

1a)

$$\|x - u_1\| = \|x - u_2\|$$

$$\|x\| + \|u_1\| - 2u_1 \cdot x = \|x\| + \|u_2\| - 2u_2 \cdot x$$

$$2(u_1 - u_2) \cdot x + \|u_2\| - \|u_1\| = 0$$

$$(u_1 - u_2) \cdot x + \frac{(\|u_2\| - \|u_1\|)}{2} = 0$$

$$\hat{y}(x) = w^T x + w_0$$

$$\text{with } w^T = u_1 - u_2$$

$$w_0 = \frac{(\|u_2\| - \|u_1\|)}{2} = 0$$

1b)

$$\mu_1 = \mu_2$$

$$\mu_{-1} = \mu_2$$

$$(\mu_1 - \mu_2) \cdot x + \frac{(\|\mu_2\| - \|\mu_1\|)}{2} = 0$$

$$2(\mu_1 - \mu_2) \cdot x + \|\mu_2\| - \|\mu_1\| = 0$$

$$2\mu_1 \cdot x - 2\mu_2 \cdot x + \|\mu_2\| - \|\mu_1\| = 0$$

$$\|\mu_1\| - 2\mu_1 \cdot x = \|\mu_2\| - 2\mu_2 \cdot x$$

$$\|x - \mu_1\| = \|x - \mu_2\|$$

line between  $\mu_1$  &  $\mu_2$   
perpendicular to the  
hyperplane