



3D Modeling

COS 426, Spring 2020

Princeton University

Felix Heide

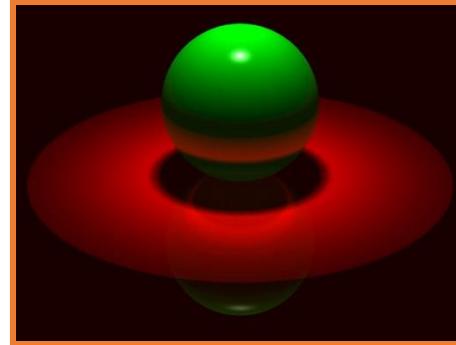


Syllabus

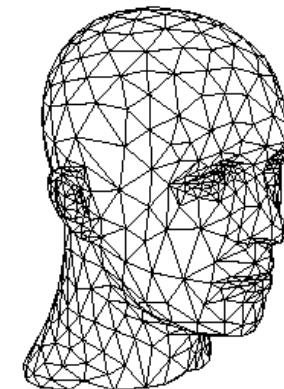
- I. Image processing
- II. Modeling
- III. Rendering
- IV. Animation



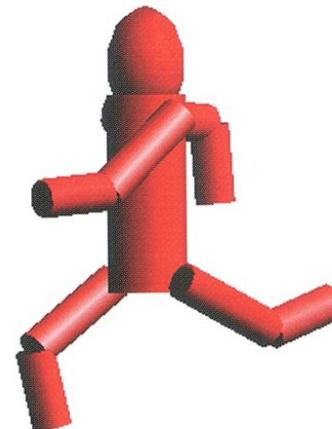
Image Processing
(Rusty Coleman, CS426, Fall99)



Rendering
(Michael Bostock, CS426, Fall99)



Modeling
(Denis Zorin, CalTech)

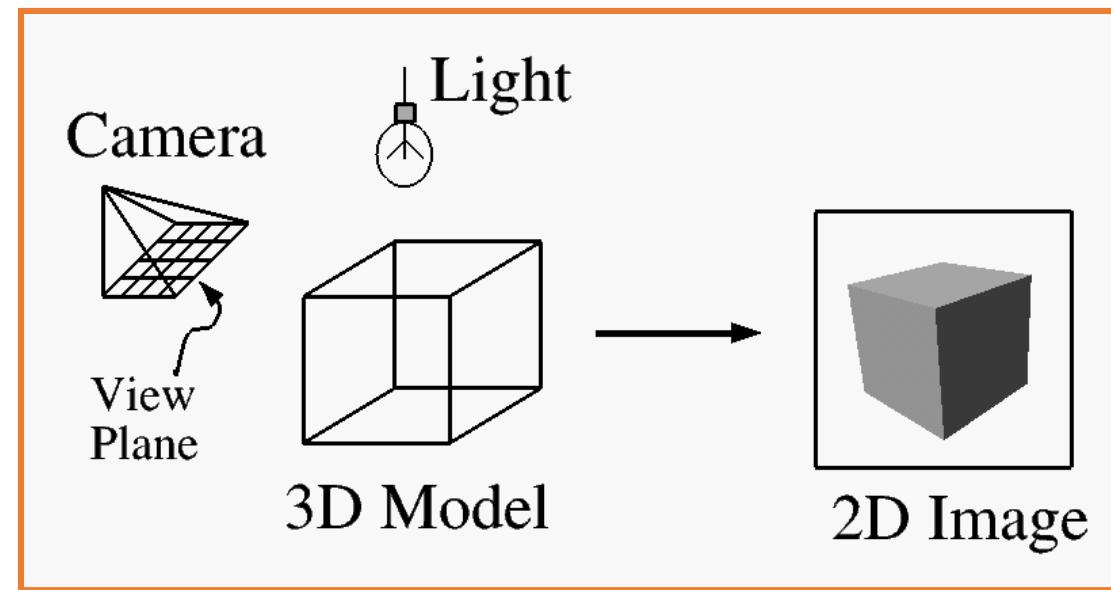


Animation
(Angel, Plate 1)



What is 3D Modeling?

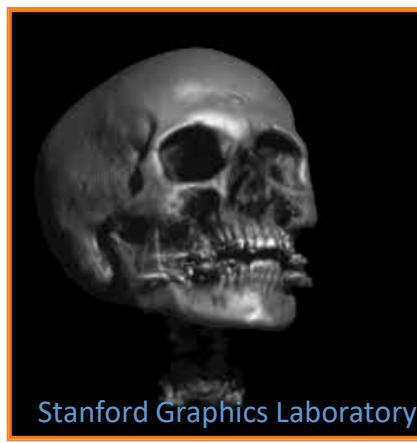
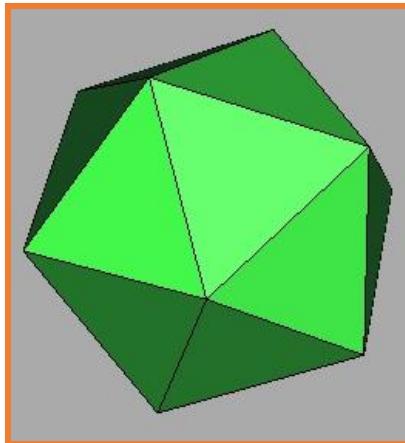
- Topics in computer graphics
 - Imaging = *representing 2D images*
 - Modeling = *representing 3D objects*
 - Rendering = *constructing 2D images from 3D models*
 - Animation = *simulating changes over time*



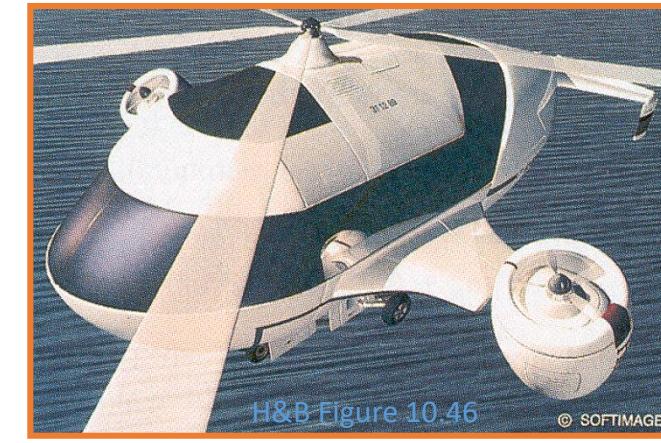


Modeling

- How do we ...
 - Represent 3D objects in a computer?
 - Acquire computer representations of 3D objects?
 - Manipulate computer representations of 3D objects?



Stanford Graphics Laboratory



H&B Figure 10.46

© SOFTIMAGE



Modeling Background

- Scene is usually approximated by 3D primitives
 - Point
 - Vector
 - Line segment
 - Ray
 - Line
 - Plane
 - Polygon



3D Point

- Specifies a location
 - Represented by three coordinates
 - Infinitely small

```
typedef struct {  
    Coordinate x;  
    Coordinate y;  
    Coordinate z;  
} Point;
```

•(x,y,z)

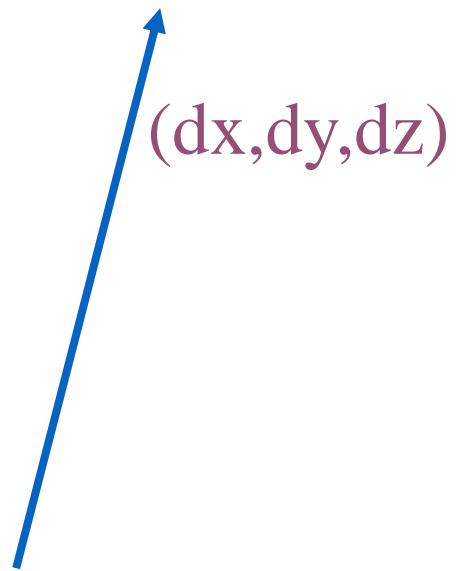




3D Vector

- Specifies a direction and a magnitude
 - Represented by three coordinates
 - Magnitude $\|V\| = \sqrt{dx^2 + dy^2 + dz^2}$
 - Has no location

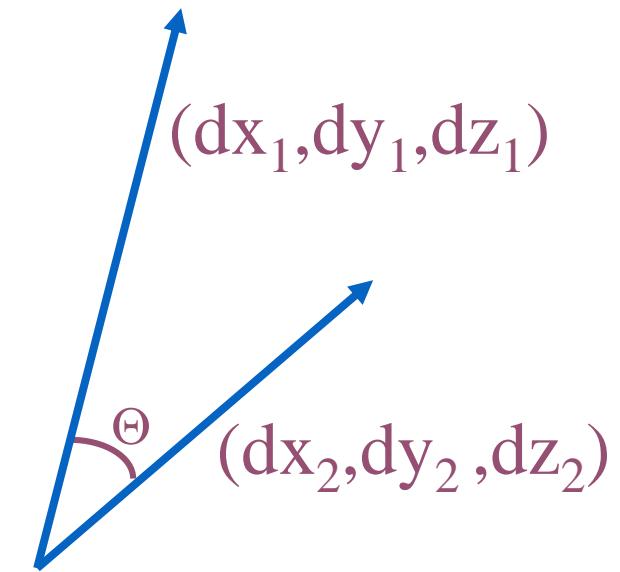
```
typedef struct {  
    Coordinate dx;  
    Coordinate dy;  
    Coordinate dz;  
} Vector;
```





3D Vector

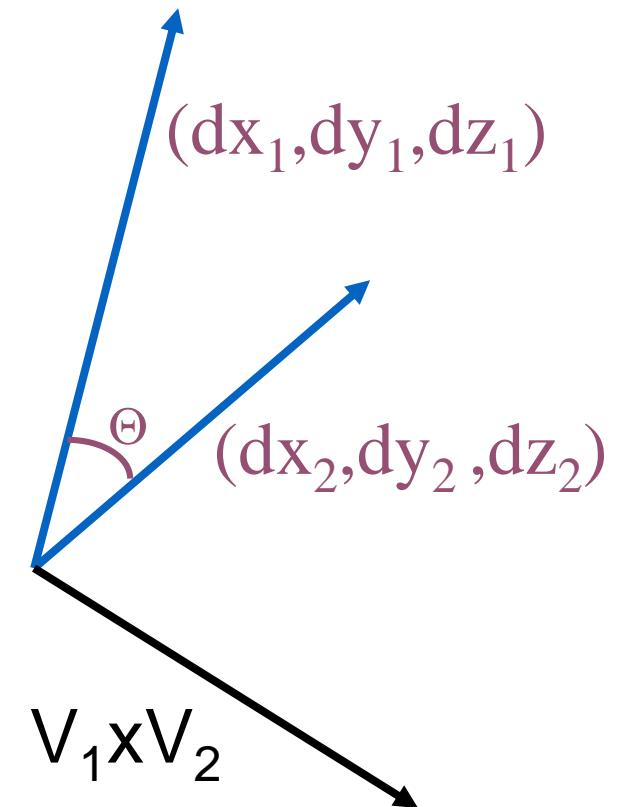
- Dot product of two 3D vectors
 - $\mathbf{V}_1 \cdot \mathbf{V}_2 = \|\mathbf{V}_1\| \|\mathbf{V}_2\| \cos(\Theta)$





3D Vector

- Cross product of two 3D vectors
 - $V_1 \times V_2 =$ vector perpendicular to both V_1 and V_2
 - $\|V_1 \times V_2\| = \|V_1\| \|V_2\| \sin(\Theta)$





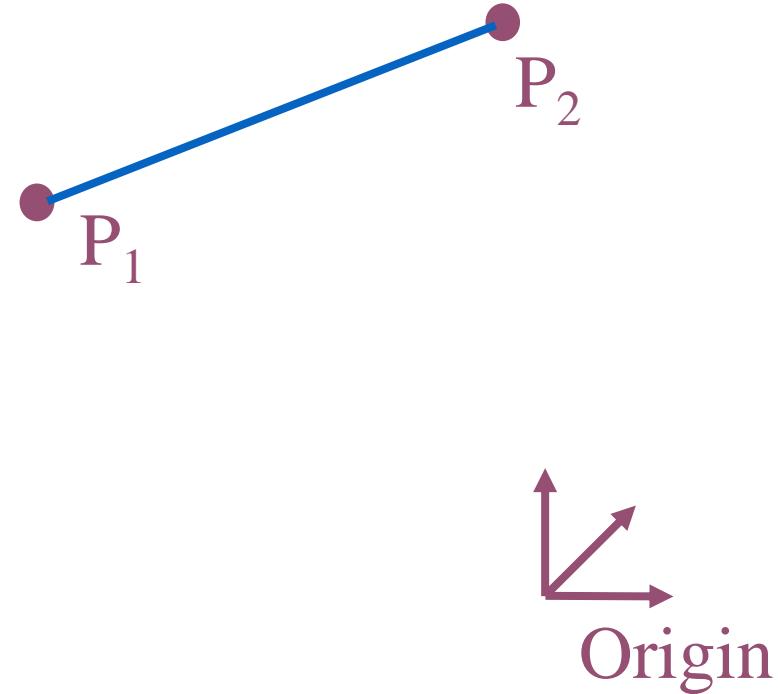
3D Line Segment

- Linear path between two points

- Parametric representation:

- $P = P_1 + t (P_2 - P_1), \quad (0 \leq t \leq 1)$

```
typedef struct {  
    Point P1;  
    Point P2;  
} Segment;
```





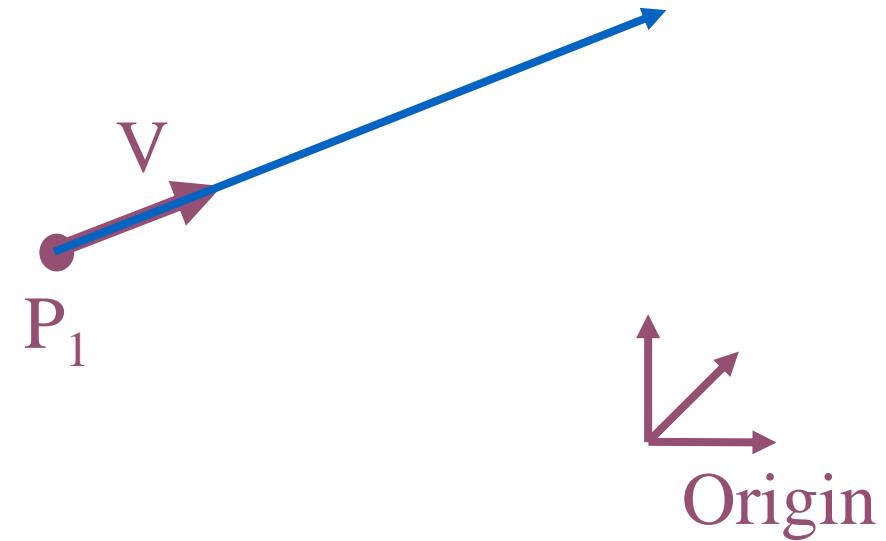
3D Ray

- Line segment with one endpoint at infinity

- Parametric representation:

- $P = P_1 + t V, \quad (0 \leq t < \infty)$

```
typedef struct {
    Point P1;
    Vector V;
} Ray;
```





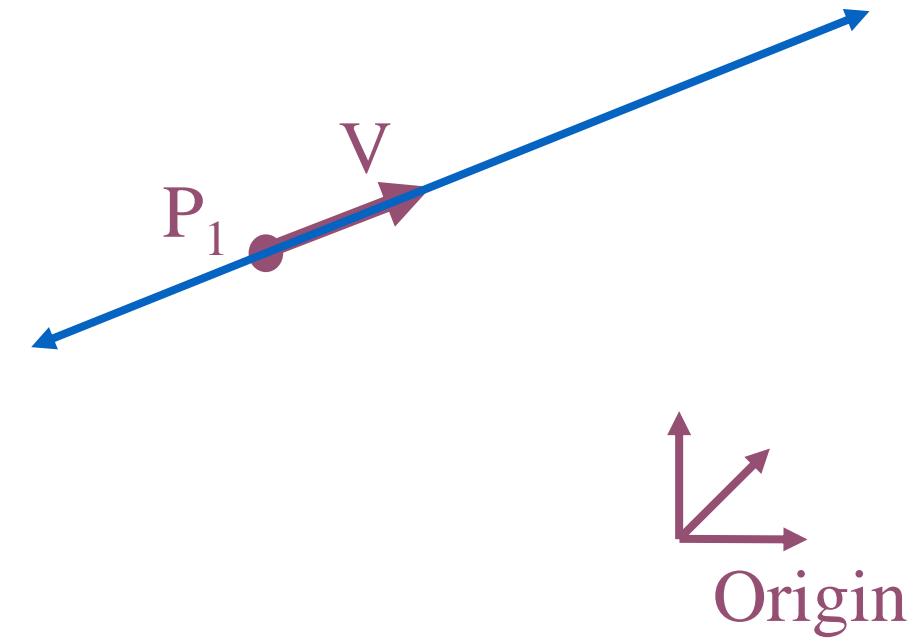
3D Line

- Line segment with both endpoints at infinity

- Parametric representation:

- $P = P_1 + t V, \quad (-\infty < t < \infty)$

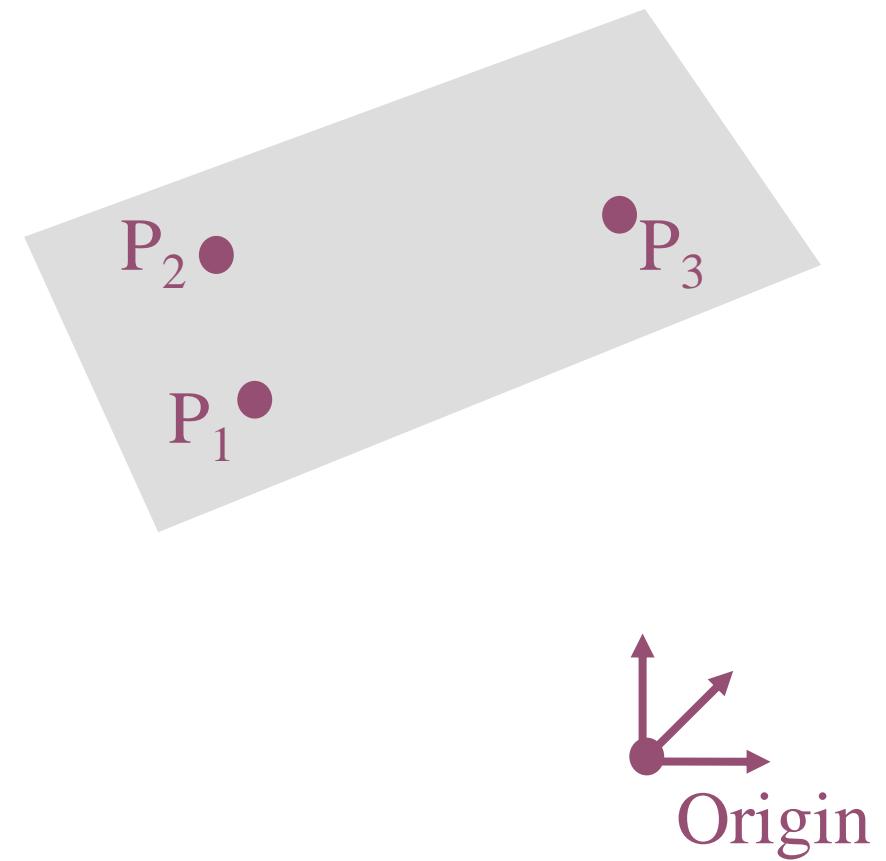
```
typedef struct {  
    Point P1;  
    Vector V;  
} Line;
```





3D Plane

- A linear combination of three points





3D Plane

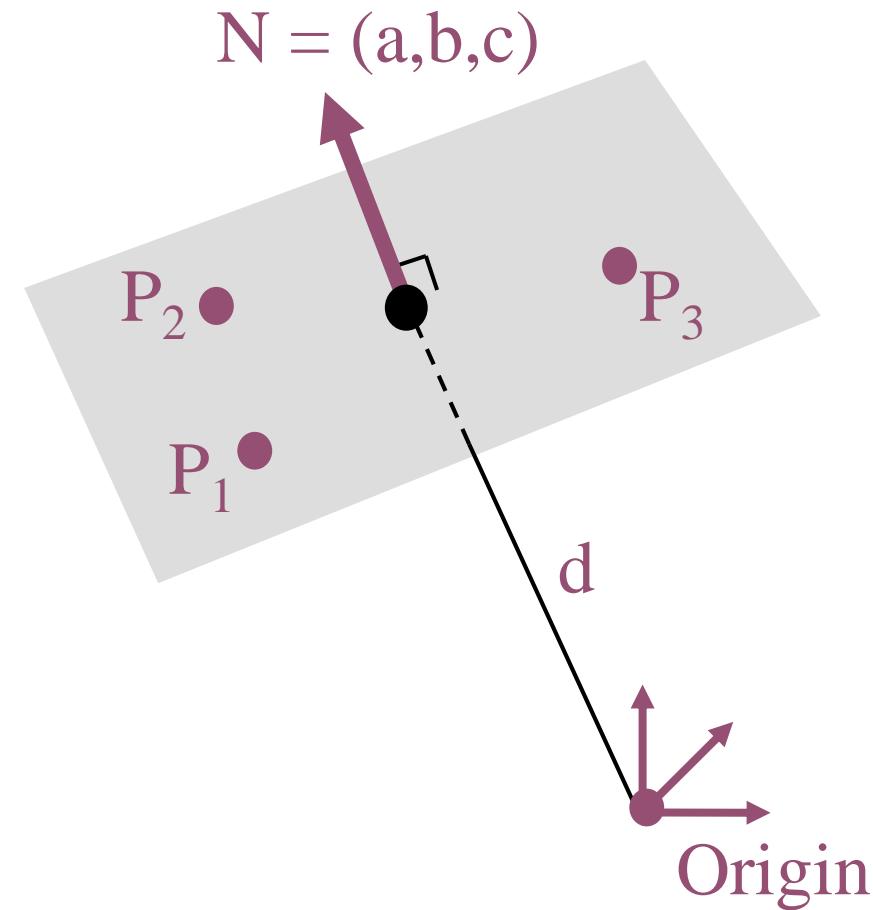
- A linear combination of three points

- Implicit representation:

- $\mathbf{P} \cdot \mathbf{N} - d = 0$, or
 - $ax + by + cz + d = 0$

```
typedef struct {  
    Vector N;  
    Distance d;  
} Plane;
```

- \mathbf{N} is the plane “normal”
 - Unit-length vector
 - Perpendicular to plane

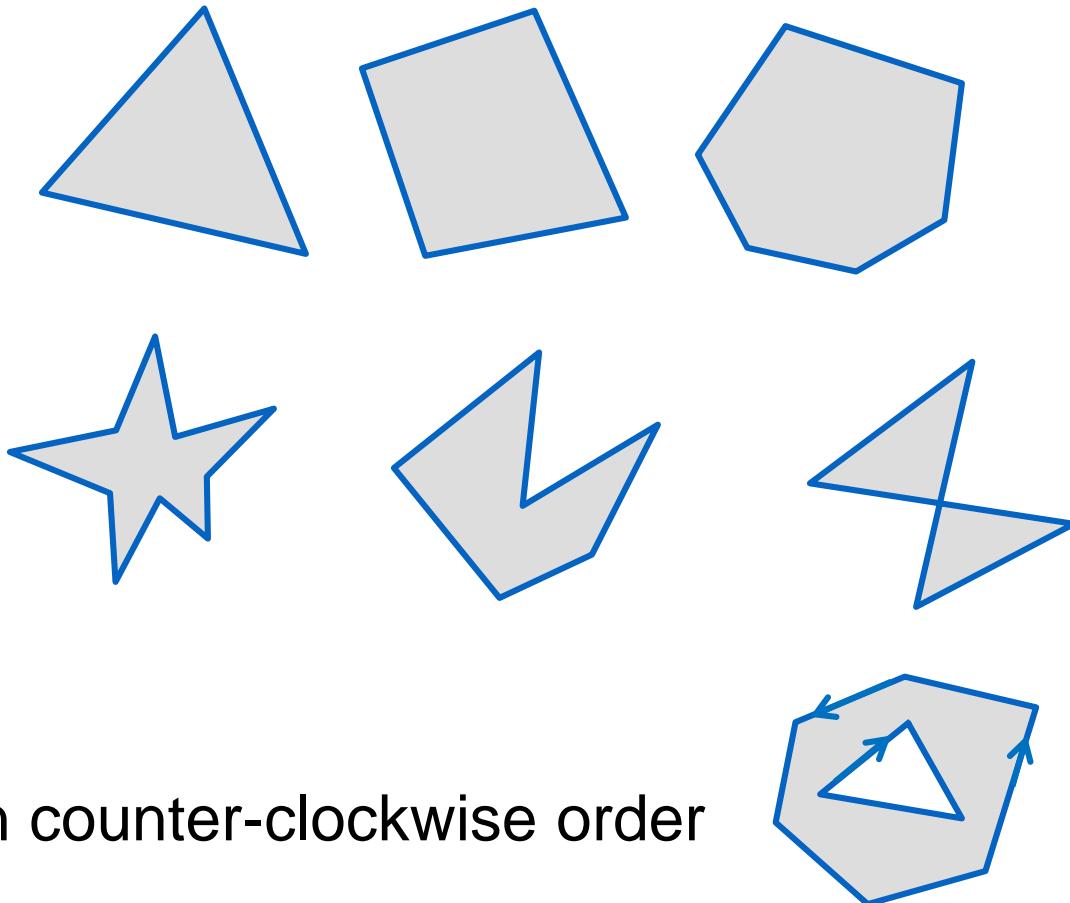




3D Polygon

- Set of points “inside” a sequence of coplanar points

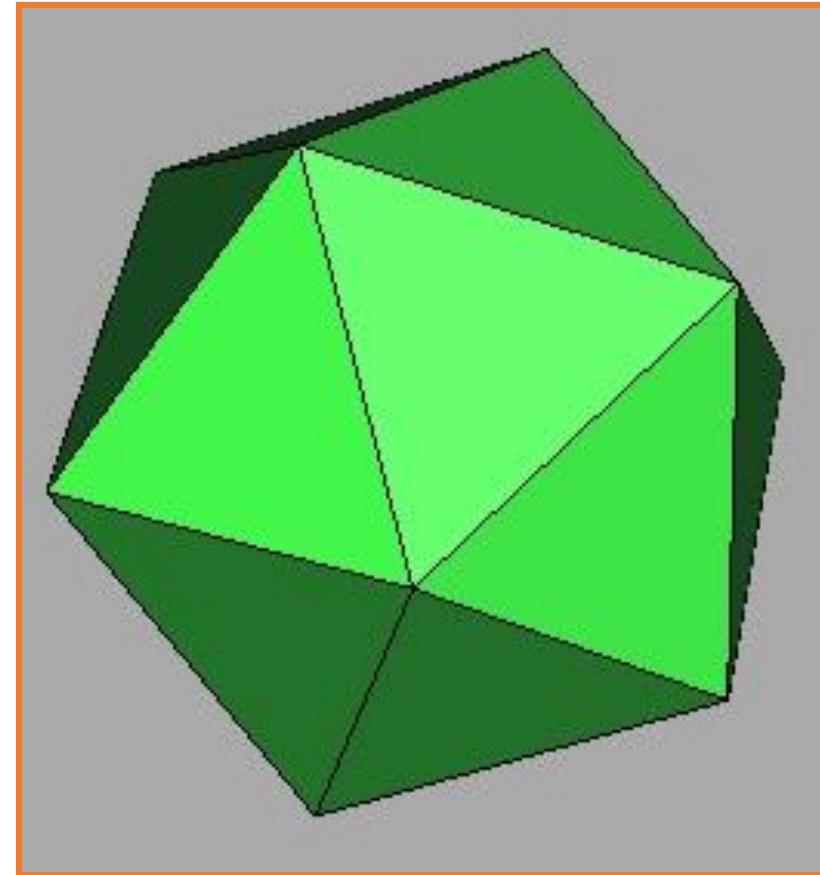
```
typedef struct {  
    Point *points;  
    int npoints;  
} Polygon;
```



Points are in counter-clockwise order



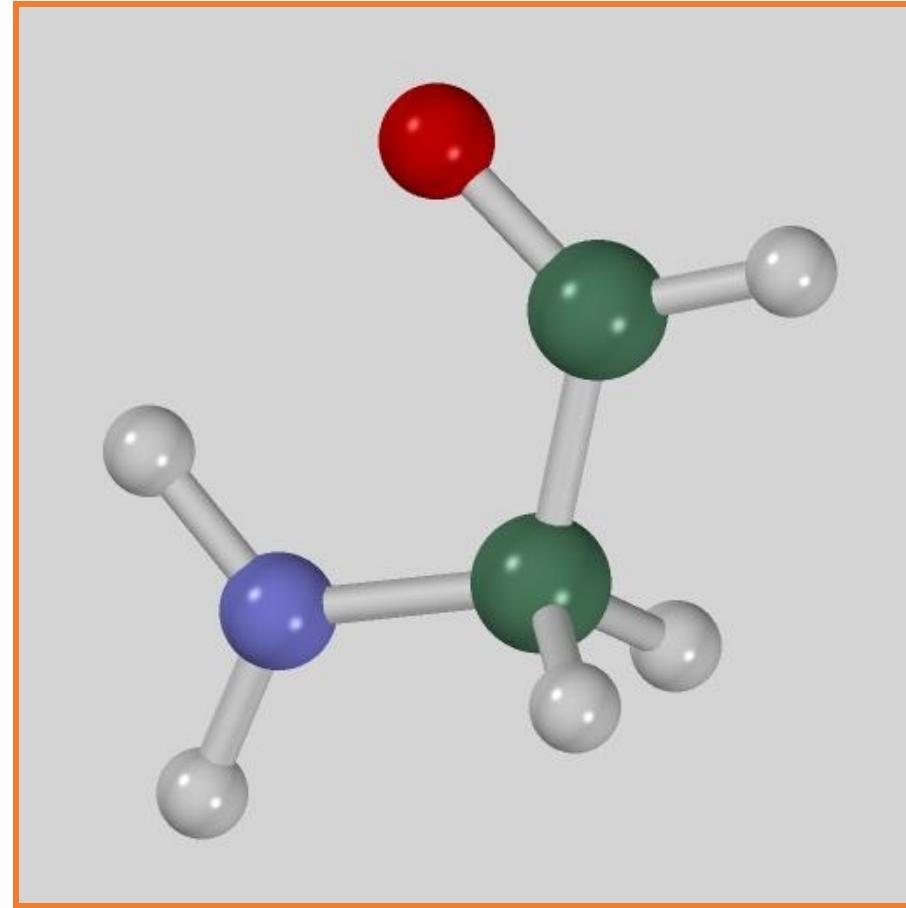
3D Object Representations



How can this object be represented in a computer?



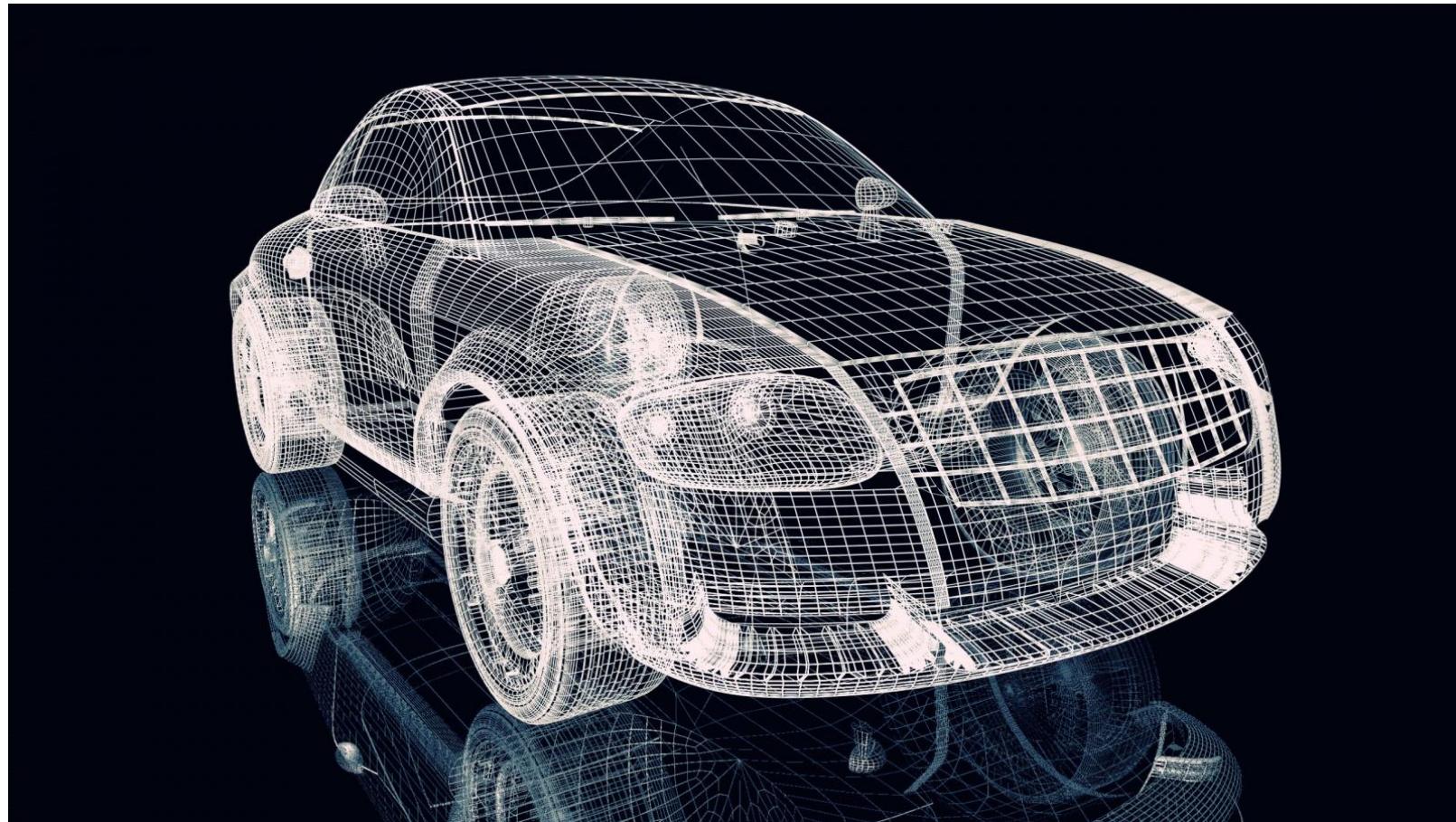
3D Object Representations



How about this one?



3D Object Representations

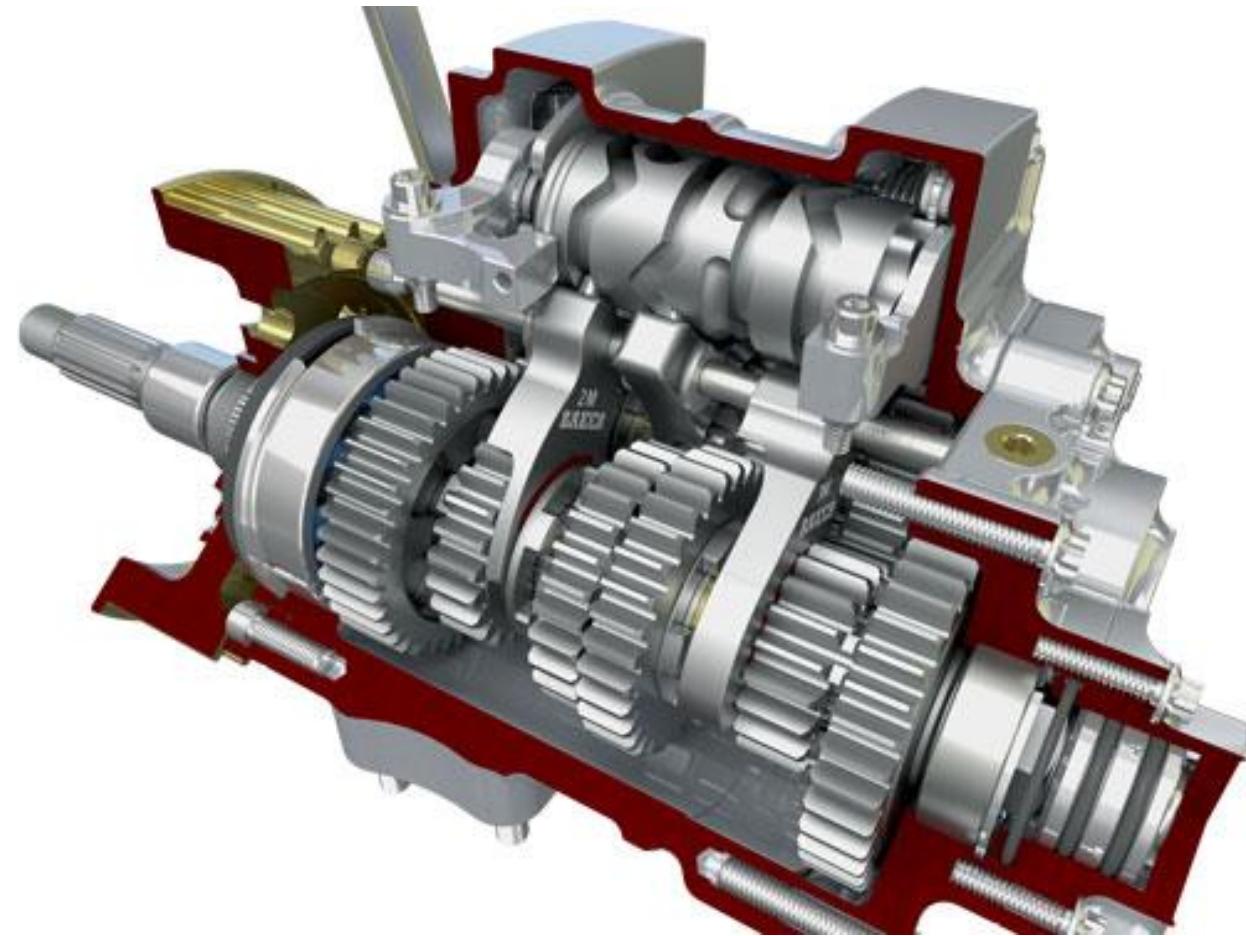


This one?

Wallpapersonly.net



3D Object Representations

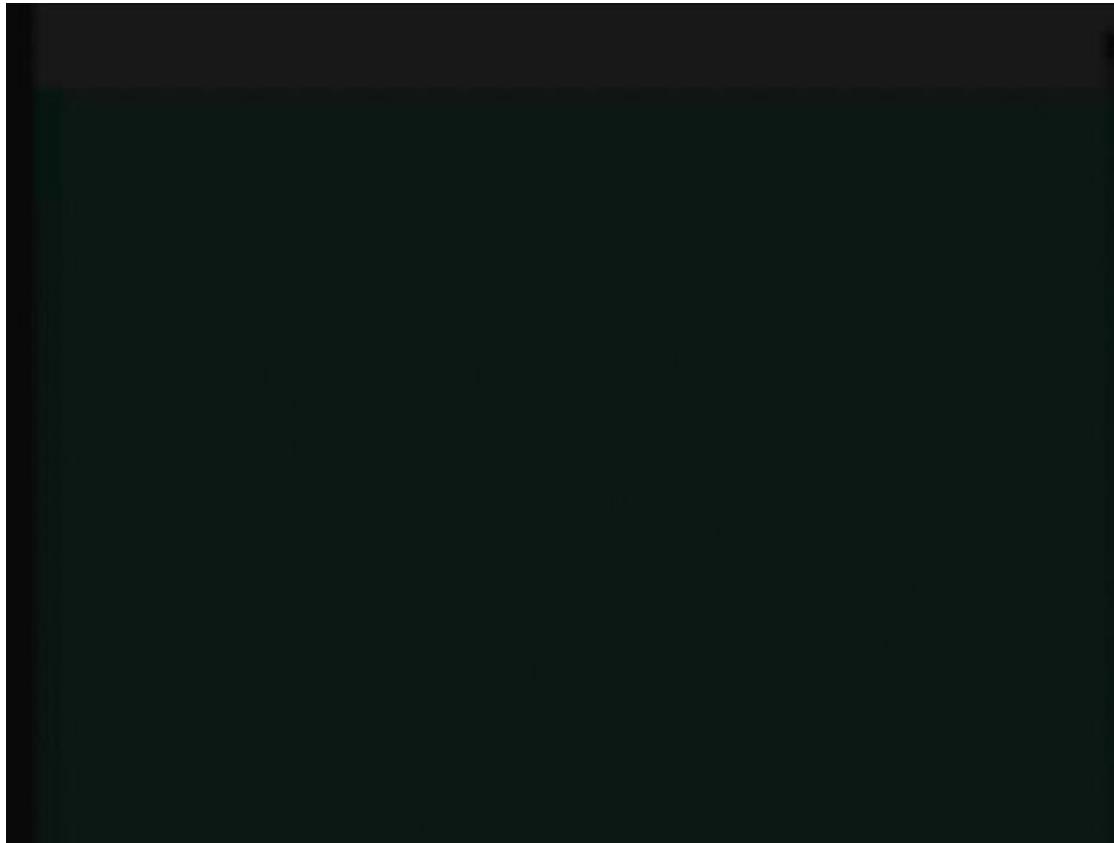


This one?

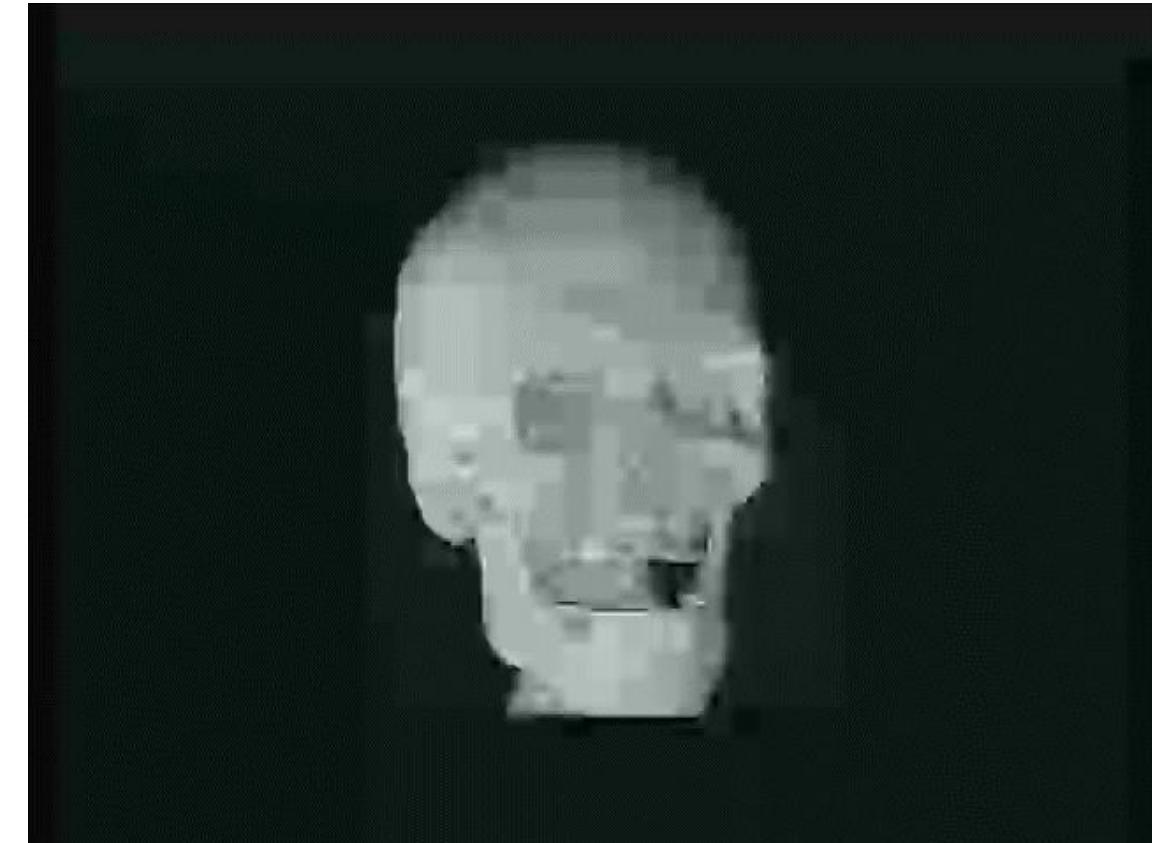
Solidworks



3D Object Representations

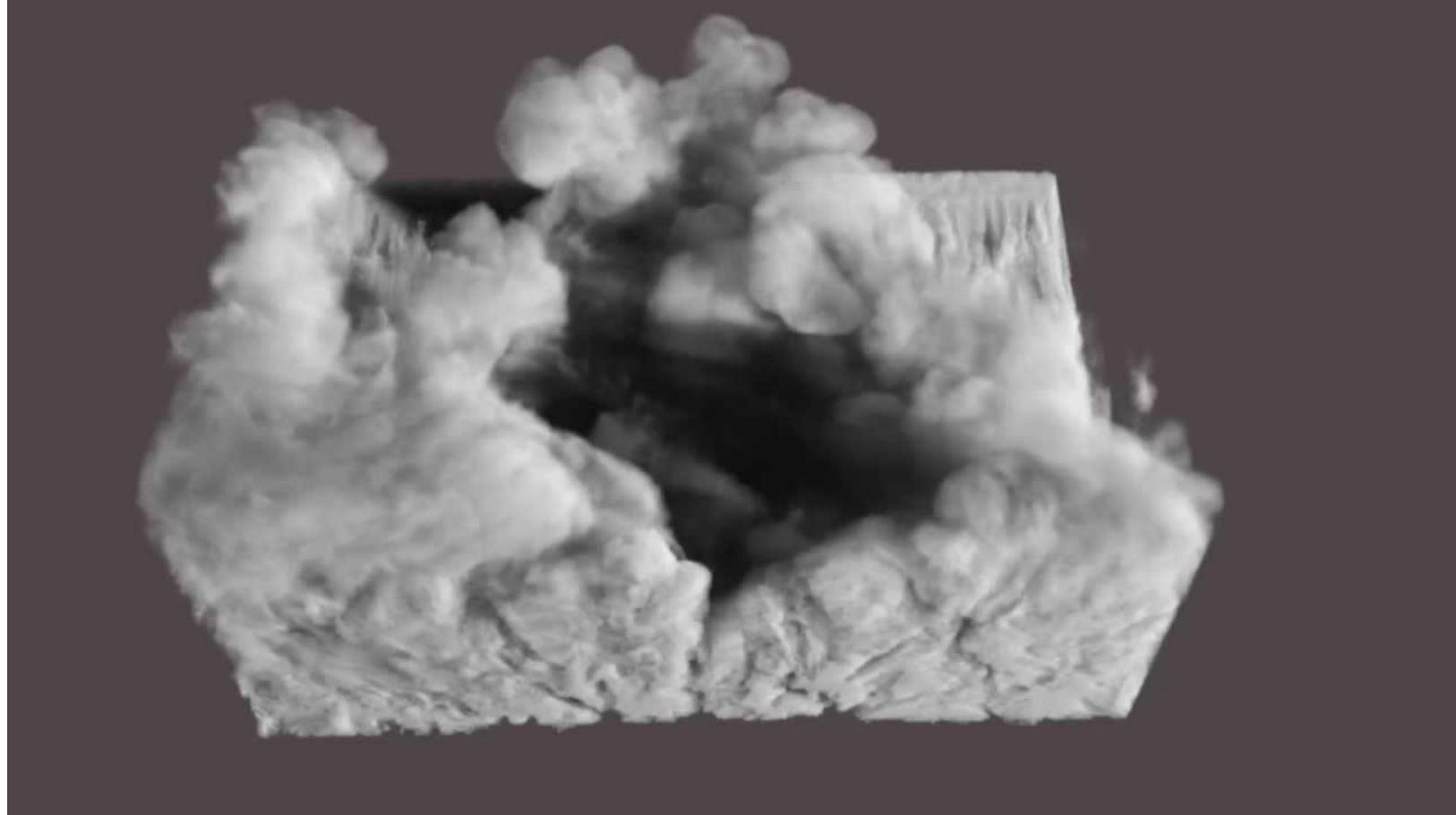


This one?



The visible human

3D Object Representations



This one?

FumeFx



3D Object Representations

- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific



Equivalence of Representations

- Thesis:
 - Each representation has enough expressive power to model the shape of any geometric object
 - It is possible to perform all geometric operations with any fundamental representation
- Analogous to Turing-equivalence
 - Computers and programming languages are Turing-equivalent, but each has its benefits...



Why Different Representations?

Efficiency for different tasks

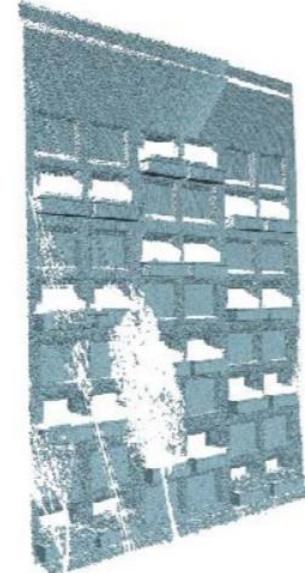
- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation

Data structures determine algorithms

Why Different Representations?

Efficiency for different tasks

- Acquisition
 - Range Scanning
- Rendering
- Analysis
- Manipulation
- Animation



Live Body Scan
Data acquired in 0.01 seconds





Why Different Representations?

Efficiency for different tasks

- Acquisition
 - Computer Vision
- Rendering
- Analysis
- Manipulation
- Animation



Indiana
University



USC Institute for
Creative Technologies

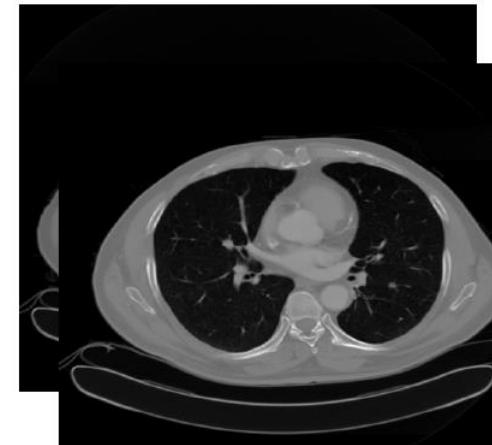


USC

Why Different Representations?

Efficiency for different tasks

- Acquisition
 - Tomography
- Rendering
- Analysis
- Manipulation
- Animation



DGP course notes, Technion

Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
 - Intersection
- Analysis
- Manipulation
- Animation



Autodesk

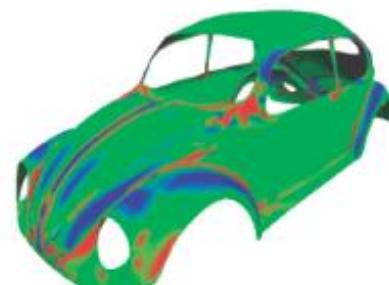


Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Curvature, smoothness
- Manipulation
- Animation

Analysis of surface quality



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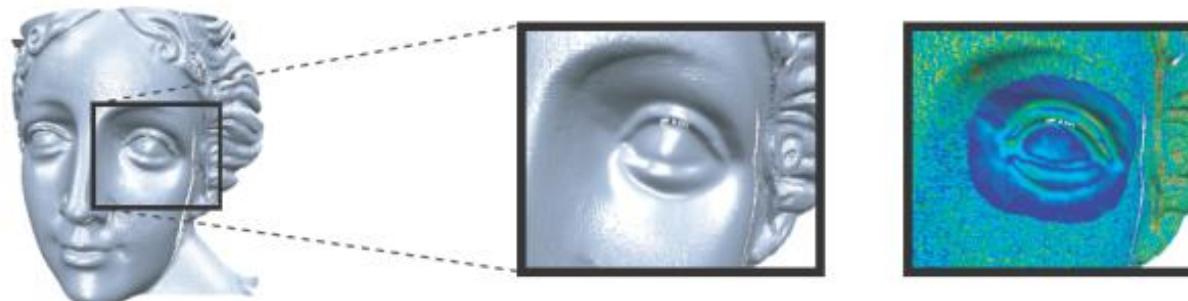


Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Fairing
- Manipulation
- Animation

Surface smoothing for noise removal

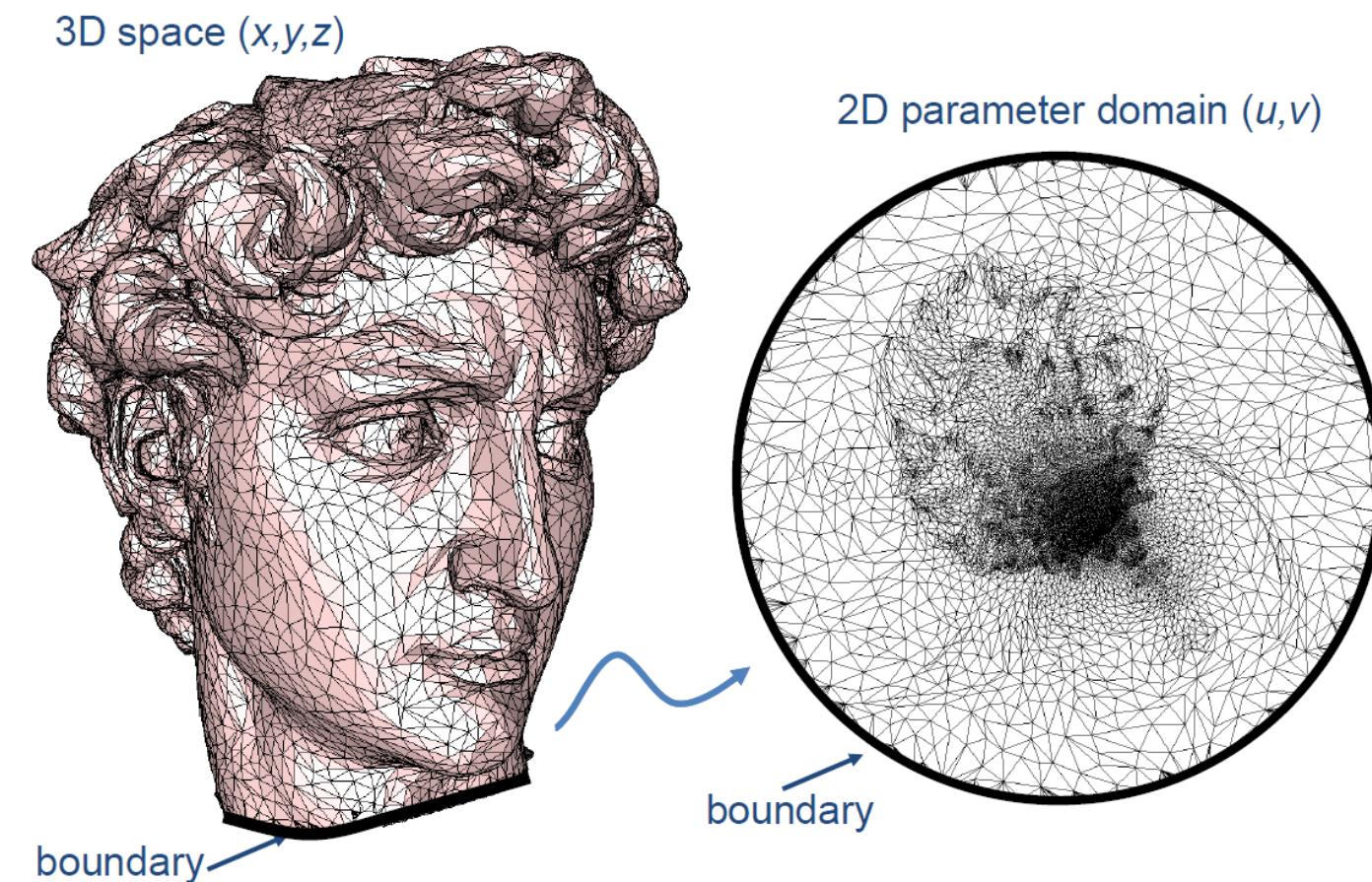


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Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Parametrization
- Manipulation
- Animation





Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Texture mapping
- Manipulation
- Animation



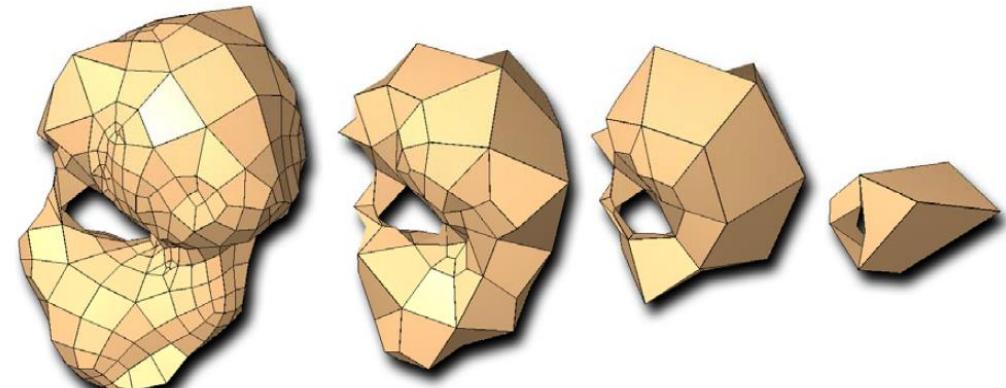
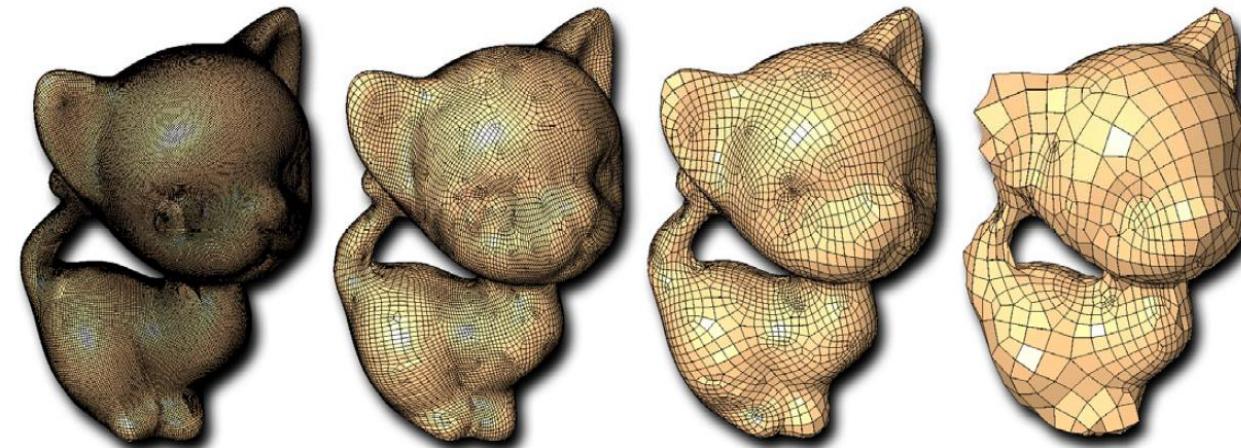
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Why Different Representations?

Efficiency for different tasks

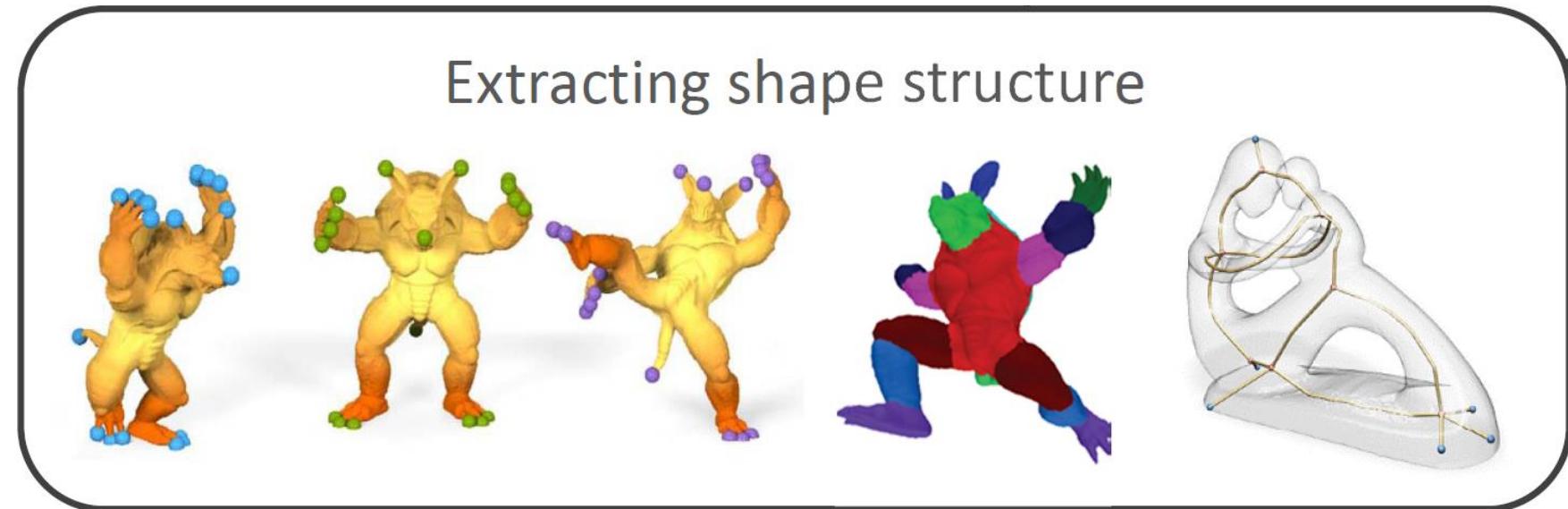
- Acquisition
- Rendering
- Analysis
 - Reduction
- Manipulation
- Animation



Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Structure
- Manipulation
- Animation

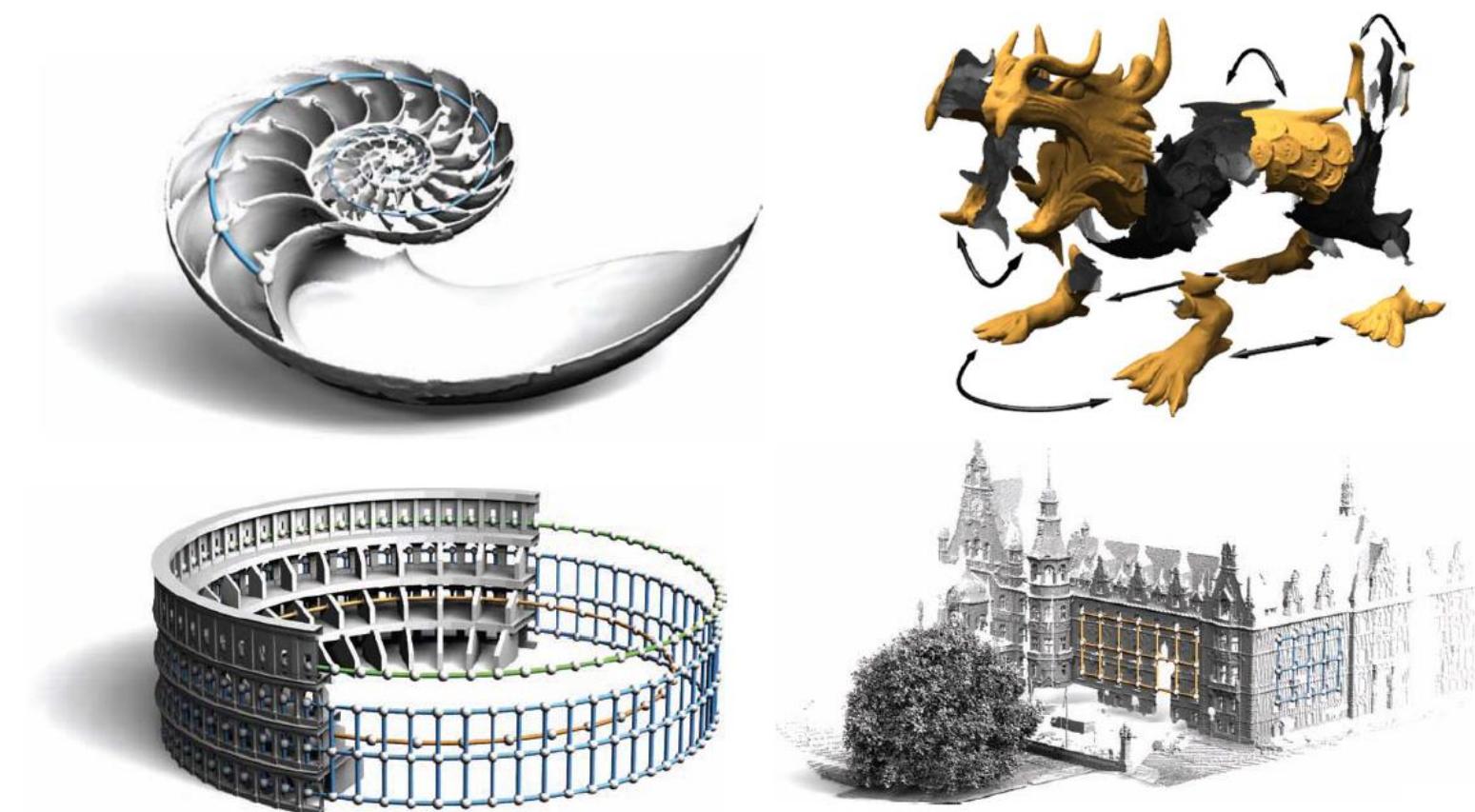


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Why Different Representations?

Efficiency for different tasks

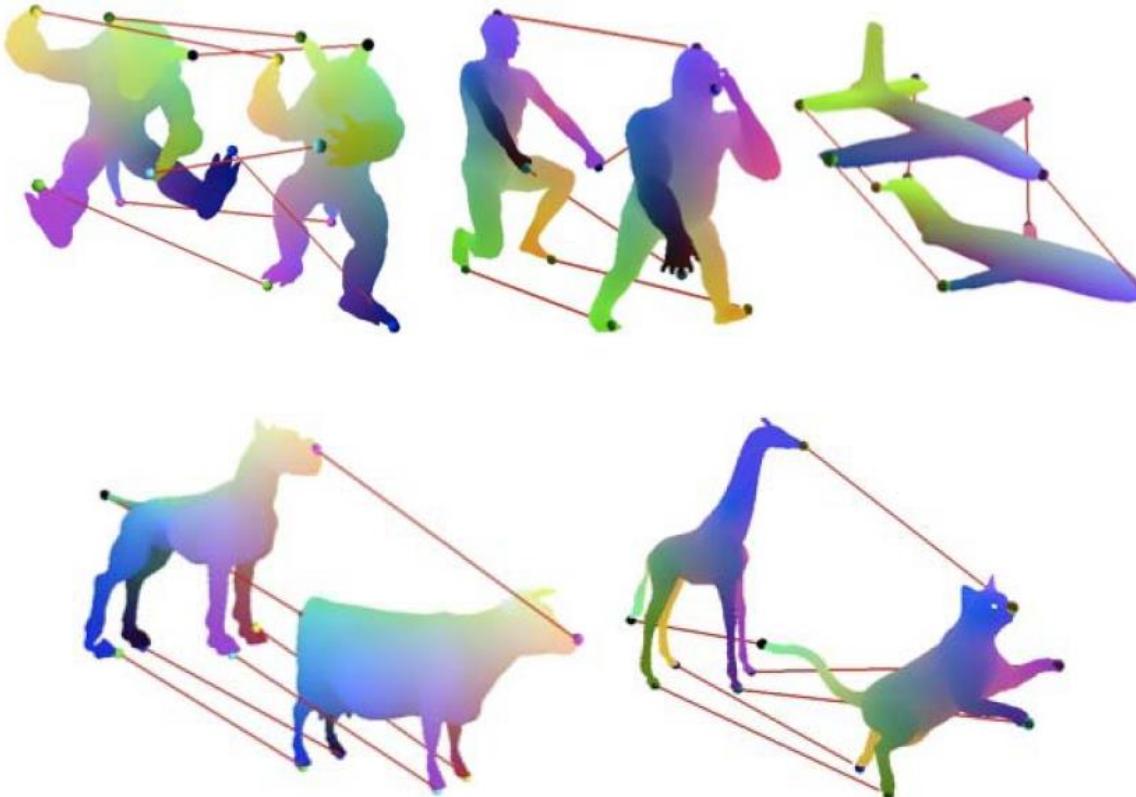
- Acquisition
- Rendering
- Analysis
 - Symmetry detection
- Manipulation
- Animation



Why Different Representations?

Efficiency for different tasks

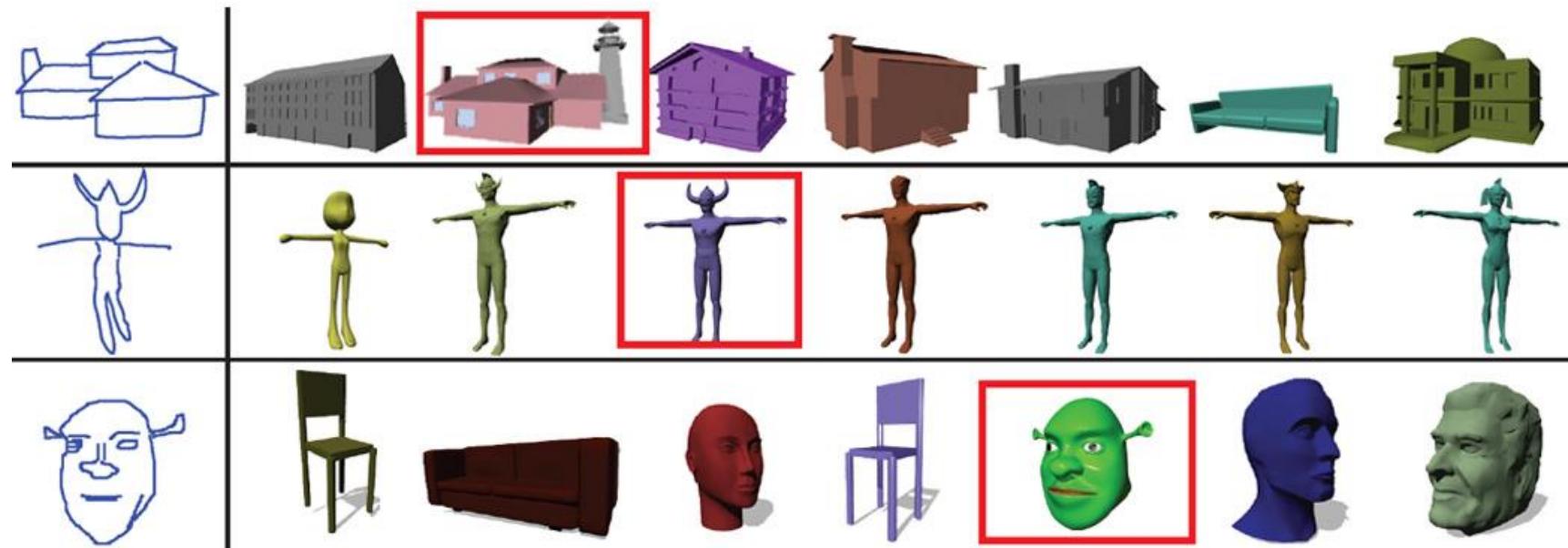
- Acquisition
- Rendering
- Analysis
 - Correspondence
- Manipulation
- Animation



Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
 - Shape retrieval
- Manipulation
- Animation



Shao et al. 2011

Why Different Representations?

Efficiency for different tasks

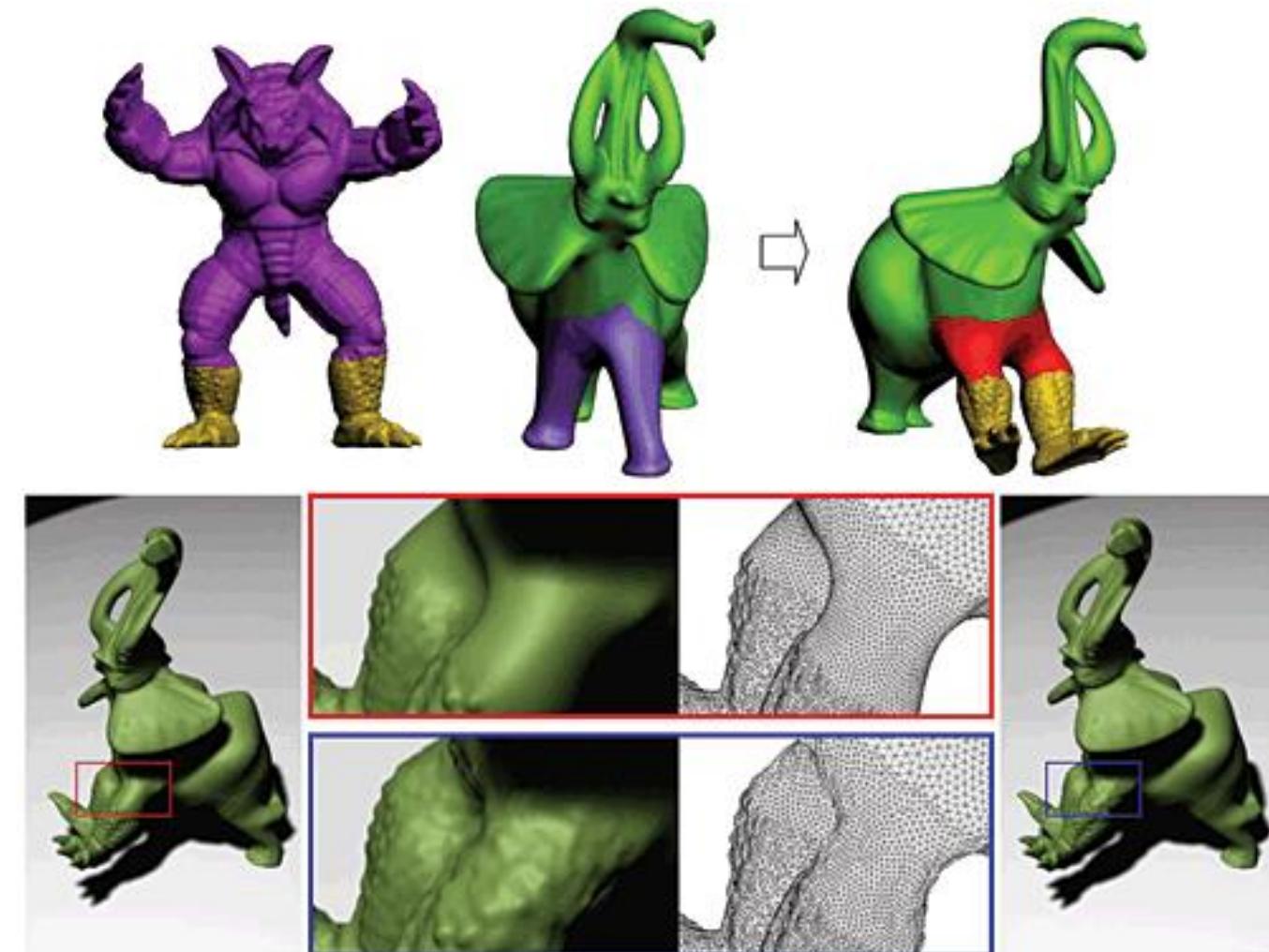
- Acquisition
- Rendering
- Analysis
 - Segmentation
- Manipulation
- Animation



Why Different Representations?

Efficiency for different tasks

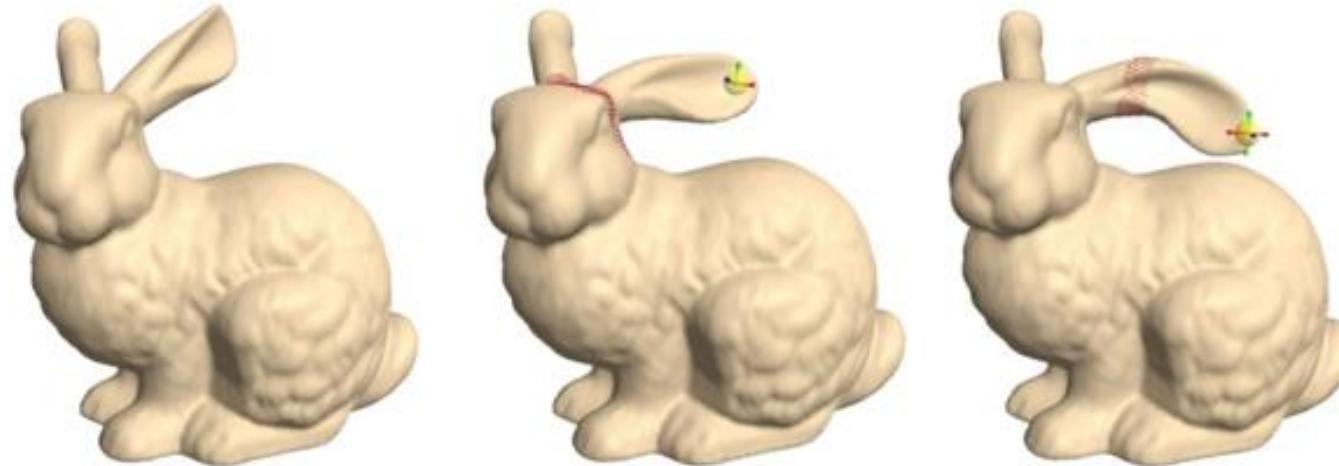
- Acquisition
- Rendering
- Analysis
 - Composition
- Manipulation
- Animation



Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
 - Deformation
- Animation



IGL



Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
 - Deformation
- Animation

Freeform and multiresolution modeling



DGP course notes, Technion



Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
 - Control
- Animation



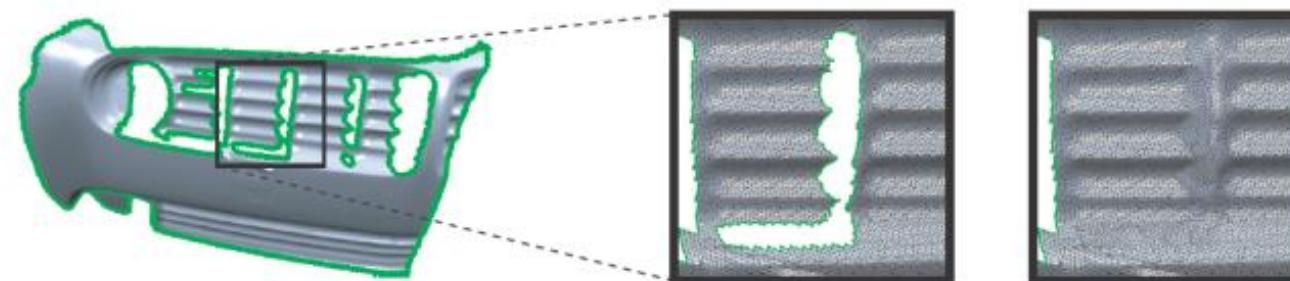


Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
 - Healing
- Animation

Removal of topological and geometrical errors



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Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation
 - Rigging

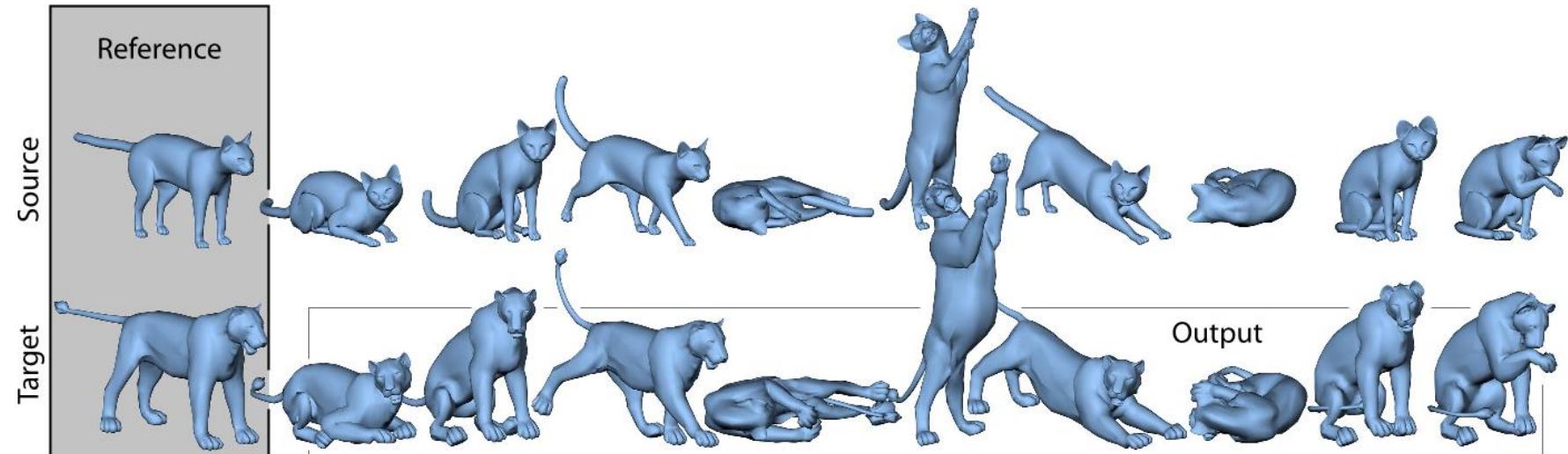


Animation
Buffet

Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation
 - Deformation transfer

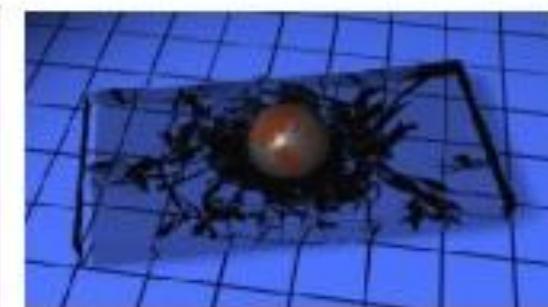


Sumner et al. 2004

Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation
 - Simulation



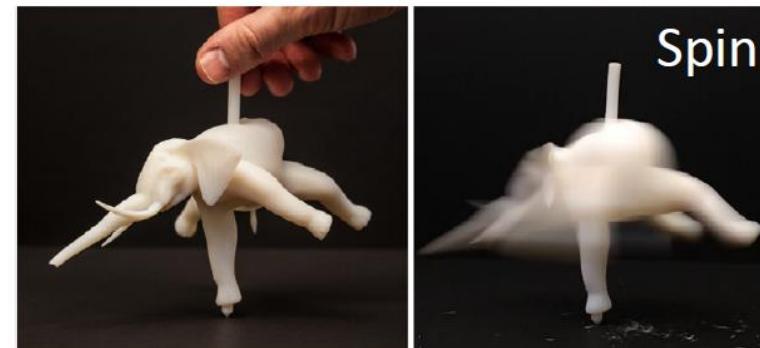
Why Different Representations?

Efficiency for different tasks

- Acquisition
- Rendering
- Analysis
- Manipulation
- Animation
- Fabrication



Stand



Spin



Float



3D Object Representations

- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific



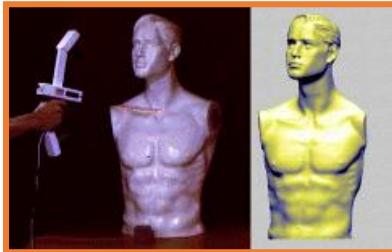
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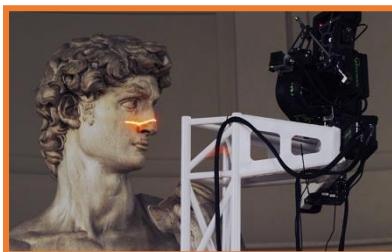
Range Image

Set of 3D points mapping to pixels of depth image

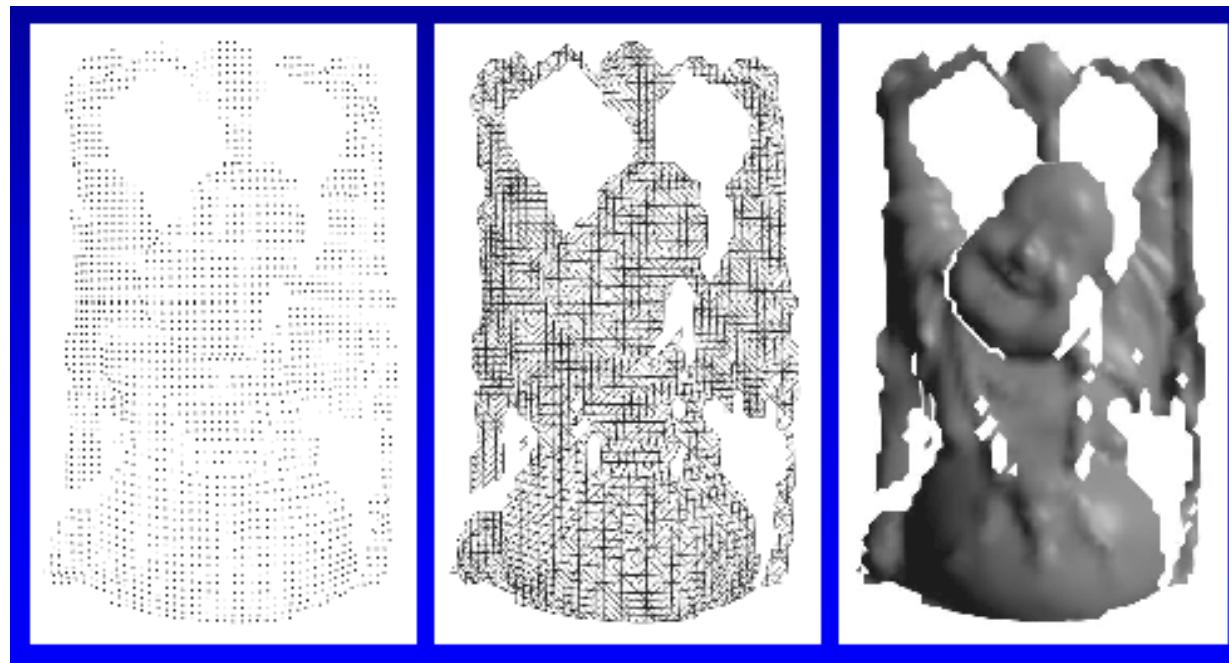
- Can be acquired from range scanner



Cyberware



Stanford



Range Image

Tesselation

Range Surface

Point Cloud

Unstructured set of 3D point samples

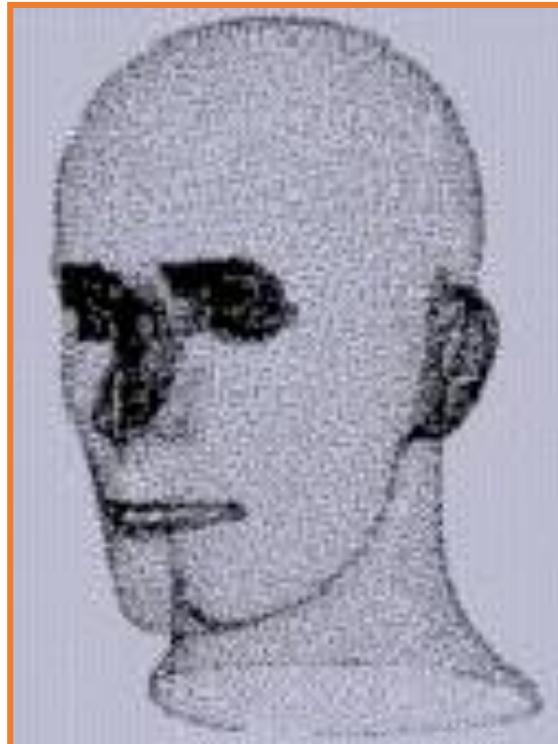
- Acquired from range finder, computer vision, etc



Polhemus



Microscribe-3D



Hoppe



Hoppe



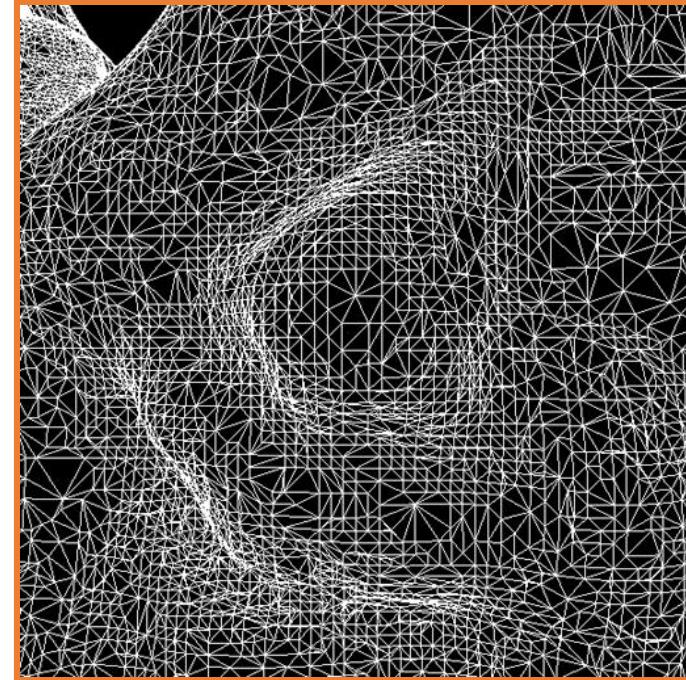
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Polygonal Mesh

Connected set of polygons (often triangles)

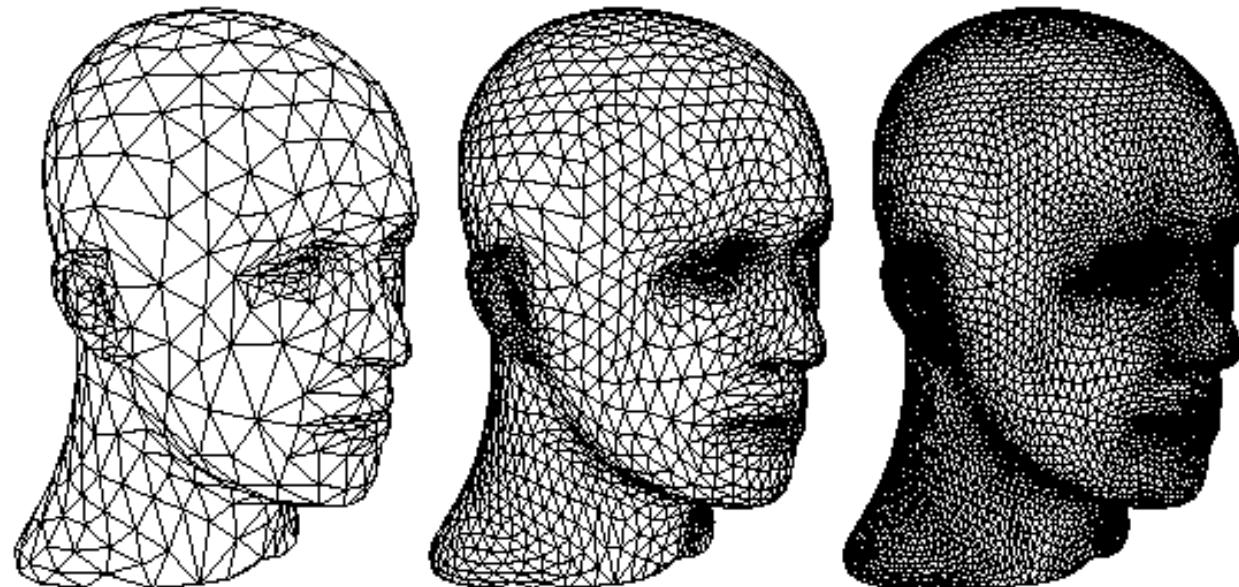




Subdivision Surface

Coarse mesh & subdivision rule

- Smooth surface is **limit** of sequence of refinements

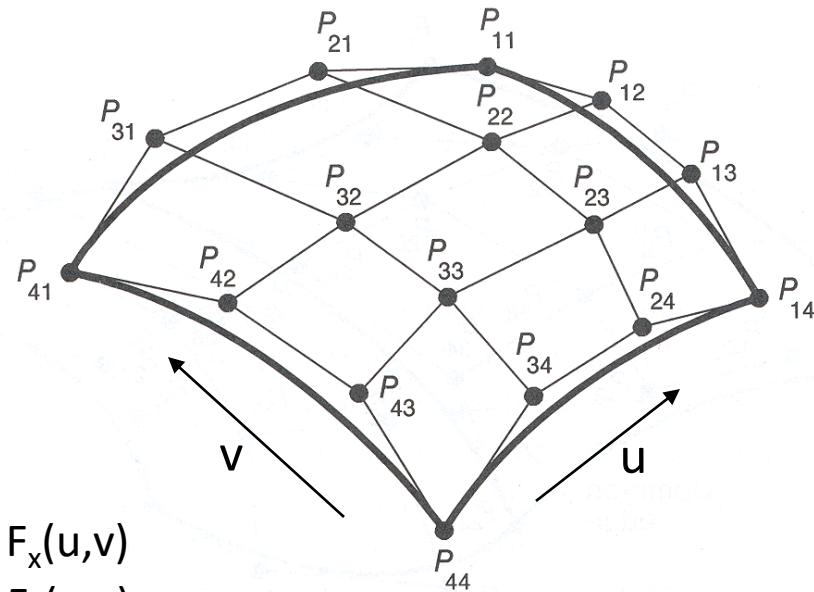


Zorin & Schroeder
SIGGRAPH 99
Course Notes

Parametric Surface

Tensor-product spline patches

- Each patch is parametric function
- Careful constraints to maintain continuity



$$x = F_x(u, v)$$

$$y = F_y(u, v)$$

$$z = F_z(u, v)$$

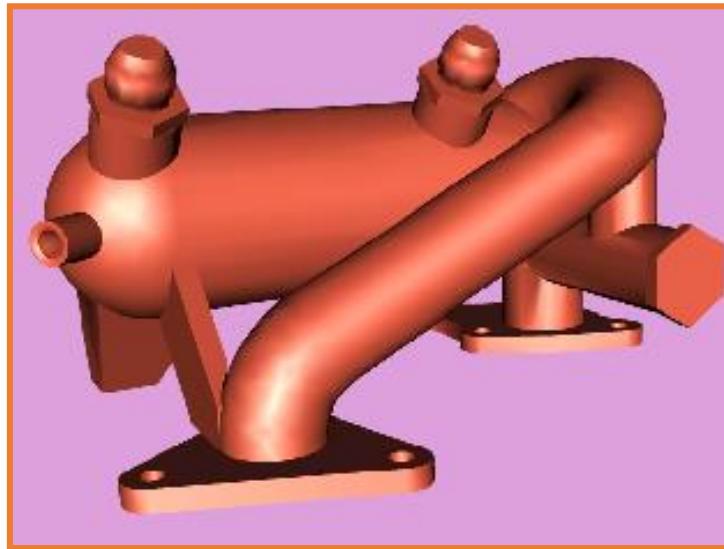


FvDFH Figure 11.44



Implicit Surface

Set of all points satisfying: $F(x,y,z) = 0$



Polygonal Model



Implicit Model

Bill Lorensen
SIGGRAPH 99
Course #4 Notes



3D Object Representations

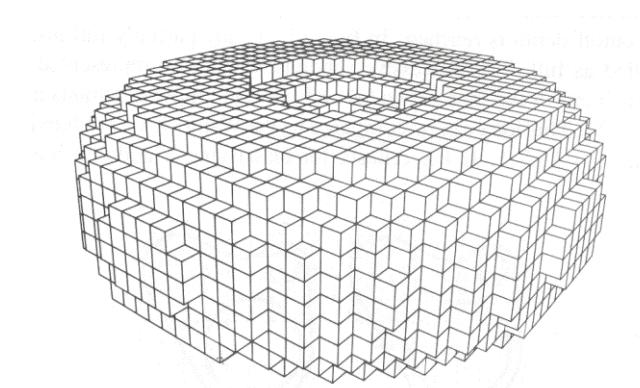
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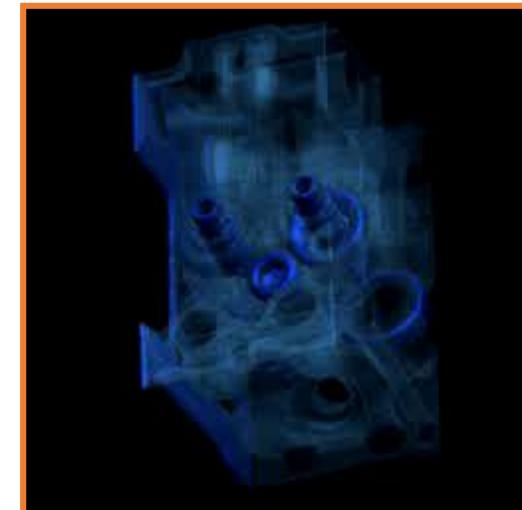
Voxel grid

Uniform volumetric grid of samples:

- Occupancy
(object vs. empty space)
- Density
- Color
- Other function
(speed, temperature, etc.)
- Often acquired via
simulation or from
CAT, MRI, etc.



FvDFH Figure 12.20

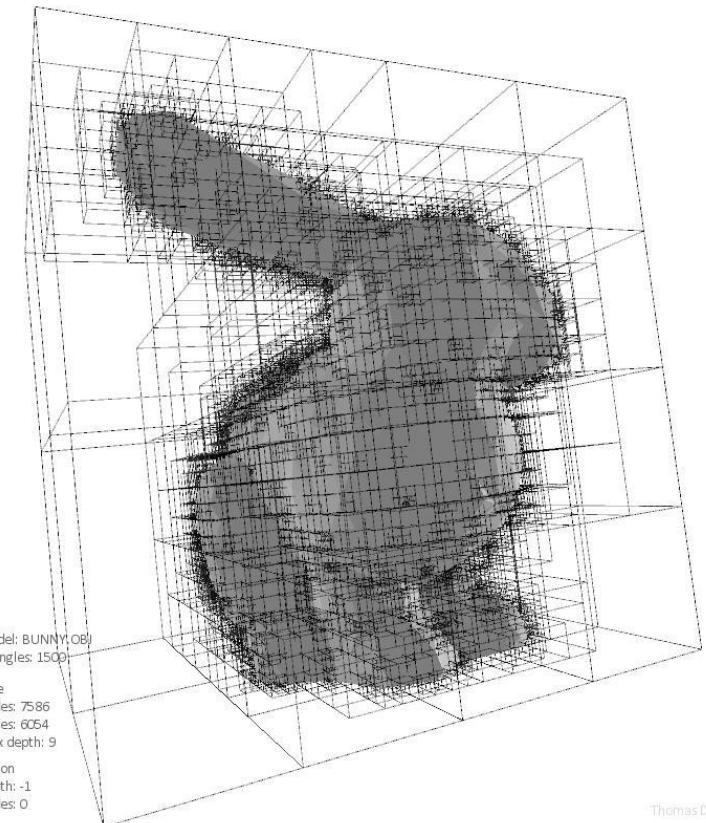
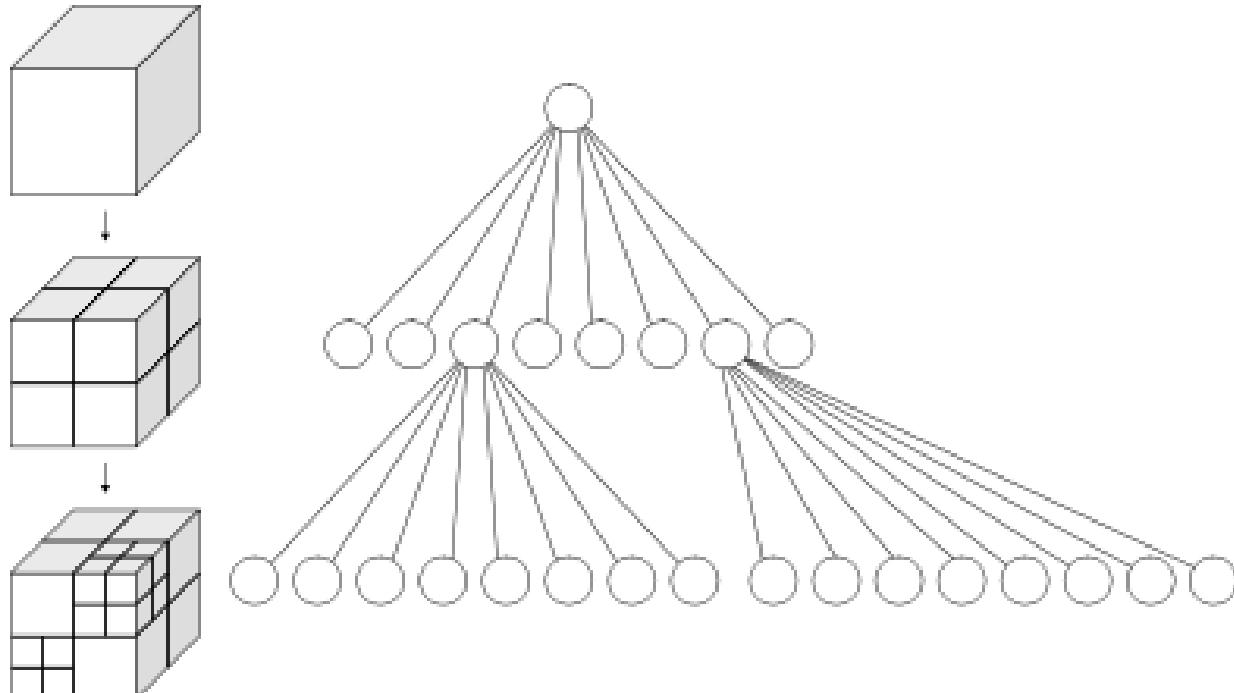


Stanford Graphics Laboratory

Octree

The adaptive version of the voxel grid

- Significantly more space efficient
- Makes operations more cumbersome



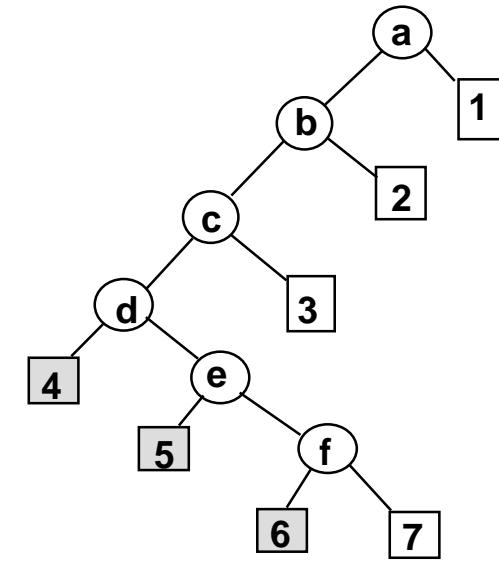
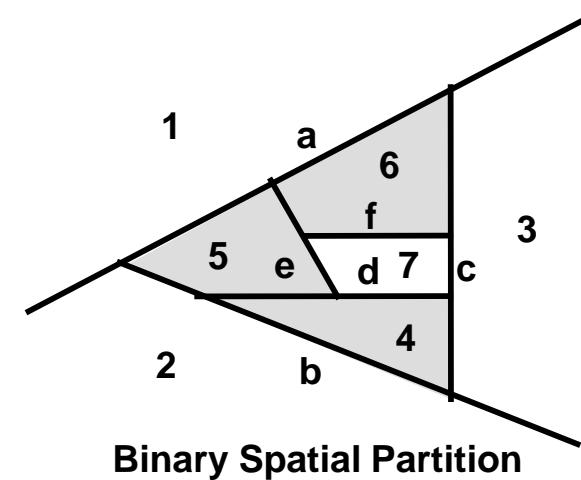
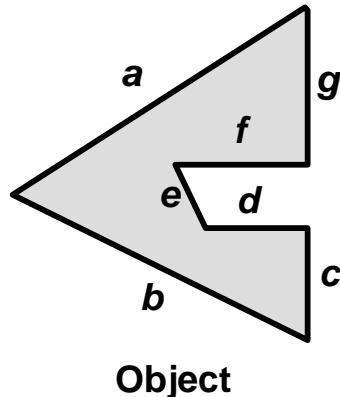
Thomas Diewald

BSP Tree



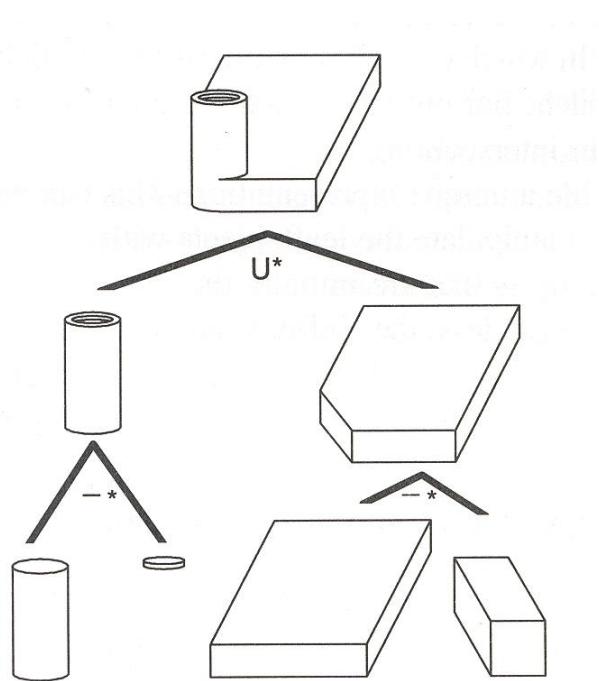
Hierarchical **Binary Space Partition** with solid/empty cells labeled

- Constructed from polygonal representations

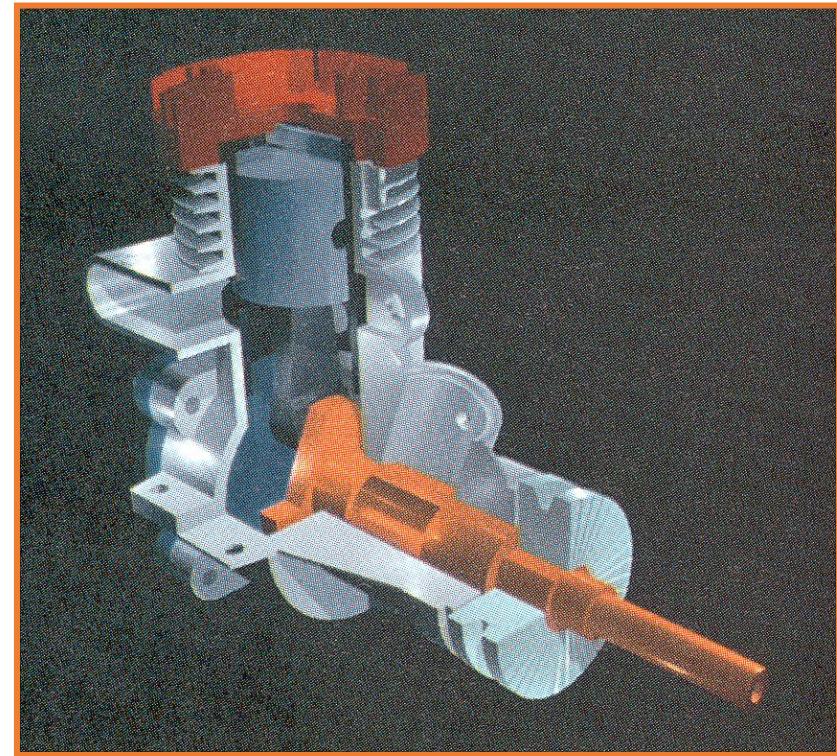


Binary Tree

Constructive Solid Geometry: set operations (union, difference, intersection) applied to simple shapes



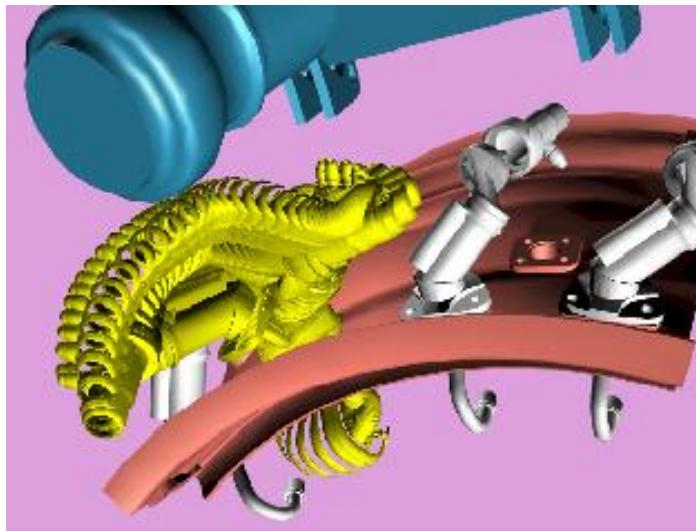
FvDFH Figure 12.27



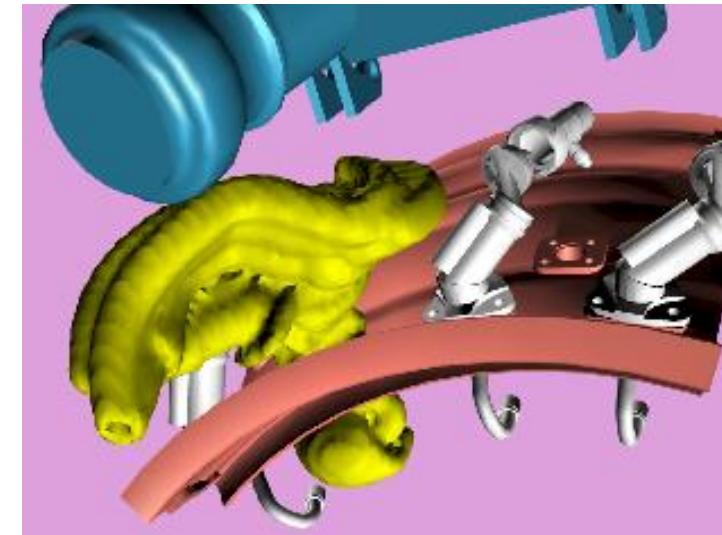
H&B Figure 9.9

Sweep

Solid swept by curve along trajectory



Removal Path



Sweep Model

Bill Lorensen
SIGGRAPH 99
Course #4 Notes



3D Object Representations

- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
- Solids
 - Voxels
 - BSP tree
 - CSG
 - Sweep
- High-level structures
 - Scene graph
 - Application specific



Scene Graph

Union of objects at leaf nodes



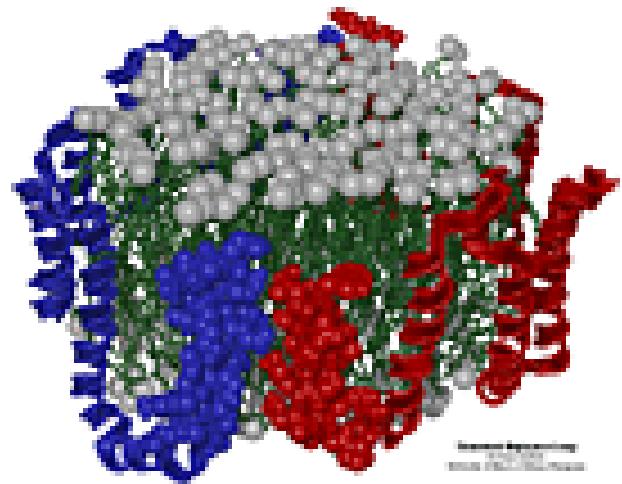
Bell Laboratories



avalon.viewpoint.com

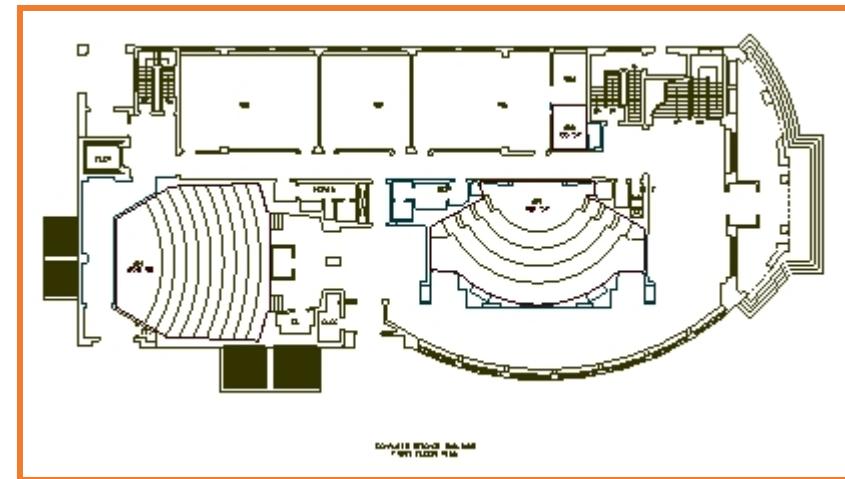


Application Specific



Apo A-1

(*Theoretical Biophysics Group,
University of Illinois at Urbana-Champaign*)

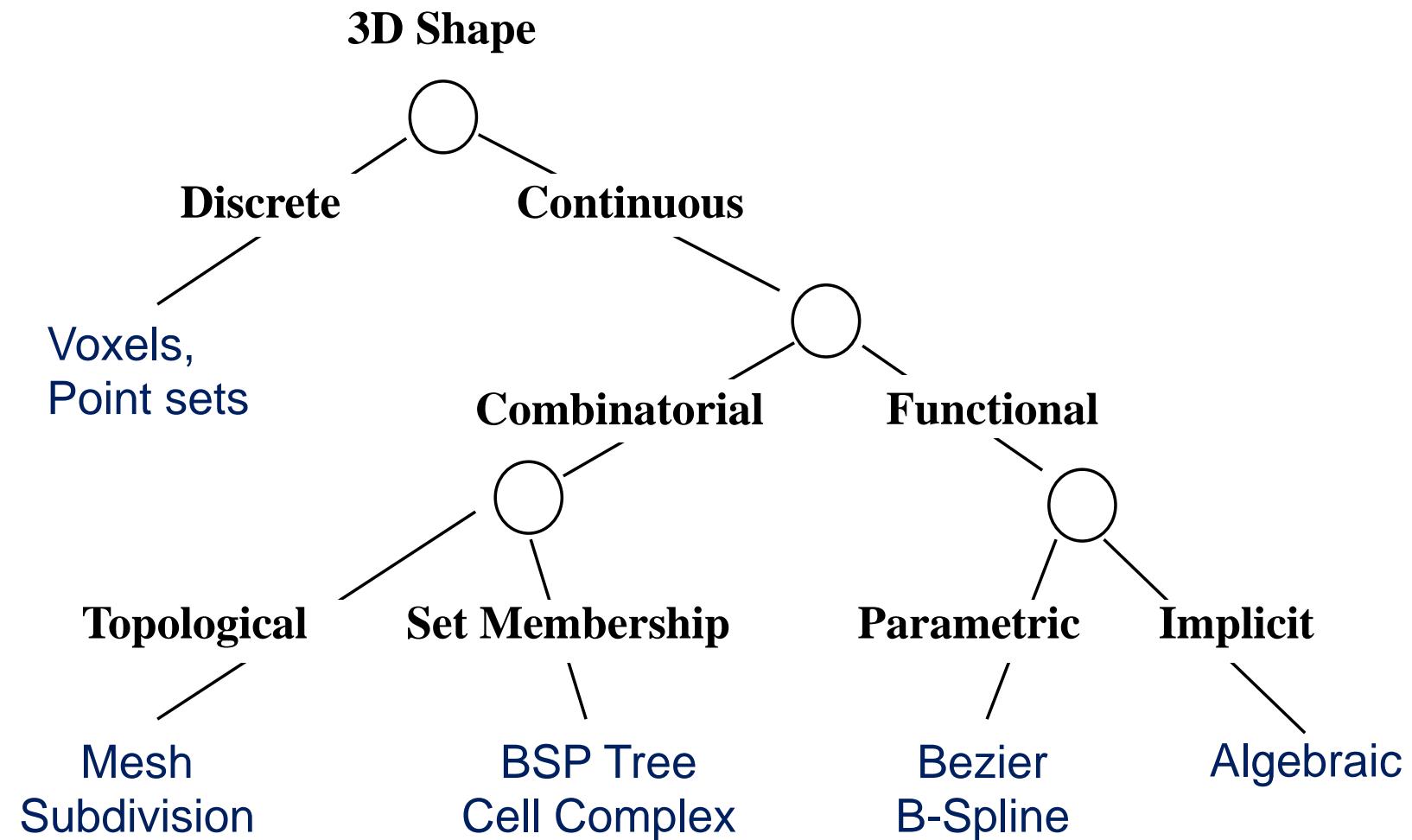


Architectural Floorplan

(*CS Building, Princeton University*)



Taxonomy of 3D Representations





Equivalence of Representations

- Thesis:
 - Each representation has enough expressive power to model the shape of any geometric object
 - It is possible to perform all geometric operations with any fundamental representation
- Analogous to Turing-equivalence
 - Computers and programming languages are Turing-equivalent, but each has its benefits...



Computational Differences

- Efficiency
 - Representational complexity (e.g. surface vs. volume)
 - Computational complexity (e.g. $O(n^2)$ vs $O(n^3)$)
 - Space/time trade-offs (e.g. tree data structures)
 - Numerical accuracy/stability (e.g. degree of polynomial)
- Simplicity
 - Ease of acquisition
 - Hardware acceleration
 - Software creation and maintenance
- Usability
 - Designer interface vs. computational engine



Upcoming Lectures

- Points
 - Range image
 - Point cloud
- Surfaces
 - Polygonal mesh
 - Subdivision
 - Parametric
 - Implicit
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