

Applying ML

Debugging learning algo

- get more training examples
- try smaller set of features (carefully select)
- try getting additional features
- try adding polynomial features
- try decreasing k
- try increasing k

Machine Learning Diagnostic

Evaluating a Hypothesis

Dataset split (70/30)

Training/Test procedure for lin regression

- Learn param θ from training data
- Compute test set error

$$J_{\text{test}}(\theta) = \frac{1}{2n_{\text{test}}} \sum_{i=1}^{n_{\text{test}}} (h_{\theta}(x_{\text{test}}^{(i)}) - y_{\text{test}}^{(i)})^2$$

Procedure for logistic regression

- learn param θ from training data
- Compute error

$$J_{\text{test}}(\theta) = \frac{1}{n_{\text{test}}} \sum_{i=1}^{n_{\text{test}}} [y_{\text{test}}^{(i)} \log h_{\theta}(x_{\text{test}}^{(i)}) + (1 - y_{\text{test}}^{(i)}) \log (1 - h_{\theta}(x_{\text{test}}^{(i)}))]$$

- Misclassification Error (0/1 ME)

$$\text{err}(h_\theta(x), y) = \begin{cases} 1 & \text{if } h_\theta(x) \geq 0.5, y=0 \\ 0 & \text{if } h_\theta(x) < 0.5, y=1 \\ 0 & \text{otherwise} \end{cases} \text{ error}$$

Model Selection Problems

d = degree of polynomial

$$1. d=1 \quad h_\theta(x) = \theta_0 + \theta_1 x \rightarrow \theta^{(1)} \rightarrow J_{\text{train}}(\theta^{(1)})$$

$$2. d=2 \quad h_\theta(x) = \theta_0 + \theta_1 x + \theta_2 x^2 \rightarrow \theta^{(2)} \rightarrow J_{\text{train}}(\theta^{(2)})$$

$$3. d=3 \quad h_\theta(x) = \theta_0 + \theta_1 x + \theta_2 x^2 + \theta_3 x^3 \rightarrow \theta^{(3)} \rightarrow J_{\text{train}}(\theta^{(3)})$$

⋮

$$10. d=10 \quad h_\theta(x) = \theta_0 + \theta_1 x + \dots + \theta_{10} x^{10} \rightarrow \theta^{(10)} \rightarrow J_{\text{train}}(\theta^{(10)})$$

Choose $\theta_0 + \dots + \theta_5 x^5$

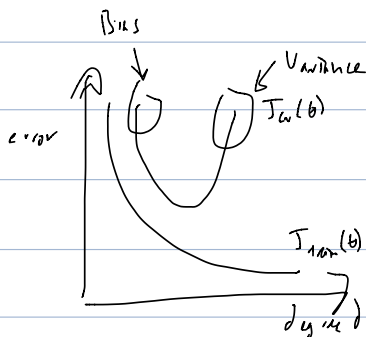
How well generalized? \rightarrow fit to test set

H. or fix?

Split dataset into 3 pieces: training, cross validation (CV), test (60/20/20)

train/validation/test error

Diagnosing Bias vs. Variance



Bias (underfit):

$J_{\text{train}}(\theta)$ high

$J_{\text{cv}}(\theta) \approx J_{\text{train}}(\theta)$

Variance (overfit):

$$J_{\text{train}}(\theta) \downarrow$$

$$J_{\text{cv}}(\theta) \gg J_{\text{train}}(\theta)$$

Regularization and Bias/Variance

(choosing λ)

$$1. \text{ try } \lambda=0 \rightarrow \min_{\theta} J(\theta) \rightarrow \theta^{(1)} \rightarrow J_{\text{cv}}(\theta^{(1)})$$

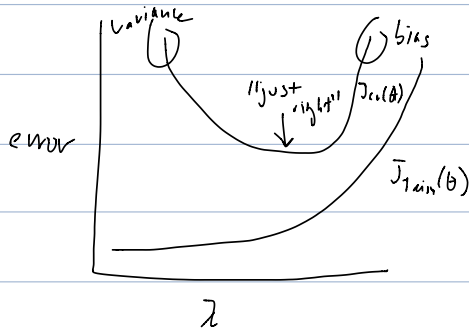
$$2. \text{ try } \lambda=0.01 \rightarrow \min_{\theta} (J\theta) \rightarrow \theta^{(2)} \rightarrow J_{\text{cv}}(\theta^{(2)})$$

$$\lambda=0.02 \longrightarrow \theta^{(3)} \rightarrow J_{\text{cv}}(\theta^{(3)})$$

$$\lambda=0.04$$



$$12. \lambda=0.24 \longrightarrow \theta^{(12)} \rightarrow J_{\text{cv}}(\theta^{(12)})$$



Learning Curves

Deciding What To Do Next

- get more training examples \rightarrow fixes high variance
- try smaller set of features (carefully select) \rightarrow fixes high variance
- try getting additional features \rightarrow fixes high bias

- try adding polynomial features \rightarrow fixes high bias
- try decreasing $\lambda \rightarrow$ fixes high bias
- try increasing $\lambda \rightarrow$ fixes high variance

Spam Classifiers

Error Analysis

$$\text{Precision: } \frac{\text{True pos}}{\text{true pos} + \text{false pos}} = \frac{\text{true positives}}{\text{\# predicted positives}}$$

$y=1$ in 'spam' class

$$\text{Recall: } \frac{\text{true pos}}{\text{true pos} + \text{false neg}} = \frac{\text{true positives}}{\text{\# actual positives}}$$

$$F_1 \text{ Score: } 2 \frac{PR}{P+R}$$

$$P = 0.0872 \quad \sim 14.824$$

$$R = 0.85$$