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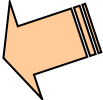
# **Data Warehousing and Data Mining**

**—Xike Xie —**

Slides are based on Prof. Han and Prof. Tan's works.

# Chapter 2: Getting to Know Your Data

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- Data Objects and Attribute Types 
- An Example of Clustering
- Basic Statistical Descriptions of Data
- Measuring Data Similarity and Dissimilarity
- Summary

# What is Data?

- Collection of data objects and their attributes
- An attribute is a property or characteristic of an object
  - Examples: eye color of a person, temperature, etc.
  - Attribute is also known as variable, field, characteristic, or feature
- A collection of attributes describe an object
  - Object is also known as record, point, case, sample, entity, or instance

Attributes



<i>Tid</i>	Refund	Marital Status	Taxable Income	Cheat
1	Yes	Single	125K	No
2	No	Married	100K	No
3	No	Single	70K	No
4	Yes	Married	120K	No
5	No	Divorced	95K	Yes
6	No	Married	60K	No
7	Yes	Divorced	220K	No
8	No	Single	85K	Yes
9	No	Married	75K	No
10	No	Single	90K	Yes

# Attributes

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- **Attribute (or dimensions, features, variables):**  
a data field, representing a characteristic or feature of a data object.
  - *E.g., customer\_ID, name, address*
- **Types:**
  - Nominal
  - Binary
  - Numeric: quantitative
    - Interval-scaled
    - Ratio-scaled

# Attribute Types

- **Nominal:** categories, states, or “names of things”
  - *Hair\_color* = {*auburn, black, blond, brown, grey, red, white*}
  - marital status, occupation, ID numbers, zip codes
- **Binary**
  - Nominal attribute with only 2 states (0 and 1)
  - Symmetric binary: both outcomes equally important
    - e.g., gender
  - Asymmetric binary: outcomes not equally important.
    - e.g., medical test (positive vs. negative)
    - Convention: assign 1 to most important outcome (e.g., HIV positive)
- **Ordinal**
  - Values have a meaningful order (ranking) but magnitude between successive values is not known.
  - *Size* = {*small, medium, large*}, grades, army rankings

# Numeric Attribute Types

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- Quantity (integer or real-valued)
- **Interval**
  - Measured on a scale of **equal-sized units**
  - Values have order
    - E.g., *temperature in  $C^{\circ}$  or  $F^{\circ}$ , calendar dates*
  - No true zero-point
- **Ratio**
  - Inherent **zero-point**
  - We can speak of values as being an order of magnitude larger than the unit of measurement ( $10\text{ K}^{\circ}$  is twice as high as  $5\text{ K}^{\circ}$ ).
    - e.g., *temperature in Kelvin, length, counts, monetary quantities*

# Properties of Attribute Values

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- The type of an attribute depends on which of the following properties it possesses:
  - Distinctness:  $= \neq$
  - Order:  $< >$
  - Addition:  $+ -$
  - Multiplication:  $* /$
- Nominal attribute: distinctness
- Ordinal attribute: distinctness & order
- Interval attribute: distinctness, order & addition
- Ratio attribute: all 4 properties

Attribute Type	Description	Examples	Operations
Nominal	The values of a nominal attribute are just different names, i.e., nominal attributes provide only enough information to distinguish one object from another. ( $=$ , $\neq$ )	zip codes, employee ID numbers, eye color, sex: $\{male, female\}$	mode, entropy, contingency correlation, $\chi^2$ test
Ordinal	The values of an ordinal attribute provide enough information to order objects. ( $<$ , $>$ )	hardness of minerals, $\{good, better, best\}$ , grades, street numbers	median, percentiles, rank correlation, run tests, sign tests
Interval	For interval attributes, the differences between values are meaningful, i.e., a unit of measurement exists. ( $+$ , $-$ )	calendar dates, temperature in Celsius or Fahrenheit	mean, standard deviation, Pearson's correlation, $t$ and $F$ tests
Ratio	For ratio variables, both differences and ratios are meaningful. ( $*$ , $/$ )	temperature in Kelvin, monetary quantities, counts, age, mass, length, electrical current	geometric mean, harmonic mean, percent variation



Attribute Level	Transformation	Comments
Nominal	Any permutation of values	If all employee ID numbers were reassigned, would it make any difference?
Ordinal	An order preserving change of values, i.e., $new\_value = f(old\_value)$ where $f$ is a monotonic function.	An attribute encompassing the notion of good, better best can be represented equally well by the values {1, 2, 3} or by { 0.5, 1, 10}.
Interval	$new\_value = a * old\_value + b$ where a and b are constants	Thus, the Fahrenheit and Celsius temperature scales differ in terms of where their zero value is and the size of a unit (degree).
Ratio	$new\_value = a * old\_value$	Length can be measured in meters or feet.

# Discrete vs. Continuous Attributes

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## ■ Discrete Attribute

- Has only a finite or countably infinite set of values
  - E.g., zip codes, profession, or the set of words in a collection of documents
- Sometimes, represented as integer variables
- Note: Binary attributes are a special case of discrete attributes

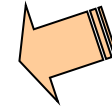
## ■ Continuous Attribute

- Has real numbers as attribute values
  - E.g., temperature, height, or weight
- Practically, real values can only be measured and represented using a finite number of digits
- Continuous attributes are typically represented as floating-point variables

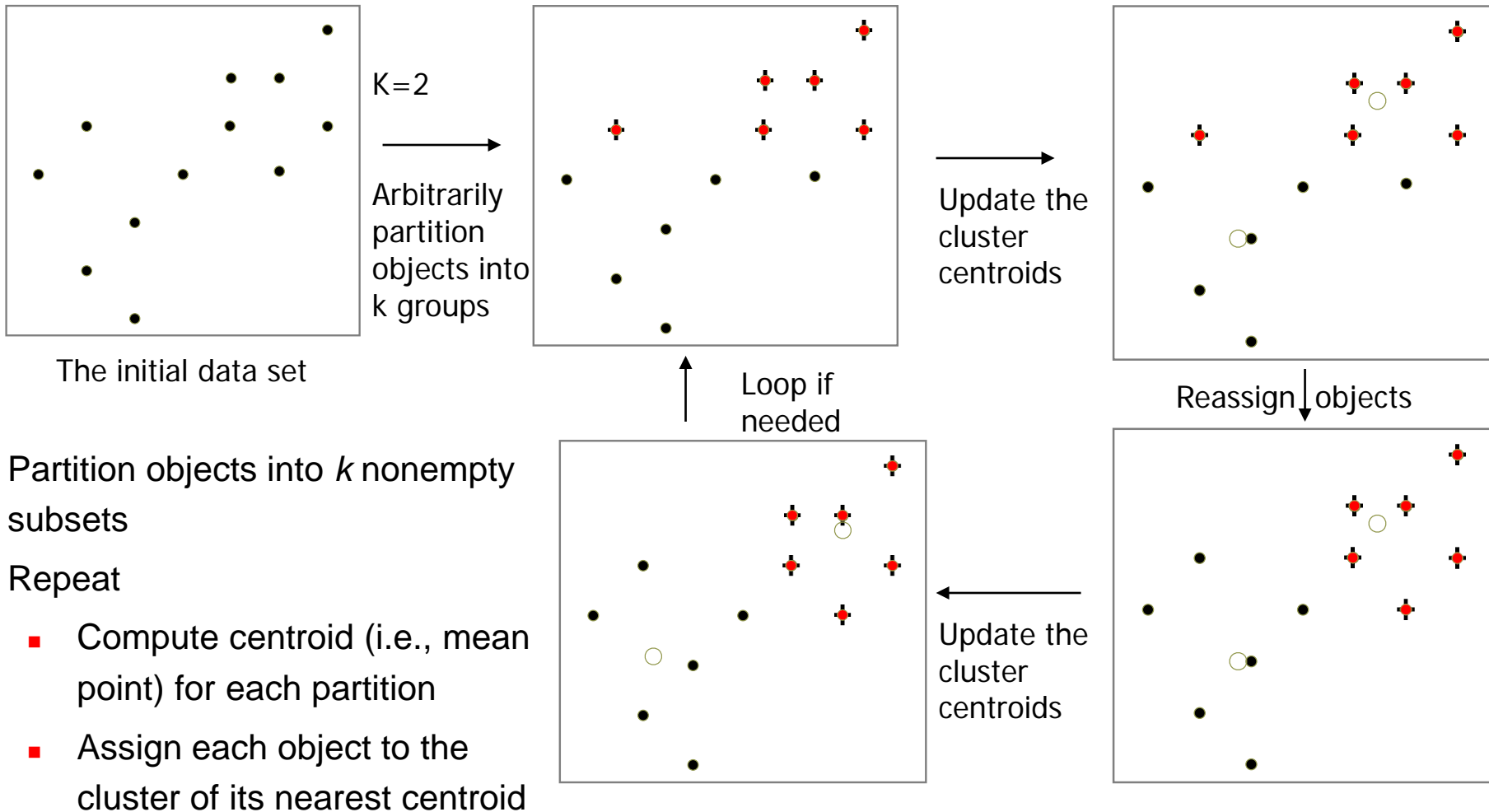
# Chapter 2: Getting to Know Your Data

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- An Example of Clustering
- Basic Statistical Descriptions of Data
- Measuring Data Similarity and Dissimilarity
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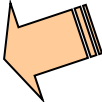
# An Example of *K*-Means Clustering



- Partition objects into  $k$  nonempty subsets
- Repeat
  - Compute centroid (i.e., mean point) for each partition
  - Assign each object to the cluster of its nearest centroid
- Until no change

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# Basic Statistical Descriptions of Data

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- Motivation
  - To better understand the data: central tendency, variation and spread
- Data dispersion characteristics
  - median, max, min, quantiles, outliers, variance, etc.
- Numerical dimensions correspond to sorted intervals
  - Data dispersion: analyzed with multiple granularities of precision
  - Boxplot or quantile analysis on sorted intervals
- Dispersion analysis on computed measures
  - Folding measures into numerical dimensions
  - Boxplot or quantile analysis on the transformed cube

# Measuring the Central Tendency

- Mean (algebraic measure) (sample vs. population):

Note:  $n$  is sample size and  $N$  is population size.

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i$$

$$\mu = \frac{\sum x}{N}$$

  - Weighted arithmetic mean:
  - Trimmed mean: chopping extreme values
- Median:

$$\bar{x} = \frac{\sum_{i=1}^n w_i x_i}{\sum_{i=1}^n w_i}$$

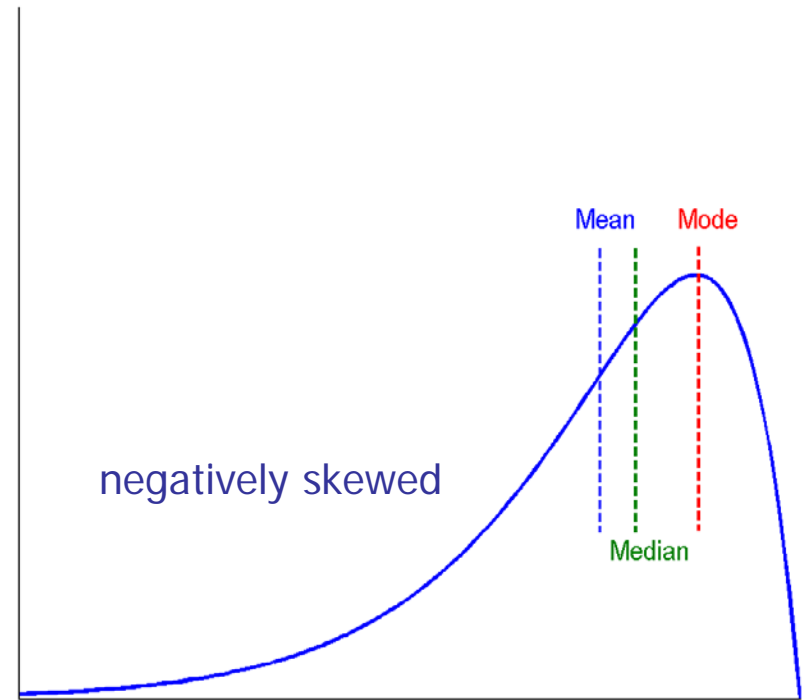
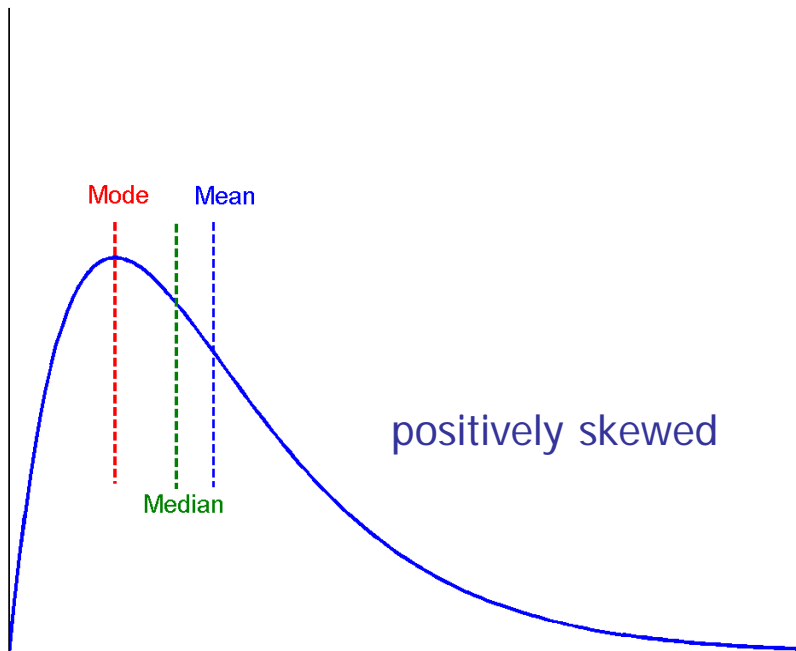
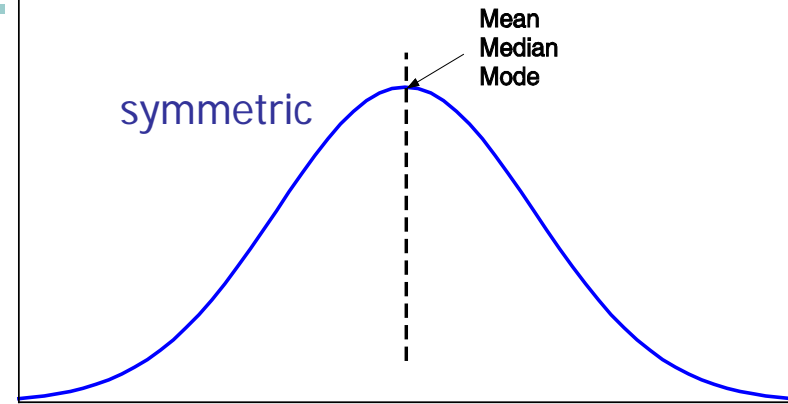
  - Middle value if odd number of values, or average of the middle two values otherwise
  - Estimated by interpolation (for *grouped data*):

$$median = L_1 + \left( \frac{n/2 - (\sum freq)l}{freq_{median}} \right) width$$
- Mode
  - Value that occurs most frequently in the data
  - Unimodal, bimodal, trimodal
  - Empirical formula:  $mean - mode = 3 \times (mean - median)$

age	frequency
1-5	200
6-15	450
16-20	300
21-50	1500
51-80	700
81-110	44

# Symmetric vs. Skewed Data

- Median, mean and mode of symmetric, positively and negatively skewed data





# Measuring the Dispersion of Data

- Quartiles, outliers and boxplots

- **Quartiles:**  $Q_1$  (25<sup>th</sup> percentile),  $Q_3$  (75<sup>th</sup> percentile)
- **Inter-quartile range:**  $IQR = Q_3 - Q_1$
- **Five number summary:** min,  $Q_1$ , median,  $Q_3$ , max
- **Boxplot:** ends of the box are the quartiles; median is marked; add whiskers, and plot outliers individually
- **Outlier:** usually, a value higher/lower than  $1.5 \times IQR$

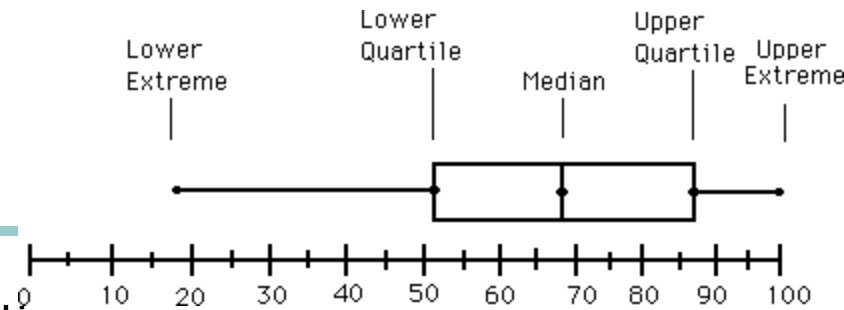
- Variance and standard deviation (*sample:  $s$ , population:  $\sigma$* )

- **Variance:** (algebraic, scalable computation)

$$s^2 = \frac{1}{n-1} \sum_{i=1}^n (x_i - \bar{x})^2 = \frac{1}{n-1} \left[ \sum_{i=1}^n x_i^2 - \frac{1}{n} \left( \sum_{i=1}^n x_i \right)^2 \right] \quad \sigma^2 = \frac{1}{N} \sum_{i=1}^n (x_i - \mu)^2 = \frac{1}{N} \sum_{i=1}^n x_i^2 - \mu^2$$

- **Standard deviation  $s$  (or  $\sigma$ )** is the square root of variance  $s^2$  (or  $\sigma^2$ )

# Boxplot Analysis

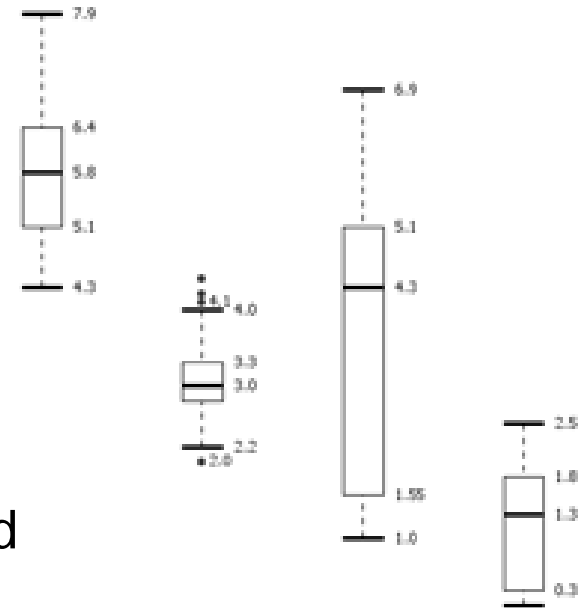


- **Five-number summary** of a distribution

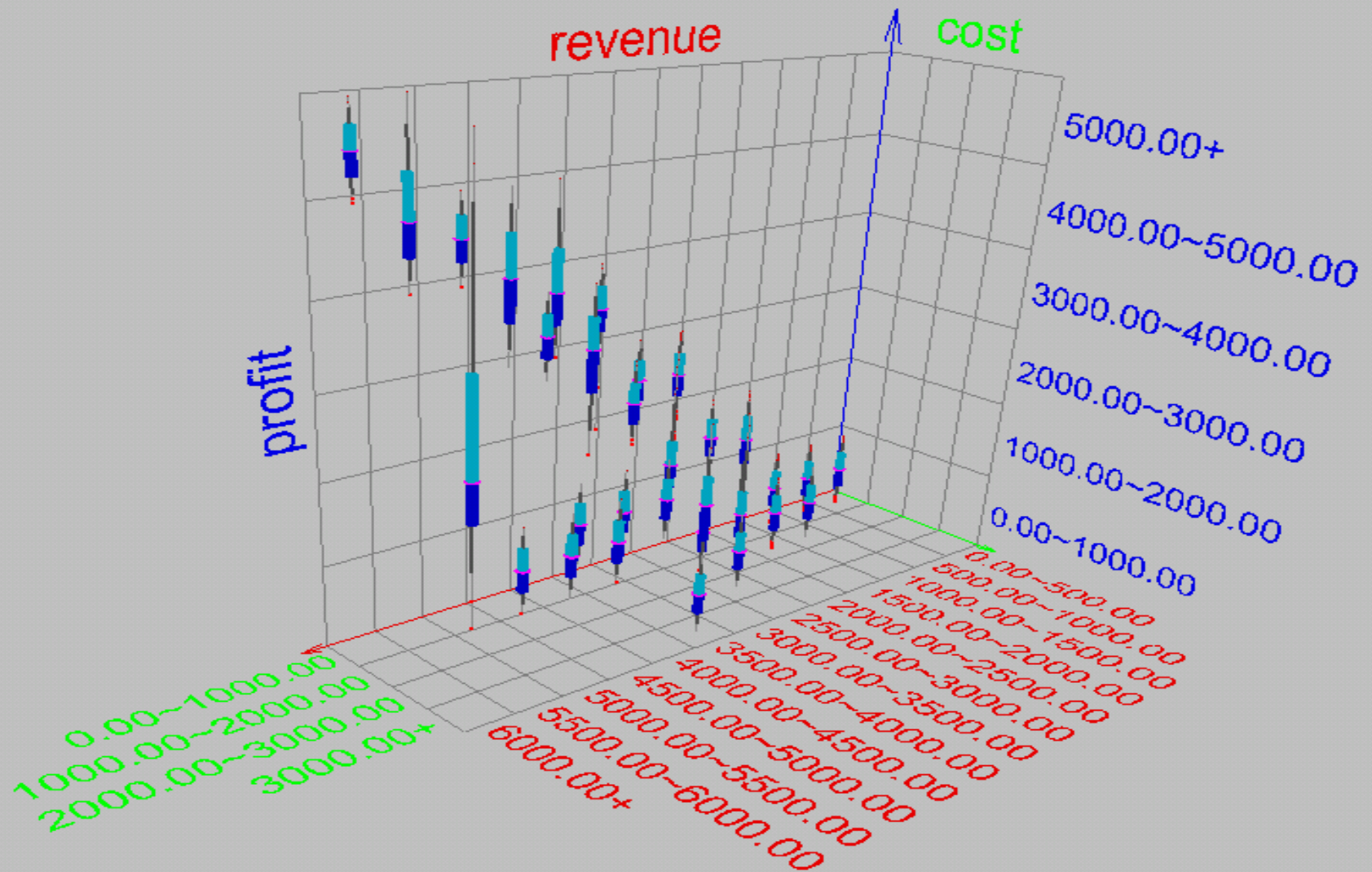
- Minimum, Q1, Median, Q3, Maximum

- **Boxplot**

- Data is represented with a box
- The ends of the box are at the first and third quartiles, i.e., the height of the box is IQR
- The median is marked by a line within the box
- Whiskers: two lines outside the box extended to Minimum and Maximum
- Outliers: points beyond a specified outlier threshold, plotted individually

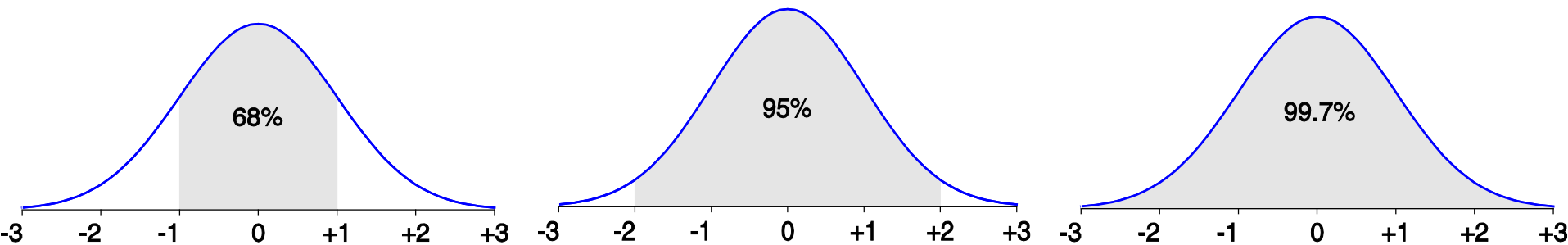


# Visualization of Data Dispersion: 3-D Boxplots



# Properties of Normal Distribution Curve

- The normal (distribution) curve
  - From  $\mu - \sigma$  to  $\mu + \sigma$ : contains about 68% of the measurements ( $\mu$ : mean,  $\sigma$ : standard deviation)
  - From  $\mu - 2\sigma$  to  $\mu + 2\sigma$ : contains about 95% of it
  - From  $\mu - 3\sigma$  to  $\mu + 3\sigma$ : contains about 99.7% of it



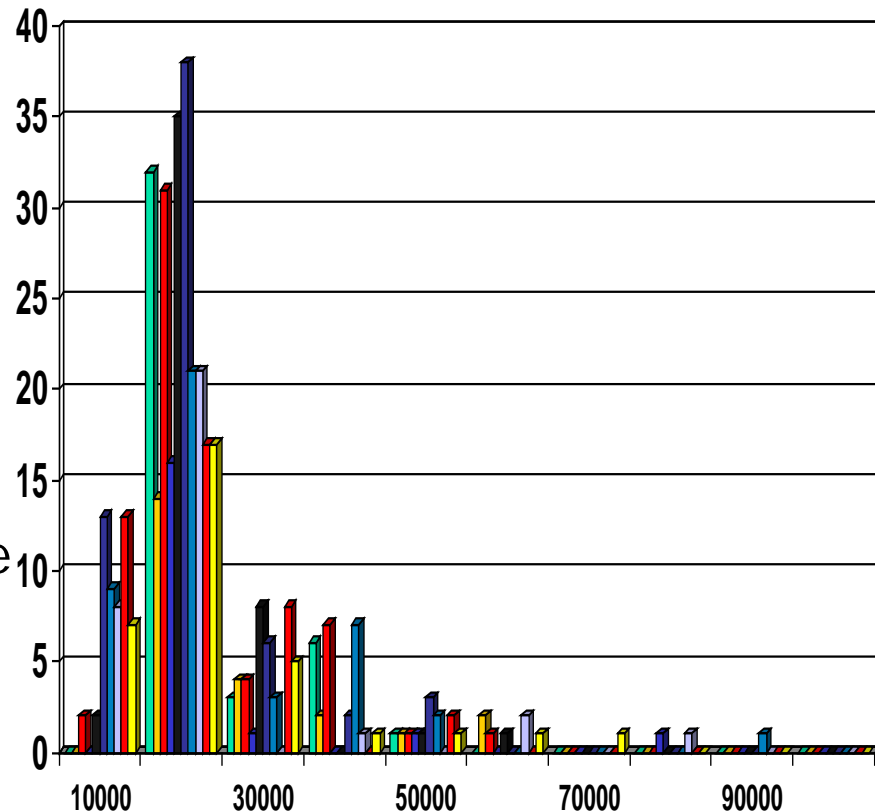
# Graphic Displays of Basic Statistical Descriptions

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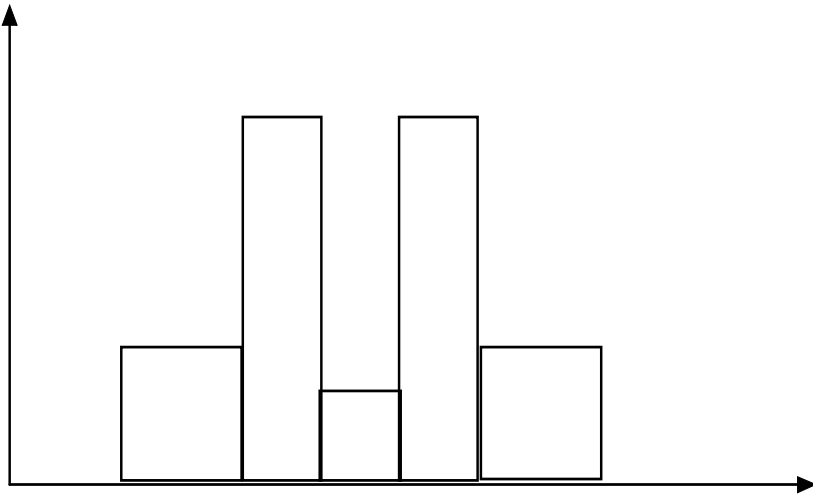
- **Boxplot:** graphic display of five-number summary
- **Histogram:** x-axis are values, y-axis repres. frequencies
- **Quantile plot:** each value  $x_i$  is paired with  $f_i$  indicating that approximately 100  $f_i$ % of data are  $\leq x_i$
- **Quantile-quantile (q-q) plot:** graphs the quantiles of one univariant distribution against the corresponding quantiles of another
- **Scatter plot:** each pair of values is a pair of coordinates and plotted as points in the plane

# Histogram Analysis

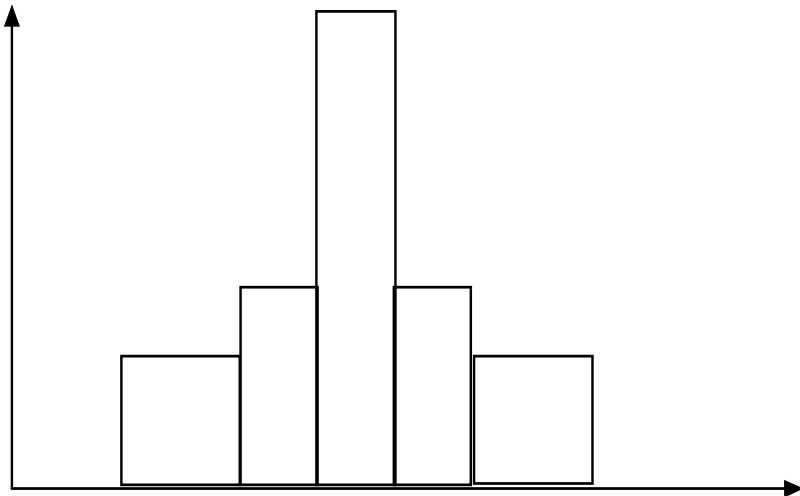
- Histogram: Graph display of tabulated frequencies, shown as bars
- It shows what proportion of cases fall into each of several categories
- Differs from a bar chart in that it is the *area* of the bar that denotes the value, not the height as in bar charts, a crucial distinction when the categories are not of uniform width
- The categories are usually specified as non-overlapping intervals of some variable. The categories (bars) must be adjacent



# Histograms Often Tell More than Boxplots

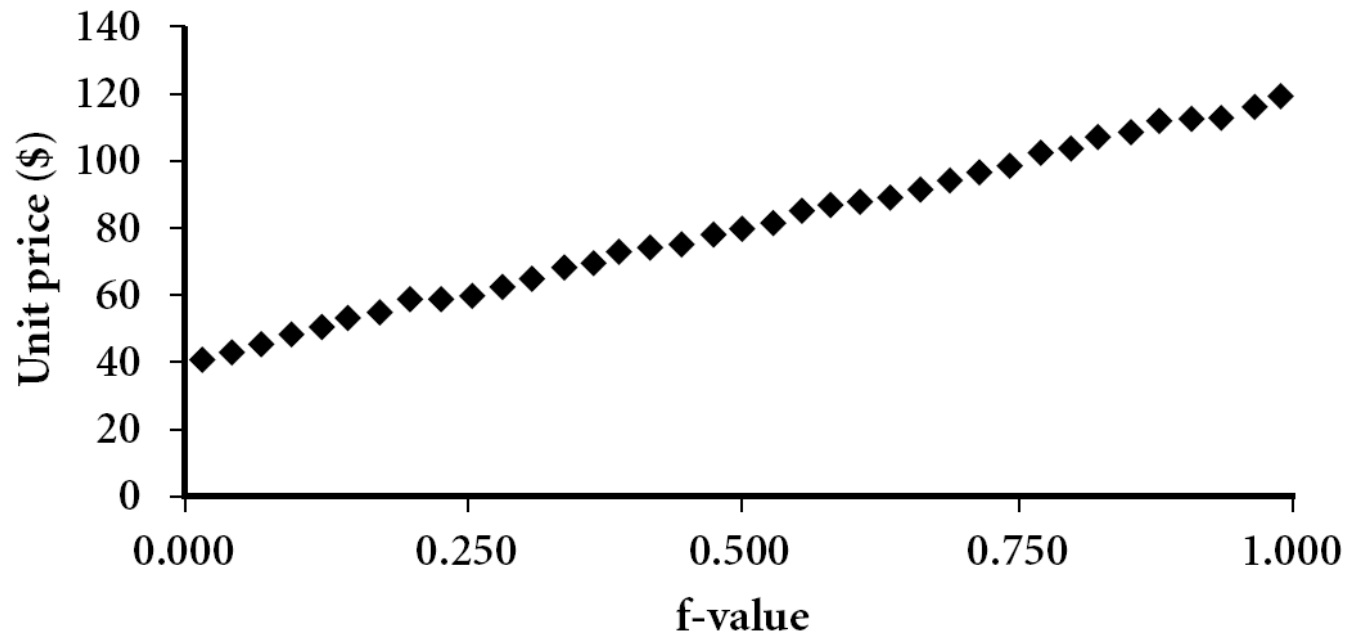


- The two histograms shown in the left may have the same boxplot representation
  - The same values for: min, Q1, median, Q3, max
- But they have rather different data distributions



# Quantile Plot

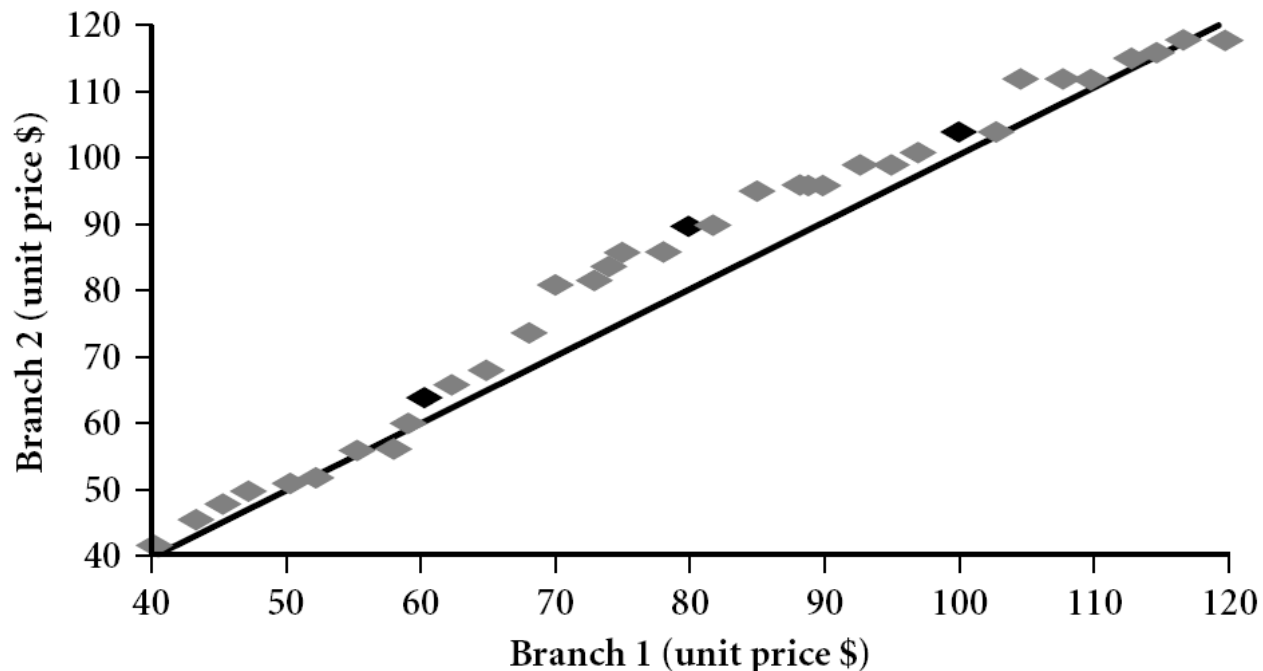
- Displays all of the data (allowing the user to assess both the overall behavior and unusual occurrences)
- Plots **quantile** information
  - For a data  $x_i$  data sorted in increasing order,  $f_i$  indicates that approximately 100  $f_i$ % of the data are below or equal to the value  $x_i$





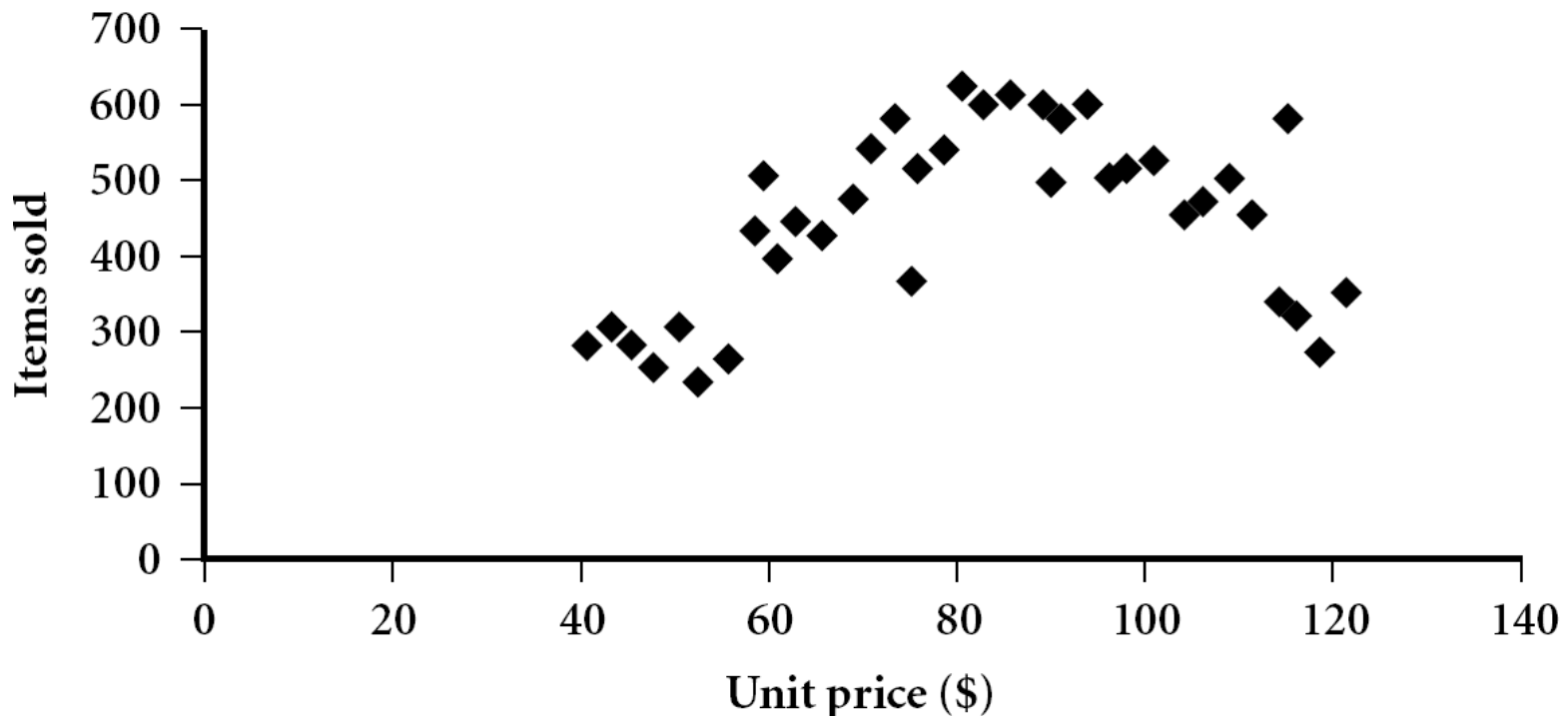
# Quantile-Quantile (Q-Q) Plot

- Graphs the quantiles of one univariate distribution against the corresponding quantiles of another
- View: Is there is a shift in going from one distribution to another?
- Example shows unit price of items sold at Branch 1 vs. Branch 2 for each quantile. Unit prices of items sold at Branch 1 tend to be lower than those at Branch 2.

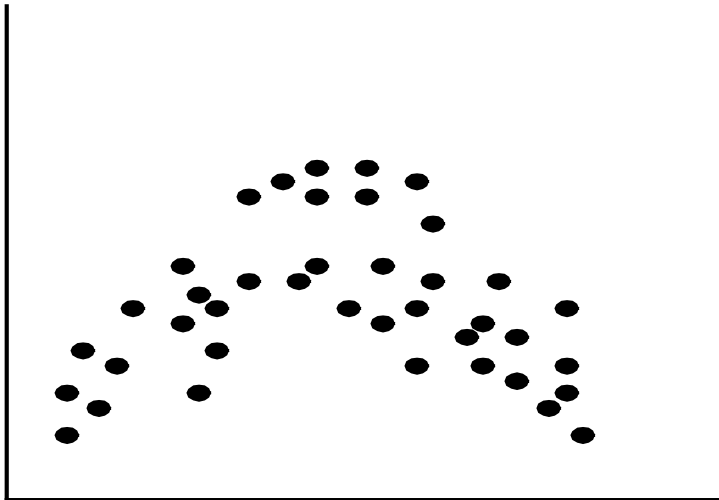
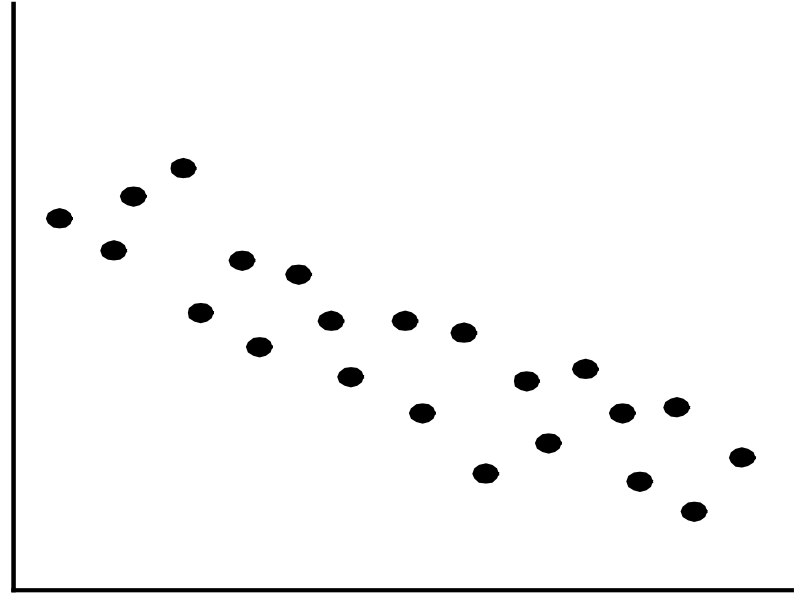
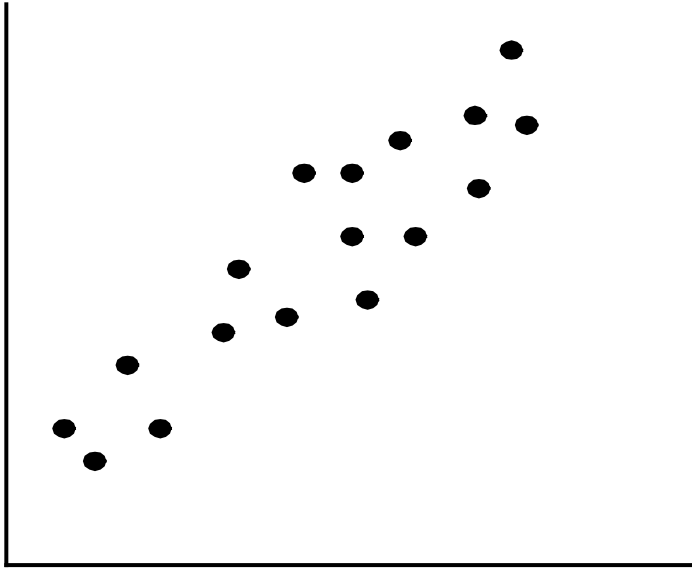


# Scatter plot

- Provides a first look at bivariate data to see clusters of points, outliers, etc
- Each pair of values is treated as a pair of coordinates and plotted as points in the plane



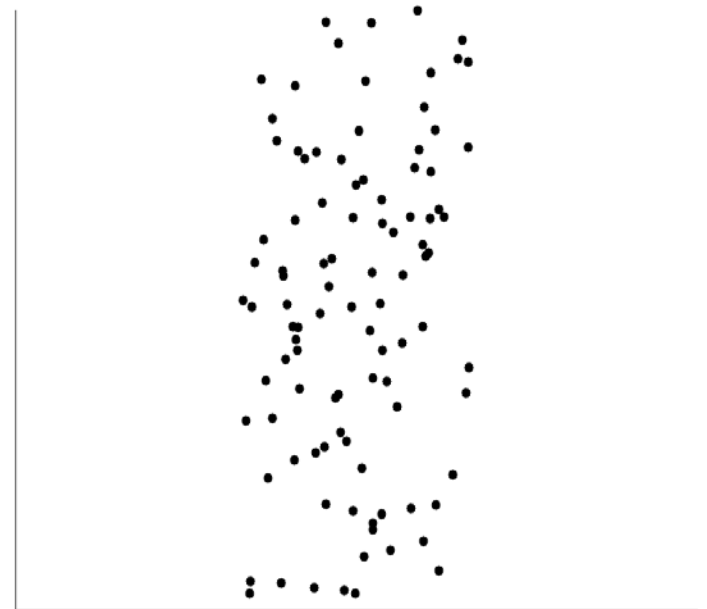
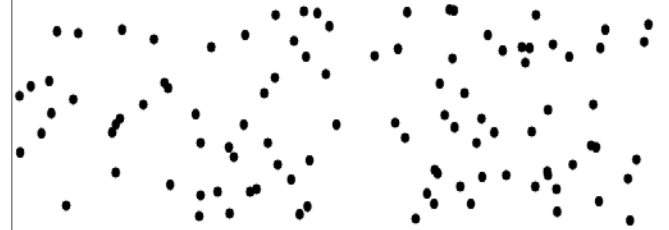
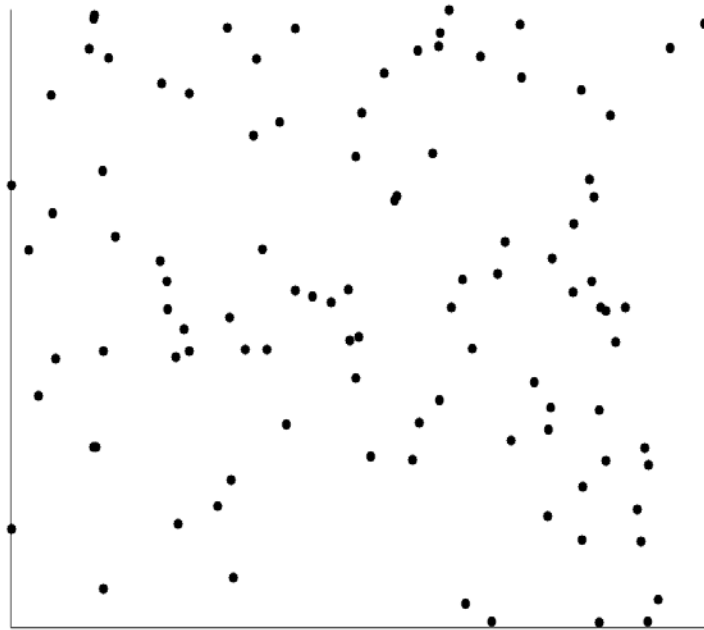
# Positively and Negatively Correlated Data



- The left half fragment is positively correlated
- The right half is negative correlated

# Uncorrelated Data

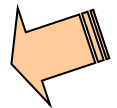
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# Chapter 2: Getting to Know Your Data

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# Similarity and Dissimilarity

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- **Similarity**

- Numerical measure of how alike two data objects are
- Value is higher when objects are more alike
- Often falls in the range  $[0,1]$

- **Dissimilarity** (e.g., distance)

- Numerical measure of how different two data objects are
- Lower when objects are more alike
- Minimum dissimilarity is often 0
- Upper limit varies

- **Proximity** refers to a similarity or dissimilarity

# Data Matrix and Dissimilarity Matrix

## ■ Data matrix

- n data points with p dimensions
- Two modes

$$\begin{bmatrix} x_{11} & \dots & x_{1f} & \dots & x_{1p} \\ \dots & \dots & \dots & \dots & \dots \\ x_{i1} & \dots & x_{if} & \dots & x_{ip} \\ \dots & \dots & \dots & \dots & \dots \\ x_{n1} & \dots & x_{nf} & \dots & x_{np} \end{bmatrix}$$

## ■ Dissimilarity matrix

- n data points, but registers only the distance
- A triangular matrix
- Single mode

$$\begin{bmatrix} 0 & & & & \\ d(2,1) & 0 & & & \\ d(3,1) & d(3,2) & 0 & & \\ \vdots & \vdots & \vdots & & \\ d(n,1) & d(n,2) & \dots & \dots & 0 \end{bmatrix}$$

# Proximity Measure for Nominal Attributes

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- Can take 2 or more states, e.g., red, yellow, blue, green (generalization of a binary attribute)
- Method 1: Simple matching
  - $m$ : # of matches,  $p$ : total # of variables
$$d(i, j) = \frac{p - m}{p}$$
- Method 2: Use a large number of binary attributes
  - creating a new binary attribute for each of the  $M$  nominal states



# Proximity Measure for Binary Attributes

- A contingency table for binary data

		Object $j$		
		1	0	sum
Object $i$	1	$q$	$r$	$q + r$
	0	$s$	$t$	$s + t$
sum		$q + s$	$r + t$	$p$

- Distance measure for symmetric binary variables:
- Distance measure for asymmetric binary variables:
- Jaccard coefficient (*similarity* measure for *asymmetric* binary variables):

$$d(i, j) = \frac{r + s}{q + r + s + t}$$

$$d(i, j) = \frac{r + s}{q + r + s}$$

$$sim_{Jaccard}(i, j) = \frac{q}{q + r + s}$$

- Note: Jaccard coefficient is the same as "coherence":

$$coherence(i, j) = \frac{sup(i, j)}{sup(i) + sup(j) - sup(i, j)} = \frac{q}{(q + r) + (q + s) - q}$$

# Dissimilarity between Binary Variables

## ■ Example

Name	Gender	Fever	Cough	Test-1	Test-2	Test-3	Test-4
Jack	M	Y	N	P	N	N	N
Mary	F	Y	N	P	N	P	N
Jim	M	Y	P	N	N	N	N

- Gender is a symmetric attribute
- The remaining attributes are asymmetric binary
- Let the values Y and P be 1, and the value N 0

$$d(jack, mary) =$$

$$d(jack, jim) =$$

$$d(jim, mary) =$$

# Dissimilarity between Binary Variables

## ■ Example

Name	Gender	Fever	Cough	Test-1	Test-2	Test-3	Test-4
Jack	M	Y	N	P	N	N	N
Mary	F	Y	N	P	N	P	N
Jim	M	Y	P	N	N	N	N

- Gender is a symmetric attribute
- The remaining attributes are asymmetric binary
- Let the values Y and P be 1, and the value N 0

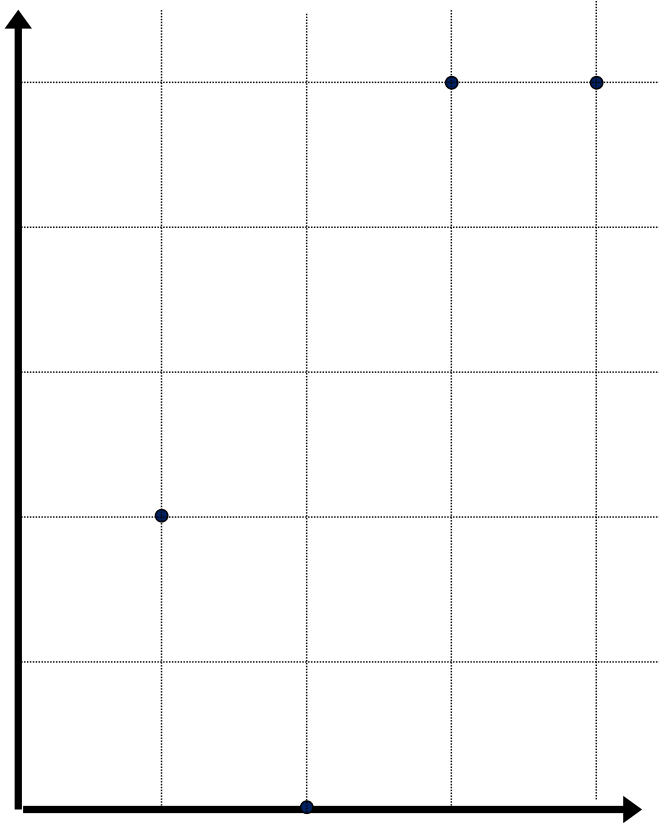
$$d(jack, mary) = \frac{0 + 1}{2 + 0 + 1} = 0.33$$

$$d(jack, jim) = \frac{1 + 1}{1 + 1 + 1} = 0.67$$

$$d(jim, mary) = \frac{1 + 2}{1 + 1 + 2} = 0.75$$

# Example:

## Data Matrix and Dissimilarity Matrix



**Data Matrix**

point	attribute1	attribute2
<i>x1</i>	1	2
<i>x2</i>	3	5
<i>x3</i>	2	0
<i>x4</i>	4	5

**Dissimilarity Matrix**  
(with Euclidean Distance)

	<i>x1</i>	<i>x2</i>	<i>x3</i>	<i>x4</i>
<i>x1</i>	0			
<i>x2</i>	3.61	0		
<i>x3</i>	5.1	5.1	0	
<i>x4</i>	4.24	1	5.39	0

# Distance on Numeric Data: Minkowski Distance

- *Minkowski distance*: A popular distance measure

$$d(i, j) = \sqrt[h]{|x_{i1} - x_{j1}|^h + |x_{i2} - x_{j2}|^h + \cdots + |x_{ip} - x_{jp}|^h}$$

where  $i = (x_{i1}, x_{i2}, \dots, x_{ip})$  and  $j = (x_{j1}, x_{j2}, \dots, x_{jp})$  are two  $p$ -dimensional data objects, and  $h$  is the order (the distance so defined is also called L- $h$  norm)

- Properties
  - $d(i, j) > 0$  if  $i \neq j$ , and  $d(i, i) = 0$  (Positive definiteness)
  - $d(i, j) = d(j, i)$  (Symmetry)
  - $d(i, j) \leq d(i, k) + d(k, j)$  (Triangle Inequality)
- A distance that satisfies these properties is a **metric**

# Special Cases of Minkowski Distance

- $h = 1$ : **Manhattan** (city block,  $L_1$  norm) **distance**
  - E.g., the Hamming distance: the number of bits that are different between two binary vectors

$$d(i, j) = |x_{i1} - x_{j1}| + |x_{i2} - x_{j2}| + \dots + |x_{ip} - x_{jp}|$$

- $h = 2$ : ( $L_2$  norm) **Euclidean** distance

$$d(i, j) = \sqrt{(|x_{i1} - x_{j1}|^2 + |x_{i2} - x_{j2}|^2 + \dots + |x_{ip} - x_{jp}|^2)}$$

- $h \rightarrow \infty$ . **“supremum”** ( $L_{\max}$  norm,  $L_{\infty}$  norm) distance.
  - This is the maximum difference between any component (attribute) of the vectors

$$d(i, j) = \lim_{h \rightarrow \infty} \left( \sum_{f=1}^p |x_{if} - x_{jf}|^h \right)^{\frac{1}{h}} = \max_f |x_{if} - x_{jf}|$$

# Example: Minkowski Distance

point	attribute 1	attribute 2
x1	1	2
x2	3	5
x3	2	0
x4	4	5

## Manhattan ( $L_1$ )

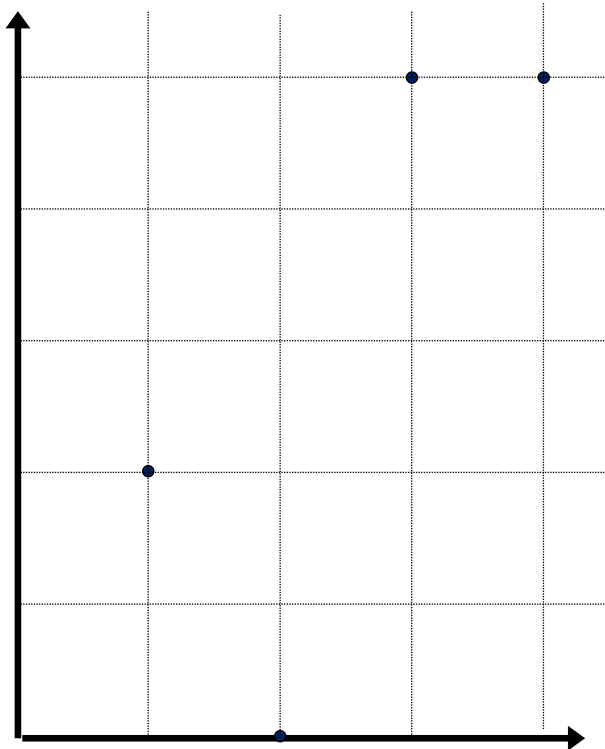
L	x1	x2	x3	x4
x1				
x2				
x3				
x4				

## Euclidean ( $L_2$ )

L2	x1	x2	x3	x4
x1	0			
x2	3.61	0		
x3	2.24	5.1	0	
x4	4.24	1	5.39	0

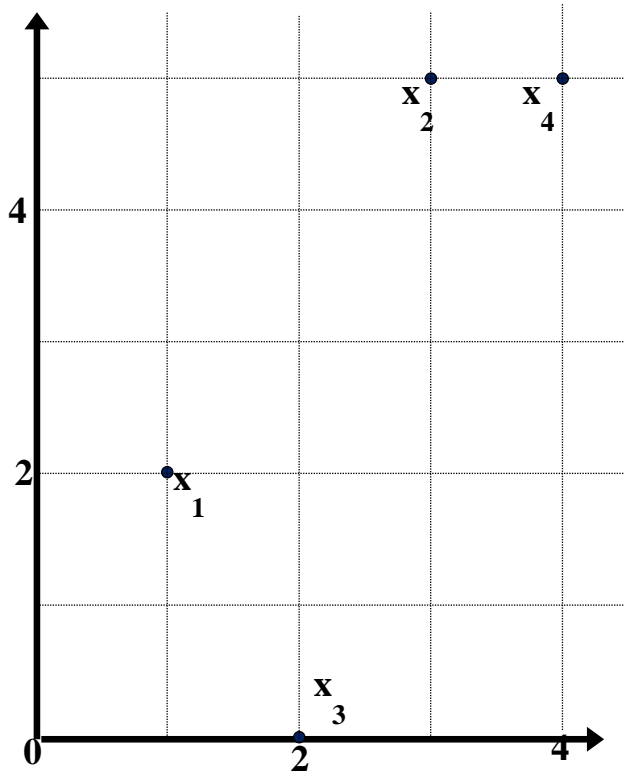
## Supremum

$L_\infty$	x1	x2	x3	x4
x1				
x2				
x3				
x4				



# Example: Minkowski Distance

point	attribute 1	attribute 2
x1	1	2
x2	3	5
x3	2	0
x4	4	5



## Manhattan ( $L_1$ )

L	x1	x2	x3	x4
x1	0			
x2	5	0		
x3	3	6	0	
x4	6	1	7	0

## Euclidean ( $L_2$ )

L2	x1	x2	x3	x4
x1	0			
x2	3.61	0		
x3	2.24	5.1	0	
x4	4.24	1	5.39	0

## Supremum

$L_\infty$	x1	x2	x3	x4
x1	0			
x2	3	0		
x3	2	5	0	
x4	3	1	5	0



# Distance between data

## Comparison between Ordinal Attributes:

### 1. Questions:

1. The grade of example have 5 levels such as A,B,C,D,E, how to judge the grade of two students in 5 courses
2. There are  $\sum_{i=1}^N x_i$  people participate in the election, and there are 20 juries, how to give the final results by integrating the results of these 20 juries?

### 2. Way Out:

1. Convert the result of level into corresponding number
2. Convert all different attributes which have different levels into  $[0,1]$
3. Use the way to calculate the distance after converting all ordinal attributes to numeric attributes

# Distance between data

## Ordinal Attributes: Complex Examples

1. In the given table, the three attributes is nominal, ordinal and numeric attribute, and we need to calculate the distance
2. Problem: we can calculate the distance for each individual attribute, but how to integrate them? Since all attributes have different physical meanings
3. Assuming fair=0, good=0.5, excellent=1

Table 2.2: A sample data table containing attributes of mixed type.

<i>object identifier</i>	<i>test-1 (nominal)</i>	<i>test-2 (ordinal)</i>	<i>test-3 (numeric)</i>
1	code-A	excellent	45
2	code-B	fair	22
3	code-C	good	64
4	code-A	excellent	28

$$Dist(test - 1) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 1 \\ 0 & 1 & 1 & 0 \end{bmatrix}$$

$$Dist(test - 2) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 1.0 & 0.5 & 0.5 & 0 \\ 0 & 1.0 & 0.5 & 0 \end{bmatrix}$$

$$Dist(test - 3) = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0.55 & 1 & 0.86 & 0.40 \\ 0.45 & 1 & 0.86 & 0 \end{bmatrix}$$

4. Convert the distance of each dimension into [0,1], and then calculate the weighted sum of all dimensions. Assuming the weight of each dimension is equivalent, we have  $\mathcal{D} = (Dist(test - 1) + Dist(test - 2) + Dist(test - 3)) / 3$

How to determine the weight of each dimension?

$$\mathcal{D} = \begin{bmatrix} 0 & 0 & 0 & 0 \\ 0.85 & 0.83 & 0.79 & 0.40 \\ 0.65 & 0.71 & 0.86 & 0 \end{bmatrix}$$

# Cosine Similarity

- A **document** can be represented by thousands of attributes, each recording the *frequency* of a particular word (such as keywords) or phrase in the document.

Document	teamcoach		hockey	baseball	soccer	penalty	score	win	loss	season
Document1	5	0	3	0	2	0	0	2	0	0
Document2	3	0	2	0	1	1	0	1	0	1
Document3	0	7	0	2	1	0	0	3	0	0
Document4	0	1	0	0	1	2	2	0	3	0

- Other vector objects: gene features in micro-arrays, ...
- Applications: information retrieval, biologic taxonomy, gene feature mapping, ...
- Cosine measure: If  $d_1$  and  $d_2$  are two vectors (e.g., term-frequency vectors), then

$$\cos(d_1, d_2) = (d_1 \bullet d_2) / ||d_1|| ||d_2|| ,$$

where  $\bullet$  indicates vector dot product,  $||d||$ : the length of vector  $d$

# Example: Cosine Similarity

- $\cos(d_1, d_2) = (d_1 \bullet d_2) / ||d_1|| ||d_2||$ ,  
where  $\bullet$  indicates vector dot product,  $||d||$ : the length of vector  $d$
- Ex: Find the **similarity** between documents 1 and 2.

$$d_1 = (5, 0, 3, 0, 2, 0, 0, 2, 0, 0)$$

$$d_2 = (3, 0, 2, 0, 1, 1, 0, 1, 0, 1)$$

$$d_1 \bullet d_2 = 5*3 + 0*0 + 3*2 + 0*0 + 2*1 + 0*1 + 0*1 + 2*1 + 0*0 + 0*1 = 25$$


$$||d_1|| = (5*5 + 0*0 + 3*3 + 0*0 + 2*2 + 0*0 + 0*0 + 2*2 + 0*0 + 0*0)^{0.5} = (42)^{0.5} \\ = 6.481$$

$$||d_2|| = (3*3 + 0*0 + 2*2 + 0*0 + 1*1 + 1*1 + 0*0 + 1*1 + 0*0 + 1*1)^{0.5} = (17)^{0.5} \\ = 4.12$$

$$\cos(d_1, d_2) = 0.94$$

# Chapter 2: Getting to Know Your Data

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- Data Objects and Attribute Types
- Basic Statistical Descriptions of Data
- An Example of Data Clustering
- Measuring Data Similarity and Dissimilarity
- Summary 

# Summary

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- Data attribute types: nominal, binary, ordinal, interval-scaled, ratio-scaled
- Many types of data sets, e.g., numerical, text, graph, Web, image.
- Gain insight into the data by:
  - Basic statistical data description: central tendency, dispersion, graphical displays
  - Data visualization: map data onto graphical primitives
  - Measure data similarity
- Above steps are the beginning of data preprocessing.
- Many methods have been developed but still an active area of research.

# References

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- W. Cleveland, Visualizing Data, Hobart Press, 1993
- T. Dasu and T. Johnson. Exploratory Data Mining and Data Cleaning. John Wiley, 2003
- U. Fayyad, G. Grinstein, and A. Wierse. Information Visualization in Data Mining and Knowledge Discovery, Morgan Kaufmann, 2001
- L. Kaufman and P. J. Rousseeuw. Finding Groups in Data: an Introduction to Cluster Analysis. John Wiley & Sons, 1990.
- H. V. Jagadish, et al., Special Issue on Data Reduction Techniques. Bulletin of the Tech. Committee on Data Eng., 20(4), Dec. 1997
- D. A. Keim. Information visualization and visual data mining, IEEE trans. on Visualization and Computer Graphics, 8(1), 2002
- D. Pyle. Data Preparation for Data Mining. Morgan Kaufmann, 1999
- S. Santini and R. Jain, "Similarity measures", IEEE Trans. on Pattern Analysis and Machine Intelligence, 21(9), 1999
- E. R. Tufte. The Visual Display of Quantitative Information, 2nd ed., Graphics Press, 2001
- C. Yu , et al., Visual data mining of multimedia data for social and behavioral studies, Information Visualization, 8(1), 2009