(1) Pt. fc. g. R2-R, g(x,y) = x3+ 3xy2-15x-22y ri pet.

a) 24(a), H(2)(a), d22(a)

 $\Delta t(y) = (0^{3}0)$ * $\Delta t(x^{1}A) = \left(\frac{9x}{9t}(x^{1}A), \frac{9A}{9t}(x^{1}A)\right) = \left(3x_{5} + 3A_{5} - 72\right) e^{-13}$

 $+ H(x)(x^{2}A) = \begin{pmatrix} \frac{3x^{3}}{3x^{5}} & \frac{3A_{3}x}{3x^{5}} \\ \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \end{pmatrix} = \begin{pmatrix} e^{3} & e^{3x} \\ e^{3x} & e^{3x} \end{pmatrix}$ $+ H(x)(x^{2}A) = \begin{pmatrix} \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \\ \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \end{pmatrix} = \begin{pmatrix} e^{3x} & e^{3x} \\ e^{3x} & e^{3x} \end{pmatrix}$ $+ H(x)(x^{2}A) = \begin{pmatrix} \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \\ \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \end{pmatrix} = \begin{pmatrix} e^{3x} & e^{3x} \\ e^{3x} & e^{3x} \end{pmatrix}$ $+ H(x)(x^{2}A) = \begin{pmatrix} \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \\ \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \end{pmatrix} = \begin{pmatrix} e^{3x} & e^{3x} \\ e^{3x} & e^{3x} \end{pmatrix}$ $+ H(x)(x^{2}A) = \begin{pmatrix} \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \\ \frac{9x_{5}}{3x^{5}} & \frac{9A_{3}x}{3x^{5}} \end{pmatrix} = \begin{pmatrix} e^{3x} & e^{3x} \\ e^{3x} & e^{3x} \end{pmatrix}$

 $H(\xi)(g) = \begin{pmatrix} -e & -75 \\ -75 & -e \end{pmatrix}$

" 95\$ (x28) (112/112) = 35\$ (x18) · 11 5 + 35\$ (x18) · 115 +5 35\$ (x28) 117

= ex. no + ex. no + vsh. nons

(= diferentiala de

 $954(9)(n^{3/113/2} - 15n^{7} - 15n^{7} - 75n^{7}$

ordinal 2)

=-12 (U2+ U2+ U1U2)

6) matura pet. a a [pet. minim pet. Ba Lz=Rzz Dz=/Rzz hzz -.. Dm=det

hzz hzz (H18/a)

Lz determinantii mateicei hersione

+ Daca de (a) este positivo definità =) a pet de minim local megativo definità =) a pet de marsim local indefinità => a pet sa

*
$$\alpha$$
 e pund cutic $(\nabla f(\alpha) = (0_10))$.
 $\Delta_{\lambda} = -12 - 6$ = $144-3670$ = 0 $\Delta^2 f(\alpha)$ megative definità = 0 $\Delta^2 f(\alpha)$ maxim lacal.

3 Det. punctèle vilice si punctèle de extrem local (specificandu-le tipul) pt. sumatoaccele funcții.

a) 4, R3+R, 4(x,y,2)=2x2-xy+2x2-y+y3+22.

(P2) bautam punctele cubice. Ele sunt solutile ecuative

$$\begin{cases} x + 3 = 0 = 3 - x = 3 \\ -x + 3h_5 = 7 = 3x = 3h_5 - 7 \\ 4x - h + 3y = 0 \end{cases}$$

$$y_1 = \frac{1+7}{12} = \frac{8}{3} = \frac{2}{3} \Rightarrow x_1 = 3 \cdot \frac{1}{9} - 1 = \frac{1}{3} \Rightarrow 21 = \frac{1}{3}$$

Deci punctele cutice sunt $P_{2}(\frac{1}{3},\frac{2}{3},-\frac{1}{3})$ si $P_{2}(-\frac{1}{4},-\frac{1}{2},\frac{1}{4})$

(2)

$$H(x)(\frac{1}{2},\frac{1}{2},\frac{1}{2},-\frac{1}{2}) = \begin{pmatrix} 4 & -1 & 2 \\ -1 & 4 & 0 \\ 2 & 0 & 2 \end{pmatrix}$$

$$\nabla^{3} = \begin{vmatrix} -7 & H \\ -7 \end{vmatrix} = 70^{-7} = 7250$$

=)
$$d^2 = (\frac{1}{3}, \frac{2}{3}, -\frac{1}{3})$$
 positive definità
=) P_2 pot. de minum becal

* Pt. Pa:

$$H(2)\left(-\frac{1}{4}, -\frac{1}{4}, \frac{1}{4}\right) = \begin{pmatrix} -1 & 2 \\ -1 & -3 & 0 \\ 2 & 0 & 2 \end{pmatrix}$$

$$\nabla^3 = \left| \frac{-7}{4} - \frac{-9}{-7} \right| = -75 - 7 = -73 < 0$$

$$q_5 t (x^i h^i x) (n^{2i} \pi^{5i} \pi^{2j}) = \frac{9x_5}{95t} (x^i h^i x) \cdot \pi_5^7 + \frac{9h_5}{95t} (-) \cdot \pi_5^5 + \frac{9x_5}{95t} (-) \cdot \pi_5$$

$$+5\frac{3\times34}{350}(-)\pi^{2}\pi^{5}+5\frac{9\times95}{350}(-)\pi^{2}\pi^{3}+5\frac{3^{3}95}{350}(-)\pi^{5}\pi^{9}$$

$$q_5 \xi \left(-\frac{1}{7}, -\frac{7}{7}, \frac{1}{7}\right) \left(0, 7, 0\right) = -970$$

$$q_5 \xi \left(-\frac{1}{7}, -\frac{7}{7}, \frac{1}{7}\right) \left(7, 0, 0\right) = 4.20$$

- 10/2/2

b)
$$y_1, y_2 = y_1$$
, $y_1 = (0,0) \Rightarrow (4x^2 - 4x^2 + 4y^2) = (0,0) \Rightarrow (2x^2 - 4x^2) = 0 \Rightarrow (2x^2 - 4x^2) = 0 \Rightarrow (2x^2 - 4x^2) = 0 \Rightarrow (2x^2 - 4x^2) \Rightarrow ($

d²q (1,0) (u1, u2) = 8 u2 20 => mu e poz. def. => mu putem stabili

\$(2,0) = -1

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 $4(x^{2}) = x_{1} + \lambda_{1} - 3x_{5} = x_{1} - 3x_{5} + \lambda + \lambda_{1} - \lambda = (x_{5} - 1) + \lambda_{1} - \lambda = 5$

=) (1,0) pet de minim.

donaleg ri (-1,0) pet de minim. (re obțin aceleari valori)

3 determinati punctele de extrem conditionat (specificand tipul la) ni valarile extreme ale fe. & relative la multimera s'indicata (stiend ca e compacta):

7. 15-3 15, 4(x,3) = (1-x)(1-3), Q= {(x,3) e 162/ x3+3=13

fant.] T.W. & marginita ni voi atinge marginile

Ton folosi d'étoda d'ultiplicatorila lui hagrange.

1) Tie F(x,y)=x2+y2-1

**

thunci S= {(x,y) ∈ R2 | F(xy) = 0}.

2) Considerarm to. $L(x,y,\lambda) = \varphi(x,y) + \lambda \cdot F(x,y)$ $L(x,y) = \varphi(x,y) + \lambda \cdot F(x,y) = (x-\infty)(x-y) + \lambda(x^2 + y^2 - 1)$

3) Resolvain nistemel $\nabla L(x, y, \lambda) = (0,0,0)$ et a determina puncte cubice.

DL(x,y,1) = (-1+y+21x, -1+x+21y, x2+y2-1) = (0,0,0)

$$\begin{cases} x_{-1} + 2\lambda x = 0 \\ x_{-1} + 2\lambda y = 0 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 0 \\ x_{-1} + 2\lambda y = 0 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 0 \\ x_{-1} + 2\lambda y = 0 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 0 \\ x_{-1} + 2\lambda y = 0 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 0 \\ x_{-1} + 2\lambda y = 0 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 0 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 0 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_{-1} - 2\lambda x = 1 \\ x_{-1} - 2\lambda x = 1 \end{cases} = \begin{cases} x_$$

Determinati valaile extreme ale urmatoarela funcții relative la multimea 3 indicată:

a) f. R3 -> R, f(x,y,2) = x+2y+3z, S= {(x,y,2) eR3/x2+y2+22=1}

4 cont., 5 compactà ™ 4 marg. vi ri atinge marginile (pct. de min. vi max. conditionat, relative la 53

\$ Enchisa = > (5= int \$U & \$)

2) in int $\beta = \{(x,y,2) \in \mathbb{R}^3 \mid x^2 + y^2 + x^2 \in \Delta^3\}$ $\nabla \mathcal{L}(x,y,2) = (0,0,0) \iff (2,2,3) = (0,0,0), \text{ impossibil} = 1$ $\forall pd. \text{ whice } \Rightarrow \not\exists \text{ min, max in int } \beta.$

2) pe $f(S=f(x,y,z)\in\mathbb{R}^3\mid x^2+y^2+z^2=1)$ Folozim metoda sultipl. lui Lagrange.

Tre F(x, y, 2) = x2+ y2+ 22-1.

-> & = { (x,y,2) e R3) F(x,y,2) = 0}

For $L(x, y, x, \lambda) = f(x, y, x) + \lambda \cdot F(x, y, x) = x + 2y + 3x + \lambda (x^2 + y^2 + x^2 - x)$

 $\Delta \Gamma(x^{1}, 3^{1}, 5^{1}, 7) = (0,0,0,0) = \int_{0}^{\infty} \frac{x_{5} + \lambda_{5} + 3_{5} - \lambda = 0}{5 + 3\gamma} \frac{x_{5} - \lambda_{5} - 3}{5 + 3\gamma} \frac{x_{5} - \lambda_{5}}{5 + 3$

 $\frac{1}{(n)} \frac{1}{1+n+3} - 1 = 0 \quad) \quad \frac{1}{(n)} \frac{1}{1+n+3} = \frac{1}{2} = \frac{1}$

$$\begin{array}{l} = \frac{1}{\sqrt{14}} \quad y = -\frac{2}{\sqrt{14}} \quad y = -\frac{2$$

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