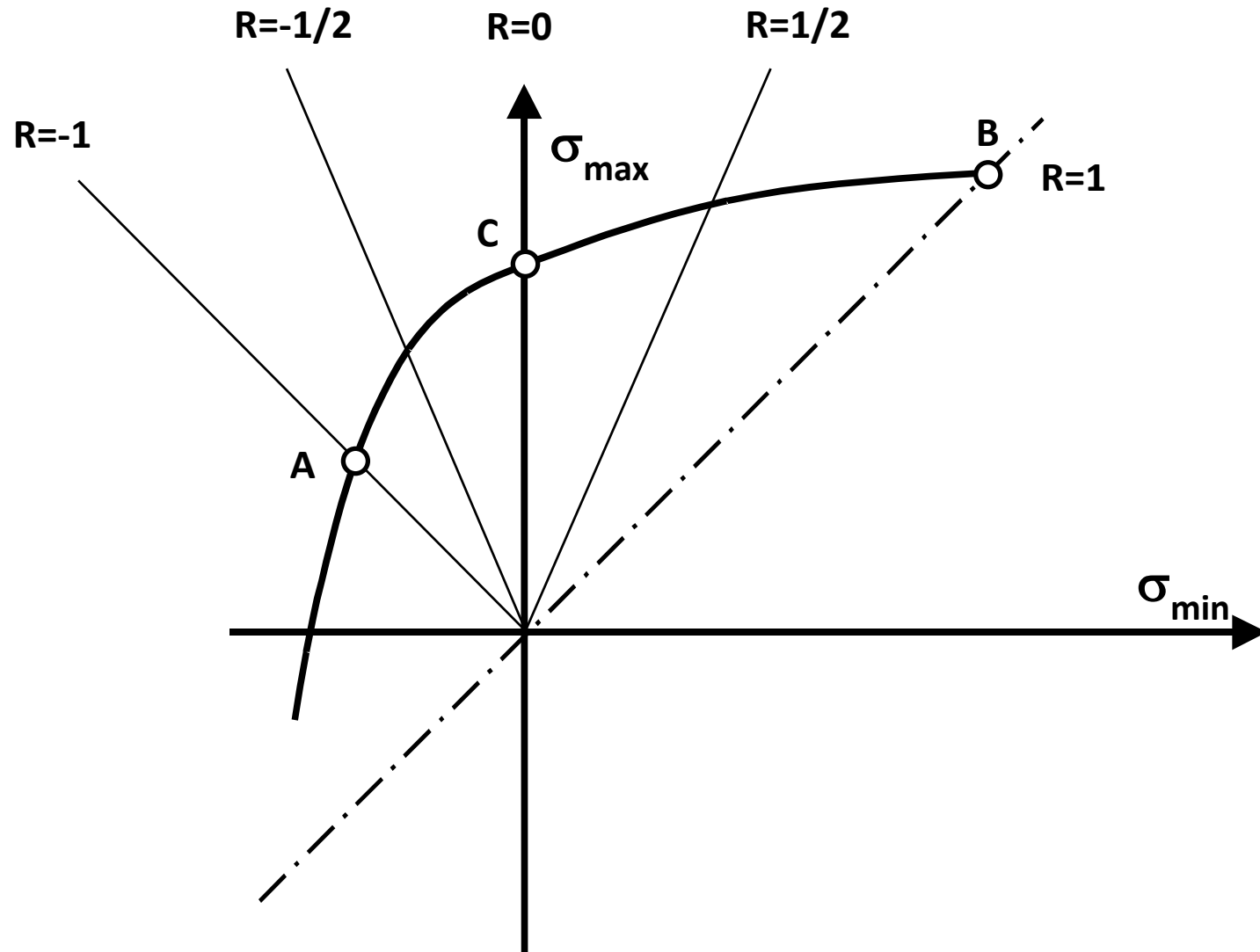
# Influence of mean stress



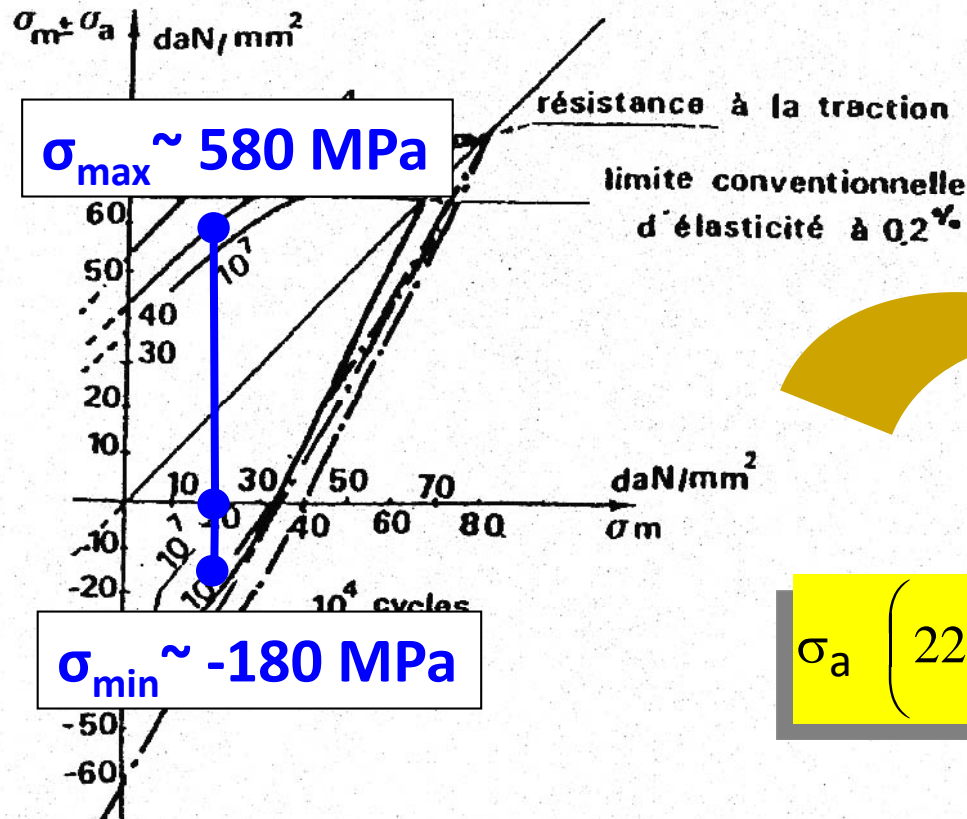
# Goodman-Smith Diagram



# Ros diagram



# Example: Goodman-Smith

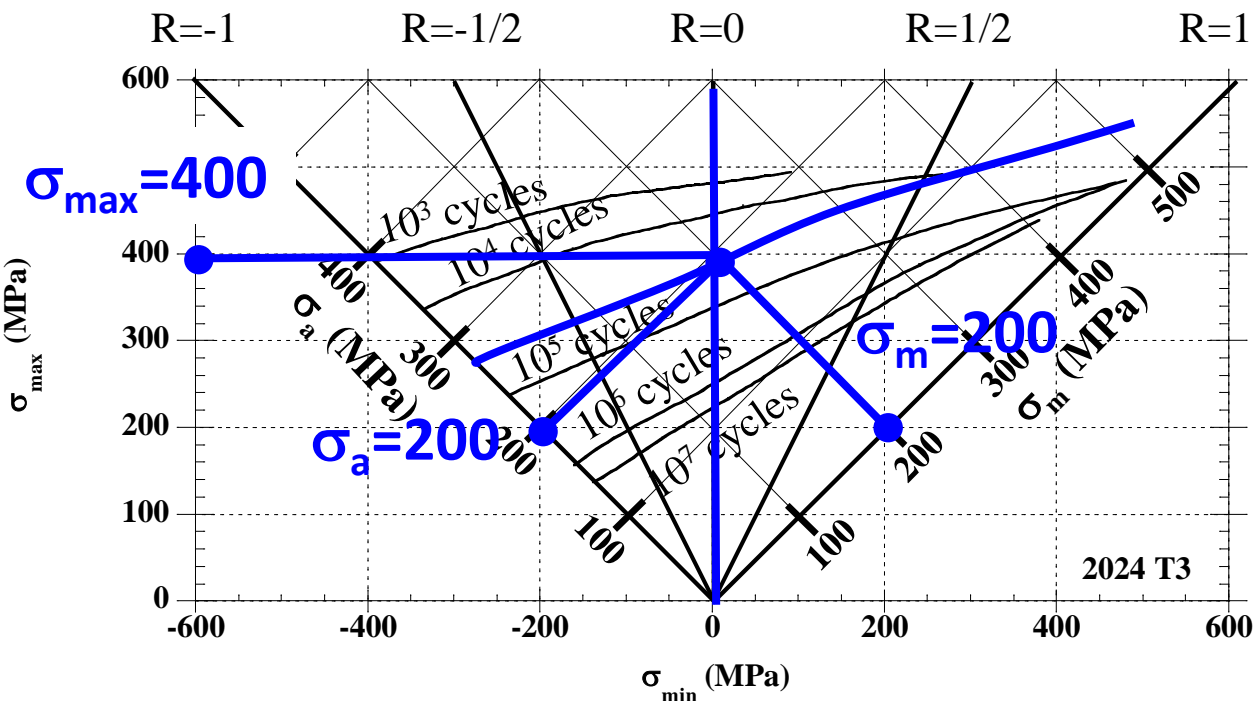


Admissible stress amplitude  $N_f = 10^5$  cycles and  $\sigma_m = 200 \text{ MPa}$  ?

$$\sigma_a \left( 220 \text{ MPa} - 10^5 \right) = 580 - 200 = 380 \text{ MPa}$$

# Example: Haigh diagram

Admissible stress amplitude at  $R=0$  with  $N_f=10^5$  cycles?

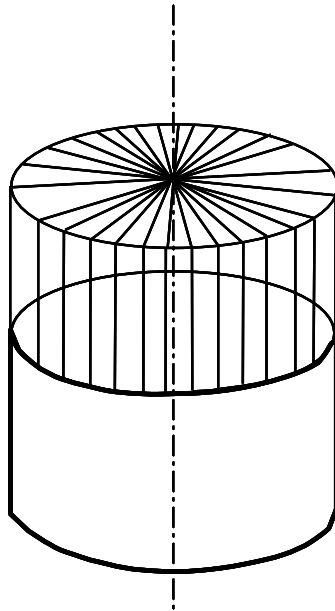


$$\sigma_a(R=0-10^5) = 200 \text{ MPa}$$

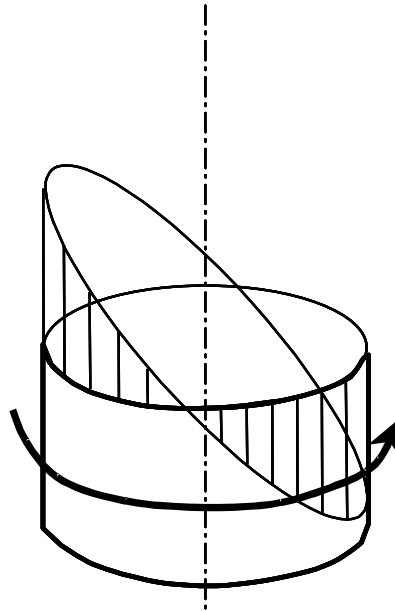
$$\sigma_{\max} = 400 \text{ MPa}$$

$$\sigma_m = 200 \text{ MPa} = \sigma_{\max} - \sigma_a$$

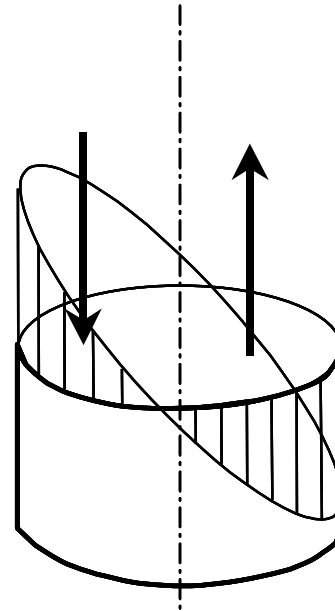
# Influence of loading mode



**Tension**



**Rotative bending**




**Plane bending**

		Plane bending	Tension / Compression	Torsion
<b>x</b>	$\sigma_D$			
<b>rotative</b>				
<b>bending</b>		1.05	0.9	0.6

# Scale effect

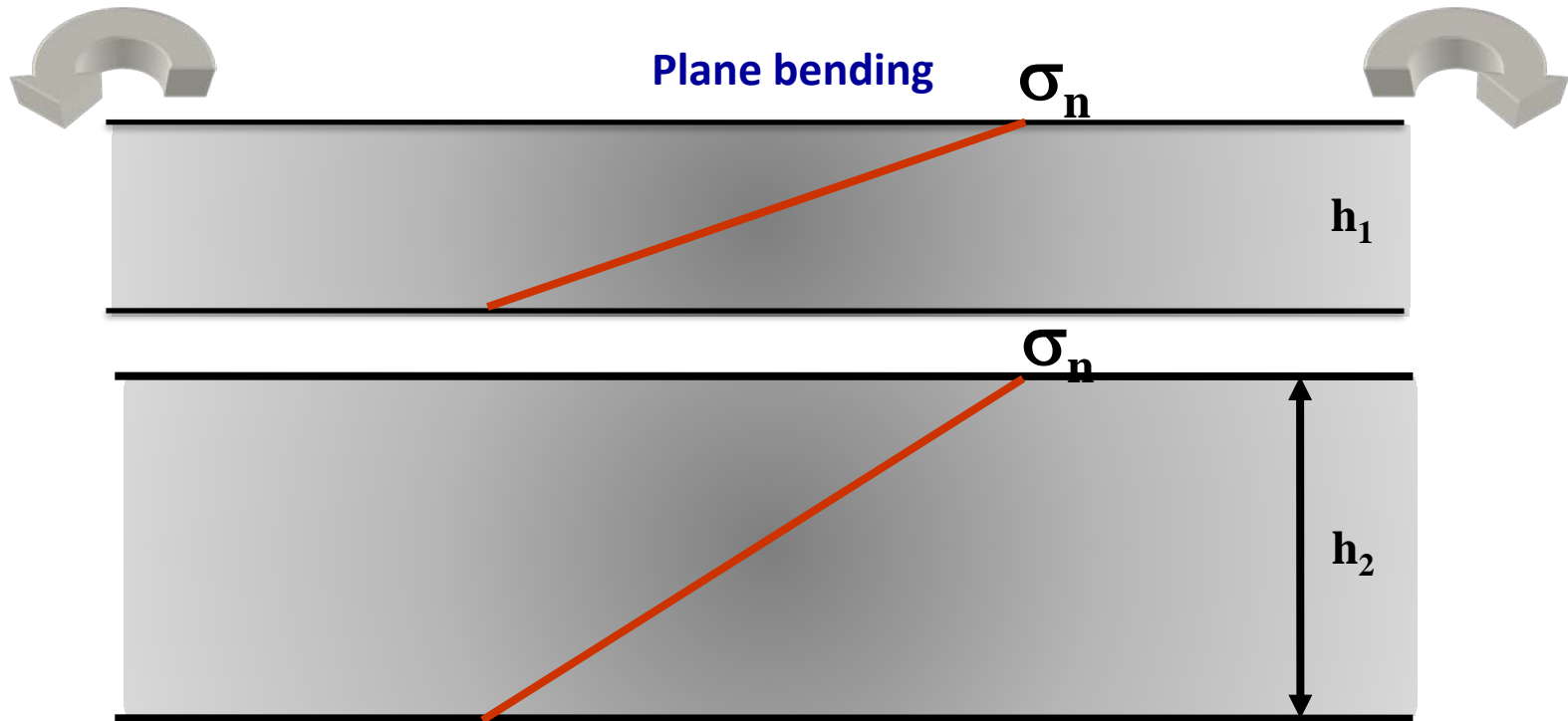
- Observation : for a given stress amplitude value, the higher the dimensions of the testpiece, the lower the fatigue strength.
- Causes :
  - mechanical;
  - probabilistic.
- Scale effect coefficient :

$$K_e = \frac{\sigma_D}{\sigma_{D_0}}$$


*Determined on a reference sample with small dimensions*



# Scale effect: stress gradient

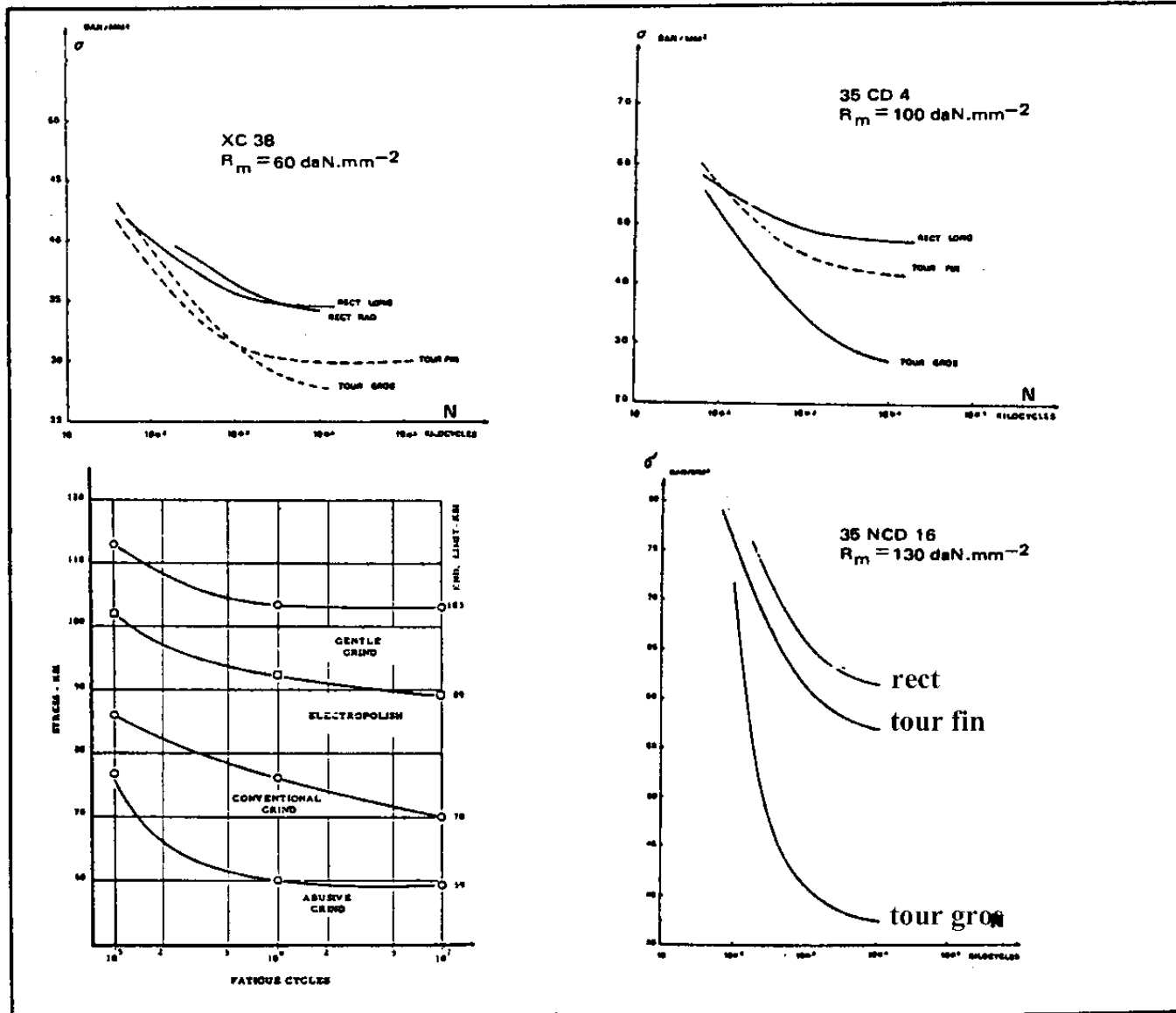


- Difference in stress gradients:
  - small thickness  $\Rightarrow$  high gradient. The less loaded layers support the highly loaded surface layers;
  - high thickness  $\Rightarrow$  small gradient. All the surface layer are nearly loaded in a similar way  $\Rightarrow$  loss in fatigue resistance

# Scale effect: probabilistic aspect

- The larger the dimensions of a component (volume, area), the more likely it is to have defects that behave as privileged initiation sites

# Influence of surface finishing



# Influence of surface finishing

Surface finishing factor:  
with :

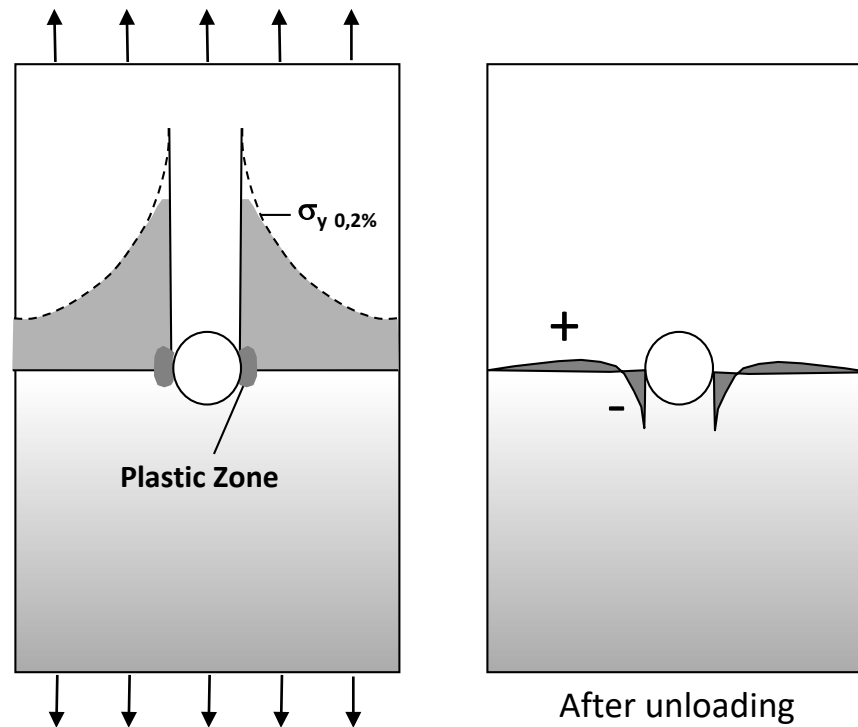
$$K_s = \frac{\sigma_{D_s}}{\sigma_D}$$

$\sigma_{D_s}$  fatigue limit with the surface finishing under consideration ;  
 $\sigma_D$  fatigue limit with a reference surface finishing.

# Residual stresses

- Induced (on purpose or not) by:
  - Inhomogeneous plastic deformations (especially in the vicinity of stress concentrators)
  - Process
  - Surface treatment (shot blasting, shot peening, coating,...)
  - Expanded holes
  - Joining

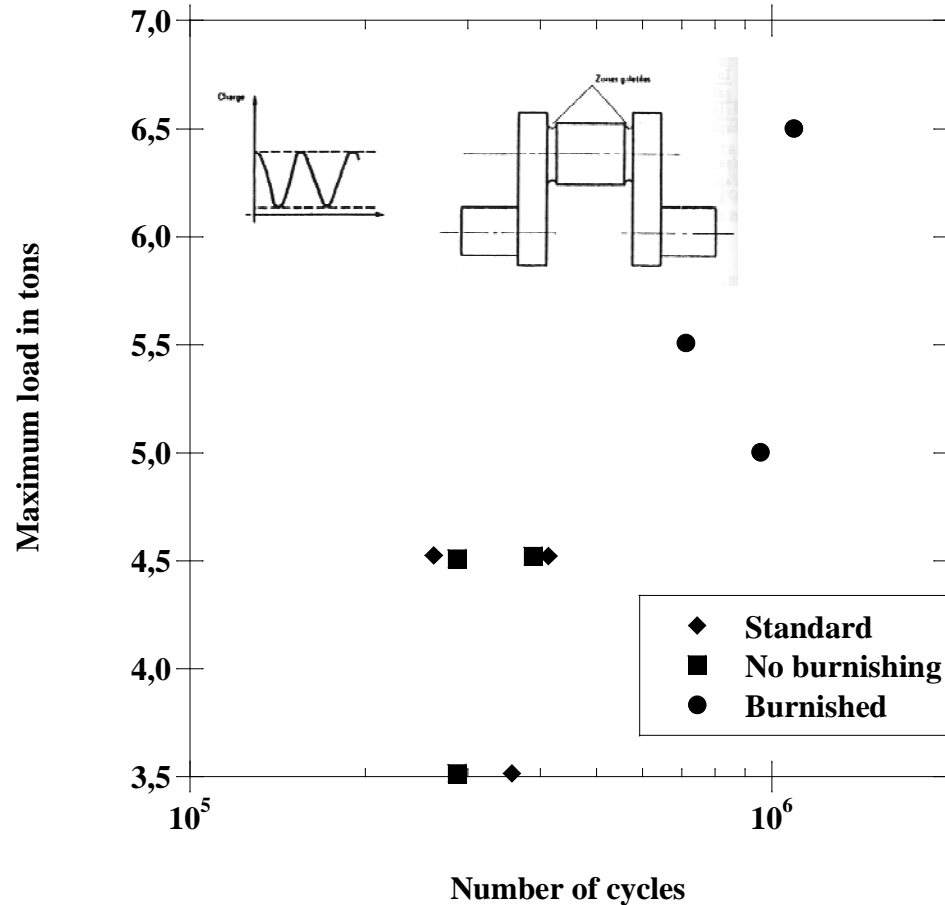
# Residual stresses near a stress concentrator



# Residual stresses induced by machining

Surface finishing	Machining parameters			Maximum surface residual stresses. (MPa)	Surface roughness ( $\mu\text{m}$ )	Fatigue limit (MPa)	
	Depth of pass (mm)	Advance (mm/tr)	Cutting speed (m/s)			Without annealing	After annealing at 650°C
Polished	0.1			-200	0.6	270	250
Turned	0.5	0.16	120	+100	17	215	240
Turned	0.5	0.32	120	+200	27	190	220
Turned	0.5	0.50	120	+600	46	175	205

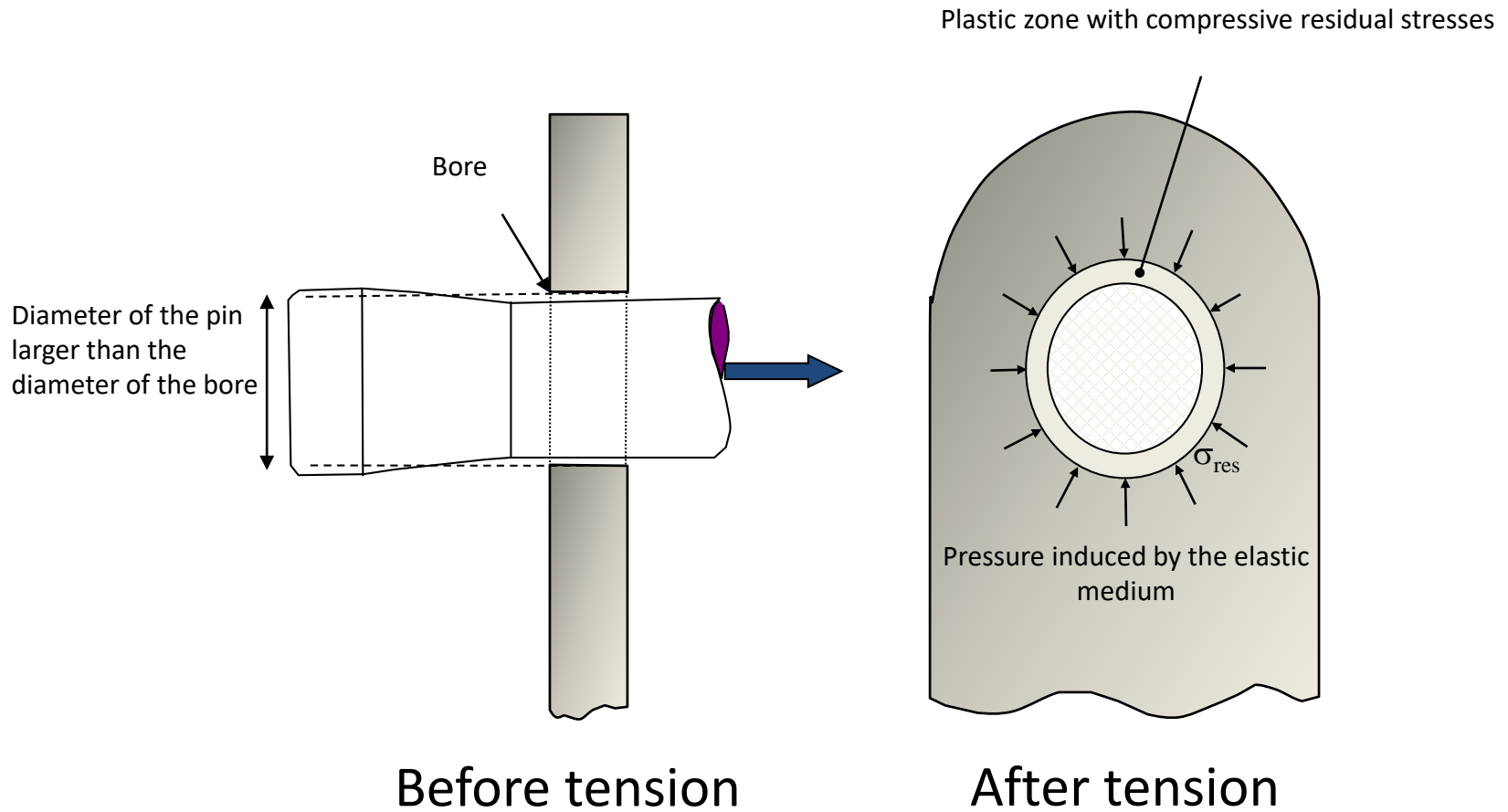
# Burnishing



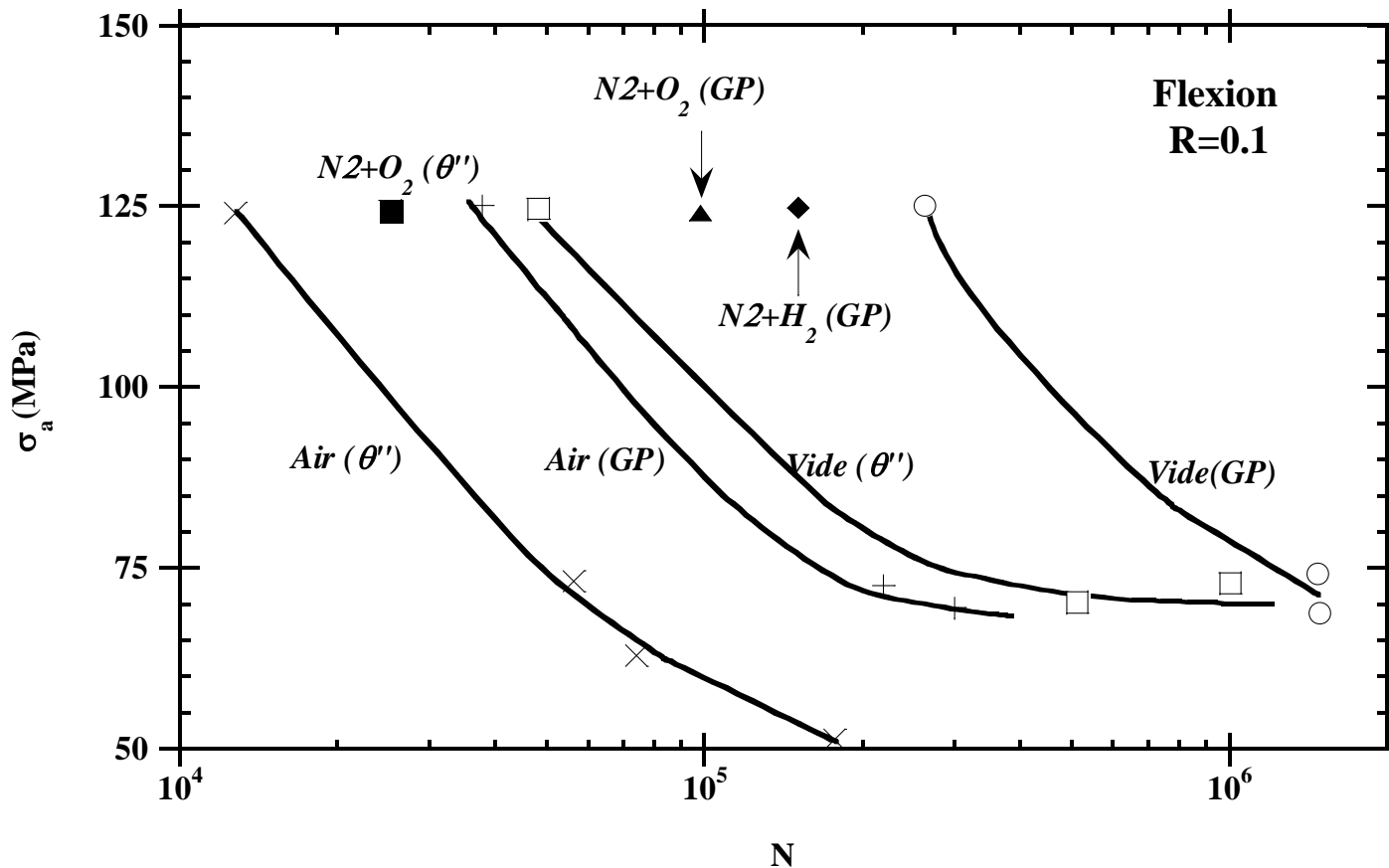
The residual stresses introduced by burnishing induce a higher fatigue resistance



# Expanded holes



# Influence of environment



- The fatigue life is lower in an active environment (air) than in an inert environment (vacuum)
- Related effect: influence of frequency